

Problem: Minimize Motorola's total purchase and administrative cost for buying 8 products from 5 suppliers given list price, discount and quantity

Solution: Build a linear integer model to minimize the total purchase and administrative cost under the given constraints on suppliers and products

Inputs: in blue in spreadsheet,

- For each product the list price and required quantity
- For each product, supplier the discount percentage
- For each supplier, \$5,000 as the admin cost of setup for Motorola

Objective function: Min (Total Purchase and Admin cost) =

$$\min_{i \in (1 \dots 8), j \in (1 \dots 5)} (\sum (X_{ij} * (P_i * (1 - D_{ij}) * Q_i)) + \sum (Y_j * C_j)), \text{ where}$$

- X_{ij} – Quantity of product i supplied by supplier j
- P_i – List price (\$) of product i
- Q_i – Quantity required (demand) of product i
- D_{ij} – Discount (%) offered on product i by supplier j
- Y_j – Binary variable to decide whether supplier j is selected or not $\in (0,1)$
- C_j – Fixed administrative cost (\$) of setting up supplier j for Motorola $\in (5000)$
- $i \in (1 \dots 8)$ for the 8 products
- $j \in (1 \dots 5)$ for the 5 suppliers

Decision variables:

- X_{ij} – Quantity of product i supplied by supplier j
- Y_j – Binary variable to decide whether supplier j is selected or not

Constraints:

1. $X_{ij} \leq 0.8 * Q_i$, a supplier cannot supply more than 80% of any products required quantity
2. $\sum_j X_{ij} \geq Q_i$ for all i , quantity supplied by all suppliers must meet demand for each product
- $X_{ij} \leq Y_j * M$, where $M \in (797)$
 - To ensure that product i is supplied by supplier j only when it is selected, which forces the model to incur the fixed administrative cost of setting up supplier j
 - **M – maximum quantity required among all products**
 - It could be any large no like 1,000 or 10,000, etc, but the result is the same
 - Smaller value will give sub-optimal result
3. $X_{ij} \in \text{int}$, only integer quantities must be supplied by each supplier
4. $X_{ij} \geq 0$, non-negativity constraint
5. $Y_j \in (0,1)$, as it is a binary decision variable
6. $\sum_j Y_j \geq 2$, we need at least 2 suppliers for each product as no supplier can supply more than 80% of each product quantity required

Result:

- Motorola's **minimum total purchase and administrative cost** is **\$ 243,550.52**