

i^1	j^2	
n	n	task 个数
1	unknown 平均 x	单个 task size
n	nx	total size

只知道 $x \sim \text{normal distribution}(\mu, \sigma_0^2)$

给定 x , 单个 task size $\sim \text{normal distribution}(\mu_x, \sigma_1^2)$

采 m 个 task, 有

$$\vec{y} = (y_1, y_2, \dots, y_m)$$

基于假设, 显然

$$P(y_i | x) = \frac{1}{\sqrt{2\pi}\sigma_1} e^{-\frac{(y_i - x)^2}{2\sigma_1^2}}$$

$$P(\vec{y} | x) = \prod_{i=1}^m \frac{1}{\sqrt{2\pi}\sigma_1} e^{-\frac{(y_i - x)^2}{2\sigma_1^2}}$$

通过 \vec{y} 估计 x , 有

$$P(x | \vec{y}) = \frac{P(\vec{y} | x) P(x)}{P(\vec{y})}$$

$$= \frac{P(\vec{y} | x) \cdot P(x)}{\int_x P(\vec{y} | x) \cdot P(x) dx}$$

$$= \frac{1}{\sqrt{2\pi}} \left[\frac{m}{\sigma_1^2} + \frac{1}{\sigma_0^2} \right]^{\frac{1}{2}} e^{-\left(\frac{m}{2\sigma_1^2} + \frac{1}{2\sigma_0^2}\right) \left(x - \frac{\sum_{i=1}^m \frac{1}{\sigma_1^2} y_i + \frac{1}{\sigma_0^2} \mu}{\frac{m}{\sigma_1^2} + \frac{1}{\sigma_0^2}}\right)^2}$$

也就显然, 给定 \vec{y} , x 也符合 normal distribution