Improving Topic Coherence with Latent Feature Word Representations in MAP Estimation for Topic Modeling

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Abstract

Probabilistic topic models are widely used to discover latent topics in document collections, while latent feature word vectors have been used to obtain high performance in many natural language processing (NLP) tasks. In this paper, we present a new approach by incorporating word vectors to directly optimize the maximum a posteriori (MAP) estimation in a topic model. Preliminary results show that the word vectors induced from the experimental corpus can be used to improve the assignments of topics to words.

Keywords: MAP estimation, LDA, Topic model, Word vectors, Topic coherence

1 Introduction

Topic modeling algorithms, such as Latent Dirichlet Allocation (LDA) (Blei et al., 2003) and related methods (Blei, 2012), are often used to learn a set of latent topics for a corpus of documents and to infer document-to-topic and topic-to-word distributions from the co-occurrence of words within the documents (Wallach, 2006; Blei and McAuliffe, 2008; Wang et al., 2007; Johnson, 2010; Yan et al., 2013; Xie et al., 2015; Yang et al., 2015). With enough training data there is sufficient information in the corpus to accurately estimate the distributions. However, most topic models consider each document as a bag-of-words, i.e. the word order or the window-based local context information is not taken into account.

Topic models have also been constructed using latent features (Salakhutdinov and Hinton, 2009; Srivastava et al., 2013; Cao et al., 2015). Latent feature vectors have been recently successfully exploited for a wide range of NLP tasks (Glorot et al., 2011; Socher et al., 2013; Pennington et al., 2014). Rather than relying solely on word count information as the standard multinomial LDA does, or using only distributed feature representations, as in Salakhutdinov and Hinton (2009), Srivastava et al. (2013) and Cao et al. (2015), Nguyen et al. (2015) integrated pre-trained latent feature word representations containing external information from very large corpora into existing topic models and obtained significant improvements on small document collections and short text datasets. However, their implementation is computationally quite expensive because they have to compute a MAP estimate in each Gibbs sampling iteration.

In this paper, we experiment with MAP estimation using word vectors for LDA. Instead of mixing the Gibbs sampling and MAP estimation, we propose to optimize the MAP estimation of the full model directly. In addition, instead of using the pre-trained word vectors learned on external large corpora, we propose to learn the internal word vectors from the same topic-modeling corpus that we induce the document-to-topic and topic-to-word distributions from. In this manner, we can also handle the words that are not found in the list of the pre-trained word vectors. Furthermore, the internal word vectors can capture various aspects including word order information or local context information in the topic-modeling corpus. Preliminary results show that the internal word vectors can also help to significantly improve the topic-to-word assignments.

2 Related work

LDA (Blei et al., 2003) represents each document d in the document collection D as a mixture $\boldsymbol{\theta}_d$ over T topics, where each topic z is modeled by a probability distribution $\boldsymbol{\phi}_z$ over words in a vocab-

ulary W. As presented in Figure 1, where α and β are hyper-parameters, the generative process for LDA is described as follows:

$$\begin{aligned}
\boldsymbol{\theta}_d &\sim \mathrm{Dir}(\alpha) & z_{d_i} &\sim \mathrm{Cat}(\boldsymbol{\theta}_d) \\
\boldsymbol{\phi}_z &\sim \mathrm{Dir}(\beta) & w_{d_i} &\sim \mathrm{Cat}(\boldsymbol{\phi}_{z_{d_i}})
\end{aligned}$$

where Dir and Cat stand for a Dirichlet distribution and a categorical distribution, and z_{d_i} is the topic indicator for the ith word w_{d_i} in document d. Inference for LDA is typically performed by variational inference or Gibbs sampling (Blei et al., 2003; Griffiths and Steyvers, 2004; Teh et al., 2006; Porteous et al., 2008; Yao et al., 2009; Foulds et al., 2013).
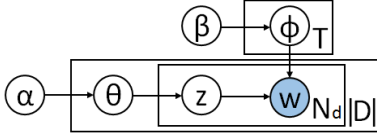

Figure 1: Graphical representation of LDA

When we ignore the Dirichlet priors and apply the Expectation Maximization (EM) algorithm to optimize the likelihood over the document-to-topic and topic-to-word parameters $\theta_{d,z}$ and $\phi_{z,w}$, we obtain the Probabilistic Latent Semantic Analysis model (Hofmann, 1999; Girolami and Kabán, 2003). Optimizing the MAP estimation for the LDA model has been suggested before. Chien and Wu (2008), Asuncion et al. (2009) and Taddy (2012) proposed EM algorithms for estimating $\theta_{d,z}$ and $\phi_{z,w}$, while we use direct gradient-based optimization methods. Sontag and Roy (2011) optimized the MAP estimates of $\phi_{z,w}$ and $\theta_{d,z}$ in turn by integrating out $\theta_{d,z}$ and $\phi_{z,w}$ respectively. We, on the other hand, estimate all parameters jointly in a single optimization step.

In addition to Taddy (2012)'s approach, applying MAP estimation to learn log-linear models for topic models is also found in Eisenstein et al. (2011) and Paul and Dredze (2015). Our MAP model is also defined in log-linear representation. However, unlike our MAP approach, those approaches do not use latent feature word vectors to characterize the topic-to-word distributions.

Furthermore, Berg-Kirkpatrick et al. (2010) proposed a direct optimization approach of the objective function for Hidden Markov Model-like generative models. However, they applied the approach to various unsupervised NLP tasks, such as part-of-speech induction, grammar induction, word alignment, and word segmentation, but not to topic models.

3 Direct MAP estimation approach

In this section, we describe our new direct MAP estimation approach using word vectors for LDA.

Following the likelihood principle, the document-to-topic and topic-to-word distributions $\boldsymbol{\theta}_d$ and $\boldsymbol{\phi}_z$ are determined by maximizing the log likelihood function:

$$\mathcal{L} = \sum_{d \in D} \sum_{w \in W} n_{d,w} \log \sum_z \theta_{d,z} \phi_{z,w} \quad (1)$$

where $n_{d,w}$ is the number of times the word type w appears in document d.

Estimating the parameters $\theta_{d,z}$ and $\phi_{z,w}$ in the original simplex space requires constraints: $\theta_{d,z} \geq 0, \phi_{z,w} \geq 0, \sum_z \theta_{d,z} = 1$ and $\sum_w \phi_{z,w} = 1$. In order to avoid those constraints and to improve estimation efficiency, we transfer the parameters into the natural exponential family parameterization. So we define $\theta_{d,z}$ and $\phi_{z,w}$ as follows:

$$\begin{aligned}
\theta_{d,z} &= \frac{\exp(\xi_{d,z})}{\sum_{z'} \exp(\xi_{d,z'})} \\
\phi_{z,w} &= \frac{\exp(\boldsymbol{v}_w \cdot \boldsymbol{\mu}_z + \psi_{z,w})}{\sum_{w' \in W} \exp(\boldsymbol{v}_{w'} \cdot \boldsymbol{\mu}_z + \psi_{z,w'})}
\end{aligned} \quad (2)$$

where $\boldsymbol{v}_w$ is the m-dimensional vector associated with word w, while $\boldsymbol{\mu}_z$ is the m-dimensional topic vector associated with topic z. Here $\boldsymbol{v}$ is fixed, and we will learn $\boldsymbol{\mu}$ together with $\boldsymbol{\xi}$ and $\boldsymbol{\psi}$.

With L_2 and L_1 regularizers, we have a new objective function as follows:

$$\begin{aligned}
\mathcal{L} = &\sum_{d \in D} \sum_{w \in W} n_{d,w} \log \sum_z \left(\frac{\frac{\exp(\xi_{d,z})}{\sum_{z'} \exp(\xi_{d,z'})} \times}{\frac{\exp(\boldsymbol{v}_w \cdot \boldsymbol{\mu}_z + \psi_{z,w})}{\sum_{w' \in W} \exp(\boldsymbol{v}_{w'} \cdot \boldsymbol{\mu}_z + \psi_{z,w'})}} \right) \\
&- \sum_{d \in D} \left(\lambda_2 \|\boldsymbol{\xi}_d\|_2^2 + \lambda_1 \|\boldsymbol{\xi}_d\|_1 \right) \\
&- \sum_z \left(\pi_2 \|\boldsymbol{\mu}_z\|_2^2 + \pi_1 \|\boldsymbol{\mu}_z\|_1 \right) \\
&- \sum_z \left(\epsilon_2 \|\boldsymbol{\psi}_z\|_2^2 + \epsilon_1 \|\boldsymbol{\psi}_z\|_1 \right)
\end{aligned} \quad (3)$$

The MAP estimate of the model parameters is obtained by maximizing the regularized log likelihood $\mathcal{L}$. The derivatives with respect to the parameters $\xi_{d,z}$ and $\psi_{z,w}$ are:

$$\begin{aligned}
\frac{\partial \mathcal{L}}{\partial \xi_{d,z}} = &\sum_{w \in W} n_{d,w} \mathrm{P}(z \mid w, d) - n_d \theta_{d,z} \\
&- 2\lambda_2 \xi_{d,z} - \lambda_1 \mathrm{sign}(\xi_{d,z})
\end{aligned} \quad (4)$$

where $P(z \mid w, d) = \frac{\theta_{d,z}\phi_{z,w}}{\sum_{z'} \theta_{d,z'}\phi_{z',w}}$, and n_d is the total number of word tokens in the document d.

$$\frac{\partial \mathcal{L}}{\partial \psi_{z,w}} = \sum_{d \in D} n_{d,w} P(z \mid w, d)$$
$$- \phi_{z,w} \sum_{d \in D} \sum_{w' \in W} n_{d,w'} P(z \mid w', d) \quad (5)$$
$$- 2\epsilon_2 \psi_{z,w} - \epsilon_1 \mathrm{sign}(\psi_{z,w})$$

And the derivative with respect to the jth element of the vector for each topic z is:

$$\frac{\partial \mathcal{L}}{\partial \mu_{z,j}} = \sum_{d \in D} \sum_{w \in W} n_{d,w} P(z \mid w, d) \left(v_{w,j} - \sum_{w' \in W} v_{w',j} \phi_{z,w'} \right)$$
$$- 2\pi_2 \mu_{z,j} - \pi_1 \mathrm{sign}(\mu_{z,j})$$
$$(6)$$

We used OWL-QN[1] (Andrew and Gao, 2007) to find the topic vector $\boldsymbol{\mu}_z$ and the parameters $\xi_{d,z}$ and $\psi_{z,w}$ that maximize $\mathcal{L}$.

4 Experiments

To investigate the performance of our new approach, we compared it with two baselines on topic coherence: 1) variational inference LDA (Blei et al., 2003); and 2) Gibbs sampling LDA (Griffiths and Steyvers, 2004). The topic coherence evaluation measures the coherence of the topic-to-word associations, i.e. it directly evaluates how the high-probability words in each topic are semantically coherent (Chang et al., 2009; Newman et al., 2010; Mimno et al., 2011; Stevens et al., 2012; Lau et al., 2014; Röder et al., 2015).

4.1 Experimental setup

We conducted experiments on the standard benchmark 20-Newsgroups dataset.[2]

In addition to converting into lowercase and removing non-alphabetic characters, we removed stop-words found in the stop-word list in the Mallet toolkit (McCallum, 2002). We then removed words shorter than 3 characters or words appearing less than 10 times. Table 1 presents details of the experimental dataset.

As pointed out in Levy and Goldberg (2014) and Pennington et al. (2014), the prediction-based methods and count-based methods for learning word vectors are not qualitatively different on a

Dataset	#docs	#w/d	$|\mathbf{W}|$
20-Newsgroups	18,820	105	20,940

Table 1: Details of the experimental dataset. #docs: number of documents; #w/d: the average number of words per document; $|\mathbf{W}|$: the number of word types.

range of semantic evaluation tasks. Thus, we simply use the Word2Vec toolkit[3] (Mikolov et al., 2013) to learn 25-dimensional word vectors on the experimental dataset, using a local 10-word window context.[4]

The numbers of topics is set to 20. For variational inference LDA, we use Blei's implementation.[5] For Gibbs sampling LDA, we use the jLDADMM package[6] (Nguyen, 2015) with common hyper-parameters $\beta = 0.01$ and $\alpha = 0.1$ (Newman et al., 2009; Hu et al., 2011; Xie and Xing, 2013). We ran Gibbs sampling LDA for 2000 iterations and evaluated the topics assigned to words in the last sample. We then used the document-to-topic and topic-to-word distributions from the last sample of Gibbs sampling LDA to initialize the parameters $\xi_{d,z}$ and $\psi_{z,w}$ while topic vectors $\boldsymbol{\mu}_z$ are initialized as zero vectors in our MAP learner. For our MAP approach, we set[7] $\lambda_2 = \pi_2 = 0.01$, $\lambda_1 = \pi_1 = 1.0e{-}6$, $\epsilon_2 = 0.1$ and $\epsilon_1 = 0.01$. We report the mean and standard deviation of the results of ten repetitions of each experiment.

4.2 Quantitative analysis

For a quantitative analysis on topic coherence, we use the normalized pointwise mutual information (NPMI) score. Lau et al. (2014) showed that human scores on a word intrusion task are strongly correlated with NPMI. A higher NPMI score indicates that the topic distributions are semantically more coherent.

Given a topic t represented by its top-N topic words $w_1, w_2, ..., w_N$, the NPMI score for t is:

$\mathrm{NPMI}(t) = \sum_{1 \leqslant i < j \leqslant N} \frac{\log \frac{P(w_i, w_j)}{P(w_i)P(w_j)}}{-\log P(w_i, w_j)}$, where the

Topic 1		Topic 2		Topic 12		Topic 18		Topic 19	
G-LDA	MAP+V	G-LDA	MAP+V	G-LDA	MAP+V	G-LDA	MAP+V	G-LDA	MAP+V
car	car	power	sale	game	game	space	space	medical	medical
<u>writes</u>	cars	sale	power	team	team	nasa	nasa	disease	disease
<u>article</u>	engine	<u>work</u>	**shipping**	year	games	gov	earth	<u>article</u>	health
cars	oil	battery	**offer**	games	year	earth	gov	health	food
engine	speed	radio	battery	hockey	play	<u>writes</u>	launch	drug	drug
<u>good</u>	miles	<u>good</u>	radio	<u>writes</u>	hockey	<u>article</u>	moon	food	cancer
oil	price	high	ground	play	players	launch	orbit	cancer	**doctor**
price	**dealer**	sound	sound	players	season	moon	shuttle	msg	drugs
speed	**ford**	ground	high	season	**win**	orbit	**mission**	drugs	msg
miles	**drive**	<u>writes</u>	**cable**	<u>article</u>	**baseball**	shuttle	**henry**	<u>writes</u>	**patients**

Table 3: Examples of the 10 most probable topical words on the 20-Newsgroups dataset. G-LDA → Gibbs sampling LDA; MAP+V → Our MAP approach using internal word vectors. The words found by G-LDA and not by MAP+V are <u>underlined</u>. The words found by MAP+V but not by G-LDA are in **bold**.

Method	Top-10	Top-15	Top-20
V-LDA	-4.2 ± 0.4	-12.2 ± 0.6	-24.1 ± 0.6
G-LDA	-4.2 ± 0.4	-11.7 ± 0.7	-22.9 ± 0.9
MAP-O	-3.8 ± 0.5	-10.8 ± 0.6	-22.1 ± 1.2
MAP+V	**-3.4 ± 0.3**	**-10.1 ± 0.7**	**-20.6 ± 1.0**
Improve.	0.8	1.6	2.3

Table 2: NPMI scores (mean and standard deviation) on the 20-Newsgroups dataset with different numbers of top topical words; V-LDA → Variational inference LDA; G-LDA → Gibbs sampling LDA; MAP-O → Our MAP learner where we fix topic vectors μ as zero vectors and only learn parameters ξ and ψ; MAP+V → Our MAP learner where we learn μ together with ξ and ψ. The *Improve.* row denotes the absolute improvement accounted for MAP+V over the best result produced by the baselines V-LDA and G-LDA.

probabilities are derived from a 10-word sliding window over an external corpus.[8] The NPMI score for a topic model is the average score for all topics.

Table 2 shows that our approach using internal word vectors MAP+V produces significantly higher[9] NPMI scores than the baseline variational inference LDA and Gibbs sampling LDA models. So this indicates that the word vectors containing internal context information from experimental dataset can help to improve topic coherence.

4.3 Qualitative analysis

This section provides an example of how our approach improves topic coherence. Table 3 com-

[9]Using the two sample Wilcoxon test, the improvement is significant (p < 0.01).

pares the top-10 words produced by the baseline Gibbs sampling LDA and our MAP+V approach on the 20-Newsgroups dataset. It is clear that all top-10 words learned with our MAP+V model are qualitatively more coherent. For example, topic 19 of the Gibbs sampling LDA model consists of words related to "medicine" together with other unrelated words, whereas our MAP+V approach produced a purer topic 19 only about "medicine."

On 20-Newsgroups dataset, it is common that the baseline variational inference LDA and Gibbs sampling LDA models include the frequent words such as "writes" and "article" as top topical words in many topics. However, our MAP+V model using the internal word vectors is able to exclude these words out of the top words in these topics.

5 Conclusions and future work

In this paper, we proposed a new approach of fully direct MAP estimation for the LDA topic model inference, incorporating latent feature representations of words. Preliminary results show that the latent feature representations trained from the experimental topic-modeling corpus can improve the topic-to-word mapping.

In future work, we plan to investigate the effects of the context window size as well as the size of the word vectors further. In addition, we plan to test our approach on a range of different datasets. We also plan to compare the presented results with Nguyen et al. (2015)'s model using internal word vectors. Even though we learn the internal word vectors from the experimental dataset, we believe that it is worth trying to initialize them from vectors learned from an external corpus, thus also incorporating generalizations from that corpus.

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