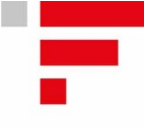


# t-SNE (t-Distributed Stochastic Neighbor Embedding)

Short Introduction, Tobias Rippel

Data Science Meet-Up Münster, 06.07.2017



# t-SNE (t-Distributed Stochastic Neighbor Embedding)

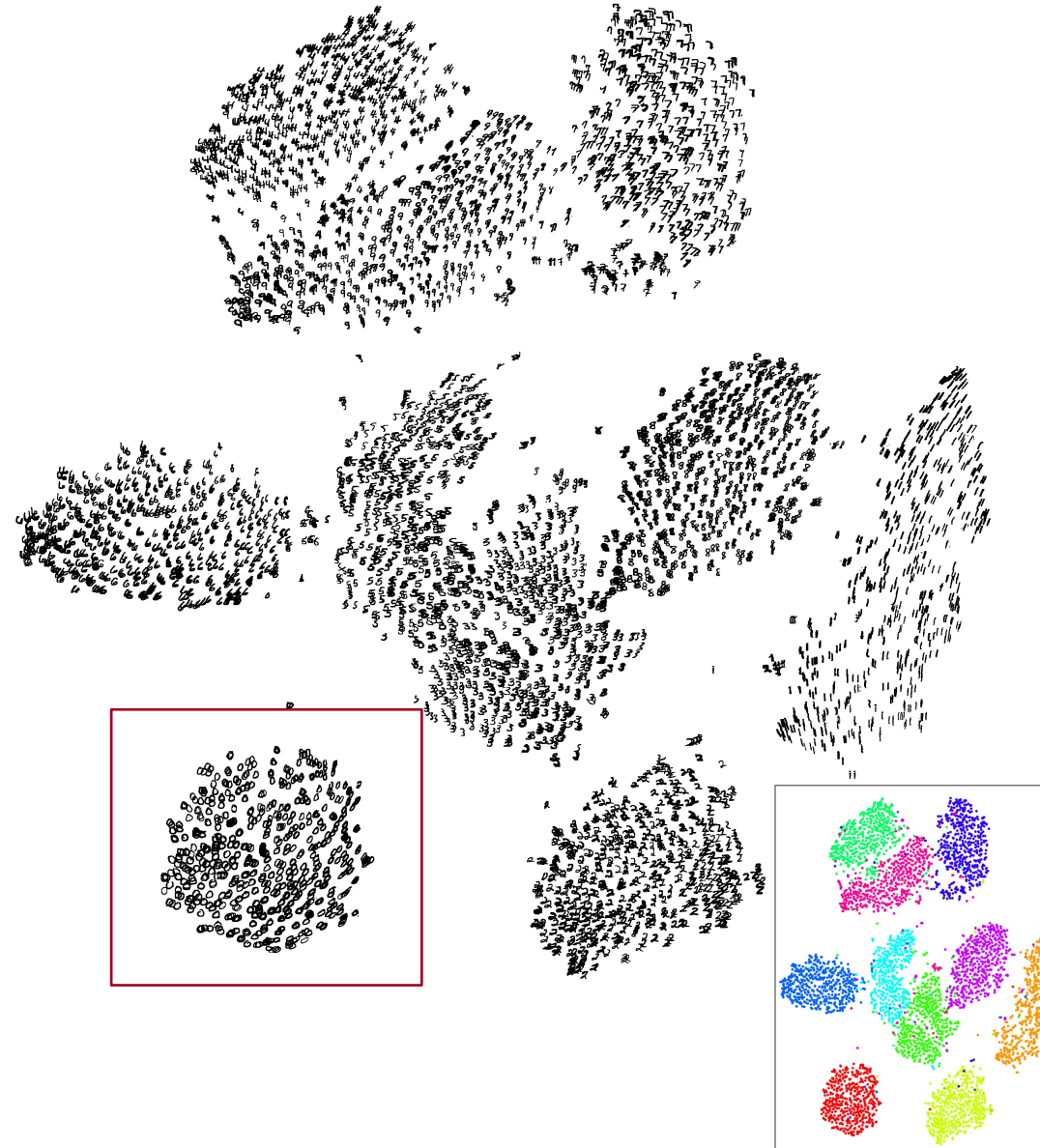
## Overview

- What is t-SNE?
  - Unsupervised learning technique
  - Dimensionality reduction (mostly into 2 dimensional space)
  - Visualizing multidimensional/ high-dimensional data

# t-SNE (t-Distributed Stochastic Neighbor Embedding)



## MNIST Example

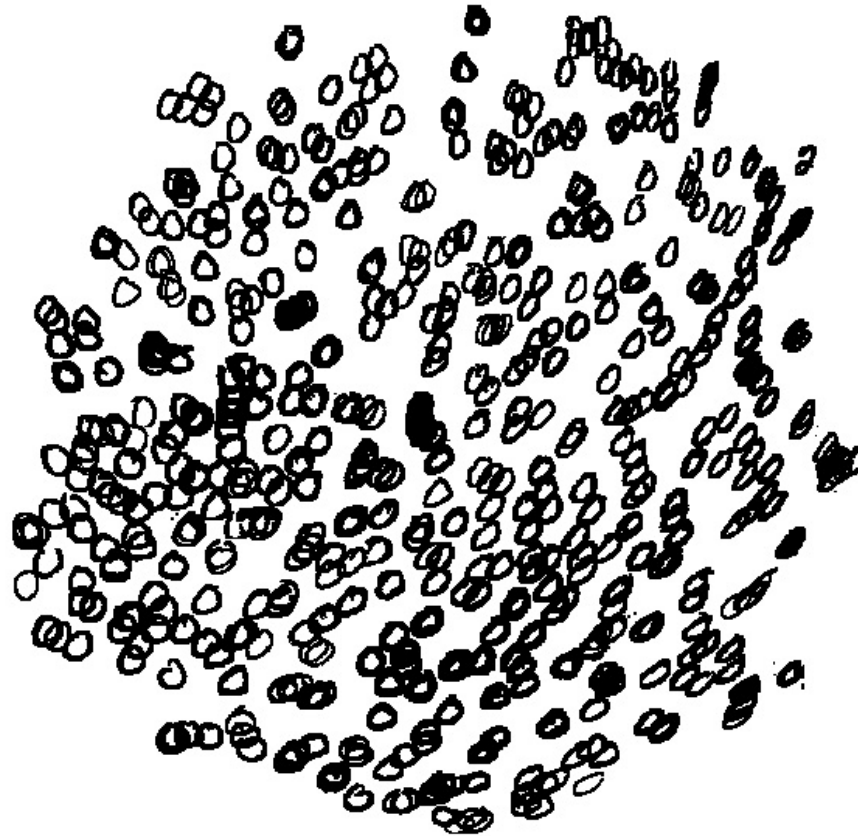


Source: <https://lvdmaaten.github.io/tsne/>

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MNIST Example



Source: <https://lvdmaaten.github.io/tsne/>

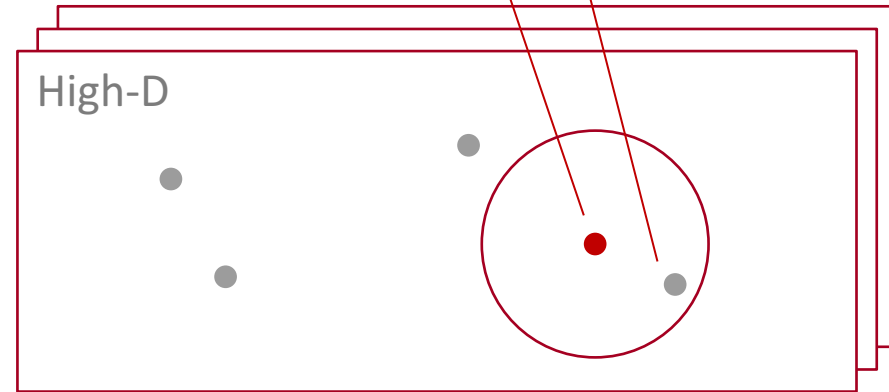


# t-SNE (t-Distributed Stochastic Neighbor Embedding)

## Algorithm Introduction

- Goal: **Minimizing the discrepancy** between **similarities in the original data** and **similarities in the map**

- Similarity in the original data:  $p_{ij} = \frac{\exp(-\|x_i - x_j\|^2 / 2\sigma^2)}{\sum_k \sum_{l \neq k} \exp(-\|x_k - x_l\|^2 / 2\sigma^2)}$





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- Similarity in the map:  $q_{ij} = \frac{(1 + \|y_i - y_j\|^2)^{-1}}{\sum_k \sum_{l \neq k} (1 + \|y_k - y_l\|^2)^{-1}}$  ← t-distribution

- Objective Function: Kullback-Leibler divergence  $KL(P \| Q) = \sum_i \sum_{j \neq i} p_{ij} * \log \left( \frac{p_{ij}}{q_{ij}} \right)$



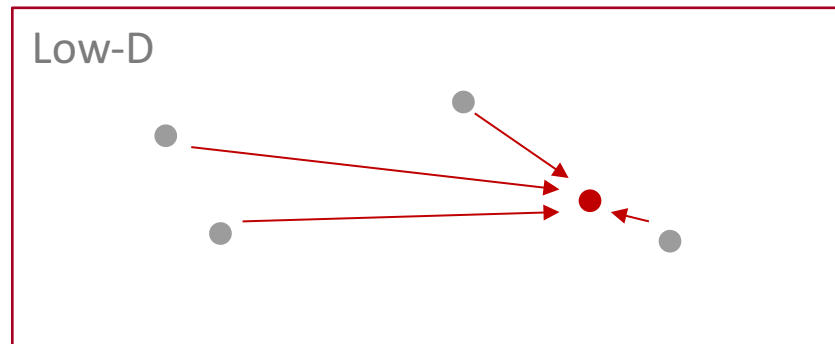
# t-SNE (t-Distributed Stochastic Neighbor Embedding)

## Algorithm Introduction

### ■ The embedding/training process

1. Initially calculate the similarity in the original data ( $p_{ij}$ )
2. Create a random generated initial mapping
3. Loop x times
  - a. Calculate the similarity in the mapping ( $q_{ij}$ )
  - b. Calculate the t-SNE gradient from the Kullback-Leibler divergence objective function
  - c. Update the map according to the gradient of each point

$$\frac{\partial \mathcal{C}}{\partial \mathbf{y}_i} = 4 \sum_{j \neq i} \underbrace{(p_{ij} - q_{ij}) \left(1 + \|\mathbf{y}_i - \mathbf{y}_j\|^2\right)^{-1}}_{\text{excertion/compression}} (\mathbf{y}_i - \mathbf{y}_j)$$



# t-SNE: MNIST Example



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Source: <https://github.com/oreillymedia/t-SNE-tutorial/blob/master/images/animation.gif>



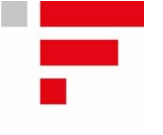
# t-SNE: Summary



- t-SNE is an unsupervised learning technique
- Used for dimensionality reduction -> visualize the data (can then be used e.g. in data exploring or to check if feature engineering is representing the expected properties of the data well)
- t-SNE preserves global + local structure of the data

Try it out yourself! Available in many Data Science languages + tools

# Tutorials + Sources



- Google Talk (~45 min) by Laurens van der Maaten:

<https://www.youtube.com/watch?v=RJVL80Gg3IA&list=UUtXKDgv1AVoG88PLl8nGXmw>

<https://www.analyticsvidhya.com/blog/2017/01/t-sne-implementation-r-python/>

<http://distill.pub/2016/misread-tsne/#perplexity=32&epsilon=4&demo=1&demoParams=100,2>

<https://github.com/oreillymedia/t-SNE-tutorial>