

# Homework 03

CS 624, 2022 Fall

Review the course homework policies before you start!

1. Problem 9.3-8 on p223.

Let  $X[1..n]$  and  $Y[1..n]$  be two arrays, each containing  $n$  numbers already in sorted order. Give an  $O(\lg n)$ -time algorithm to find the median of all  $2n$  elements in arrays  $X$  and  $Y$ .

2. Problem 12.2-5 on p293.

Show that if a node in a binary search tree has two children, then its successor has no left child and its predecessor has no right child.

3. Problem 15.4-5 on p397.

Give an  $O(n^2)$ -time algorithm to find the longest monotonically increasing subsequence of a sequence of  $n$  numbers.

4. Problem 16.2-2 on p427.

Give a dynamic-programming solution to the 0-1 knapsack problem that runs in  $O(nW)$  time, where  $n$  is the number of items and  $W$  is the maximum weight of items that the thief can put in his knapsack.

5. Problem 16.1-3 on p422.

Not just any greedy approach to the activity-selection problem produces a maximum-size set of mutually compatible activities.

- (a) Give an example to show that the approach of selecting the activity of least duration from among those that are compatible with previously selected activities does not work.
- (b) Do the same for the approach of always selecting the compatible activity that overlaps the fewest other remaining activities.
- (c) Do the same for the approach of always selecting the compatible remaining activity with the earliest start time.

6. Problem 16.2-5 on p428.

Describe an efficient algorithm that, given a set  $\{x_1, x_2, \dots, x_n\}$  of points on the real line, determines the smallest set of unit-length closed intervals that contains all of the given points. Argue that your algorithm is correct.

7. Problem 16.3-3 on p436.

What is an optimal Huffman code for the following set of frequencies, based on the first 8 Fibonacci numbers?

$a:1 \quad b:1 \quad c:2 \quad d:3 \quad e:5 \quad f:8 \quad g:13 \quad h:21$

Can you generalize your answer to find the optimal code when the frequencies are the first  $n$  Fibonacci numbers?