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1 README.md
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2 thinkdsp.py
"""This file contains code used in "Think DSP",
by Allen B. Downey, available from greenteapress.com
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from future import print function, division
import array
import copy
import math
import numpy as np
import random
import scipy
import scipy.stats
import scipy.fftpack
import struct
import subprocess
import thinkplot
import warnings
from fractions import gcd
from wave import open as open wave
import matplotlib.pyplot as pyplot
try:
    from IPython.display import Audio
except:
    warnings.warn("Can't import Audio from IPython.display; "
                  "Wave.make audio() will not work.")
PI2 = math.pi * 2
```

```
def random seed(x):
    """Initialize the random and np.random generators.
    x: int seed
    random.seed(x)
    np.random.seed(x)
class UnimplementedMethodException(Exception):
    """Exception if someone calls a method that should be
overridden."""
class WavFileWriter:
    """Writes wav files."""
         init (self, filename='sound.wav', framerate=11025):
        """Opens the file and sets parameters.
        filename: string
        framerate: samples per second
        self.filename = filename
        self.framerate = framerate
        self.nchannels = 1
        self.sampwidth = 2
        self.bits = self.sampwidth * 8
        self.bound = 2**(self.bits-1) - 1
        self.fmt = 'h'
        self.dtype = np.int16
        self.fp = open wave(self.filename, 'w')
        self.fp.setnchannels(self.nchannels)
        self.fp.setsampwidth(self.sampwidth)
        self.fp.setframerate(self.framerate)
    def write(self, wave):
        """Writes a wave.
        wave: Wave
        zs = wave.quantize(self.bound, self.dtype)
        self.fp.writeframes(zs.tostring())
    def close(self, duration=0):
        """Closes the file.
        duration: how many seconds of silence to append
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        if duration:
            self.write(rest(duration))
        self.fp.close()
def read wave(filename='sound.wav'):
    """Reads a wave file.
    filename: string
    returns: Wave
    fp = open wave(filename, 'r')
    nchannels = fp.getnchannels()
    nframes = fp.getnframes()
    sampwidth = fp.getsampwidth()
    framerate = fp.getframerate()
    z str = fp.readframes(nframes)
    fp.close()
    dtype map = {1:np.int8, 2:np.int16, 3:'special',
4:np.int32}
    if sampwidth not in dtype map:
        raise ValueError('sampwidth %d unknown' % sampwidth)
    if sampwidth == 3:
        xs = np.fromstring(z str,
dtype=np.int8).astype(np.int32)
        ys = (xs[2::3] * 256 + xs[1::3]) * 256 + xs[0::3]
    else:
        ys = np.fromstring(z str, dtype=dtype map[sampwidth])
    # if it's in stereo, just pull out the first channel
    if nchannels == 2:
        ys = ys[::2]
    #ts = np.arange(len(ys)) / framerate
    wave = Wave(vs, framerate=framerate)
    wave.normalize()
    return wave
def play wave(filename='sound.wav', player='aplay'):
    """Plays a wave file.
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filename: string
    player: string name of executable that plays wav files
    cmd = '%s %s' % (player, filename)
    popen = subprocess.Popen(cmd, shell=True)
    popen.communicate()
def find index(x, xs):
    """Find the index corresponding to a given value in an
array."""
    n = len(xs)
    start = xs[0]
    end = xs[-1]
    i = round((n-1) * (x - start) / (end - start))
    return int(i)
class SpectrumParent:
    """Contains code common to Spectrum and DCT.
    def __init__(self, hs, fs, framerate, full=False):
        """Ini\overline{\text{ti}}alizes a spectrum.
        hs: array of amplitudes (real or complex)
        fs: array of frequencies
        framerate: frames per second
        full: boolean to indicate full or real FFT
        self.hs = np.asanyarray(hs)
        self.fs = np.asanyarray(fs)
        self.framerate = framerate
        self.full = full
    @property
    def max freq(self):
        """Returns the Nyquist frequency for this spectrum."""
        return self.framerate / 2
    @property
    def amps(self):
        """Returns a sequence of amplitudes (read-only
property)."""
        return np.absolute(self.hs)
    @property
    def power(self):
        """Returns a sequence of powers (read-only
property)."""
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return self.amps ** 2
   def copy(self):
        """Makes a copy.
        Returns: new Spectrum
        return copy.deepcopy(self)
   def max diff(self, other):
        """Computes the maximum absolute difference between
spectra.
        other: Spectrum
        returns: float
        assert self.framerate == other.framerate
        assert len(self) == len(other)
        hs = self.hs - other.hs
        return np.max(np.abs(hs))
   def ratio(self, denom, thresh=1, val=0):
        """The ratio of two spectrums.
        denom: Spectrum
        thresh: values smaller than this are replaced
        val: with this value
        returns: new Wave
        ratio spectrum = self.copy()
        ratio_spectrum.hs /= denom.hs
        ratio spectrum.hs[denom.amps < thresh] = val</pre>
        return ratio spectrum
   def invert(self):
        """Inverts this spectrum/filter.
        returns: new Wave
        inverse = self.copy()
        inverse.hs = 1 / inverse.hs
        return inverse
   @property
   def freq res(self):
        return self.framerate / 2 / (len(self.fs) - 1)
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def render full(self, high=None):
        """Extracts amps and fs from a full spectrum.
        high: cutoff frequency
        returns: fs, amps
        hs = np.fft.fftshift(self.hs)
        amps = np.abs(hs)
        fs = np.fft.fftshift(self.fs)
        i = 0 if high is None else find index(-high, fs)
        j = None if high is None else find index(high, fs) + 1
        return fs[i:j], amps[i:j]
    def plot(self, high=None, **options):
        """Plots amplitude vs frequency.
        Note: if this is a full spectrum, it ignores low and
high
        high: frequency to cut off at
        if self.full:
            fs, amps = self.render full(high)
            thinkplot.plot(fs, amps, **options)
        else:
            i = None if high is None else find index(high,
self.fs)
            thinkplot.plot(self.fs[:i], self.amps[:i],
**options)
    def plot power(self, high=None, **options):
        """Plots power vs frequency.
        high: frequency to cut off at
        if self.full:
            fs, amps = self.render_full(high)
            thinkplot.plot(fs, amps**2, **options)
            i = None if high is None else find index(high,
self.fs)
            thinkplot.plot(self.fs[:i], self.power[:i],
**options)
    def estimate slope(self):
        """Runs linear regression on log power vs log
frequency.
        returns: slope, inter, r2, p, stderr
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11 11 11
        x = np.log(self.fs[1:])
        y = np.log(self.power[1:])
        t = scipy.stats.linregress(x,y)
        return t
    def peaks(self):
        """Finds the highest peaks and their frequencies.
        returns: sorted list of (amplitude, frequency) pairs
        t = list(zip(self.amps, self.fs))
        t.sort(reverse=True)
        return t
class Spectrum( SpectrumParent):
    """Represents the spectrum of a signal."""
    def __len__(self):
        """Length of the spectrum."""
        return len(self.hs)
    def add (self, other):
        """Ad\overline{ds} two spectrums elementwise.
        other: Spectrum
        returns: new Spectrum
        if other == 0:
            return self.copy()
        assert all(self.fs == other.fs)
        hs = self.hs + other.hs
        return Spectrum(hs, self.fs, self.framerate,
self.full)
    ___radd___ = __add___
    def mul (self, other):
        """Multiplies two spectrums elementwise.
        other: Spectrum
        returns: new Spectrum
        assert all(self.fs == other.fs)
        hs = self.hs * other.hs
        return Spectrum(hs, self.fs, self.framerate,
```

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self.full)
    def convolve(self, other):
        """Convolves two Spectrums.
        other: Spectrum
        returns: Spectrum
        assert all(self.fs == other.fs)
        if self.full:
            hs1 = np.fft.fftshift(self.hs)
            hs2 = np.fft.fftshift(other.hs)
            hs = np.convolve(hs1, hs2, mode='same')
            hs = np.fft.ifftshift(hs)
        else:
            # not sure this branch would mean very much
            hs = np.convolve(self.hs, other.hs, mode='same')
        return Spectrum(hs, self.fs, self.framerate,
self.full)
    @property
    def real(self):
        """Returns the real part of the hs (read-only
property)."""
        return np.real(self.hs)
    @property
    def imag(self):
        """Returns the imaginary part of the hs (read-only
property)."""
        return np.imag(self.hs)
    @property
    def angles(self):
        """Returns a sequence of angles (read-only
property)."""
        return np.angle(self.hs)
    def scale(self, factor):
        """Multiplies all elements by the given factor.
        factor: what to multiply the magnitude by (could be
complex)
        self.hs *= factor
    def low pass(self, cutoff, factor=0):
        """Attenuate frequencies above the cutoff.
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cutoff: frequency in Hz
    factor: what to multiply the magnitude by
    self.hs[abs(self.fs) > cutoff] *= factor
def high pass(self, cutoff, factor=0):
    """Attenuate frequencies below the cutoff.
    cutoff: frequency in Hz
    factor: what to multiply the magnitude by
    self.hs[abs(self.fs) < cutoff] *= factor</pre>
def band stop(self, low cutoff, high cutoff, factor=0):
    """Attenuate frequencies between the cutoffs.
    low cutoff: frequency in Hz
    high cutoff: frequency in Hz
    factor: what to multiply the magnitude by
    # TODO: test this function
    fs = abs(self.fs)
    indices = (low cutoff < fs) & (fs < high cutoff)
    self.hs[indices] *= factor
def pink filter(self, beta=1):
    """Apply a filter that would make white noise pink.
    beta: exponent of the pink noise
    denom = self.fs ** (beta/2.0)
    denom[0] = 1
    self.hs /= denom
def differentiate(self):
    """Apply the differentiation filter.
    returns: new Spectrum
    new = self.copy()
    new.hs *= PI2 * 1j * new.fs
    return new
def integrate(self):
    """Apply the integration filter.
    returns: new Spectrum
    new = self.copy()
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new.hs /= PI2 * 1j * new.fs
        return new
    def make integrated spectrum(self):
        """Makes an integrated spectrum.
        cs = np.cumsum(self.power)
        cs /= cs[-1]
        return IntegratedSpectrum(cs, self.fs)
    def make wave(self):
        """Transforms to the time domain.
        returns: Wave
        if self.full:
            ys = np.fft.ifft(self.hs)
        else:
            ys = np.fft.irfft(self.hs)
        #NOTE: whatever the start time was, we lose it when
        # we transform back; we could fix that by saving start
        # time in the Spectrum
        # ts = self.start + np.arange(len(ys)) /
self.framerate
        return Wave(ys, framerate=self.framerate)
class IntegratedSpectrum:
    """Represents the integral of a spectrum."""
          init__(self, cs, fs):
        """Initializes an integrated spectrum:
        cs: sequence of cumulative amplitudes
        fs: sequence of frequencies
        self.cs = np.asanyarray(cs)
        self.fs = np.asanyarray(fs)
    def plot power(self, low=0, high=None, expo=False,
**options):
        """Plots the integrated spectrum.
        low: int index to start at
        high: int index to end at
        cs = self.cs[low:high]
        fs = self.fs[low:high]
```

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if expo:
            cs = np.exp(cs)
        thinkplot.plot(fs, cs, **options)
    def estimate slope(self, low=1, high=-12000):
        """Runs linear regression on log cumulative power vs
log frequency.
        returns: slope, inter, r2, p, stderr
        #print self.fs[low:high]
        #print self.cs[low:high]
        x = np.log(self.fs[low:high])
        y = np.log(self.cs[low:high])
        t = scipy.stats.linregress(x,y)
        return t
class Dct( SpectrumParent):
    """Represents the spectrum of a signal using discrete
cosine transform """
    @property
    def amps(self):
        """Returns a sequence of amplitudes (read-only
property).
        Note: for DCTs, amps are positive or negative real.
        return self.hs
    def add (self, other):
        """Adds two DCTs elementwise.
        other: DCT
        returns: new DCT
        if other == 0:
            return self
        assert self.framerate == other.framerate
        hs = self.hs + other.hs
        return Dct(hs, self.fs, self.framerate)
    ___radd___ = __add
    def make wave(self):
        """Transforms to the time domain.
```

```
returns: Wave
        N = len(self.hs)
        ys = scipy.fftpack.idct(self.hs, type=2) / 2 / N
        #NOTE: whatever the start time was, we lose it when
        # we transform back
        #ts = self.start + np.arange(len(ys)) / self.framerate
        return Wave(ys, framerate=self.framerate)
class Spectrogram:
    """Represents the spectrum of a signal."""
          init (self, spec map, seg length):
       """Initialize the spectrogram.
        spec map: map from float time to Spectrum
        seg length: number of samples in each segment
        self.spec map = spec map
        self.seg length = seg length
    def any spectrum(self):
        """Returns an arbitrary spectrum from the
spectrogram."""
        index = next(iter(self.spec map))
        return self.spec map[index]
    @property
    def time res(self):
        """Time resolution in seconds."""
        spectrum = self.any spectrum()
        return float(self.seg_length) / spectrum.framerate
    @property
    def freq res(self):
        """Frequency resolution in Hz."""
        return self.any spectrum().freq res
    def times(self):
        """Sorted sequence of times.
        returns: sequence of float times in seconds
        ts = sorted(iter(self.spec map))
        return ts
    def frequencies(self):
        """Sequence of frequencies.
```

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returns: sequence of float frequencies in Hz.
        fs = self.any spectrum().fs
        return fs
    def plot(self, high=None, **options):
        """Make a pseudocolor plot.
        high: highest frequency component to plot
        fs = self.frequencies()
        i = None if high is None else find index(high, fs)
        fs = fs[:i]
        ts = self.times()
        # make the array
        size = len(fs), len(ts)
        array = np.zeros(size, dtype=np.float)
        # copy amplitude from each spectrum into a column of
the array
        for j, t in enumerate(ts):
            spectrum = self.spec map[t]
            array[:, j] = spectrum.amps[:i]
        thinkplot.pcolor(ts, fs, array, **options)
    def make wave(self):
        """Inverts the spectrogram and returns a Wave.
        returns: Wave
        .. .. ..
        res = []
        for t, spectrum in sorted(self.spec map.items()):
            wave = spectrum.make wave()
            n = len(wave)
            window = 1 / np.hamming(n)
            wave.window(window)
            i = wave.find index(t)
            start = i - n // 2
            end = start + n
            res.append((start, end, wave))
        starts, ends, waves = zip(*res)
        low = min(starts)
        high = max(ends)
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ys = np.zeros(high-low, np.float)
        for start, end, wave in res:
            ys[start:end] = wave.ys
        # ts = np.arange(len(ys)) / self.framerate
        return Wave(ys, framerate=wave.framerate)
class Wave:
    """Represents a discrete-time waveform.
    11 11 11
         init (self, ys, ts=None, framerate=None):
    def
        """Initializes the wave.
        ys: wave array
        ts: array of times
        framerate: samples per second
        self.ys = np.asanyarray(ys)
        self.framerate = framerate if framerate is not None
else 11025
        if ts is None:
            self.ts = np.arange(len(ys)) / self.framerate
        else:
            self.ts = np.asanyarray(ts)
    def copy(self):
        """Makes a copy.
        Returns: new Wave
        return copy.deepcopy(self)
    def __len__(self):
        return len(self.ys)
    @property
    def start(self):
        return self.ts[0]
    @property
    def end(self):
        return self.ts[-1]
    @property
    def duration(self):
        """Duration (property).
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returns: float duration in seconds
        return len(self.ys) / self.framerate
         _add__(self, other):
        """Adds two waves elementwise.
        other: Wave
        returns: new Wave
        if other == 0:
            return self
        assert self.framerate == other.framerate
        # make an array of times that covers both waves
        start = min(self.start, other.start)
        end = max(self.end, other.end)
        n = int(round((end - start) * self.framerate)) + 1
        ys = np.zeros(n)
        ts = start + np.arange(n) / self.framerate
        def add ys(wave):
            i = find index(wave.start, ts)
            # make sure the arrays line up reasonably well
            diff = ts[i] - wave.start
            dt = 1 / wave.framerate
            if (diff / dt) > 0.1:
                warnings.warn("Can't add these waveforms;
their "
                              "time arrays don't line up.")
            j = i + len(wave)
            ys[i:j] += wave.ys
        add ys(self)
        add ys(other)
        return Wave(ys, ts, self.framerate)
    radd = add
    def __or__(self, other):
        """Concatenates two waves.
        other: Wave
        returns: new Wave
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11 11 11
        if self.framerate != other.framerate:
            raise ValueError('Wave. or : framerates do not
agree')
        ys = np.concatenate((self.ys, other.ys))
        # ts = np.arange(len(ys)) / self.framerate
        return Wave(ys, framerate=self.framerate)
         mul (self, other):
    def
        """Multiplies two waves elementwise.
        Note: this operation ignores the timestamps; the
result
        has the timestamps of self.
        other: Wave
        returns: new Wave
        # the spectrums have to have the same framerate and
duration
        assert self.framerate == other.framerate
        assert len(self) == len(other)
        ys = self.ys * other.ys
        return Wave(ys, self.ts, self.framerate)
    def max diff(self, other):
        """Computes the maximum absolute difference between
waves.
        other: Wave
        returns: float
        assert self.framerate == other.framerate
        assert len(self) == len(other)
        ys = self.ys - other.ys
        return np.max(np.abs(ys))
    def convolve(self, other):
        """Convolves two waves.
        Note: this operation ignores the timestamps; the
result
        has the timestamps of self.
        other: Wave or NumPy array
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returns: Wave
        if isinstance(other, Wave):
            assert self.framerate == other.framerate
            window = other.ys
        else:
            window = other
        ys = np.convolve(self.ys, window, mode='full')
        #ts = np.arange(len(ys)) / self.framerate
        return Wave(ys, framerate=self.framerate)
    def diff(self):
        """Computes the difference between successive
elements.
        returns: new Wave
        ys = np.diff(self.ys)
        ts = self.ts[1:].copy()
        return Wave(ys, ts, self.framerate)
    def cumsum(self):
        """Computes the cumulative sum of the elements.
        returns: new Wave
        ys = np.cumsum(self.ys)
        ts = self.ts.copy()
        return Wave(ys, ts, self.framerate)
    def quantize(self, bound, dtype):
        """Maps the waveform to quanta.
        bound: maximum amplitude
        dtype: numpy data type or string
        returns: quantized signal
        return quantize(self.ys, bound, dtype)
    def apodize(self, denom=20, duration=0.1):
        """Tapers the amplitude at the beginning and end of
the signal.
        Tapers either the given duration of time or the given
        fraction of the total duration, whichever is less.
        denom: float fraction of the segment to taper
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duration: float duration of the taper in seconds
        self.ys = apodize(self.ys, self.framerate, denom,
duration)
    def hamming(self):
        """Apply a Hamming window to the wave.
        self.ys *= np.hamming(len(self.ys))
    def window(self, window):
        """Apply a window to the wave.
        window: sequence of multipliers, same length as
self.ys
        self.ys *= window
    def scale(self, factor):
        """Multplies the wave by a factor.
        factor: scale factor
        self.ys *= factor
    def shift(self, shift):
        """Shifts the wave left or right in time.
        shift: float time shift
        # TODO: track down other uses of this function and
check them
        self.ts += shift
    def roll(self, roll):
        """Rolls this wave by the given number of locations.
        self.ys = np.roll(self.ys, roll)
    def truncate(self, n):
        """Trims this wave to the given length.
        n: integer index
        11 11 11
        self.ys = truncate(self.ys, n)
        self.ts = truncate(self.ts, n)
    def zero pad(self, n):
        """Trims this wave to the given length.
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n: integer index

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self.ys = zero pad(self.ys, n)
        self.ts = self.start + np.arange(n) / self.framerate
    def normalize(self, amp=1.0):
        """Normalizes the signal to the given amplitude.
        amp: float amplitude
        self.ys = normalize(self.ys, amp=amp)
    def unbias(self):
        """Unbiases the signal.
        self.ys = unbias(self.ys)
    def find index(self, t):
        """Find the index corresponding to a given time."""
        n = len(self)
        start = self.start
        end = self.end
        i = round((n-1) * (t - start) / (end - start))
        return int(i)
    def segment(self, start=None, duration=None):
        """Extracts a segment.
        start: float start time in seconds
        duration: float duration in seconds
        returns: Wave
        11 11 11
        if start is None:
            start = self.ts[0]
            i = 0
        else:
            i = self.find index(start)
        j = None if duration is None else
self.find index(start + duration)
        return self.slice(i, j)
    def slice(self, i, j):
        """Makes a slice from a Wave.
        i: first slice index
        j: second slice index
        ys = self.ys[i:j].copy()
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ts = self.ts[i:j].copy()
        return Wave(ys, ts, self.framerate)
    def make spectrum(self, full=False):
        """Computes the spectrum using FFT.
        returns: Spectrum
        n = len(self.ys)
        d = 1 / self.framerate
        if full:
            hs = np.fft.fft(self.ys)
            fs = np.fft.fftfreq(n, d)
        else:
            hs = np.fft.rfft(self.ys)
            fs = np.fft.rfftfreq(n, d)
        return Spectrum(hs, fs, self.framerate, full)
    def make dct(self):
        """\overline{\text{Computes}} the DCT of this wave.
        N = len(self.ys)
        hs = scipy.fftpack.dct(self.ys, type=2)
        fs = (0.5 + np.arange(N)) / 2
        return Dct(hs, fs, self.framerate)
    def make spectrogram(self, seg length, win flag=True):
        """Computes the spectrogram of the wave.
        seg length: number of samples in each segment
        win flag: boolean, whether to apply hamming window to
each segment
        returns: Spectrogram
        if win flag:
            window = np.hamming(seg length)
        i, j = 0, seg length
        step = int(seg_length // 2)
        # map from time to Spectrum
        spec map = \{\}
        while j < len(self.ys):
            segment = self.slice(i, j)
            if win flag:
                 segment.window(window)
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# the nominal time for this segment is the
midpoint
            t = (segment.start + segment.end) / 2
            spec map[t] = segment.make spectrum()
            i += step
            j += step
        return Spectrogram(spec map, seg length)
    def get xfactor(self, options):
        try:
            xfactor = options['xfactor']
            options.pop('xfactor')
        except KeyError:
            xfactor = 1
        return xfactor
    def plot(self, **options):
        """Plots the wave.
        11 11 11
        xfactor = self.get xfactor(options)
        thinkplot.plot(self.ts * xfactor, self.ys, **options)
    def plot_vlines(self, **options):
        """Plots the wave with vertical lines for samples.
        xfactor = self.get xfactor(options)
        thinkplot.vlines(self.ts * xfactor, 0, self.ys,
**options)
    def corr(self, other):
        """Correlation coefficient two waves.
        other: Wave
        returns: float coefficient of correlation
        corr = np.corrcoef(self.ys, other.ys)[0, 1]
        return corr
    def cov mat(self, other):
        """

Tovariance matrix of two waves.
        other: Wave
        returns: 2x2 covariance matrix
```

```
return np.cov(self.ys, other.ys)
def cov(self, other):
    """Covariance of two unbiased waves.
    other: Wave
    returns: float
    total = sum(self.ys * other.ys) / len(self.ys)
    return total
def cos cov(self, k):
    """Covariance with a cosine signal.
    freq: freq of the cosine signal in Hz
    returns: float covariance
    n = len(self.ys)
    factor = math.pi * k / n
    ys = [math.cos(factor * (i+0.5)) for i in range(n)]
    total = 2 * sum(self.ys * ys)
    return total
def cos_transform(self):
    """Discrete cosine transform.
    returns: list of frequency, cov pairs
    n = len(self.ys)
    res = []
    for k in range(n):
        cov = self.cos_cov(k)
        res.append((k, cov))
    return res
def write(self, filename='sound.wav'):
    """Write a wave file.
    filename: string
    print('Writing', filename)
    wfile = WavFileWriter(filename, self.framerate)
   wfile.write(self)
   wfile.close()
def play(self, filename='sound.wav'):
    """Plays a wave file.
```

```
filename: string
        self.write(filename)
        play wave(filename)
    def make audio(self):
        """Makes an IPython Audio object.
        audio = Audio(data=self.ys.real, rate=self.framerate)
        return audio
def unbias(ys):
    """Shifts a wave array so it has mean 0.
    ys: wave array
    returns: wave array
    return ys - ys.mean()
def normalize(ys, amp=1.0):
    """Normalizes a wave array so the maximum amplitude is
+amp or -amp.
    ys: wave array
    amp: max amplitude (pos or neg) in result
    returns: wave array
    high, low = abs(max(ys)), abs(min(ys))
    return amp * ys / max(high, low)
def shift right(ys, shift):
    """Shīfts a wave array to the right and zero pads.
    ys: wave array
    shift: integer shift
    returns: wave array
    res = np.zeros(len(ys) + shift)
    res[shift:] = vs
    return res
def shift left(ys, shift):
```

```
"""Shifts a wave array to the left.
    ys: wave array
    shift: integer shift
    returns: wave array
    return ys[shift:]
def truncate(ys, n):
    """Trims a wave array to the given length.
    ys: wave array
    n: integer length
    returns: wave array
    return ys[:n]
def quantize(ys, bound, dtype):
    """Maps the waveform to quanta.
    ys: wave array
    bound: maximum amplitude
    dtype: numpy data type of the result
    returns: quantized signal
    if max(ys) > 1 or min(ys) < -1:
        warnings.warn('Warning: normalizing before
quantizing.')
        ys = normalize(ys)
    zs = (ys * bound).astype(dtype)
    return zs
def apodize(ys, framerate, denom=20, duration=0.1):
    """Tapers the amplitude at the beginning and end of the
signal.
    Tapers either the given duration of time or the given
    fraction of the total duration, whichever is less.
    ys: wave array
    framerate: int frames per second
    denom: float fraction of the segment to taper
    duration: float duration of the taper in seconds
```

```
returns: wave array
    # a fixed fraction of the segment
    n = len(ys)
    k1 = n // denom
    # a fixed duration of time
    k2 = int(duration * framerate)
    k = min(k1, k2)
    w1 = np.linspace(0, 1, k)
    w2 = np.ones(n - 2*k)
    w3 = np.linspace(1, 0, k)
    window = np.concatenate((w1, w2, w3))
    return ys * window
class Signal:
    """Represents a time-varying signal."""
    def add (self, other):
        """Ad\overline{ds} two signals.
        other: Signal
        returns: Signal
        if other == 0:
            return self
        return SumSignal(self, other)
    ___radd___ = __add___
    @property
    def period(self):
        """Period of the signal in seconds (property).
        Since this is used primarily for purposes of plotting,
        the default behavior is to return a value, 0.1
seconds,
        that is reasonable for many signals.
        returns: float seconds
        return 0.1
    def plot(self, framerate=11025):
```

```
"""Plots the signal.
        The default behavior is to plot three periods.
        framerate: samples per second
        duration = self.period * 3
        wave = self.make wave(duration, start=0,
framerate=framerate)
        wave.plot()
    def make wave(self, duration=1, start=0, framerate=11025):
        """Makes a Wave object.
        duration: float seconds
        start: float seconds
        framerate: int frames per second
        returns: Wave
        n = round(duration * framerate)
        ts = start + np.arange(n) / framerate
        ys = self.evaluate(ts)
        return Wave(ys, ts, framerate=framerate)
def infer framerate(ts):
    """Given ts, find the framerate.
    Assumes that the ts are equally spaced.
    ts: sequence of times in seconds
    returns: frames per second
    #TODO: confirm that this is never used and remove it
    dt = ts[1] - ts[0]
    framerate = 1.0 / dt
    return framerate
class SumSignal(Signal):
    """Represents the sum of signals."""
        init (self, *args):
        """Initializes the sum.
        args: tuple of signals
        self.signals = args
```

```
@property
    def period(self):
        """Period of the signal in seconds.
        Note: this is not correct; it's mostly a placekeeper.
        But it is correct for a harmonic sequence where all
        component frequencies are multiples of the
fundamental.
        returns: float seconds
        return max(sig.period for sig in self.signals)
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ts = np.asarray(ts)
        return sum(sig.evaluate(ts) for sig in self.signals)
class Sinusoid(Signal):
    """Represents a sinusoidal signal."""
    def init (self, freq=440, amp=1.0, offset=0,
func=np.sin):
        """Initializes a sinusoidal signal.
        freq: float frequency in Hz
        amp: float amplitude, 1.0 is nominal max
        offset: float phase offset in radians
        func: function that maps phase to amplitude
        self.freq = freq
        self.amp = amp
        self.offset = offset
        self.func = func
    @property
    def period(self):
        """Period of the signal in seconds.
        returns: float seconds
        return 1.0 / self.freq
```

```
def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ts = np.asarray(ts)
        phases = PI2 * self.freq * ts + self.offset
        ys = self.amp * self.func(phases)
        return ys
def CosSignal(freq=440, amp=1.0, offset=0):
    """Makes a cosine Sinusoid.
    freq: float frequency in Hz
    amp: float amplitude, 1.0 is nominal max
    offset: float phase offset in radians
    returns: Sinusoid object
    return Sinusoid(freq, amp, offset, func=np.cos)
def SinSignal(freq=440, amp=1.0, offset=0):
    """Makes a sine Sinusoid.
    freq: float frequency in Hz
    amp: float amplitude, 1.0 is nominal max
    offset: float phase offset in radians
    returns: Sinusoid object
    return Sinusoid(freq, amp, offset, func=np.sin)
def Sinc(freq=440, amp=1.0, offset=0):
    """Makes a Sinc function.
    freq: float frequency in Hz
    amp: float amplitude, 1.0 is nominal max
    offset: float phase offset in radians
    returns: Sinusoid object
    return Sinusoid(freg, amp, offset, func=np.sinc)
```

```
class ComplexSinusoid(Sinusoid):
    """Represents a complex exponential signal."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ts = np.asarray(ts)
        phases = PI2 * self.freq * ts + self.offset
        ys = self.amp * np.exp(1j * phases)
        return ys
class SquareSignal(Sinusoid):
    """Represents a square signal."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ts = np.asarray(ts)
        cycles = self.freq * ts + self.offset / PI2
        frac, _ = np.modf(cycles)
        ys = self.amp * np.sign(unbias(frac))
        return ys
class SawtoothSignal(Sinusoid):
    """Represents a sawtooth signal."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ts = np.asarray(ts)
        cycles = self.freq * ts + self.offset / PI2
        frac, = np.modf(cycles)
        ys = normalize(unbias(frac), self.amp)
        return ys
```

```
class ParabolicSignal(Sinusoid):
    """Represents a parabolic signal."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ts = np.asarray(ts)
        cycles = self.freq * ts + self.offset / PI2
        frac, = np.modf(cycles)
        vs = (\overline{frac} - 0.5)**2
        ys = normalize(unbias(ys), self.amp)
        return ys
class CubicSignal(ParabolicSignal):
    """Represents a cubic signal."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ys = ParabolicSignal.evaluate(self, ts)
        ys = np.cumsum(ys)
        ys = normalize(unbias(ys), self.amp)
        return vs
class GlottalSignal(Sinusoid):
    """Represents a periodic signal that resembles a glottal
signal."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ts = np.asarray(ts)
        cycles = self.freq * ts + self.offset / PI2
        frac, _ = np.modf(cycles)
        ys = frac**2 * (1-frac)
        ys = normalize(unbias(ys), self.amp)
```

return ys

```
class TriangleSignal(Sinusoid):
    """Represents a triangle signal."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ts = np.asarray(ts)
        cycles = self.freq * ts + self.offset / PI2
        frac, _ = np.modf(cycles)
        ys = np.abs(frac - 0.5)
        ys = normalize(unbias(ys), self.amp)
        return ys
class Chirp(Signal):
    """Represents a signal with variable frequency."""
    def init (self, start=440, end=880, amp=1.0):
       """Initializes a linear chirp.
        start: float frequency in Hz
        end: float frequency in Hz
        amp: float amplitude, 1.0 is nominal max
        self.start = start
        self.end = end
        self.amp = amp
    @property
    def period(self):
        """Period of the signal in seconds.
        returns: float seconds
        return ValueError('Non-periodic signal.')
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
```

```
freqs = np.linspace(self.start, self.end, len(ts)-1)
        return self. evaluate(ts, freqs)
    def evaluate(self, ts, freqs):
        """Helper function that evaluates the signal.
        ts: float array of times
        fregs: float array of frequencies during each interval
        dts = np.diff(ts)
        dps = PI2 * freqs * dts
        phases = np.cumsum(dps)
        phases = np.insert(phases, 0, 0)
        ys = self.amp * np.cos(phases)
        return ys
class ExpoChirp(Chirp):
    """Represents a signal with varying frequency."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        start, end = np.log10(self.start), np.log10(self.end)
        freqs = np.logspace(start, end, len(ts)-1)
        return self. evaluate(ts, freqs)
class SilentSignal(Signal):
    """Represents silence."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        return np.zeros(len(ts))
class Impulses(Signal):
    """Represents silence."""
    def init (self, locations, amps=1):
        <u>self.locations</u> = np.asanyarray(locations)
```

```
self.amps = amps
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ys = np.zeros(len(ts))
        indices = np.searchsorted(ts, self.locations)
        ys[indices] = self.amps
        return ys
class Noise(Signal):
    """Represents a noise signal (abstract parent class)."""
    def init (self, amp=1.0):
       """Initializes a white noise signal.
        amp: float amplitude, 1.0 is nominal max
        self.amp = amp
    @property
    def period(self):
        """Period of the signal in seconds.
        returns: float seconds
        return ValueError('Non-periodic signal.')
class UncorrelatedUniformNoise( Noise):
    """Represents uncorrelated uniform noise."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ys = np.random.uniform(-self.amp, self.amp, len(ts))
        return vs
class UncorrelatedGaussianNoise( Noise):
    """Represents uncorrelated gaussian noise."""
```

```
def evaluate(self, ts):
        """Evaluates the signal at the given times.
        ts: float array of times
        returns: float wave array
        ys = np.random.normal(0, self.amp, len(ts))
        return ys
class BrownianNoise( Noise):
    """Represents Brownian noise, aka red noise."""
    def evaluate(self, ts):
        """Evaluates the signal at the given times.
        Computes Brownian noise by taking the cumulative sum
of
        a uniform random series.
        ts: float array of times
        returns: float wave array
        dys = np.random.uniform(-1, 1, len(ts))
        #ys = scipy.integrate.cumtrapz(dys, ts)
        ys = np.cumsum(dys)
        ys = normalize(unbias(ys), self.amp)
        return ys
class PinkNoise( Noise):
    """Represents Brownian noise, aka red noise."""
          init (self, amp=1.0, beta=1.0):
        """Initializes a pink noise signal.
        amp: float amplitude, 1.0 is nominal max
        11 11 11
        self.amp = amp
        self.beta = beta
    def make wave(self, duration=1, start=0, framerate=11025):
        """Makes a Wave object.
        duration: float seconds
        start: float seconds
        framerate: int frames per second
```

```
returns: Wave
        signal = UncorrelatedUniformNoise()
        wave = signal.make wave(duration, start, framerate)
        spectrum = wave.make spectrum()
        spectrum.pink_filter(beta=self.beta)
        wave2 = spectrum.make wave()
        wave2.unbias()
        wave2.normalize(self.amp)
        return wave2
def rest(duration):
    """Makes a rest of the given duration.
    duration: float seconds
    returns: Wave
    signal = SilentSignal()
    wave = signal.make wave(duration)
    return wave
def make_note(midi_num, duration, sig cons=CosSignal,
framerate=11025):
    """Make a MIDI note with the given duration.
    midi num: int MIDI note number
    duration: float seconds
    sig_cons: Signal constructor function
    framerate: int frames per second
    returns: Wave
    freq = midi to freq(midi num)
    signal = sig_cons(freq)
    wave = signal.make wave(duration, framerate=framerate)
    wave.apodize()
    return wave
def make chord(midi nums, duration, sig cons=CosSignal,
framerate=11025):
    """Make a chord with the given duration.
    midi nums: sequence of int MIDI note numbers
```

```
duration: float seconds
    sig cons: Signal constructor function
    framerate: int frames per second
    returns: Wave
    freqs = [midi_to_freq(num) for num in midi_nums]
    signal = sum(sig cons(freq) for freq in freqs)
    wave = signal.make wave(duration, framerate=framerate)
    wave.apodize()
    return wave
def midi to freq(midi num):
    """Converts MIDI note number to frequency.
    midi num: int MIDI note number
    returns: float frequency in Hz
    x = (midi num - 69) / 12.0
    freq = 44\overline{0}.0 * 2**x
    return freq
def sin wave(freq, duration=1, offset=0):
    """\overline{M}akes a sine wave with the given parameters.
    freq: float cycles per second
    duration: float seconds
    offset: float radians
    returns: Wave
    signal = SinSignal(freq, offset=offset)
    wave = signal.make wave(duration)
    return wave
def cos wave(freq, duration=1, offset=0):
    """Makes a cosine wave with the given parameters.
    freq: float cycles per second
    duration: float seconds
    offset: float radians
    returns: Wave
    signal = CosSignal(freq, offset=offset)
    wave = signal.make wave(duration)
```

return wave def mag(a): """Computes the magnitude of a numpy array. a: numpy array returns: float return np.sqrt(np.dot(a, a)) def zero_pad(array, n): """Extends an array with zeros. array: numpy array n: length of result returns: new NumPy array res = np.zeros(n)res[:len(array)] = array return res def main(): cos basis = cos wave(440)sin_basis = sin_wave(440) wave = $\cos \text{ wave}(440, \text{ offset=math.pi/2})$ cos cov = cos basis.cov(wave)sin_cov = sin_basis.cov(wave) print(cos cov, sin cov, mag((cos cov, sin cov))) return wfile = WavFileWriter() for sig cons in [SinSignal, TriangleSignal, SawtoothSignal, GlottalSignal, ParabolicSignal, SquareSignal]: print(sig_cons) sig = sig cons(440)wave = sig.make wave(1)wave.apodize() wfile.write(wave) wfile.close()

return

```
signal = GlottalSignal(440)
    signal.plot()
    pyplot.show()
    return
    wfile = WavFileWriter()
    for m in range (60, 0, -1):
        wfile.write(make note(m, 0.25))
    wfile.close()
    return
    wave1 = make note(69, 1)
   wave2 = make\_chord([69, 72, 76], 1)
    wave = wave1 | wave2
    wfile = WavFileWriter()
    wfile.write(wave)
    wfile.close()
    return
    sig1 = CosSignal(freg=440)
    sig2 = CosSignal(freg=523.25)
    sig3 = CosSignal(freq=660)
    sig4 = CosSignal(freg=880)
    sig5 = CosSignal(freg=987)
    sig = sig1 + sig2 + sig3 + sig4
    #wave = Wave(sig, duration=0.02)
    #wave.plot()
    wave = sig.make wave(duration=1)
    #wave.normalize()
    wfile = WavFileWriter(wave)
    wfile.write()
    wfile.close()
if __name__ == '__main__':
    main()
--- === ---
"""This file contains code for use with "Think Stats",
by Allen B. Downey, available from greenteapress.com
Copyright 2014 Allen B. Downey
License: GNU GPLv3 http://www.gnu.org/licenses/gpl.html
from future import print function
```

```
import math
import matplotlib
import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
import warnings
# customize some matplotlib attributes
#matplotlib.rc('figure', figsize=(4, 3))
#matplotlib.rc('font', size=14.0)
#matplotlib.rc('axes', labelsize=22.0, titlesize=22.0)
#matplotlib.rc('legend', fontsize=20.0)
#matplotlib.rc('xtick.major', size=6.0)
#matplotlib.rc('xtick.minor', size=3.0)
#matplotlib.rc('ytick.major', size=6.0)
#matplotlib.rc('ytick.minor', size=3.0)
class Brewer(object):
    """Encapsulates a nice sequence of colors.
    Shades of blue that look good in color and can be
distinguished
    in grayscale (up to a point).
    Borrowed from http://colorbrewer2.org/
    color iter = None
    colors = ['#f7fbff', '#deebf7', '#c6dbef',
               '#9ecae1', '#6baed6', '#4292c6', '#2171b5', '#08519c', '#08306b'][::-1]
    # lists that indicate which colors to use depending on
how many are used
    which colors = [[],
                     [1],
                     [1, 3],
                     [0, 2, 4],
                     [0, 2, 4, 6],
                     [0, 2, 3, 5, 6],
                     [0, 2, 3, 4, 5, 6],
                     [0, 1, 2, 3, 4, 5, 6],
                     [0, 1, 2, 3, 4, 5, 6, 7],
                     [0, 1, 2, 3, 4, 5, 6, 7, 8],
```

```
]
    current figure = None
    @classmethod
    def Colors(cls):
        """Returns the list of colors.
        return cls.colors
    @classmethod
    def ColorGenerator(cls, num):
        """Returns an iterator of color strings.
        n: how many colors will be used
        for i in cls.which colors[num]:
            yield cls.colors[i]
        raise StopIteration('Ran out of colors in Brewer.')
    @classmethod
    def InitIter(cls, num):
        """Initializes the color iterator with the given
number of colors."""
        cls.color iter = cls.ColorGenerator(num)
        fig = plt.gcf()
        cls.current figure = fig
    @classmethod
    def ClearIter(cls):
        """Sets the color iterator to None."""
        cls.color iter = None
        cls.current figure = None
    @classmethod
    def GetIter(cls, num):
        """Gets the color iterator."""
        fig = plt.gcf()
        if fig != cls.current figure:
            cls.InitIter(num)
            cls.current figure = fig
        if cls.color iter is None:
            cls.InitIter(num)
        return cls.color iter
def UnderrideColor(options):
    """If color is not in the options, chooses a color.
```

```
11 11 11
    if 'color' in options:
        return options
    # get the current color iterator; if there is none, init
one
    color iter = Brewer.GetIter(5)
    try:
        options['color'] = next(color iter)
    except StopIteration:
        # if you run out of colors, initialize the color
iterator
        # and try again
        warnings.warn('Ran out of colors. Starting over.')
        Brewer.ClearIter()
        UnderrideColor(options)
    return options
def PrePlot(num=None, rows=None, cols=None):
    """Takes hints about what's coming.
    num: number of lines that will be plotted
    rows: number of rows of subplots
    cols: number of columns of subplots
    \Pi \ \Pi \ \Pi
    if num:
        Brewer.InitIter(num)
    if rows is None and cols is None:
        return
    if rows is not None and cols is None:
        cols = 1
    if cols is not None and rows is None:
        rows = 1
    # resize the image, depending on the number of rows and
cols
    size_map = \{(1, 1): (8, 6),
                (1, 2): (12, 6),
                (1, 3): (12, 6),
                (1, 4): (12, 5),
                (1, 5): (12, 4),
                (2, 2): (10, 10),
                 (2, 3): (16, 10),
                 (3, 1): (8, 10),
```

```
(4, 1): (8, 12),
    if (rows, cols) in size map:
        fig = plt.gcf()
        fig.set size inches(*size map[rows, cols])
    # create the first subplot
    if rows > 1 or cols > 1:
        ax = plt.subplot(rows, cols, 1)
        global SUBPLOT ROWS, SUBPLOT COLS
        SUBPLOT ROWS = rows
        SUBPLOT COLS = cols
    else:
        ax = plt.gca()
    return ax
def SubPlot(plot_number, rows=None, cols=None, **options):
    """Configures the number of subplots and changes the
current plot.
    rows: int
    cols: int
    plot number: int
    options: passed to subplot
    rows = rows or SUBPLOT ROWS
    cols = cols or SUBPLOT COLS
    return plt.subplot(rows, cols, plot number, **options)
def _Underride(d, **options):
    """Add key-value pairs to d only if key is not in d.
    If d is None, create a new dictionary.
    d: dictionary
    options: keyword args to add to d
    if d is None:
        d = \{\}
    for key, val in options.items():
        d.setdefault(key, val)
    return d
```

```
def Clf():
    """Clears the figure and any hints that have been set."""
    global LOC
    LOC = None
    Brewer.ClearIter()
    plt.clf()
    fig = plt.gcf()
    fig.set size inches(8, 6)
def Figure(**options):
    """Sets options for the current figure."""
    Underride(options, figsize=(6, 8))
    plt.figure(**options)
def Plot(obj, ys=None, style='', **options):
    """Plots a line.
    Args:
      obj: sequence of x values, or Series, or anything with
Render()
      ys: sequence of y values
      style: style string passed along to plt.plot
      options: keyword args passed to plt.plot
    options = UnderrideColor(options)
    label = getattr(obj, 'label', '_nolegend_')
    options = Underride(options, linewidth=3, alpha=0.7,
label=label)
    xs = obj
    if ys is None:
        if hasattr(obj, 'Render'):
            xs, ys = obj.Render()
        if isinstance(obj, pd.Series):
            ys = obj.values
            xs = obj.index
    if ys is None:
        plt.plot(xs, style, **options)
    else:
        plt.plot(xs, ys, style, **options)
def Vlines(xs, y1, y2, **options):
    """Plots a set of vertical lines.
    Args:
      xs: sequence of x values
```

```
y1: sequence of y values
      y2: sequence of y values
      options: keyword args passed to plt.vlines
    options = _UnderrideColor(options)
    options = Underride(options, linewidth=1, alpha=0.5)
    plt.vlines(xs, y1, y2, **options)
def Hlines(ys, x1, x2, **options):
    """Plots a set of horizontal lines.
    Args:
      ys: sequence of y values
      x1: sequence of x values
      x2: sequence of x values
      options: keyword args passed to plt.vlines
    options = UnderrideColor(options)
    options = Underride(options, linewidth=1, alpha=0.5)
    plt.hlines(ys, x1, x2, **options)
def axvline(x, **options):
    """Plots a vertical line.
    Args:
      x: x location
      options: keyword args passed to plt.axvline
    options = UnderrideColor(options)
    options = _Underride(options, linewidth=1, alpha=0.5)
    plt.axvline(x, **options)
def axhline(y, **options):
    """Plots a horizontal line.
    Args:
      y: y location
      options: keyword args passed to plt.axhline
    options = UnderrideColor(options)
    options = _Underride(options, linewidth=1, alpha=0.5)
    plt.axhline(y, **options)
def tight layout(**options):
    """Adjust subplots to minimize padding and margins.
```

```
options = Underride(options,
                         wspace=0.1, hspace=0.1,
                         left=0, right=1,
                         bottom=0, top=1)
    plt.tight layout()
    plt.subplots adjust(**options)
def FillBetween(xs, y1, y2=None, where=None, **options):
    """Fills the space between two lines.
    Args:
      xs: sequence of x values
      y1: sequence of y values
      v2: sequence of y values
      where: sequence of boolean
      options: keyword args passed to plt.fill between
    options = UnderrideColor(options)
    options = _Underride(options, linewidth=0, alpha=0.5)
    plt.fill between(xs, y1, y2, where, **options)
def Bar(xs, ys, **options):
    """Plots a line.
    Args:
      xs: sequence of x values
      ys: sequence of y values
      options: keyword args passed to plt.bar
    options = _UnderrideColor(options)
    options = Underride(options, linewidth=0, alpha=0.6)
    plt.bar(xs, ys, **options)
def Scatter(xs, ys=None, **options):
    """Makes a scatter plot.
    xs: x values
    ys: y values
    options: options passed to plt.scatter
    options = Underride(options, color='blue', alpha=0.2,
                         s=30, edgecolors='none')
    if ys is None and isinstance(xs, pd.Series):
        ys = xs.values
        xs = xs.index
```

```
plt.scatter(xs, ys, **options)
def HexBin(xs, ys, **options):
    """Makes a scatter plot.
    xs: x values
    ys: y values
    options: options passed to plt.scatter
    options = Underride(options, cmap=matplotlib.cm.Blues)
    plt.hexbin(xs, ys, **options)
def Pdf(pdf, **options):
    """Plots a Pdf, Pmf, or Hist as a line.
    Args:
      pdf: Pdf, Pmf, or Hist object
      options: keyword args passed to plt.plot
    low, high = options.pop('low', None), options.pop('high',
None)
    n = options.pop('n', 101)
    xs, ps = pdf.Render(low=low, high=high, n=n)
    options = Underride(options, label=pdf.label)
    Plot(xs, ps, **options)
def Pdfs(pdfs, **options):
    """Plots a sequence of PDFs.
    Options are passed along for all PDFs. If you want
different
    options for each pdf, make multiple calls to Pdf.
    Args:
      pdfs: sequence of PDF objects
      options: keyword args passed to plt.plot
    for pdf in pdfs:
        Pdf(pdf, **options)
def Hist(hist, **options):
    """Plots a Pmf or Hist with a bar plot.
    The default width of the bars is based on the minimum
difference
    between values in the Hist. If that's too small, you can
```

```
override
    it by providing a width keyword argument, in the same
units
    as the values.
    Args:
      hist: Hist or Pmf object
      options: keyword args passed to plt.bar
    # find the minimum distance between adjacent values
    xs, ys = hist.Render()
    # see if the values support arithmetic
    try:
        xs[0] - xs[0]
    except TypeError:
        # if not, replace values with numbers
        labels = [str(x) for x in xs]
        xs = np.arange(len(xs))
        plt.xticks(xs+0.5, labels)
    if 'width' not in options:
        try:
            options['width'] = 0.9 * np.diff(xs).min()
        except TypeError:
            warnings.warn("Hist: Can't compute bar width
automatically."
                             "Check for non-numeric types in
Hist."
                             "Or try providing width option."
    options = Underride(options, label=hist.label)
    options = _Underride(options, align='center')
    if options['align'] == 'left':
        options['align'] = 'edge'
    elif options['align'] == 'right':
        options['align'] = 'edge'
        options['width'] *= -1
    Bar(xs, ys, **options)
def Hists(hists, **options):
    """Plots two histograms as interleaved bar plots.
    Options are passed along for all PMFs. If you want
different
    options for each pmf, make multiple calls to Pmf.
```

```
Args:
      hists: list of two Hist or Pmf objects
      options: keyword args passed to plt.plot
    for hist in hists:
        Hist(hist, **options)
def Pmf(pmf, **options):
    """Plots a Pmf or Hist as a line.
    Args:
      pmf: Hist or Pmf object
      options: keyword args passed to plt.plot
    xs, ys = pmf.Render()
    low, high = min(xs), max(xs)
    width = options.pop('width', None)
    if width is None:
        try:
            width = np.diff(xs).min()
        except TypeError:
            warnings.warn("Pmf: Can't compute bar width
automatically."
                          "Check for non-numeric types in
Pmf."
                          "Or try providing width option.")
    points = []
    lastx = np.nan
    lasty = 0
    for x, y in zip(xs, ys):
        if (x - lastx) > 1e-5:
            points.append((lastx, 0))
            points.append((x, 0))
        points.append((x, lasty))
        points.append((x, y))
        points.append((x+width, y))
        lastx = x + width
        lasty = y
    points.append((lastx, 0))
    pxs, pys = zip(*points)
    align = options.pop('align', 'center')
    if align == 'center':
        pxs = np.array(pxs) - width/2.0
    if align == 'right':
```

```
pxs = np.array(pxs) - width
    options = Underride(options, label=pmf.label)
    Plot(pxs, pys, **options)
def Pmfs(pmfs, **options):
    """Plots a sequence of PMFs.
    Options are passed along for all PMFs. If you want
different
    options for each pmf, make multiple calls to Pmf.
    Args:
      pmfs: sequence of PMF objects
      options: keyword args passed to plt.plot
    for pmf in pmfs:
        Pmf(pmf, **options)
def Diff(t):
    """Compute the differences between adjacent elements in a
sequence.
    Args:
        t: sequence of number
    Returns:
        sequence of differences (length one less than t)
    diffs = [t[i+1] - t[i] for i in range(len(t)-1)]
    return diffs
def Cdf(cdf, complement=False, transform=None, **options):
    """Plots a CDF as a line.
    Args:
      cdf: Cdf object
      complement: boolean, whether to plot the complementary
CDF
      transform: string, one of 'exponential', 'pareto',
'weibull', 'gumbel'
      options: keyword args passed to plt.plot
    Returns:
      dictionary with the scale options that should be passed
to
      Config, Show or Save.
```

```
11 11 11
    xs, ps = cdf.Render()
    xs = np.asarray(xs)
    ps = np.asarray(ps)
    scale = dict(xscale='linear', yscale='linear')
    for s in ['xscale', 'yscale']:
        if s in options:
            scale[s] = options.pop(s)
    if transform == 'exponential':
        complement = True
        scale['yscale'] = 'log'
    if transform == 'pareto':
        complement = True
        scale['yscale'] = 'log'
        scale['xscale'] = 'log'
    if complement:
        ps = [1.0-p for p in ps]
    if transform == 'weibull':
        xs = np.delete(xs, -1)
        ps = np.delete(ps, -1)
        ps = [-math.log(1.0-p) for p in ps]
        scale['xscale'] = 'log'
        scale['yscale'] = 'log'
    if transform == 'gumbel':
        xs = np.delete(xs, 0)
        ps = np.delete(ps, 0)
        ps = [-math.log(p) for p in ps]
        scale['yscale'] = 'log'
    options = _Underride(options, label=cdf.label)
    Plot(xs, ps, **options)
    return scale
def Cdfs(cdfs, complement=False, transform=None, **options):
    """Plots a sequence of CDFs.
    cdfs: sequence of CDF objects
    complement: boolean, whether to plot the complementary CDF
    transform: string, one of 'exponential', 'pareto',
'weibull', 'gumbel'
    options: keyword args passed to plt.plot
```

```
for cdf in cdfs:
        Cdf(cdf, complement, transform, **options)
def Contour(obj, pcolor=False, contour=True, imshow=False,
**options):
    """Makes a contour plot.
    d: map from (x, y) to z, or object that provides GetDict
    pcolor: boolean, whether to make a pseudocolor plot
    contour: boolean, whether to make a contour plot
    imshow: boolean, whether to use plt.imshow
    options: keyword args passed to plt.pcolor and/or
plt.contour
    try:
        d = obj.GetDict()
    except AttributeError:
        d = obj
    Underride(options, linewidth=3, cmap=matplotlib.cm.Blues)
    xs, ys = zip(*d.keys())
    xs = sorted(set(xs))
    ys = sorted(set(ys))
    X, Y = np.meshgrid(xs, ys)
    func = lambda x, y: d.get((x, y), 0)
    func = np.vectorize(func)
    Z = func(X, Y)
    x formatter =
matplotlib.ticker.ScalarFormatter(useOffset=False)
    axes = plt.gca()
    axes.xaxis.set major formatter(x formatter)
    if pcolor:
        plt.pcolormesh(X, Y, Z, **options)
    if contour:
        cs = plt.contour(X, Y, Z, **options)
        plt.clabel(cs, inline=1, fontsize=10)
    if imshow:
        extent = xs[0], xs[-1], ys[0], ys[-1]
        plt.imshow(Z, extent=extent, **options)
def Pcolor(xs, ys, zs, pcolor=True, contour=False, **options):
    """Makes a pseudocolor plot.
```

```
ys:
    zs:
    pcolor: boolean, whether to make a pseudocolor plot
    contour: boolean, whether to make a contour plot
    options: keyword args passed to plt.pcolor and/or
plt.contour
    Underride(options, linewidth=3, cmap=matplotlib.cm.Blues)
    X, Y = np.meshgrid(xs, ys)
    Z = zs
    x formatter =
matplotlib.ticker.ScalarFormatter(useOffset=False)
    axes = plt.gca()
    axes.xaxis.set major formatter(x formatter)
    if pcolor:
        plt.pcolormesh(X, Y, Z, **options)
    if contour:
        cs = plt.contour(X, Y, Z, **options)
        plt.clabel(cs, inline=1, fontsize=10)
def Text(x, y, s, **options):
    """Puts text in a figure.
    x: number
    y: number
    s: string
    options: keyword args passed to plt.text
    options = Underride(options,
                         fontsize=16,
                         verticalalignment='top',
                         horizontalalignment='left')
    plt.text(x, y, s, **options)
LEGEND = True
LOC = None
def Config(**options):
    """Configures the plot.
    Pulls options out of the option dictionary and passes
them to
    the corresponding plt functions.
```

```
names = ['title', 'xlabel', 'ylabel', 'xscale', 'yscale',
             'xticks', 'yticks', 'axis', 'xlim', 'ylim']
    for name in names:
        if name in options:
            getattr(plt, name)(options[name])
    global LEGEND
    LEGEND = options.get('legend', LEGEND)
    # see if there are any elements with labels;
    # if not, don't draw a legend
    ax = plt.gca()
    handles, labels = ax.get legend handles labels()
    if LEGEND and len(labels) > 0:
        global LOC
        LOC = options.get('loc', LOC)
        frameon = options.get('frameon', True)
            plt.legend(loc=LOC, frameon=frameon)
        except UserWarning:
            pass
    # x and y ticklabels can be made invisible
    val = options.get('xticklabels', None)
    if val is not None:
        if val == 'invisible':
            ax = plt.gca()
            labels = ax.get_xticklabels()
            plt.setp(labels, visible=False)
    val = options.get('yticklabels', None)
    if val is not None:
        if val == 'invisible':
            ax = plt.gca()
            labels = ax.get_yticklabels()
            plt.setp(labels, visible=False)
def set font size(title size=16, label size=16,
ticklabel size=14, legend size=14):
    """Set font sizes for the title, labels, ticklabels, and
legend.
    def set text size(texts, size):
        for text in texts:
            text.set size(size)
    ax = plt.qca()
```

```
# TODO: Make this function more robust if any of these
elements
   # is missing.
    # title
    ax.title.set size(title size)
    # x axis
    ax.xaxis.label.set size(label size)
    set text size(ax.xaxis.get ticklabels(), ticklabel size)
    # y axis
    ax.yaxis.label.set size(label size)
    set text size(ax.yaxis.get ticklabels(), ticklabel size)
    # legend
    legend = ax.get legend()
    if legend is not None:
        set text size(legend.texts, legend size)
def bigger_text():
    sizes = dict(title size=16, label size=16,
ticklabel size=14, legend size=14)
    set font size(**sizes)
def Show(**options):
    """Shows the plot.
    For options, see Config.
    options: keyword args used to invoke various plt functions
    clf = options.pop('clf', True)
    Config(**options)
    plt.show()
    if clf:
        Clf()
def Plotly(**options):
    """Shows the plot.
    For options, see Config.
    options: keyword args used to invoke various plt functions
    clf = options.pop('clf', True)
```

```
Config(**options)
    import plotly.plotly as plotly
    url = plotly.plot mpl(plt.gcf())
    if clf:
        Clf()
    return url
def Save(root=None, formats=None, **options):
    """Saves the plot in the given formats and clears the
figure.
    For options, see Config.
    Note: With a capital S, this is the original save,
maintained for
    compatibility. New code should use save(), which works
better
    with my newer code, especially in Jupyter notebooks.
    Args:
      root: string filename root
      formats: list of string formats
      options: keyword args used to invoke various plt
functions
    clf = options.pop('clf', True)
    save options = {}
    for option in ['bbox_inches', 'pad_inches']:
        if option in options:
            save options[option] = options.pop(option)
    # TODO: falling Config inside Save was probably a
mistake, but removing
    # it will require some work
    Config(**options)
    if formats is None:
        formats = ['pdf', 'png']
    try:
        formats.remove('plotly')
        Plotly(clf=False)
    except ValueError:
        pass
    if root:
        for fmt in formats:
            SaveFormat(root, fmt, **save options)
```

```
if clf:
        Clf()
def save(root, formats=None, **options):
    """Saves the plot in the given formats and clears the
figure.
    For options, see plt.savefig.
    Args:
      root: string filename root
      formats: list of string formats
      options: keyword args passed to plt.savefig
    if formats is None:
        formats = ['pdf', 'png']
    try:
        formats.remove('plotly')
        Plotly(clf=False)
    except ValueError:
        pass
    for fmt in formats:
        SaveFormat(root, fmt, **options)
def SaveFormat(root, fmt='eps', **options):
    """Writes the current figure to a file in the given
format.
    Args:
      root: string filename root
      fmt: string format
    _Underride(options, dpi=300)
    filename = '%s.%s' % (root, fmt)
    print('Writing', filename)
    plt.savefig(filename, format=fmt, **options)
# provide aliases for calling functions with lower-case names
preplot = PrePlot
subplot = SubPlot
clf = Clf
figure = Figure
plot = Plot
vlines = Vlines
hlines = Hlines
```

```
fill between = FillBetween
text = Text
scatter = Scatter
pmf = Pmf
pmfs = Pmfs
hist = Hist
hists = Hists
diff = Diff
cdf = Cdf
cdfs = Cdfs
contour = Contour
pcolor = Pcolor
config = Config
show = Show
def main():
    color_iter = _Brewer.ColorGenerator(7)
for color in color_iter:
         print(color)
if __name__ == '__main__':
    main()
```