## ee21b137 week5

## March 8, 2023

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[]: | # Magic command below to enable interactivity in the JupyterLab interface
     %matplotlib ipympl
     # Some basic imports that are useful
     import numpy as np
     import matplotlib.pyplot as plt
     from matplotlib.animation import FuncAnimation
     fig, ax = plt.subplots()
     xdata, ydata = [], []
     ln, = ax.plot([], [], 'r')
[]: def init():
         ax.set_xlim(-1.2, 1.2)
         ax.set_ylim(-1.2, 1.2)
         return ln,
     def update(frame):
         if frame <= 1:xdata, ydata = morph(xs, ys, xt, yt, frame)</pre>
         elif frame <= 2:xdata, ydata = morph(xp, yp, xs, ys, frame-1)</pre>
         elif frame <= 3:xdata, ydata = morph(xh, yh, xp, yp, frame-2)
         elif frame <= 4:xdata, ydata = morph(xhp, yhp, xh, yh, frame-3)
         elif frame <= 5:xdata, ydata = morph(xo, yo, xhp, yhp, frame-4)
         elif frame <= 6:xdata, ydata = morph(xhp, yhp, xo, yo, frame-5)
         elif frame <= 7:xdata, ydata = morph(xh, yh, xhp, yhp, frame-6)
         elif frame <= 8:xdata, ydata = morph(xp, yp, xh, yh, frame-7)</pre>
         elif frame <= 9:xdata, ydata = morph(xs, ys, xp, yp, frame-8)
         elif frame <= 10:xdata, ydata = morph(xt, yt, xs, ys, frame-9)</pre>
         ln.set_data(xdata, ydata)
         return ln,
     def morph(x1, y1, x2, y2, alpha):
         xm = alpha * x1 + (1-alpha) * x2
         ym = alpha * y1 + (1-alpha) * y2
         return xm, ym
[]: def triangle(t):
         11 = int(len(t) / 4)
         ts = np.linspace(-0.5, 1, 11)
         ty = np.linspace(0,np.sqrt(3)/2,11)
         ty2 = (1-ts)/np.sqrt(3)
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xt = np.concatenate([-0.5*np.ones(11),ts,ts[::-1], -0.5*np.ones(11)])
         yt = np.concatenate([ty,ty2,-ty2[::-1],-ty[::-1]])
         return xt, yt
def square(t):
         xs = t
         ys = np.concatenate([1-np.absolute(xs[:100]),-1+np.absolute(xs[100:])])
         return xs, ys
def pentagon(t):
         tp = np.linspace(-0.68, 1, 67)
         tp0 = np.linspace(0,+0.514,33)
         xp = np.concatenate([-0.68*np.ones(33),tp,tp[::-1],-0.68*np.ones(33)])
         ty1 = 0.95+0.373*(tp[:46]-0.4567)
         ty2 = -1.85*(tp[46:]-1)
         yp = np.concatenate([tp0,ty1,ty2,-ty2[::-1],-ty1[::-1],-tp0[::-1]])
         return xp,yp
def hexagon(t):
         xh = t
         ty = np.sqrt(3)*(xh[:25]+1)
         yh = np.concatenate([ty,np.sqrt(3)/2*np.ones(50),ty[::-1],-ty,-np.sqrt(3)/
  42*np.ones(50),-ty[::-1]]
         return xh, yh
def heptagon(t):
         13 = int(len(t) / 2)
         th = np.linspace(-0.68, 1, 75)
         th0 = np.linspace(0,+0.434,25)
         th1 = th[::-1]
         xhp = np.concatenate([-0.901*np.ones(25),th,th[::-1],-0.901*np.ones(25)])
         theta = 3.14/7
         ty1 = np.sin(theta) + (1/np.tan(2*theta))*(th[:21]+np.cos(theta))
         ty2 = np.sin(2*theta)-np.tan(theta/2)*(th[21:58]-np.cos(2*theta))
         ty3 = (-1/np.tan(theta))*(th[58:] - 1)
         yhp = np.concatenate([th0,ty1,ty2,ty3,-ty3[::-1],-ty2[::-1],-ty1[::-1])
  ←-1],-th0[::-1]])
         return xhp, yhp
def octagon(t):
         theta = 3.14/4
         xo = t
         ty1 = (np.sin(theta)/(1-np.cos(theta)))*(xo[:15]+1)
         ty2 = 1 + (1-np.sin(theta))/np.cos(theta)*(xo[15:50])
         yo = np.concatenate([ty1,ty2,ty2[::-1],ty1[::-1],-ty1,-ty2,-ty2[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[::-1],-ty1[
   ⇔:-1]])
         return xo, yo
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[]: t = np.concatenate([np.linspace(-1,1,100),np.linspace(1,-1,100)])
if len(t) % 4 != 0:
    raise BaseException("Number of points should be multiple of 4...")
xt,yt = triangle(t)
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xs,ys = square(t)
xp,yp = pentagon(t)
xh,yh = hexagon(t)
xhp,yhp = heptagon(t)
xo,yo = octagon(t)
ani = FuncAnimation(fig, update, frames=np.linspace(0, 10, 400),
init_func=init, blit=True, interval=15, repeat=True)
plt.show()
```

## 0.1 Explanation

- Here i defined all 6 polygons as function differently.
- For all the polygon function i took 200 points.
- Triangle function is defined by taking x from -0.5 to 1. and constructing y values from left to right with corresponding x-values.
- similarly all the polygons are defined by getting y values from by deriving a function in terms of x.
- Here for all the polygons i got a constant for some x-values and straight line for another x-values.
- Those straight lines equation are provided manually by doing geometry.
- With the help of FuncAnimation() we can generate the frames and go to a update changes the x and y values such that these are in between the two shape then it will plot it.
- In morph function is used to generate x and y intermidate to provided x and y values.
- Interval is the time for one frame.it will be in milliseconds.

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