Lecture 02

신호및시스템표현

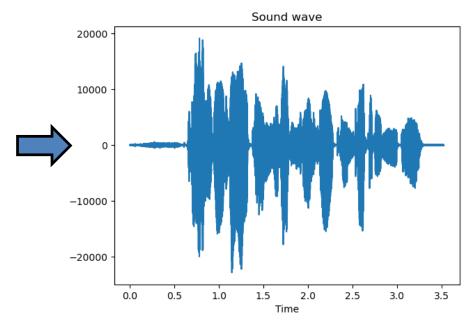
신호(signal)



- 하나 이상의 독립 변수의 함수로 정의되며, 보통 어떤 현상 의 성질에 관한 정보를 포함함
 - x(t)는 시간 t의 함수로 표시되는 물리적인 양 x를 나타냄

■ 예, 사람의 음성

저의 회사에 방문해 주셔서 감사드립니다.

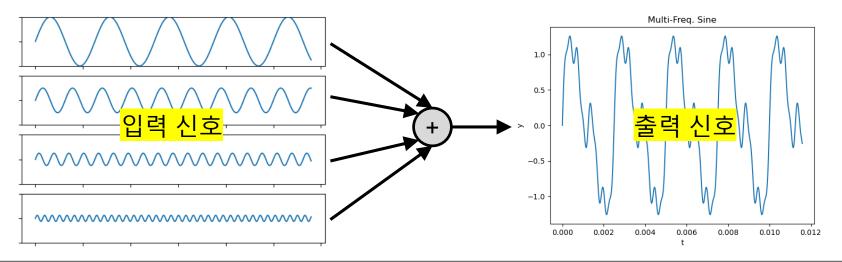


Source: Kyubyong Park, KSS Dataset, https://kaggle.com/bryanpark/korean-single-speaker-speech-dataset (accessed on 2024.08.06)

시스템(system)

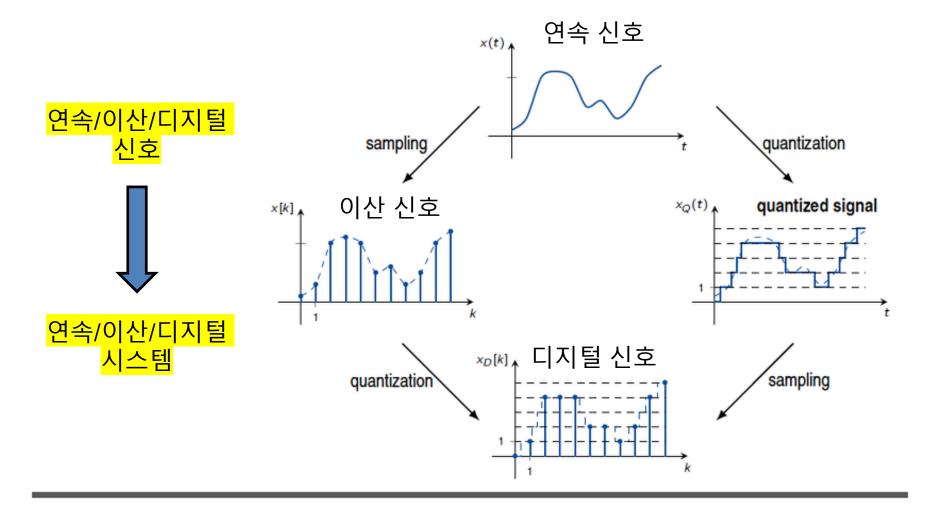


- 어떠한 목적을 달성하기 위하여 필요한 만큼의 성분과 요소 들로 구성됨
- 주어진 신호에 반응하여 또 다른 신호를 발생하는 계통임
 - 신호 변형(signal transformation)
 - 신호 처리(signal processing)



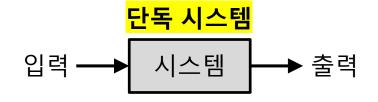
연속, 이산, 디지털



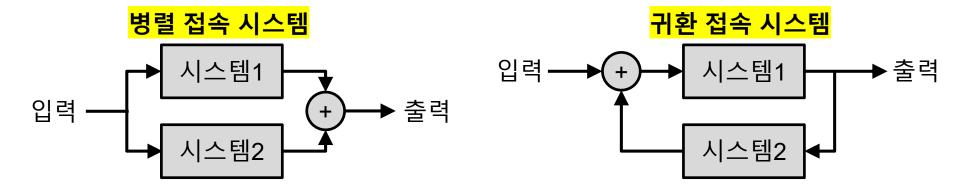


시스템



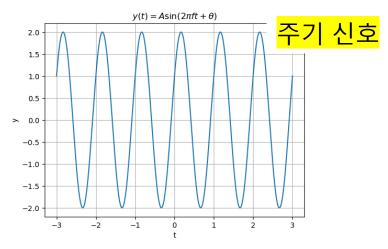


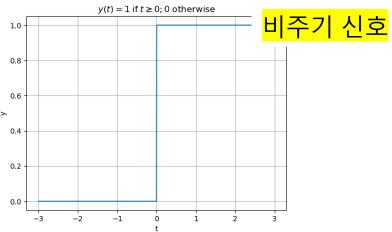


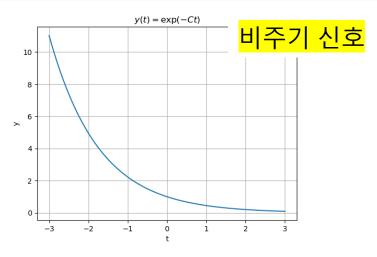


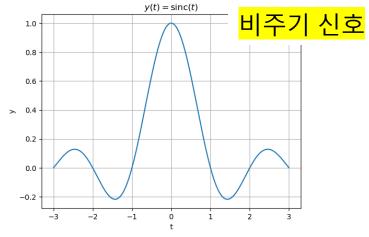
연속 신호





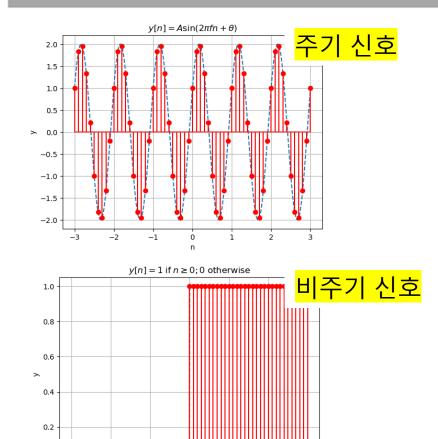




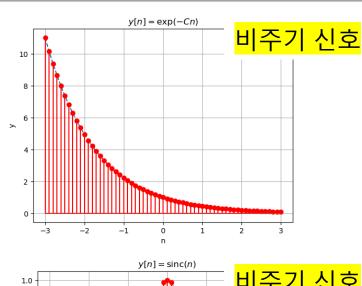


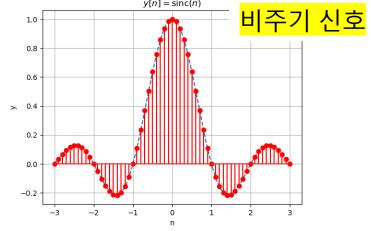
이산 신호





0.0

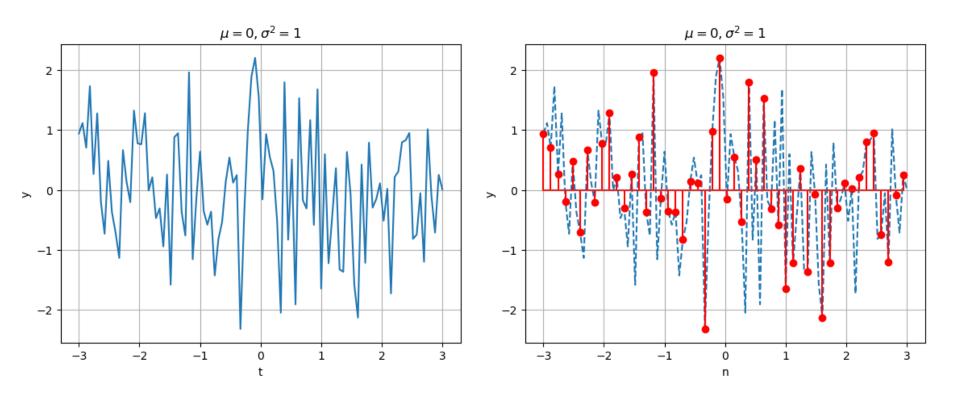




불규칙 신호

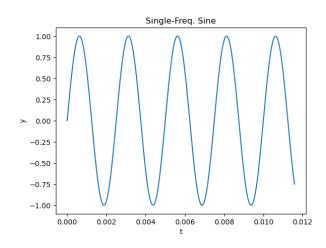


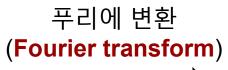
백색 가우스 잡음(white Gaussian noise)

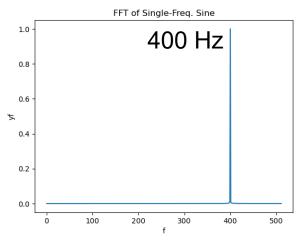


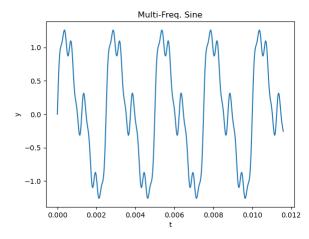
주파수 해석

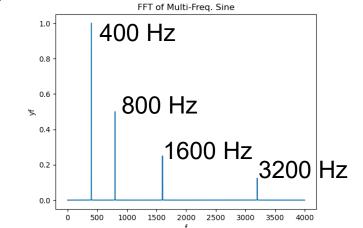












컨벌루션(convolution)



- 선형 시불편 시스템(Linear Time-Invariant System)
 - 시간에 따라 변화하지 않은 시스템
 - 중첩의 원리(principle of superposition)를 만족하는 시스템
 - 가산성(additivity) : $f(x_1 + x_2) = f(x_1) + f(x_2)$
 - 균일성(homogeneity) : $f(ax_1) = af(x_1)$



$$f(ax_1 + bx_2) = af(x_1) + bf(x_2)$$

■ LTI 시스템을 통과하는 입력 신호 x(t)와 시스템의 임펄스 응답 h(t) 사이의 관계를 나타내는 수학적 컨벌루션이라고 함

건벌루션(convolution)



■ 연속 LTI 시스템 : 컨벌루션 적분

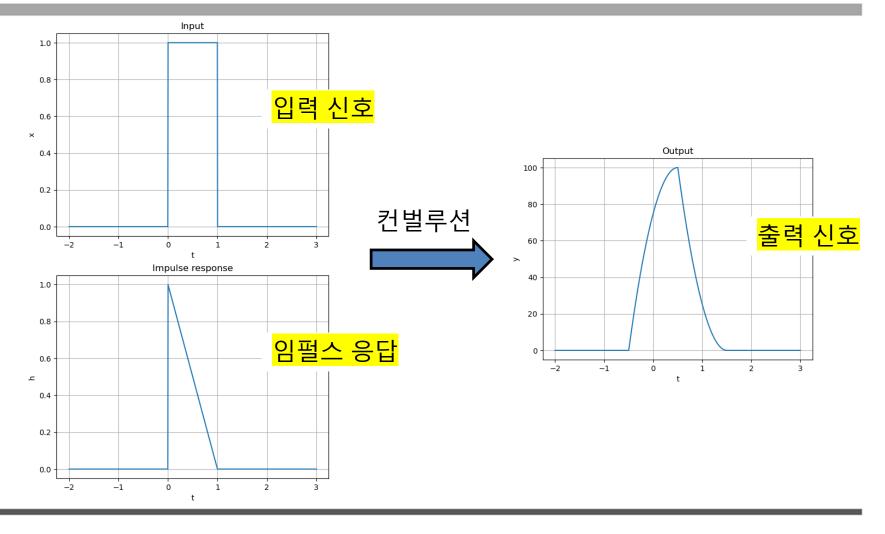
$$x(t)$$
 - 연속 시스템
$$h(t)$$
 $y(t) = x(t) * h(t) = \int_{-\infty}^{\infty} x(\tau)h(t-\tau)d\tau$

■ 이산 LTI 시스템 : 컨벌루션 합

$$x[n]$$
 이산 시스템
$$h[n] \longrightarrow y[n] = x[n] * h[n] = \sum_{k=-\infty}^{\infty} x[k]h[n-k]$$

컨벌루션(convolution)







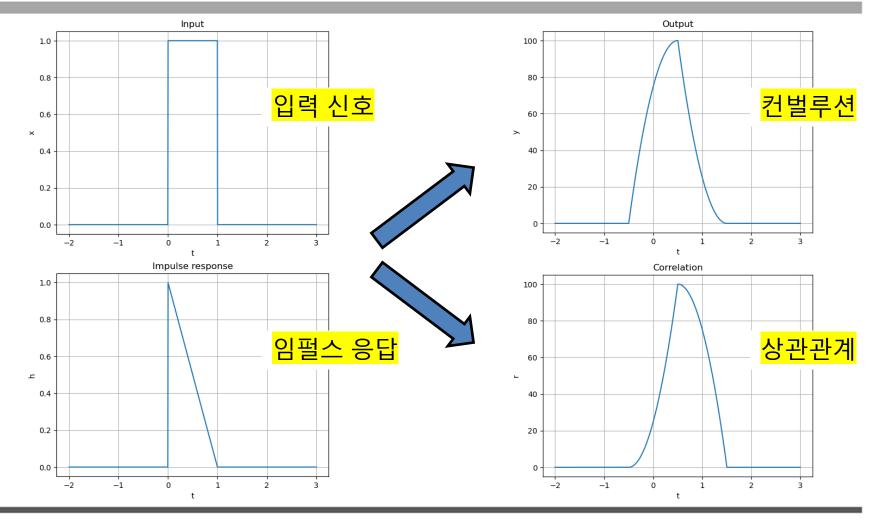
- 비주기 신호를 처리할 때, 서로 다른 2개의 신호 사이에서 혹은 동일한 신호 내에서 신호간의 유사성 혹은 상관도를 평가함
 - 상호 상과 함수(cross-correlation function)

$$R_{12}(\tau) = \int_{-\infty}^{\infty} x_1(t)x_2(t-\tau)dt$$

■ 자기 상관 함수(auto-correlation function)

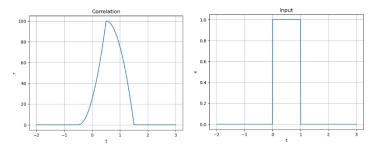
$$R_X(\tau) = \int_{-\infty}^{\infty} x(t)x(t-\tau)dt$$

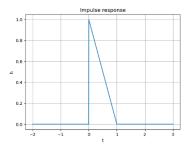




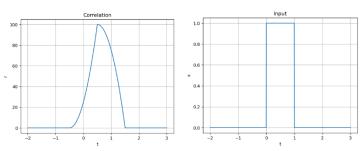




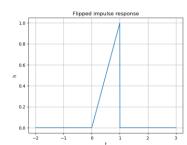




출력 신호 = 입력 신호 (컨벌루션) 뒤집된 임펄스 응답



같다





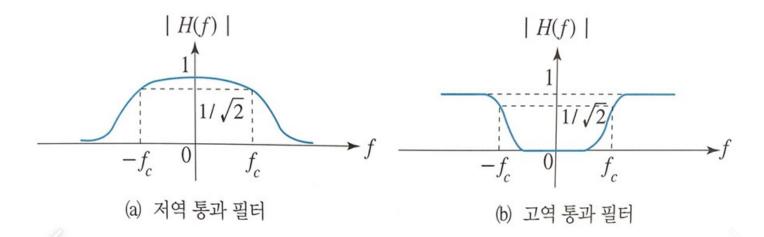
■ 컨벌루션의 Fourier transform

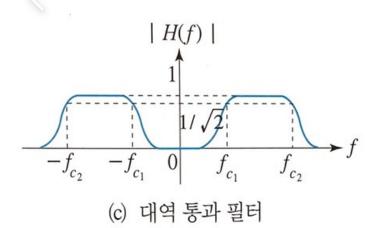
$$y(t) = x(t) * h(t)$$

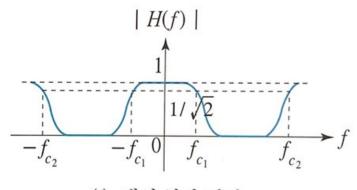
$$V(f) = X(f)H(f)$$

■ 상관관계의 Fourier transform





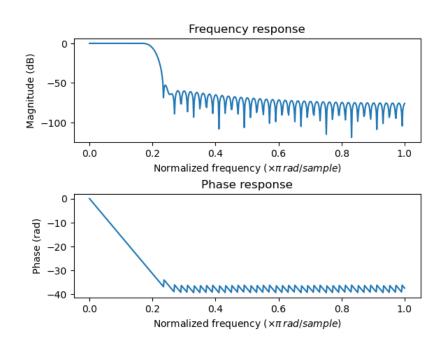


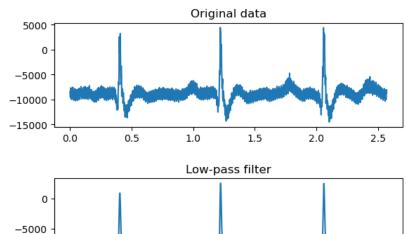


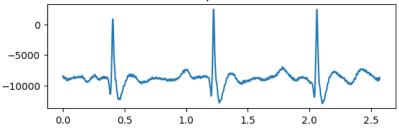
(d) 대역 차단 필터



■ 저역 통과 필터(low-pass filter)

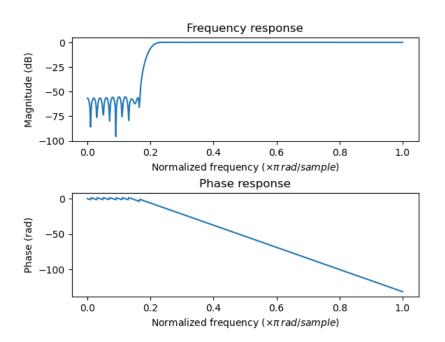


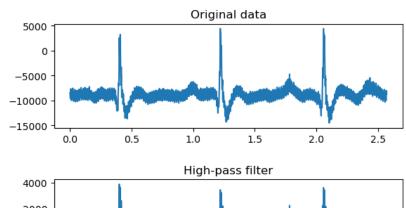


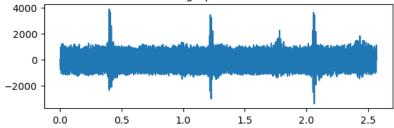




■ 고역 통과 필터(high-pass filter)

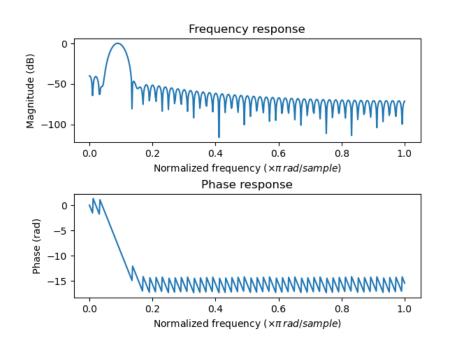


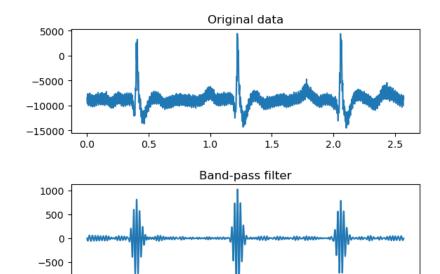






대역 통과 필터(band-pass filter)





1.0

1.5

2.0

2.5

2024. 03. 04.

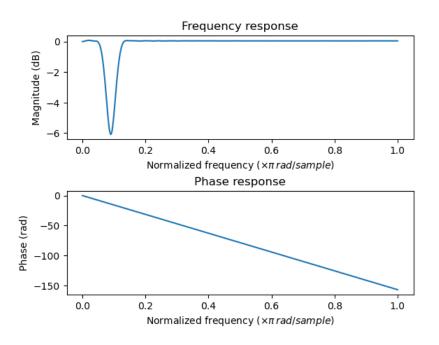
-1000

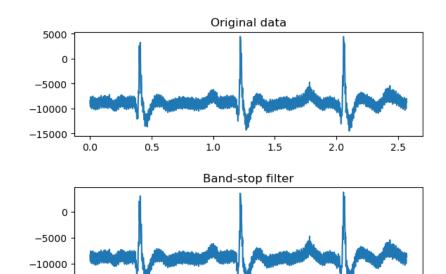
0.0

0.5



■ 대역 차단 필터(band-stop filter)





1.0

1.5

2.0

2.5

0.5

2024. 03. 04.

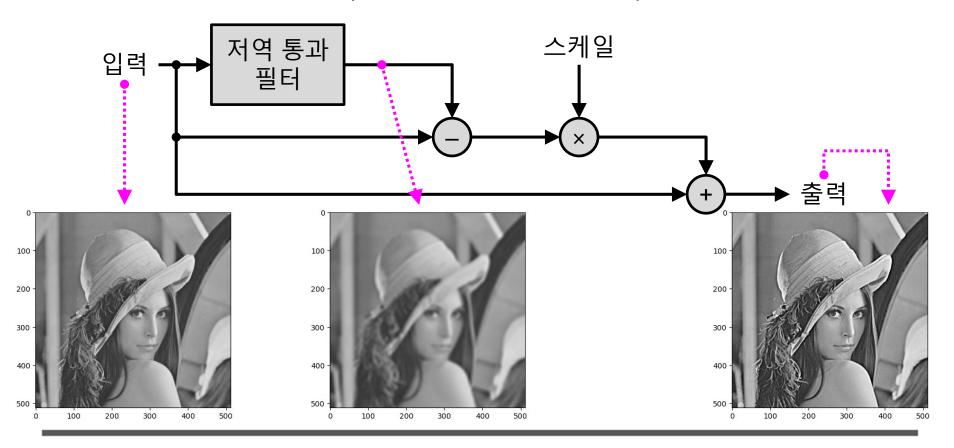
-15000

0.0

영상처리 시스템의 사례



■ 디테일 인핸스먼트(detail enhancement)



영상처리 시스템의 사례



