

Algorithms and Data Structures

Heap Sort, Queues (revisited)

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Spring 2019

Warm Up

Www.menti.com, check.

Hand-in Assignments, check.

Queues

Priority Queues

Heap Sort

Some Pretty Animations

Hand-in Assignment #3

Check on Content and Scope.

Work together in Classroom (if time permits)

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Weekly quiz

- ☐ Go to www.menti.com, and participate. Try to submit your answer *before* looking at the whiteboard.
- ☐ How did we do?

Hand-in assignment #3 (Airport Queue)

- ☐ Handed in? - Yes? - No?
- ☐ Conducted peer review on Hand-in #1? Yes? No?
- ☐ Are the assignments doable in finite time?

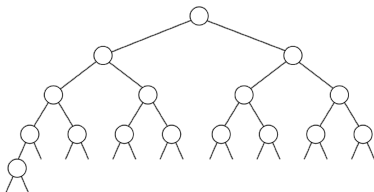
Interface of Priority Queues

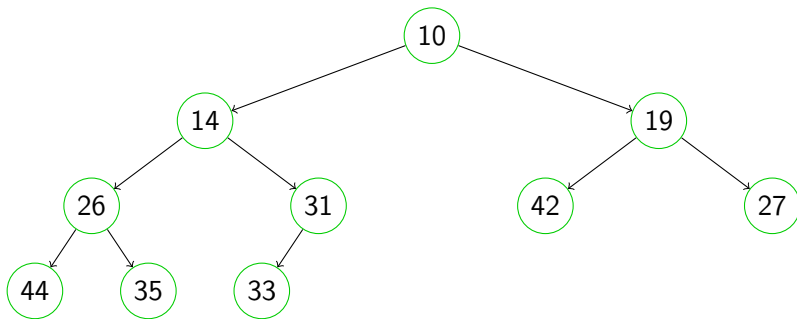
```
interface PriorityQueue<T extends Comparable<T>> {  
    void enqueue(T item);  
    T dequeue() throws NoSuchElementException;  
    T peek() throws NoSuchElementException;  
    int size();  
    default boolean isEmpty() { return size() == 0; }  
}
```

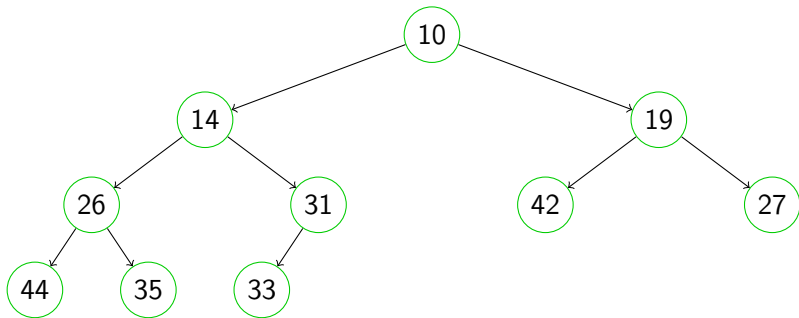
- Search for top item every time.
 - insert: $O(1)$
 - dequeue: $O(n)$
- Sort data structure, keep sorted at inserts
 - insert: $O(n)$
 - dequeue: $O(1)$
- **Use a semisorted structure, a heap**
 - **insert:** $O(\log n)$
 - **dequeue:** $O(\log n)$

Heaps are semisorted binary trees:

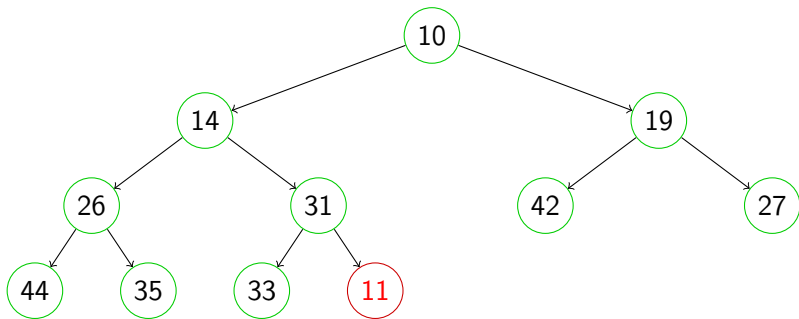
- Heap Root holds the extreme element (max/min)
- The branches of a heap are:
 - Heaps themselves
 - Empty nodes
- Heaps are balanced, they are *Complete Binary Trees*
- Filled from “left” to “right”



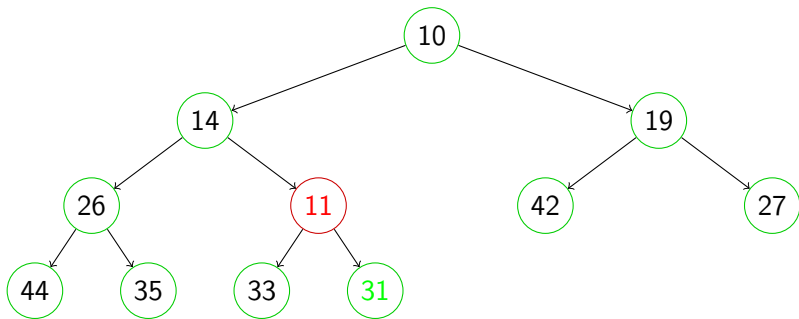




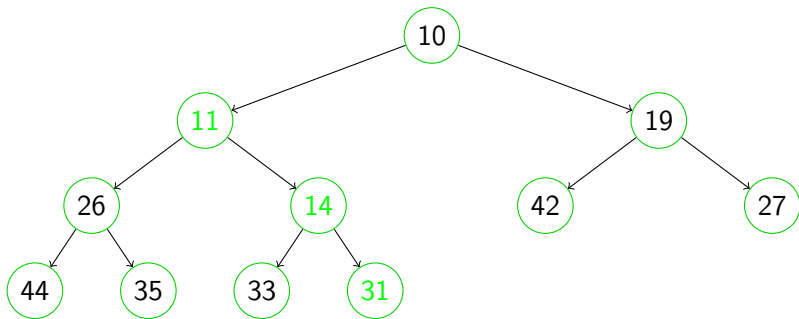
enqueue



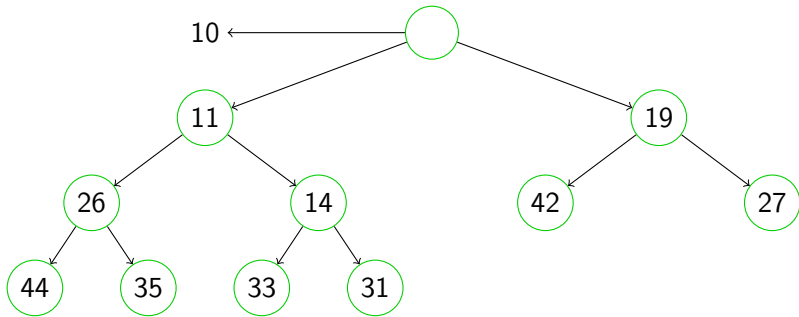
enqueue



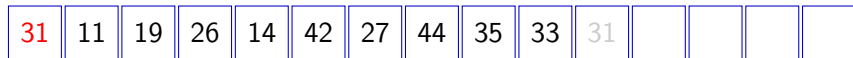
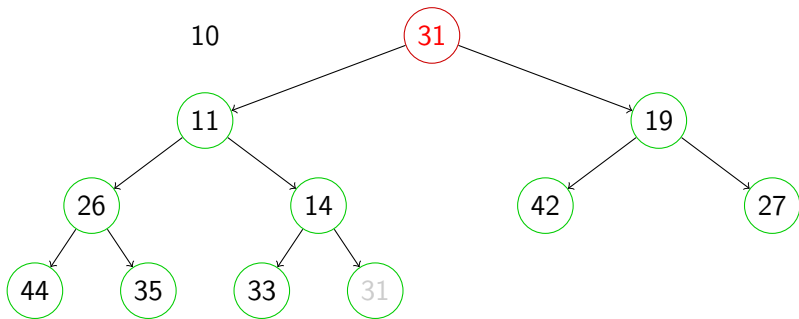
enqueue



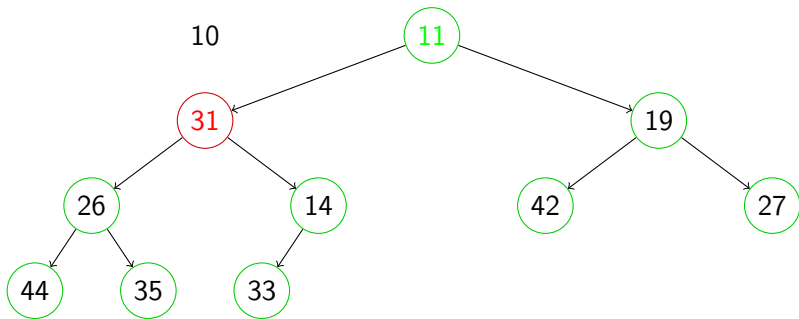
dequeue



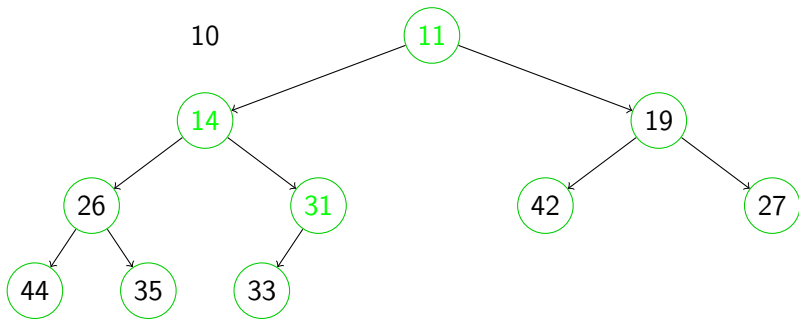
dequeue



dequeue

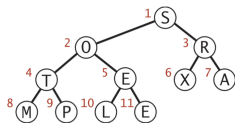


dequeue



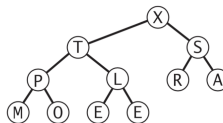
Heap Sort is a natural consequence of the heap data structure. It has two basic parts:

- **Heap Construction** (data are not in heap order), $\mathcal{O}(2N)$
- **Heap Sort-down**, $\mathcal{O}(2N \log N)$.



"Random" initial condition

| | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| S | O | R | T | E | X | A | M | P | L | E |



Heap Constructed

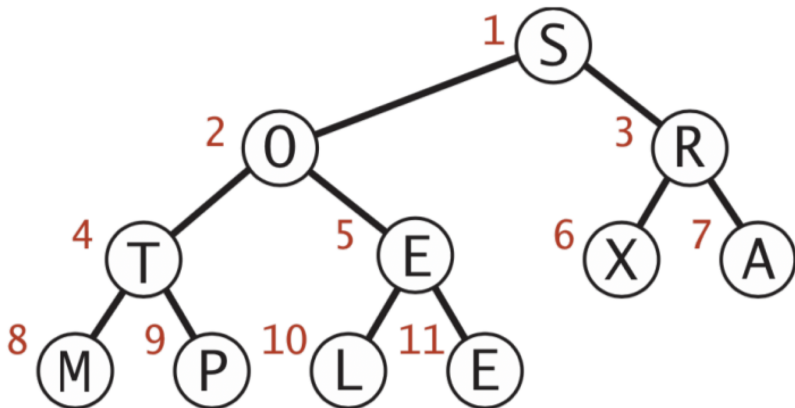
| | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| X | T | S | P | L | R | A | M | O | E | E |



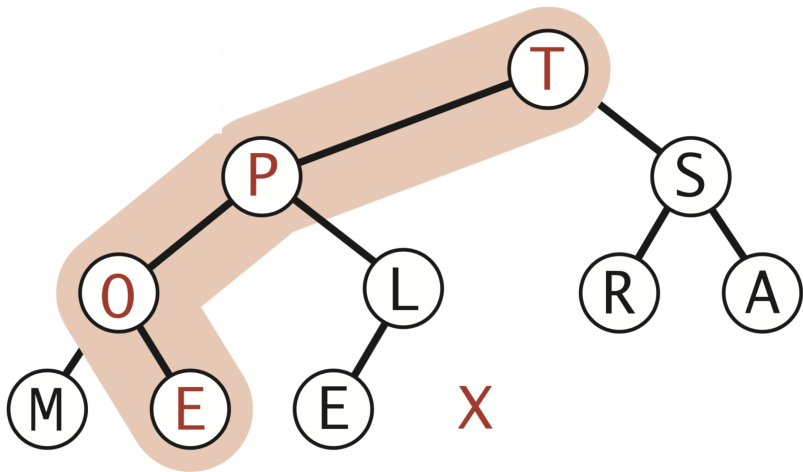
Array sorted

| | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| A | E | E | L | M | O | P | R | S | T | X |

Build the heap, bottom-up. Someone do it on the blackboard?



Sort the array by exchange/deletion + sinking top, to re-heapify.



By your own choice of method – i.e. pen+-pencil or whiteboard or computer – build a (max-oriented) heap from the keys:

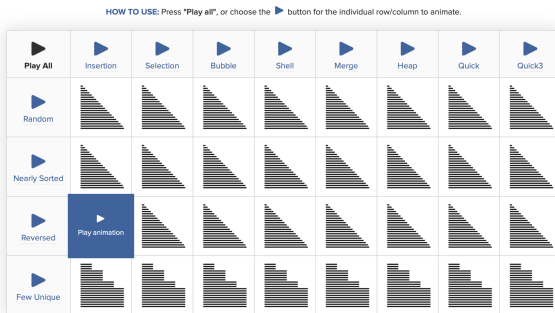
A M U C H L O N G R E X P T H N B F.

- Note that the characters above now are unique.
- There is some code which might help you in the repository `./cphbusiness/algorithm/examples/....`.
- If you use the helper code, try to make the code accept chars (instead of integers).

By your own choice of method – i.e. pen+pencil or whiteboard or computer – sort-down the heap from Exercise 1.

[Here is a nice animation](#) of the trace of fundamental algorithms.

<https://www.toptal.com/developers/sorting-algorithms>



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Airport Prioritized Queue

You *may* (but must not) use the template provided in the Week 09 folder on GitHub.

In groups:

Implement a prioritized queueing system for an airport. You can use any priority queue algorithm, but you must be able to argue that the time complexity is no worse than $O(\log n)$ for enqueue and dequeue respectively.

You should implement the priority queue in a setup that simulates passengers arriving to an airport, and passengers passing security.

Passenger priority can be derived from the passenger category and arrival time:

1. Late to flight
2. Business class
3. Disabled
4. Family
5. Monkey

Work together in Classroom (if time permits)