# Report

July 20, 2021

- 1 Report of Project 05: Implementation and Evaluation of Machine Learning (Support Vector Machine) Segmentation
- 1.1 Data analysis project B.Sc. Molecular Biotechnology Heidelberg University
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## 2 Abstract

Support Vector Machines, also known as SVMs, are supervised learning models with associated learning algorithms that analyze data for classification and regression analysis. One of their many uses is in nuclei segmentation for cell counting and cancer grading. This report describes an algorithm designed around an SVM, which was developed using three sets of microscopic images. Pursuing the overall goal to implement and evaluate an SVM for cell nuclei segmentation, the algorithm contains four pre-processing methods: Gaussian filtering, Otsu thresholding, Watershed and Principal Component Analysis (PCA). The SVM uses both the original images and synthetically generated cell images in its training phase. It is furtherly tested with a validation set. To evaluate the algorithms' performance the Dice Score was used. We found that using all pre-processing methods produced the best segmentation results throughout all datasets. For N2DH-GOWT1 the best dice score is 0,79, when pre-processed with Gauss and Otsu. For N2DL-HeLa the best dice score is 0.63, which we achieved by applying all filters. For NIH3T3 the best dice score is 0.86, when pre-processed with PCA.

# 3 Table of contents

1. Introduction 2. The Dataset 3. The algorithm's pipeline 4. Pre-processing 4.1 Gaussian filter 4.2 Watershed 4.3 Otsu thresholding 4.4 Principle Component Analysis 5. Data reduction 5.2 Tiles 6. Synthetic Images 6.1 Definition and Goal 6.2 Image composition 6.3 Domain randomization 7. Support Vector Machine 7.1 The Mathematical Background 7.2 The loss function 7.3 Stochastic gradient decent to minimize the loss gradient 7.4 K-Fold Cross validation 8. Evaluation using the Dice coefficient 8.1 The Theory behind the Dice Coefficient 8.2 Unittesting the Dice Coefficient 9. Results 10. Discussion 11. Bibliography

# 4 List of abbreviations

Abbreviation	Full name
$\overline{\mathrm{CD}}$	cluster of differentiation
CV	K-Fold Cross validation
FN	false negative
FP	false positive
GFP	Green fluorescent protein
ML	machine learning
PCA	Principle Component Analysis
PC	Principle Component
$\operatorname{SGD}$	Stochastic Gradient Descent
SVM	Support Vector Machine
TP	True positive

## 5 1. Introduction

Image segmentation is a process, during which important features of a picture are extracted, to aid analysis and retrieval of information. This is done by assigning labels to all pixels of the image. Pixels sharing defined traits, are assigned the same label. (Khan and Ravi, 2013) Nuclei segmentation is a subform of image segmentation. Its goal is to automatically separate nuclei from their background. This allows machine counting of nuclei and cells (Schüffler et al., 2013).

During laboratory work, manual cell counting of microscopic images is a cumbersome and errorprone process. However, since the number of cells contains important information, counting remains indispensable. Automatic cell counting via nuclei segmentation is therefore used to accelerate and improve the overall procedure. (Schüffler et al., 2013)

In addition to its use in biological laboratories, nuclei segmentation also advances cancer grading in medical practice. Cancer grading describes the process of classifying and grading a cancer based on cancer histopathology. It is an essential step in quantifying the degree of malignancy and thus key to predict patient prognosis and prescribe a treatment. Currently, cancer grading is still often done manually via visual analysis of tissue samples. This method is somewhat problematic given its inter- and intra-observer variability regarding the gradings quality, its low reproducibility as well as the disproportionate time needed for completion. (Veta et al., 2013; Schüffler et al., 2013)

Using an SVM, is an auspicious way to accomplish nuclei segmentation (Schüffler et al., 2013). We use the SVM to differentiate between foreground and background pixels. Foreground pixels are subsequently labeled as nuclei and displayed white. Background pixels are colored black.

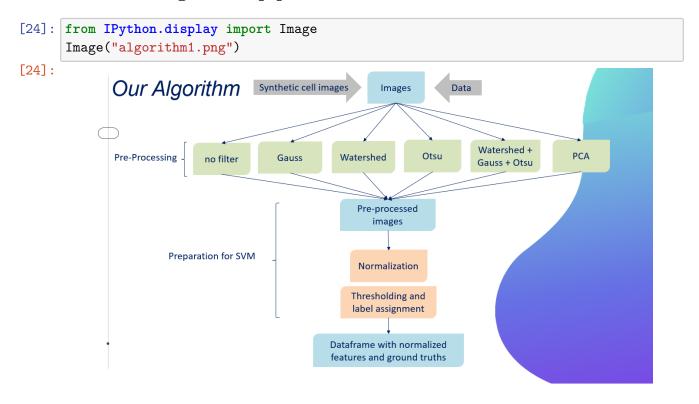
The images require pre-processing to enhance the picture quality, a crucial prerequisite for an effective image segmentation via SVM. To evaluate the segmentation quality, the Dice Coefficient is used.

## 6 2. The Dataset

The data consist of three datasets with a total of 28 images, all showing nuclei. The pictures of the first dataset show GFP-transfected GOWT1 mouse embryonic stem cells. The second set of

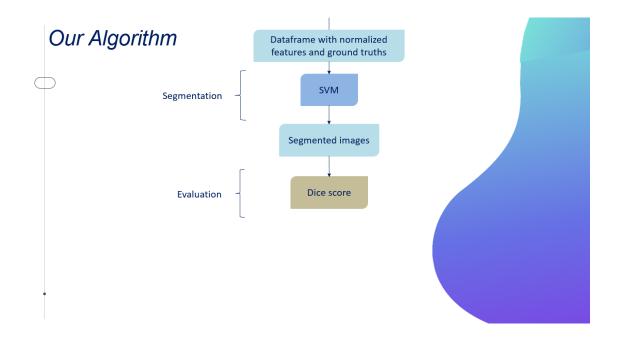
images display Histone-2B-GFP expressing HeLa cells, while our third set consists of pictures of mouse embryonic fibroblasts, in which CD-antigens were tagged with enhanced-GFP. All images are microscopic images of nuclei, however the three sets vary greatly in other features with additional challenges for our image analysis. • different formats (1024 x 1024, 1100 x 700, 1344 x 1024), • acquired differently • different numbers of nuclei, within a range of 15-65 nuclei per image. • different brightness and resolution • white flashes, clustering of nuclei or nuclei leaving the image or undergoing mitosis.

# 7 3. The algorithm pipeline



```
[25]: from IPython.display import Image
Image("algorithm2.png")
```

[25]:



# 8 4. Pre-processing

We implemented two different pre-processing methods in our SVM algorithm in order to improve the raw images quality and consequently achieve better segmentation results.

#### 8.1 4.1 Gaussian filter

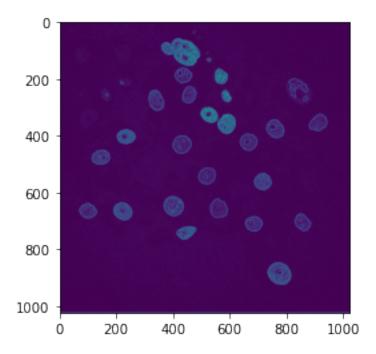
As our first pre-processing method, we used a Gaussian filter. This technique was shown to be particularly useful for the filtering of noisy pictures. This is the case, since the results of the filtering show a relative independence on the variance value of the Gaussian kernel (Gedraite, E. et al. 2011). It might turn out to be problematic that the use of Gaussian filters can give rise to edge position displacement, edges vanishing, and phantom edges (Deng, G. et al. 1993).

#### 8.2 4.2 Watershed

As our second pre-processing method, we used Watershed, a gradient-ascend-based super pixel algorithm that has its origins in mathematical morphology. In watershed segmentation an image is regarded as a topographic landscape with ridges and valleys. The elevation values of the landscape are typically defined by the gray values of the respective pixels or their gradient magnitude.

To make Watershed easier to understand, one can think of an image as a surface. The bright pixels represent mountain tops, while the dark pixels symbolize valleys. The surface is punctured in some valleys and then slowly submerged into a water bath. As the water pours into each puncture, it starts to fill the valleys. However, the water from different punctures should not mix. Therefore, dams need to be built where different waters first touch. These dams at the boundaries of the water basins are equivalent to the boundaries of image objects. The output image of a watershed algorithm thus is the original image, in which every object is encircled.

```
[1]: from SVM_Segmentation.preprocessing.watershed import watershed
import matplotlib.pyplot as plt
ws = watershed("Data/N2DH-GOWT1/img/t52.tif")
plt.imshow(ws)
plt.show()
```



#### 8.3 4.3 Otsu thresholding

Additionally we used the Otsu-treshold method, which is supposed to find the optimal treshold, to segment an image (Otsu N., 1979). The tresholded images are then used as an additional feature for the segmentation with the SVM-algorithm. For this purpose we cooperated with team 03 and used their algorithm to implement this method, to analyze whether the SVM overall improves segmentation.

## 8.4 4.4 Principal Component Analysis

Principal component analysis simplifies the complexity of high-dimensional data by geometrically projecting them onto lower dimensions called principal components (PCs) while preserving as much of the data's variation as possible (Lever, 2017). These principal components are eigenvectors of the data's covariance matrix and often computed by eigendecomposition of the data covariance matrix. (Hedge, A. 2006)

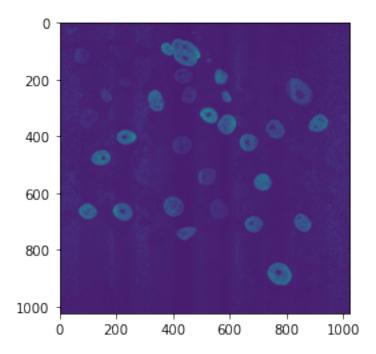
PCA essentially rotates the set of points around their mean in order to align them with the principal components. This moves as much of the variance as possible into the first few dimensions. The values in the remaining dimensions, therefore, tend to be small and may be dropped with minimal loss of information. (Jolliffe, I. 2016)

We perform the PCA as part of our pre-processing. By retaining a selected number of PCs that together explain 95% of the variance of the image, we aim to reduce noise and increase contrast of the original image. Therewith we hope to improve the quality of the SVMs segmentation.

After selecting the PCs, the image is uptransformed to its initial size.

Because SVM is an algorithm that requires its features to be normalized, the PCA is performed with StandardScaler applied. This function scales the features to have zero as the mean and a standard deviation of 1, to give it the feel and the properties of a standard normal distribution. As a positive side effect this also refines the SVMs prediction accuracy.

```
[3]: from SVM_Segmentation.preprocessing.pca import convert_pca
from skimage import io
import matplotlib.pyplot as plt
image_read1 = io.imread('Data/N2DH-GOWT1/img/t52.tif')
pca1 = convert_pca(image_read1, 0.9)
plt.imshow(pca1)
plt.show()
```



# 9 5. Data Reduction

As the images in our dataset consist of more than one million pixels each, running the SVM would take a lot of computational power and runtime. To decrease both, data reduction should be performed beforehand. The two possibilities we thought of, are resize form skimage and cutting the image into tiles before averaging over each tile.

Resize from skimage cuts the image into a pre-defined scaling factor. We cut all images to 250 x

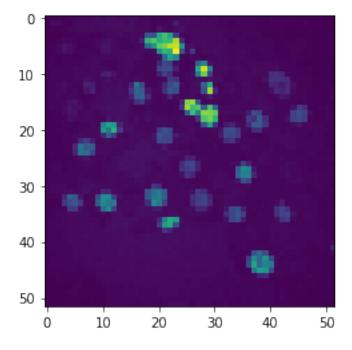
250.

#### 9.1 5.1 Tiles

While PCA reduces data specifically, tiles-rendering is a simple approach that reduces data unspecifically by exploiting the fundamental properties of a problem space. The concept behind tiles is to save computational power, by splitting the image into multiple sets of N x N tiles and then calculate the average of each tile. The average intensity value of a specific tile is assigned to all pixels, belonging to this tile. Lastly, all tiles are reassembled to form the resulting image. (Rastar, A. 2019)

As our tiles algorithm reduced the images quality in large measure, we decided to not use it as part of our algorithm.

```
[28]: from SVM_Segmentation.preprocessing.tiles import tiles
from SVM_Segmentation.pixel_conversion import one_d_array_to_two_d_array
from skimage import io
image = io.imread('Data/N2DH-GOWT1/img/t52.tif')
tiled = tiles(image, 50)
tiled = one_d_array_to_two_d_array(tiled)
plt.imshow(tiled)
plt.show()
```



# 10 6. Synthetic Images

#### 10.1 6.1 Definition and Goal

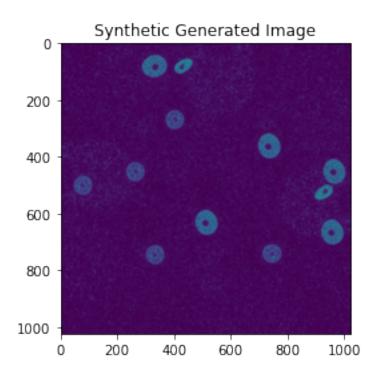
The basic idea behind creating synthetic images is to use algorithms and already available images to generate new images (Dunn et al., 2019). Our first objective was to simply use these new images to test our code for the dice score. But while researching on this topic, we realized that synthetic images have an immense potential, especially for the training phase of a machine learning algorithm. This is particularly useful as our data encompasses only 28 images, which leads to a training data set of 27 images at max. By expanding our training set with diverse images of good quality, we expect a more accurate model (Mayer et al., 2017). There are various methods for the generation of synthetic images (Ward et al., 2019). Because of the scope of our project and the kind of images we wanted to produce, we focused on image composition and domain randomization.

# 10.2 6.2 Image composition

To produce synthetic masks, a white circle is drawn on top of a black background. While the background stays the same across all images, the circle size and position gets modified. Our algorithm iterates through the random position and scaling generator. This produces random, black-and-white only images. These masks are used to test our Dice Score.

## 10.3 6.3 Domain randomization

In order to create synthetic microscopic cell images, we used a method called domain randomization. It requires collecting various foreground images, either by separating the images from their backgrounds or by using images in .png format. These foreground images are then pasted onto different backgrounds. (Tripathi, 2019) To obtain more variety among the resulting synthetic images, the foreground images can be modified using different contrasts, zooms or rotations (Ward et al., 2019; Alghonaim and Johns, 2020). For this project, we used domain randomization to generate a new set of images with cells cut from one image from our different data sets. After rotating and scaling the cells from that image, they were pasted at random positions onto a background, which had also been cut and scaled from the chosen image. These new synthetic masks were used further on to enlarge and enrich our training data set. We took into consideration that the image from which the synthetic images were created cannot be used as part of the test set of our SVM; because it would be a data leakage, so we trained our SVM with the synthetic images but tested it with the remaining images from the original dataset.



# 11 7. Support Vector Machine

In 1992, Vapnik and coworkers proposed a supervised algorithm, developed from statistical learning, to solve classification problems (Vapnik et al., 1992). Since then, their machine learning method evolved into what is now known as SVM: a class of algorithms for classification, regression and other applications that represents the current state of the art in the field (Suthaharan, 2016; Guanasekaran, 2010; Christianini and Ricci, 2008).

By providing a training data set with binary labels, the SVM is able to learn how to classify data points using certain features. This capability can subsequently be used to classify new data, called test data, using its features (Thai et al., 2012). SVMs have been successfully applied to several applications, ranging from time series prediction and face recognition to biological data processing for medical diagnosis (Evgeniou, 2001). In image processing, SVMs are used for one of the classical challenges: image classification (Evgeniou, 2001).

## 11.1 7.1 The Mathematical Background

The mathematical concepts are key to understand how SVMs work. The goal of an SVM is, to separate data points into two groups of provided labels with an optimal hyperplane. This hyperplane is described by

(2) 
$$w x + b = 0$$
 (1)

and fulfilling the following condition

(3) 
$$h = \begin{cases} +1 & if \ w \ x_i + b + 1 - \varepsilon_i \\ -1 & if \ w \ x_i + b < -1 - \varepsilon_i \end{cases} \quad \varepsilon \ge 0 \ \forall_i \ ; \ i = 1...m$$
 (2)

whilst for two dimensions w = (a, -1), whereas a is the slope of the line, and  $x = (x_1, x_2)$  and represents a data point.  $\varepsilon$  is a variable, standing for the inaccuracy of the hyperplane. It is added to the constraint to prevent overfitting of the model onto the training set. Without  $\varepsilon$  the geometric margin M is called a hard margin, as it does not allow data points of one group to be incorrectly labeled as members of the other group. This does not result in the best model, as single incorrectly assigned data points, can have a lower impact on the quality of the model, than a suboptimal hyperplane. Therefore,  $\varepsilon$  is introduced and thereupon M is called a soft margin.

To choose the optimal hyperplane we need to minimize the margin as follows.

(4) 
$$M = \min_{i=1...m} y_i \left( \frac{w}{||w||} x + \frac{b}{||w||} \right)$$
 (3)

The largest margin M out of all margins computed in our training phase, will be selected. The variables w and b are divided by the length of the vector w calculated with the Euclidean norm formula, as they need to be scale invariant. The aim is, to find the values for w and b, corresponding to the largest margin.

This leads us to the following optimization problem. We want to maximize M:

(5) 
$$\max_{w,h,\varepsilon} M$$
 (4)

This maximization problem is equivalent to

(6) 
$$\max_{w,b,\varepsilon} \frac{1}{||w||} + \sum_{i=1}^{m} \varepsilon_i$$
 (5)

and can be rewritten as the following minimalization problem.

(7) 
$$min_{w,b,\varepsilon} \frac{1}{2}||w||^2 + C\sum_{i=1}^m \varepsilon_i subject \ to \ y_i(w \ x_i + b) \ 1 - \varepsilon_i \ , \varepsilon \ge 0 \ \forall_i \ , \ i = 1...m$$
 (6)

The regularization parameter C is chosen by the user and determines the weight of  $\varepsilon$ . A larger C leads to a higher penalty for errors and therefore to a harder margin.

In order to solve this constrained optimization problem, in which we want to maximize the margin while fulfilling our conditions or constraints, Lagrange multipliers are used. The idea behind this mathematical concept is that at the optimum, the gradient of our objective function is parallel or antiparallel to the gradient of the constraint function. Therefore, both have to be equal or a multiple of each other, which is what the Lagrange multiplier is showcasing.

(8) 
$$\nabla f(x) - \alpha \nabla g(x) = 0$$
 (7)

When we insert our functions, we get the following Lagrangian function:

$$(9) f(x) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i (10) g(x) = y_i(w \ x_i + b) - 1 + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \varepsilon_i - \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i + b) - 1] + \varepsilon_i (11) \mathcal{L}(w, b, \alpha) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^{m} \alpha_i [y_i(w \ x_i +$$

In order to solve this Lagrange problem, it is relaxed into a dual problem: The constraints are incorporated into the function, resulting in it only depending on the Lagrange multipliers. This facilitates the solving. Below, the two constraints for the dual problem are described:

$$(12) \nabla_w \mathcal{L}(w, b, \alpha) = w - \sum_{i=1}^m \alpha_i y_i x_i = 0$$

$$(13) \nabla_b \mathcal{L}(w, b, \alpha) = -\sum_{i=1}^m \alpha_i y_i = 0$$

$$(9)$$

If they are inserted into the Lagrange function, the result of the dual problem is the following:

(14) 
$$\max_{\alpha} \sum_{i=1}^{m} \alpha_i - \frac{1}{2} \sum_{i=1}^{m} \sum_{j=1}^{m} \alpha_i \alpha_j y_i y_j x_i \cdot x_j subject \ to \ 0 \ \alpha_i \ C, i = 1...m, \sum_{i=1}^{m} \alpha_i y_i = 0$$
 (10)

From the above equation, it becomes clear that the maximization depends solely on the dot product of the support vectors  $x_i \cdot x_j$ . This is an advantage when dealing with data that is not linearly separable. The 'trick' is to transform the data into a higher dimension, in which a separating hyperplane can be found. However, for a large dataset, calculating the transformation would be a very time-consuming operation. For that reason, instead of actually calculating the transformation, the Kernel trick is used. This means a function is used, which calculates the dot product of  $x_i \cdot x_j$  as if the two were in a higher dimension.

(Burges, 1998)

Whenever this transformation is needed because data that is not linearly separable, non-linear kernels like the Gaussian radial basis function (RBF) are used. For linearly separable data, mapping the data points into a higher dimensional space is not needed and therefore a linear kernel is sufficient. (Hsu, 2016) The linear kernel function can be described as follows:

$$(15) K(x_i, x_j) = \phi(x_i) \cdot phi(x_j)$$

$$(11)$$

So it only describes the vector product. Other kernel functions implement other parameters into this function so that, it can calculate the vector product in higher dimensions.

Non-linear kernels allow for better predictive performance than the linear kernel, because the linear kernel is a degenerate version of the RBF kernel and thus its predictive performance cannot pass that of the RBF kernel (Keerthi, 2003).

However, linear kernels have some advantages over non-linear kernels. Training an SVM with a linear kernel is much faster than with a non-linear kernel. Additionally, when working with a dataset that has many features and a smaller amount of training examples, there is no significant difference in the performance of linear kernels compared to non-linear kernels. In this case, non-linear mapping does not improve the performance. (Hsu, 2016)

# 11.2 7.2 Theory to Practice: The loss function

The loss quantifies the error for misclassified samples, when the classification predicted by the SVM, and the actual classification are unequal. For samples where both are the same, the loss is 0. The loss thus serves as a measure for how bad our model is doing in classifying the training sets samples. (Jakkula, 2006; Evgeniou et. al, 2000)

Equation (7) describes the so-called loss function. It contains w squared to penalize higher weights, and it also depends on the hinge loss, which is a value for the misclassified samples, and their importance, depending on our regularization parameter or soft margin factor, C. The bigger C, the harder our margin, because misclassified samples will have a big impact on the cost function and make it bigger. (Burges, 1998) C is defined to balance out both margin maximization and loss. (Friedrichs and Igel, 2005)

As described above, the loss function (7) should be minimized to maximize the margin. It is the objective function of our machine learning algorithm. The important part of the loss function, the part that helps to maximize the margin, is the hinge loss, the second part of equation (7). (Jakkula, 2006)

To explain it more clearly, (7) could also be written as follows:

(17) 
$$hingeloss = C \sum_{i=1}^{m} \varepsilon_i = C \left[ \frac{1}{N} \sum_{i=1}^{m} max(0, 1 - y_i (w x_i + b)) \right] (18) loss = \frac{1}{2} ||w||^2 + hingeloss$$
(12)

# 11.3 7.3 Theory to Practice: Stochastic gradient decent to minimize the loss gradient

In order to minimize the loss function, its gradient is calculated. A common method to minimize this function is called Gradient Descent. The gradient P() of an objective function P(), which is parameterized by the model's parameters, is calculated. P() represents the slope with the highest inclination of our function. During Gradient Decent, the parameters are updated in the opposite direction of the gradient. This process is repeated until a (local) minimum is reached, by taking steps determined beforehand by the learning rate. Or, to put it differently, the direction of the slope of the surface described by P() is followed downwards to its lowest point. (Ruder, 2017) Different kinds of gradient descents mostly only differ in the amount of data they use to compute the gradient. Essentially, there is a trade-off between accuracy of the parameter update, and the runtime. As part of our SVM, we used Stochastic Gradient Descent (SGD). In contrast to the basic gradient descent, SGD does not use all the data for its calculation, but only a randomly selected part of it, called stochastic representation (Johnson and Zhang, 2013). This reduces computation time significantly and makes the program faster (Johnson and Zhang, 2013).

## 11.4 7.4 K-Fold Cross validation

Validation is a widely used technique in data science to evaluate how stable a machine learning (ML) model is and to assess how well the model would generalize to new, independent data. Relevant for these two characteristics is the ML's ability to differentiate between relevant patterns and noise in the data available (Vabalas et. al, 2019). As a measure for how good the ML is able to achieve this, the bias-variance trade-off can be used (Geman et. al, 1992; Berrar, 2019). Bias and variance are

both sources of error in ML generalization. With increasing model complexity, bias decreases and variance increases monotonically (Yang et. al, 2020). In short: High bias indicates an 'underfitting' model, which is neither able to classify its training data nor new data well, because it captures too little patterns. High variance indicates an 'overfitting' model that is overly sensitive to inherent noise and random pattern in it's training data and for that reason performs poorly on new data. (Yang et. al, 2020) Optimally both bias and variance could be minimized (Geman et. al, 1992; Berrar, 2019). However, in reality just the right balance is needed to create an optimal model (Yang et. al, 2020).

One validation technique is k-fold cross validation (CV). In CV, the data available is split into k subsets. The data encompasses n dissimilar samples. k is a random integer between 1 and n. For each iteration, k-1 subsets are used as training data, while the remaining subsets are used to test the model and are thus part of the validation set. To put it differently: each data sample is part of the testing data once and part of the training data for all other iterations. (Vabalas et. al, 2019) This approach substantially reduces bias, as it uses most data points for fitting. Simultaneously variance also decreases. But as only one datapoint is used for testing in each iteration, higher variation in testing model effectiveness can occur (Berrar, 2019).

For the implementation, we used Stratified K-Fold, which creates different splits from the train set. The test set is separated from the training process and does not undergo splitting by cross validation, so that the segmentation results are not biased. Then, for the different splits of the train sets, the weight vector is calculated. In order to obtain a single weight vector for the model, the mean from all weight vectors is computed, and then used to segment our test set. Like this, the possible biases derived from different varibles like learning rate, epoch number or regularization factor can be avoided.

# 12 8. Dice Coefficient

# 12.1 8.1 The Theory behind the Dice Coefficient

The dice coefficient is a score to evaluate and compare the accuracy of a segmentation. Needed for its calculation are the segmented image, as well as a corresponding binary reference point also called ground truth. (Bertels et al., 2019) Researchers mostly use the segmentation result of humans as ground truth image. We will use the ground truth images provided with the data sets, which we suspect to be generated by this method. Using the ground truth image, the labels true positive (TP), false positive (FP) and false negative (FN) are assigned to each pixel of the segmented image (Menze et al., 2015). This information is then used to calculate the dice coefficient using formula (1):

(1) 
$$dice = \frac{2TP}{2TP + FP + FN} \quad \varepsilon \quad [0, 1]$$
 (13)

(Menze et al., 2015)

A dice score of 0 indicates that the ground truth and the segmentation result do not have any overlap. A dice score of 1 on the other hand, shows a 100% overlap of ground truth and segmented image (Bertels et al., 2019).

# 12.2 8.2. Unittesting the Dice Coefficient

To test the code for the dice coefficient, we used a frequently used method of software testing: unittests. Unittests are a way of validating that a specific code chunk, a unit, performs as expected and thus its result is as anticipated (Hamill, 2005).

We implemented two kinds of unit tests. The dice coefficient of an image with itself is always 1.0. For our first unit test, we used this knowledge to test our code. For this first test we generated synthetic masks (see #6.2), black-and-white synthetic images, with which we performed the unit test. In addition, we compared our code's result to the python-implemented fl\_score from sklearn.metrics. Both produced identical outputs.

For the second unit test, we defined two random arrays, consisting only of ones and zeros. One array represented the segmented image, while the other served as ground truth. Using formula (1) we calculated the dice manually and compared our result with our codes' output.

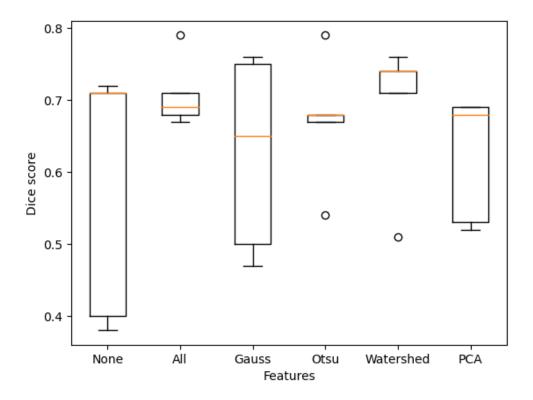
# 13 9. Results

Our goal is to determine the optimal combination of different possible pre-processing methods to enhance the segmentation results of the original images. These methods encompass Gaussian filter, Watershed, Otsu thresholding and PCA. For a more precise evaluation, we use the dice score function to compare the final, segmented images. We compare with each other: • images without Pre-processing • images pre-processed with Gaussian filter • images pre-processed with Otsu thresholding • images pre-processed with Watershed • images pre-processed with PCA • images pre-processed with Gaussian filter, Otsu thresholding, Watershed and PCA.

In the following, we aim to visualize the differences that pre-processing makes in our segmentation results. For that reason, the segmentation result of t01 from the N2DH-GOWT1 dataset will be shown seven times. Each time a different pre-processing method from the list above was applied before the SVM.

The following boxplots compare the Dice Scores of the different possible pre-processing methods each dataset.

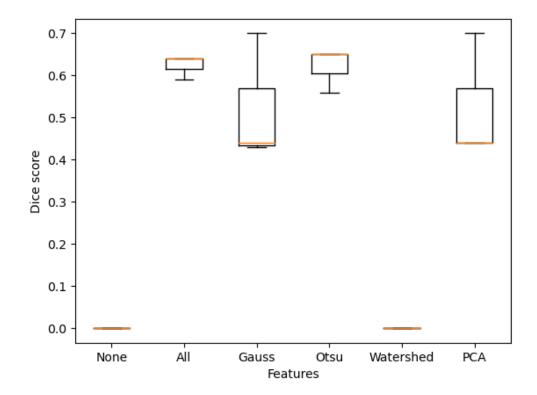
```
[29]: from IPython.display import Image
Image("Data/boxplots/boxplot_N2DH-GOW1-lr-1e-07.png")
[29]:
```



In this boxplot it becomes clear, that not using any features besides from pixel intensities gives the worst results, at least in terms of the highest variance in the dice scores. On the other hand, using all features gives a worse dice score mean, but its variance is much lower, so the images are better segmented all in all. The reduced mean can be explained because using many different features makes it harder for the SVM to find the minimum of the cost function, as there are many conditions to consider. In regard to the single filters, Gauss does not provide a great improvement from not applying a filter at all. Otsu provides a good dice score, and most importantly its variance is very small. Watershed, as expected, gives the best dice score mean, because it already segments the images, and so the SVM can get very valuable information from it. Lastly, because we use PCA to reduce our images to 95% variance. However, its values are probably highly correlated to the pixel intensities, which explains why the dice score mean from PCA is lower than no filter at all.

```
[26]: from IPython.display import Image Image("Data/boxplots/boxplot_N2DL-HeLa-lr-1e-07.png")
```

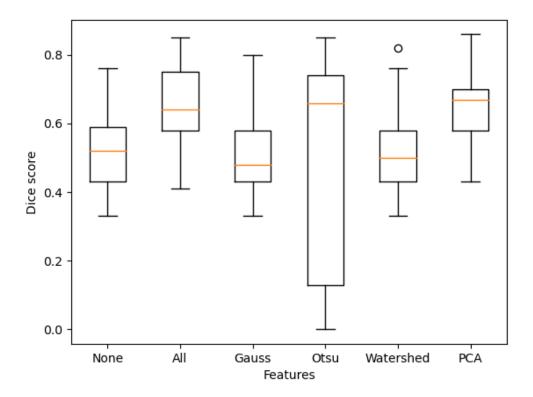
[26]:



From this boxplot we learn that applying all filters produces the best segmentation results. Otsu thresholding seems to play the biggest role in this, while Gauss filtering and PCA both enhance the segmentation result less. Watershed does not seem to have a huge positive effect on the Dice Score. The average Dice score for N2DL-HeLa cell images with all filters as pre-processing was 0.63.

```
[33]: from IPython.display import Image Image("Data/boxplots/boxplot_NIH3T3-lr-1e-07.png")
```

[33]:



This boxplot shows that not using any extra features gives a similar dice score as only using Gauss or Watershed. The reason for this can be the quality from the images is not good enough for the watershed algorithm to work properly, that is why its segmentation is similar to the one that comes from our SVM with only pixel intensities. Otsu and PCA both give very good dice scores, but Otsu also has a very high variance, so it does not work with all images as well.

We found that throughout all datasets the best setting is not always the same. For N2DH-GOWT1 the best dice score is 0,79, when pre-processed with Gauss and Otsu. For N2DL-HeLa the best dice score is 0.63, which we achieved by applying all filters. For NIH3T3 the best dice score is 0.86, when pre-processed with PCA.

Ten synthetic images were created from a single original image from each dataset set using domain randomization. We used these images to enlarge each original image set during the SVMs training phase. The quality of the segmentation, measured by the Dice Score, stayed the same, when synthetic images were added to the training data set. We thus concluded, that they are as good as the original images in training the SVM. To be able to segment all but one of the original images, we therefore filled the training set with synthetic images only, but took the image used to create the synthetic images from the test set to avoid data leakage. This allowed us the put almost all original images into the validation set and thus made it possible to segment all but one of the original images.

# 14 10. Discussion

The SVM is a potent algorithm to segment images, as the dice scores proof. However, there are further issues that could be tackled in order to improve its segmentation capacities and obtain better results.

First, we implemented a linear kernel to classify the data. In doing so, we assumed that the pixels can be linearly classified, as this has been indeed possible. We chose the linear kernel because we considered it the most effective one, runtime-wise, for our pixels. However, it is possible that they could be better classified using RBF, so this is an aspect that could be tested and implemented to improve the dice score.

Secondly, we normalized and resized our data to reduce the number of pixels, in order to improve the runtime. In order to do so, we converted all images into squares, independently of their original dimensions. As a result, all our segmented images are squares. Although this process does not affect the quality of the segmentation, because the scaling affects both images and ground truths, it produces segmented images with dimensions that are not true to original. This is a minor issue that could be corrected in order to obtain images that are the same size as the not segmented ones. In this sense, it has to be considered that the resize algorithm also has a bias on our model, and therefore if we used other resizing or transforming algorithms, our image segmentation results would also vary. This was the case for tiles, and its effect should be further investigated.

Thirdly, we could add more features into the SVM, so that the machine learning algorithm has more information about every single pixel and can classify it better. Apart from the already implemented filters, we could use filters that give information about the edges, like Canny. Furthermore, it would be beneficial to insert information about the neighborhood of the pixel, so that the SVM can take into consideration the pixel intensities from neighboring pixels.

Furthermore, our weights vector was created always as an empty array with only zeroes. this led the SVM to always start at the same position, and therefore make the same mistakes at the beginning of every run. It would be interesting to create a random weights vector every time the SVM is ran, to see if its optimization achieves a better segmentation of the images, because it can find the local or even global minimum of the function better.

Finally, PCA could be used for dimensionality reduction instead of as a feature, like we did. Like this, the images for the SVM would contain less pixels and therefore less information. Like this, we could investigate its impact on the runtime, which should be better, but the dice score would be less accurate.

# 15 11. Bibliography

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