

Part I

```
In [73]:  
  
# imports  
import pandas as pd  
import matplotlib.pyplot as plt  
from math import log10, log2, log  
import numpy as np  
from sklearn import preprocessing  
from sklearn.preprocessing import StandardScaler
```

```
In [3]:  
  
# loading data from csv  
data = pd.read_csv('IBM.csv', parse_dates=['Date'])  
N = len(data.index)  
close = pd.Series(data['Close'], name='Close')  
dates = pd.Series(data['Date'], name='Date')
```

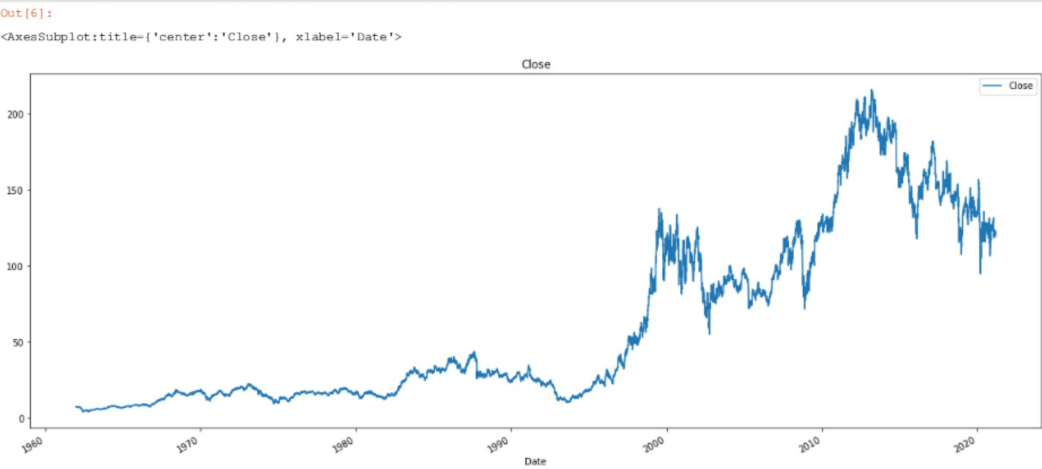
```
In [4]:  
  
data.head()
```

Out[4]:

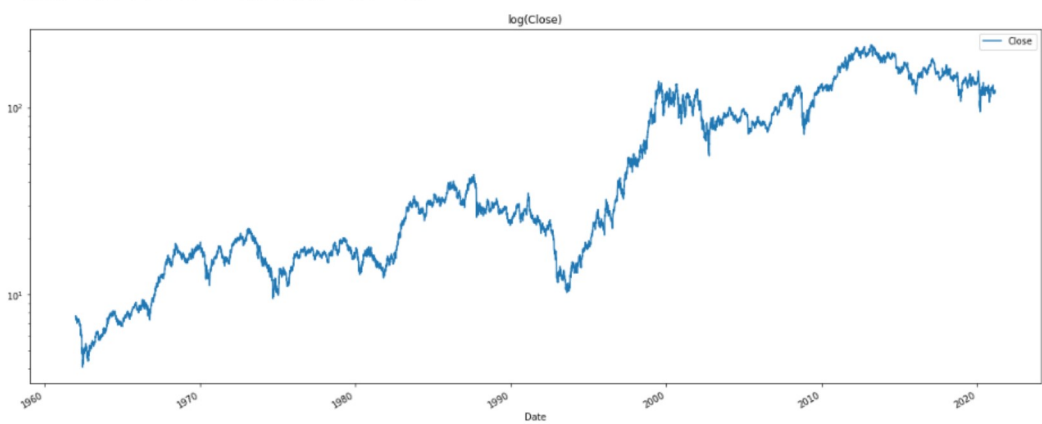
	Date	Open	High	Low	Close	Adj Close	Volume
0	1962-01-02	7.713333	7.713333	7.626667	7.626667	1.858243	390000
1	1962-01-03	7.626667	7.693333	7.626667	7.693333	1.874485	292500
2	1962-01-04	7.693333	7.693333	7.613333	7.616667	1.855805	292500
3	1962-01-05	7.606667	7.606667	7.453333	7.466667	1.819257	367500
4	1962-01-08	7.460000	7.460000	7.266667	7.326667	1.785148	547500

```
In [5]:  
  
# separation of close price data  
close = pd.DataFrame({'Date':data['Date'], 'Close':data['Close']})  
close.set_index('Date')  
pass
```

```
In [6]:  
  
close.plot(figsize=(20,8), x='Date', y='Close', title='Close')
```



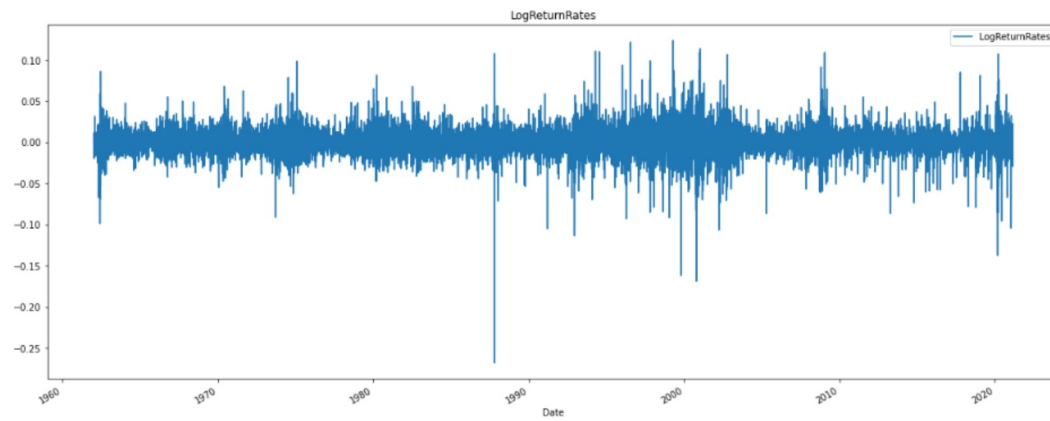
```
In [7]:  
  
close.plot(figsize=(20,8), x='Date', y='Close', logy=True, title='log(Close)')  
Out[7]:  
<AxesSubplot:title={'center':'log(Close)'}, xlabel='Date'>
```



```
In [8]:  
  
# logarithmic rates of return for close prices  
close["LogReturnRates"] = pd.Series(np.array([0.0] + [log(close['Close'][i])/close['Close'][i-1]) for i in range(1, len(close['Close']))]))
```

```
In [9]:  
  
close.plot(figsize=(20,8), x='Date', y='LogReturnRates', title='LogReturnRates')  
Out[9]:
```

```
<AxesSubplot:title={'center':'LogReturnRates'}, xlabel='Date'>
```

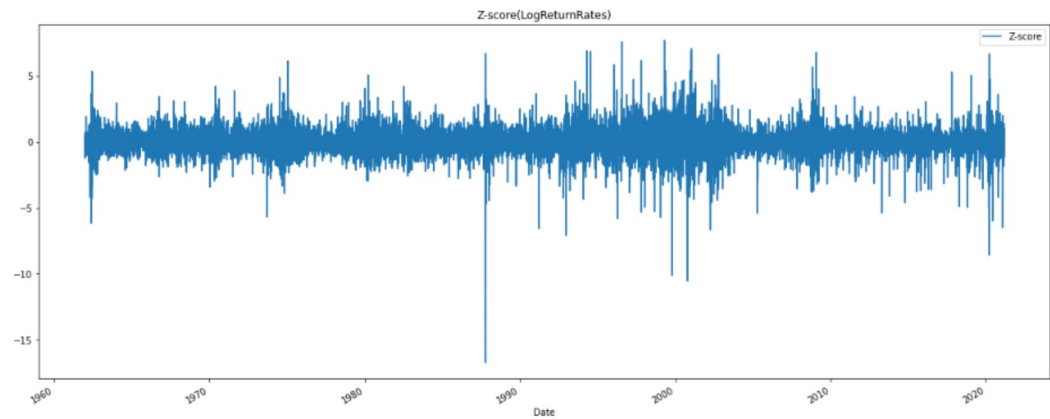


```
In [10]:
# standardized logarithmic rates of return for close prices (using z-score: std=1, mean=0)
close['Z-score'] = (close['LogReturnRates'] - close['LogReturnRates'].mean()) / close['LogReturnRates'].std()
close.head()
Out[10]:
```

	Date	Close	LogReturnRates	Z-score
0	1962-01-02	7.626667	0.000000	-0.011651
1	1962-01-03	7.693333	0.008703	0.531862
2	1962-01-04	7.616667	-0.010015	-0.637102
3	1962-01-05	7.466667	-0.019890	-1.253790
4	1962-01-08	7.326667	-0.018928	-1.193704

```
In [11]:
close.plot(figsize=(20,8), x='Date', y='Z-score', title='Z-score(LogReturnRates)')
Out[11]:
```

```
<AxesSubplot:title={'center':'Z-score(LogReturnRates)'}, xlabel='Date'>
```

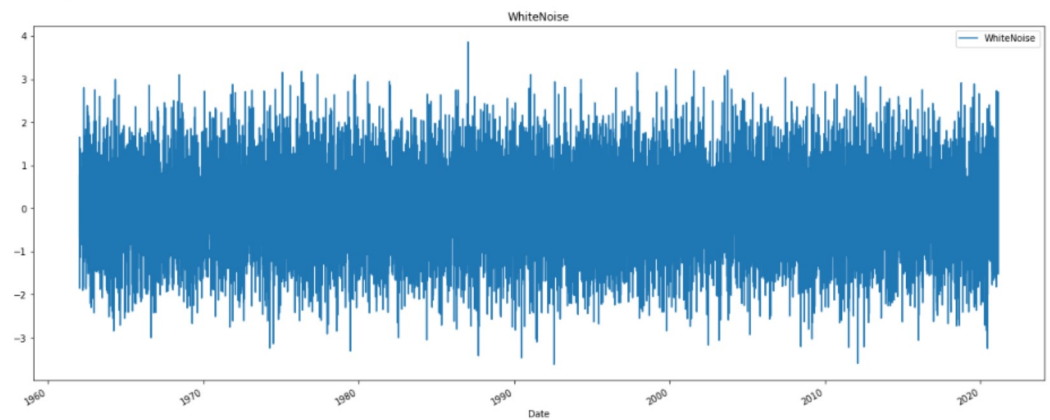


Part II

```
In [12]:
# white noise
mean = 0
std = 1
N = len(data['Close'])
white_noise = pd.DataFrame(data=np.random.normal(mean, std, size=N), columns=['WhiteNoise'], index=data['Date'])
```

```
In [13]:
white_noise.plot(figsize=(20,8), y='WhiteNoise', title='WhiteNoise')
Out[13]:
```

```
<AxesSubplot:title={'center':'WhiteNoise'}, xlabel='Date'>
```



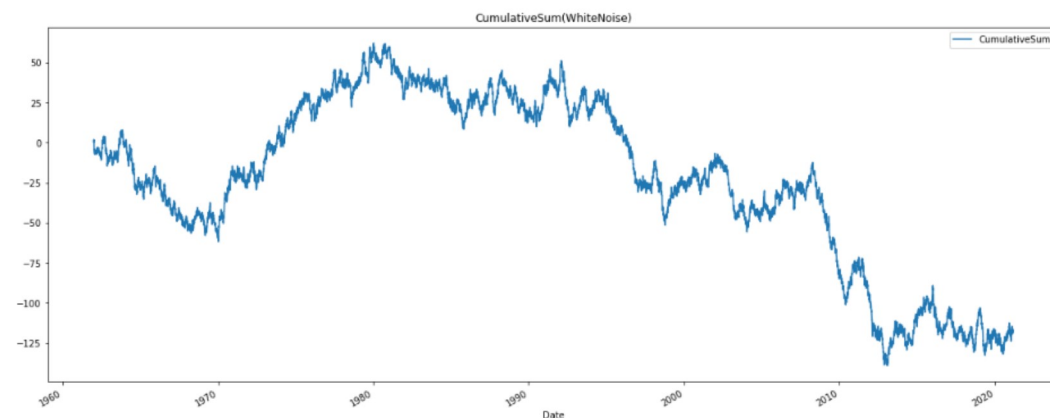
```
[14]:
# white noise cumulative sum
white_noise['CumulativeSum'] = white_noise.cumsum()
white_noise.head()

Out[14]:
```

	WhiteNoise	CumulativeSum
Date		
1962-01-02	0.764974	0.764974
1962-01-03	-0.683988	0.080986
1962-01-04	1.656510	1.737495
1962-01-05	-0.301831	1.435664
1962-01-08	0.439684	1.875348

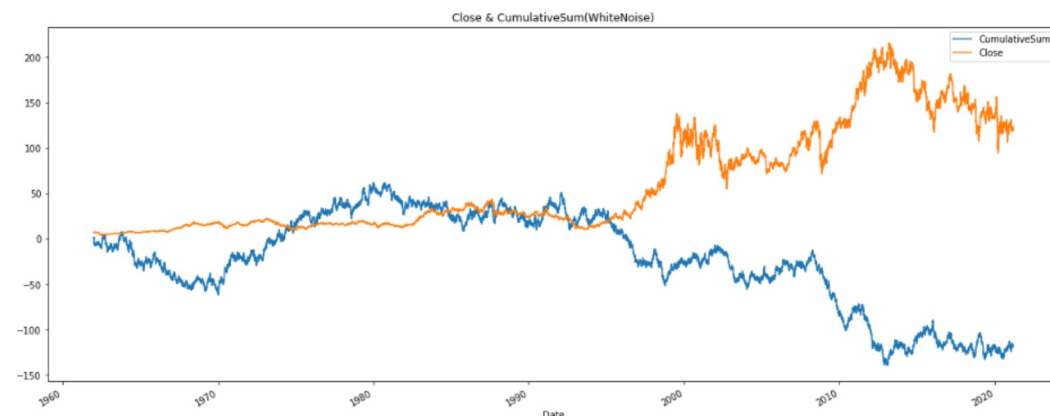
```
In [15]:
white_noise.plot(figsize=(20,8), y='CumulativeSum', title='CumulativeSum(WhiteNoise)')
```

```
Out[15]:
<AxesSubplot:title=('center': 'CumulativeSum(WhiteNoise)'), xlabel='Date'>
```



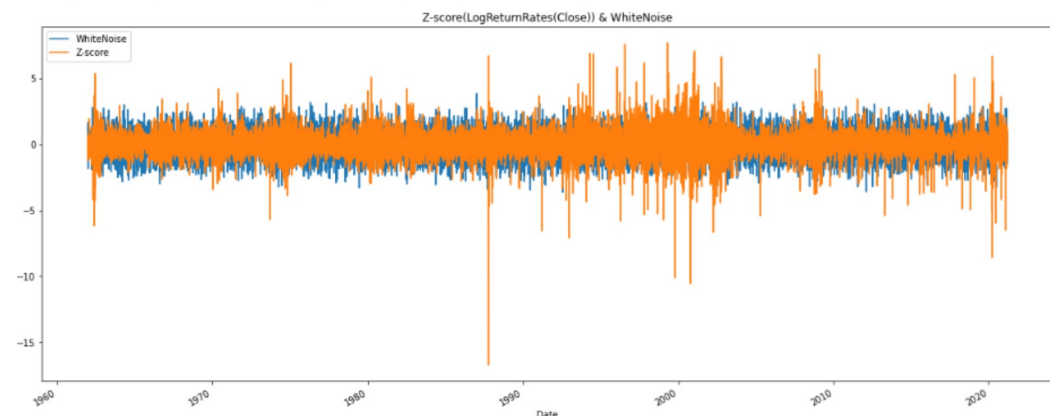
```
In [16]:
ax = white_noise.plot(y='CumulativeSum')
close.plot(figsize=(20,8), x='Date', y='Close', ax=ax, title='Close & CumulativeSum(WhiteNoise)', legend=True)
```

```
Out[16]:
<AxesSubplot:title=('center': 'Close & CumulativeSum(WhiteNoise)'), xlabel='Date'>
```



```
In [17]:
ax = white_noise.plot(y='WhiteNoise')
close.plot(figsize=(20,8), x='Date', y='Z-score', ax=ax, title='Z-score(LogReturnRates(Close)) & WhiteNoise', legend=True)
```

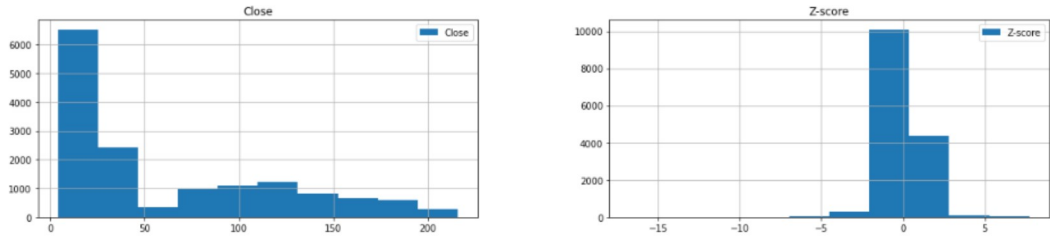
```
Out[17]:
<AxesSubplot:title=('center': 'Z-score(LogReturnRates(Close)) & WhiteNoise'), xlabel='Date'>
```



Histograms

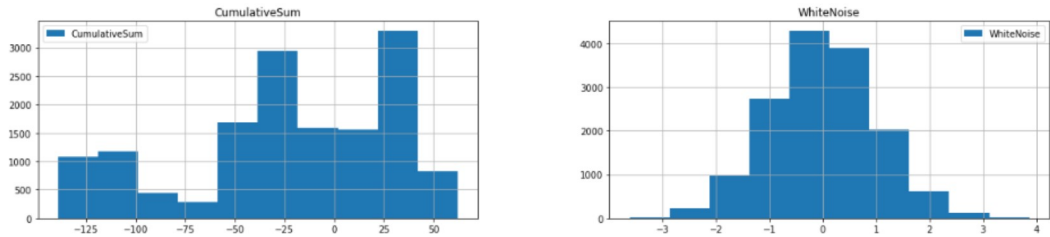
```
In [18]:
# Close prices histograms
close.hist(figsize=(20,4), column=['Close', '%z-score'], legend=True)

Out[18]:
array([[<AxesSubplot:title='center': 'Close'>,
        <AxesSubplot:title='center': '%z-score'>]], dtype=object)
```



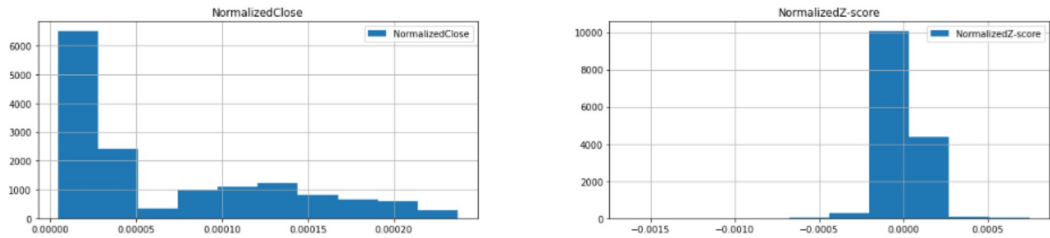
```
In [19]:
# White noise histograms
white_noise.hist(figsize=(20,4), column=['CumulativeSum', 'WhiteNoise'], legend=True)

Out[19]:
array([[<AxesSubplot:title='center': 'CumulativeSum'>,
        <AxesSubplot:title='center': 'WhiteNoise'>]], dtype=object)
```



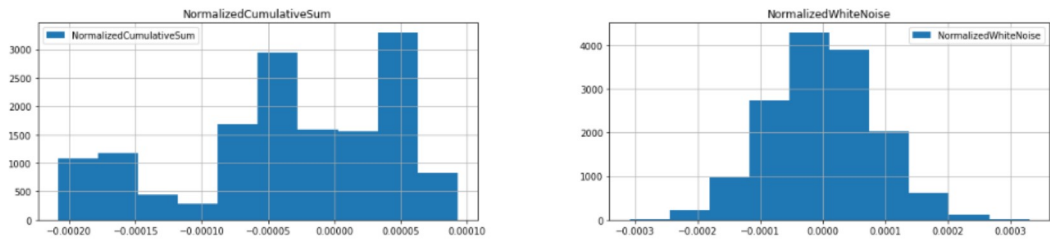
```
In [20]:
close['NormalizedClose'] = close['Close']/abs(close['Close']).sum()
close['NormalizedZ-score'] = close['%z-score']/abs(close['%z-score']).sum()
# Normalized Close prices histograms
close.hist(figsize=(20,4), column=['NormalizedClose', 'NormalizedZ-score'], legend=True)

Out[20]:
array([[<AxesSubplot:title='center': 'NormalizedClose'>,
        <AxesSubplot:title='center': 'NormalizedZ-score'>]], dtype=object)
```



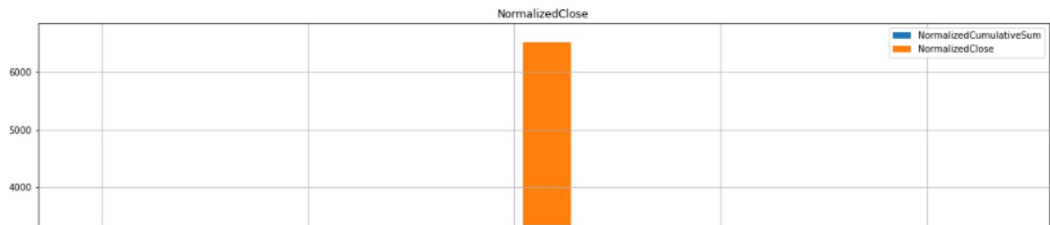
```
In [21]:
white_noise['NormalizedCumulativeSum'] = white_noise['CumulativeSum']/abs(white_noise['CumulativeSum']).sum()
white_noise['NormalizedWhiteNoise'] = white_noise['WhiteNoise']/abs(white_noise['WhiteNoise']).sum()
# Normalized White noise histograms
white_noise.hist(figsize=(20,4), column=['NormalizedCumulativeSum', 'NormalizedWhiteNoise'], legend=True)

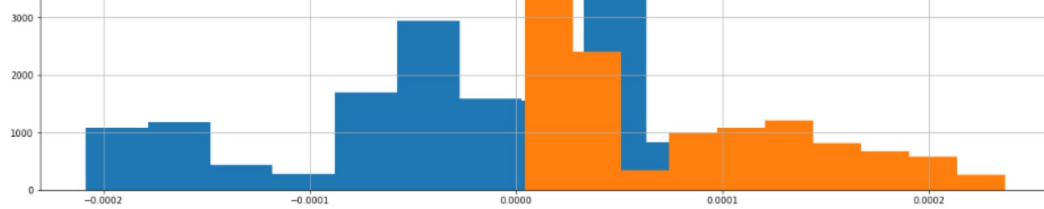
Out[21]:
array([[<AxesSubplot:title='center': 'NormalizedCumulativeSum'>,
        <AxesSubplot:title='center': 'NormalizedWhiteNoise'>]], dtype=object)
```



```
In [22]:
ax = white_noise.hist(figsize=(20,8), column=['NormalizedCumulativeSum'], legend=True)
close.hist(figsize=(20,8), column=['NormalizedClose'], ax=ax, legend=True)

Out[22]:
array([[<AxesSubplot:title='center': 'NormalizedClose'>]], dtype=object)
```



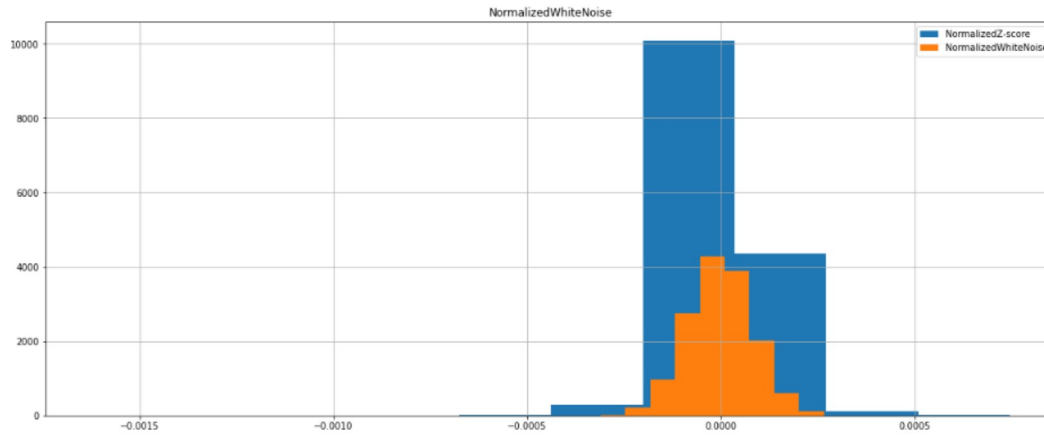


In [23]:

```
ax = close.hist(figsize=(20,8), column=['NormalizedZ-score'], legend=True)
white_noise.hist(figsize=(20,8), column=['NormalizedWhiteNoise'], ax=ax, legend=True)
```

Out[23]:

```
array([<AxesSubplot:title={'center':'NormalizedWhiteNoise'}>],
      dtype=object)
```



Distribution parameters

In [24]:

```
# close prices kurtosis
close.kurt(axis=0)
```

Out[24]:

```
Close          -0.485366
LogReturnRates 12.239468
Z-score        12.239468
NormalizedClose -0.485366
NormalizedZ-score 12.239468
dtype: float64
```

In [25]:

```
# close prices skewness
close.skew(axis=0)
```

Out[25]:

```
Close          0.924353
LogReturnRates -0.342694
Z-score        -0.342694
NormalizedClose 0.924353
NormalizedZ-score -0.342694
dtype: float64
```

In [26]:

```
# white noise kurtosis
white_noise.kurt(axis=0)
```

Out[26]:

```
WhiteNoise      -0.008483
CumulativeSum    -0.663026
NormalizedCumulativeSum -0.663026
NormalizedWhiteNoise -0.008483
dtype: float64
```

In [27]:

```
# white noise skewness
white_noise.skew(axis=0)
```

Out[27]:

```
WhiteNoise      0.004915
CumulativeSum    -0.596867
NormalizedCumulativeSum -0.596867
NormalizedWhiteNoise 0.004915
dtype: float64
```

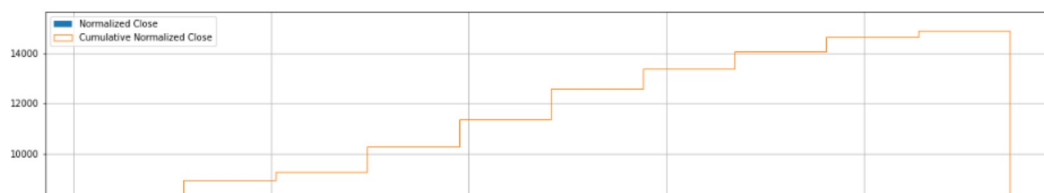
Cumulative Distribution Function for both series (close data and white noises)

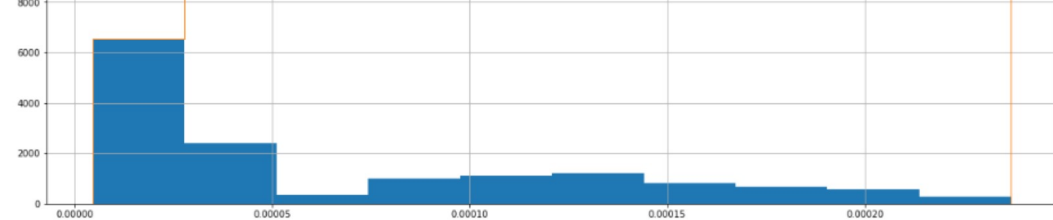
In [84]:

```
plt.figure(figsize=(20,8))
plt.grid(True)
plt.hist(close['NormalizedClose'], label="Normalized Close")
plt.hist(close['NormalizedClose'], cumulative=True, histtype='step', label="Cumulative Normalized Close")
plt.legend(loc='upper left')
```

Out[84]:

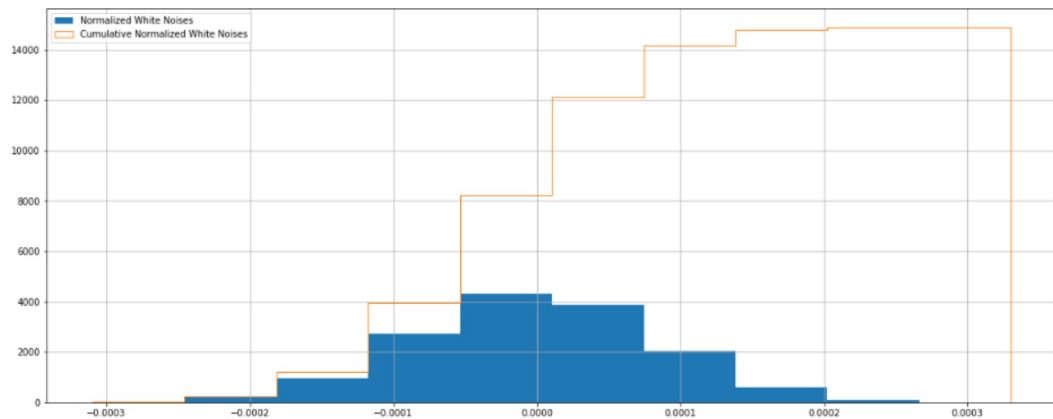
<matplotlib.legend.Legend at 0x28996f16430>





```
In [85]:  
plt.figure(figsize=(20,8))  
plt.grid(True)  
plt.hist(white_noise['NormalizedWhiteNoise'], label="Normalized White Noises")  
plt.hist(white_noise['NormalizedWhiteNoise'], cumulative=True, histtype='step', label="Cumulative Normalized White Noises")  
plt.legend(loc='upper left')
```

Out[85]:
<matplotlib.legend.Legend at 0x2899681a310>



```
In [87]:  
plt.figure(figsize=(20,8))  
plt.grid(True)  
plt.hist(close['NormalizedClose'], cumulative=True, histtype='step', label="Cumulative Normalized Close", log=True)  
plt.hist(white_noise['NormalizedWhiteNoise'], cumulative=True, histtype='step', label="Cumulative Normalized White Noises", log=True)  
plt.legend(loc='upper left')
```

Out[87]:
<matplotlib.legend.Legend at 0x289968d7d60>

