

American University of Armenia  
CS121 Data Structures  
PSS 10

**Tree Traversal**

1. Write a method for the `AbstractBinaryTree` class that returns the node with the minimum element using one of the traversal methods.
2. Design a `preorderNext(p)` methods for `AbstractBinaryTree` class, which given the position `p` will return the position visited after `p` in preorder traversal of tree `T`.
3. Let the rank of a position `p` during a traversal be defined such that the first element visited has rank 1, the second element visited has rank 2, and so on. For each position `p` in a tree `T`, let `pre(p)` be the rank of `p` in a preorder traversal of `T` and let `post(p)` be the rank of `p` in a postorder traversal of `T`. Write a method `difference(p)` that given a position `p` calculates the absolute difference between `pre(p)` and `post(p)`.

**Priority Queue**

1. Given an array of `n` numbers add them to a Priority Queue so that the key value of the given number corresponds to its frequency in the array.

**Comparators**

1. Given `b1` and `b2` nonnegative integers write a comparator that determines order based on the number of 1's in each integer's binary expansion, so that  $b1 < b2$  if the number of 1's in binary representation of `b1` is less than the number of 1's in binary representation of `b2`.

**Heaps**

1. Let Maxheap be a heap where the object in the node is greater than or equal to its descendant objects and let Minheap be a heap where the relations is less than or equal. Given the following integer keys (with no values specified): 30, 65, 22, 40, 15, 70, 80, 60, 55, 10 draw the tree representation of the heap that results when all of the above elements are added to initially empty:
  - Maximum binary heap
  - Minimum binary heap
2. Given an array of `n` numbers implement a method that returns `m` smallest numbers using Heap.
3. Given a heap `H` and a key `k`, give a method for computing all the entries in `H` having a key less than or equal to `k`.

**If time permits**

1. Trace the steps of a heap sort on the following array: 20, 40, 30, 10, 90, 70