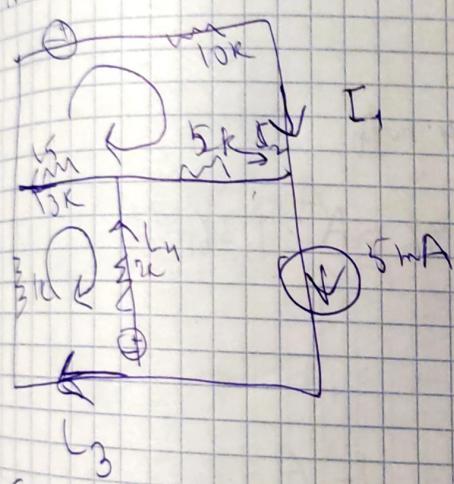


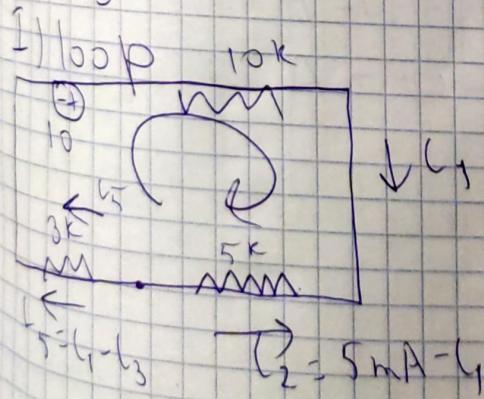
I. KCL & KVL



$$I_1 + I_2 = 5 \text{ mA}$$

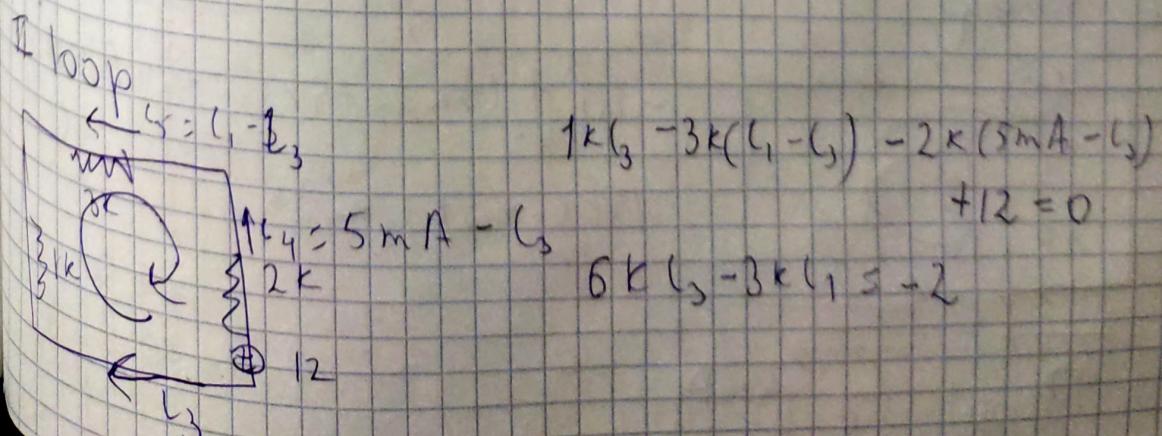
$$I_3 + I_4 = 5 \text{ mA}$$

$$I_3 + I_5 = I_1$$



$$-10 + 10k(I_1 - 5\text{mA} - I_1) + 3k(I_1 - I_2) = 0$$

$$18kI_1 - 3kI_3 = 35$$



$$1kI_3 - 3k(I_1 - I_3) - 2k(5\text{mA} - I_3) + 12 = 0$$

$$6kI_3 - 3kI_1 = -2$$

$$18kC_1 - 3kC_3 = 35$$

$$6kC_2 - 3kC_1 = -2$$

$$38kC_1 = 68$$

$$C_1 = 2.06 \text{ mA}$$

$$C_2 = 5 \text{ mA} - C_1$$

$$C_2 = 2.94 \text{ mA}$$

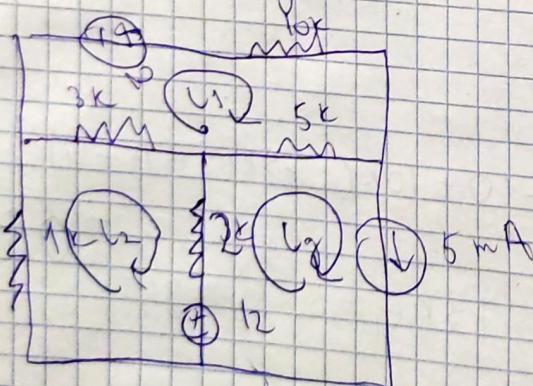
$$C_3 = (-2 + 3k \cdot 2.06 \text{ mA}) \cdot \frac{1}{6}$$

$$C_3 = \frac{4.18 \text{ mA}}{6} = 0.696 \text{ mA}$$

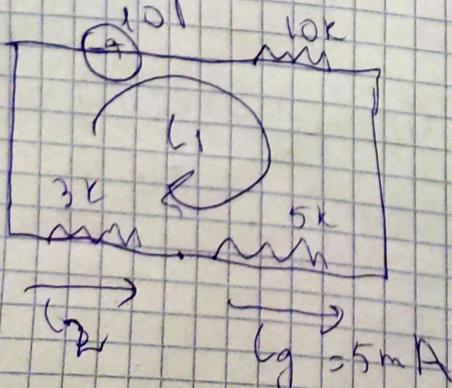
$$I_u = 5 - 0.696 \text{ mA} = 4.304 \text{ mA}$$

$$C_5 = -C_3 + C_1 = 2.06 \text{ mA} - 0.696 \text{ mA} = 1.364 \text{ mA}$$

## 2. Mesh Analysis



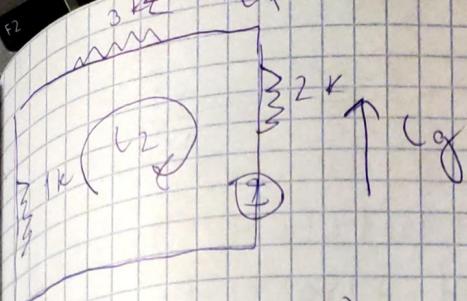
[ Loop 1 ]



$$-10 + 10k \cdot I_1 + 5k(C_1 - 5 \text{ mA}) + 3k(C_1 - 5 \text{ mA}) = 0$$

$$18kC_1 - 3kC_2 = 35$$

= 0



$$1k \cdot l_2 + 3k(l_2 - l_1) + 2k(l_2 - 5mA) + l_2 = 0$$

$$6k l_2 - 3k l_1 = -2$$

$$18k l_1 - 3k l_2 = 35$$

$$6k l_2 - 3k l_1 = -2$$

$$33k l_1 = 68$$

$$l_1 = 2.06 \text{ mA} \quad (l_{R_4})$$

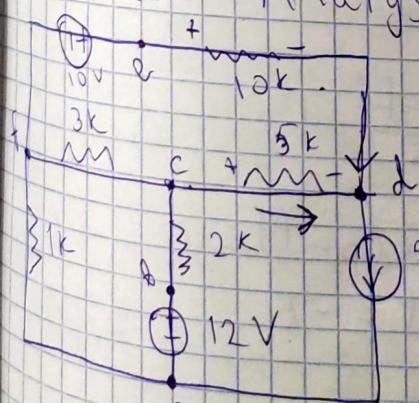
$$l_2 = 0.696 \text{ mA} \quad (l_{R_1})$$

$$l_{n_5} = l_2 = l_1 = -1.364 \text{ mA}$$

$$l_{R_2} = 5 \text{ mA} - l_2 = 4.304 \text{ mA}$$

$$l_{R_3} = 5 \text{ mA} - l_1 = 2.94 \text{ mA}$$

### 3. Nodal Analysis



I) node d.

$$5 \text{ mA} = \frac{c-d}{5k} + \frac{e-d}{10k}$$

$$\frac{c-d}{25} + \frac{e-d}{50} = 1$$

$$2(c-d) + (10 + f - d) = 50$$

$$2c - 3d + f = 40$$

$$e - f = 10$$

$$f - a = 12$$

II) node c

$$\frac{d-c}{3k} + \frac{f-c}{2k} = \frac{c-f}{10k}$$

$$6(d-c) + 15(12+a-c) = 10(c-f)$$

$$-31c + 6d + 15a + 10f = -180$$

$$f-a = 12$$

III) node f-e (supernode)

$$\frac{c-f}{3k} + \frac{a-f}{1k} = \frac{(10+f)-d}{10k}$$

$$10(c-f) + 30(a-f) = 3(10+f-d)$$

$$10c - 43f + 3d + 30a = 30$$

$$e-f = 10$$

IV) node b-a (supernode)

$$\frac{b-c}{2k} + \frac{a-f}{1k} = 5mA$$

$$\frac{b-c}{10} + \frac{a-f}{5} = 1$$

$$a+12-c + 2(a-f) = 10$$

$$3a - c - 2f = -2$$

$$b = a + 12$$

V) Solve linear equation

$$2c - 3d + f = 40$$

$$-31c + 6d + 15a + 10f = -180$$

$$10c - 43f + 3d + 30a = 30$$

$$3a - \frac{2c}{2} - 2f = -2$$

$$\begin{array}{r} 0 \ 2 \ -3 \ 1 \ 40 \\ 0 \ -31 \ 6 \ 10 \ -180 \\ 15 \ 10 \ 3 \ -43 \ 30 \\ 30 \ 10 \ 3 \ -2 \ -2 \\ 3 \ -1 \ 0 \end{array}$$

$$1 \ -\frac{31}{15} -\frac{1}{25} -\frac{2}{3} -12$$

$$\begin{array}{r} 0 \ 2 \ -3 \ 1 \ 40 \\ 0 \ 10 \ 3 \ -4 \ 30 \\ 30 \ -1 \ 0 \ -2 \ -2 \end{array}$$

$$\begin{array}{r} 0 \ -\frac{93}{15} +1 \ -\frac{1}{25} \ 0 \ -34 \\ 0 \ 2 \ -3 \ 1 \ 40 \\ 24 \ 12 \ 3 \ 0 \ 34 \\ 3 \ -1 \ 0 \ -2 \ -2 \end{array}$$

$$\begin{array}{r} 0 \ 2 \ -3 \ 1 \ 40 \\ 24 \ 13 \ -\frac{93}{15} \ 36 \ 0 \ 0 \\ 3 \ -1 \ 0 \ -2 \ 2 \end{array}$$

$$2c = 3d - f + 40$$

$$\frac{62}{15}c = -24a + (-36)d$$

$$c = 3a - 2f - 2$$

$$6a - 4f - 4 = 3d - f + 40$$

$$\begin{array}{r} 0 \ -\frac{93}{15} -\frac{1}{25} \ 0 \ -34 \\ 0 \ \frac{2}{15} +\frac{93}{15} -1 \ 0 \ \frac{1}{15} \ \frac{40}{15} +34 \\ \frac{24}{15} \ \frac{12}{15} -\frac{93}{15} +1 \ 0 \ 0 \ \frac{34}{15} -34 \\ 3 \ -1 \ 0 \ -2 \ -2 \\ 0 \ -\frac{93}{15} -6 \ 0 \ -510 \\ 0 \ 4 +93 -15 \ 0 \ 2 \ 80 +510 \\ 48 \ 24 -93 +15 \ 0 \ 0 \ 68 +510 \\ 3 \ (-1 +4 +93 -15) \ 0 \ 0 \ 78 +510 \\ 1 \ -\frac{31}{15} +\frac{1}{25} +\frac{2}{3} -12 \end{array}$$

$$\begin{array}{r} 1 \ -1,5 +0,5 \ 0 \ 20 \\ 0 \ 0 \ 1 \ -1 \ -\frac{350}{33} \\ \hline \end{array}$$

$$\begin{array}{r} 1 \ 0 \ 0 \ -1 \ \frac{23}{33} \\ 0 \ 1 \ 0 \ -1 \ \frac{45}{11} \\ 0 \ 0 \ 1 \ -1 \ -\frac{350}{33} \\ \hline \end{array}$$

$$a - f = \frac{22}{33}$$

$$B_f = \frac{45}{11}$$

$$d - f = -\frac{350}{33}$$

$$c - d = \frac{485}{33}$$

$$I_{R_3} = \frac{485}{33 \cdot 5k} = 2,94 \text{ mA}$$

$$I_{R_1} = \frac{22}{33 \cdot 1k}$$

$$0,696 \text{ mA}$$

$$c + 5k = d$$

$$I_{R_5}$$

$$3k \text{ min } c$$

$$I_{R_5} = \frac{45}{11 \cdot 3k} = 1,364 \text{ mA}$$

$$I_{R_2}$$

$$f - a = 12$$

$$c - f = \frac{45}{11}$$

$$a - f = \frac{22}{33}$$

$$c - a = \frac{113}{33}$$

$$c$$

$$2k$$

$$f$$

$$f - a = 12$$

$$c - a = \frac{113}{33}$$

$$\frac{f - c}{2k} = 12 - \frac{113}{33}$$

$$\frac{2k}{2k} = 4,304 \text{ mA}$$

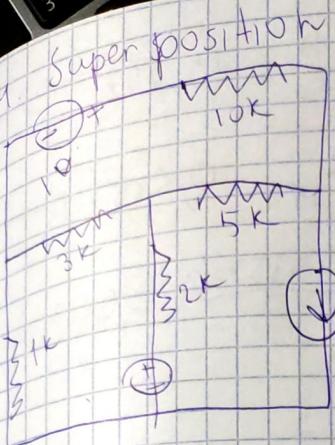
$$d - f = -\frac{350}{33}$$

$$d - e + 10 = \frac{350}{33}$$

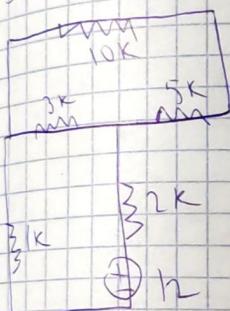
$$I_{e_1} = \frac{-\frac{350}{33} + 10}{10k} = 2,06 \text{ mA}$$

$$e \text{ } 10k$$

$$d$$



↓) Switching on  $V_3$



$$V_{eq} = 1k + 2k + \frac{15k \cdot 3k}{18k} = 5,5k$$

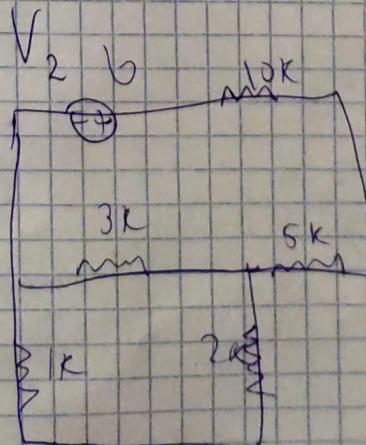
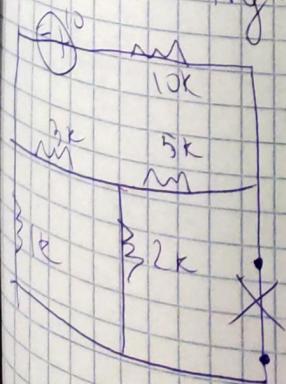
$$I_{R_2} = I_{R_1} = \frac{12}{5,5k} = 2,18mA$$

$$I_{R_3} = I_{R_4} = \frac{12 - 3 \cdot 2,18mA}{15k} = 0,364mA$$

$$I_{R_5} = \frac{12 - 3 \cdot 2,18}{3k} = 1,82mA$$



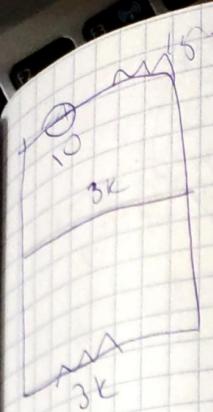
5) Switching on



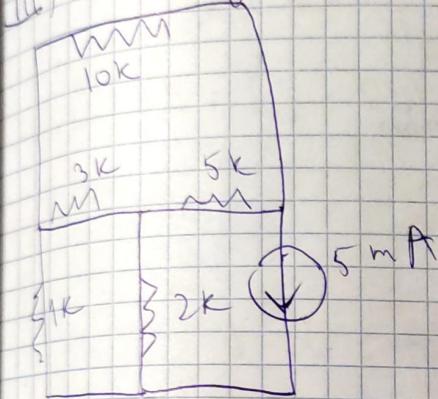
$$R_{eq} = 15k + \frac{3k \cdot 3k}{6k} = 15k + 1,5k = 16,5k$$

$$I_{res} = I_{R3} = 0,606 \text{ mA}$$

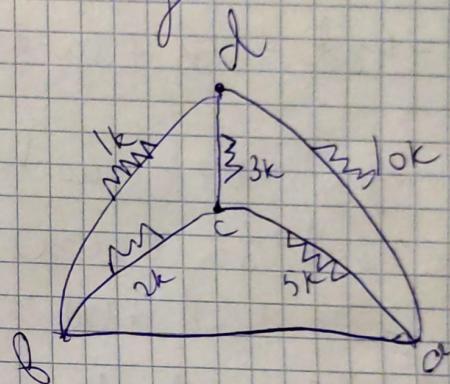
$$I_{R5=R2=R1} = 0,303 \text{ mA} = \frac{0,606 \text{ mA}}{2}$$



III) switching on  $I_1$



Redrawing

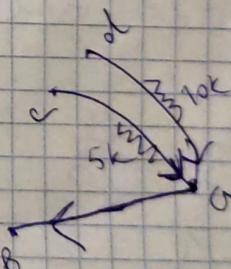


Need to solve it by Nodal analysis

I) node a

$$\frac{d-a}{10k} + \frac{c-a}{5k} = 5 \text{ mA}$$

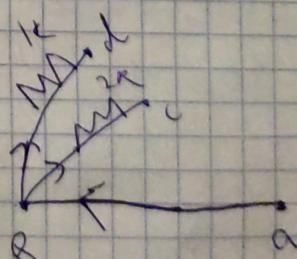
$$-3a + 2c + d = 50$$



II) node f

$$\frac{b-f}{2k} + \frac{f-d}{1k} = 5 \text{ mA}$$

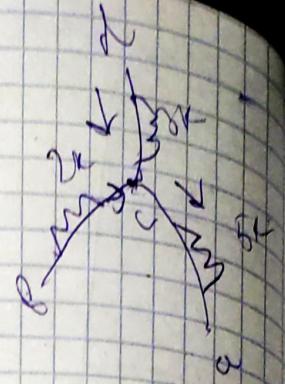
$$3f - c - 2d = 10$$



III node c

$$\frac{d-c}{3k} + \frac{f-c}{2k} - \frac{c-a}{5k}$$

$$6a - 31c + 15f + 10d = 0$$



IV) node d

$$\frac{b-d}{10k} = \frac{d-a}{10k} + \frac{d-c}{3k}$$

$$-43d + 3ab + 3a + 10c = 0$$

V) Solving the linear equation

$$-43d + 3ab + 3a + 10c = 0$$

$$6a - 31c + 15f + 10d = 0$$

$$3b - \frac{3c}{3} - 2d = 10$$

$$-3a + 2c + d = 50$$

$$\begin{array}{r} 1 \ 0 -\frac{2}{3} -\frac{1}{3} -\frac{50}{3} \\ 0 \ 3 -1 -2 \ 10 \\ 6 \ 15 -21 \ 10 \ 0 \\ 3 \ 30 \ 10 -43 \ 0 \end{array}$$

$$\begin{array}{r} 1 \ 0 -\frac{2}{3} -\frac{1}{3} -\frac{50}{3} \\ 0 \ 1 -\frac{1}{3} -\frac{2}{3} \frac{10}{3} \\ 0 \ 0 -22 \ 22 \ 50 \end{array}$$

$$\begin{array}{r} 1 \ 0 -\frac{2}{3} -\frac{1}{3} -\frac{50}{3} \\ 0 \ 3 -1 -2 \ 10 \\ 0 \ 15 -24 \ 12 \ 100 \\ 0 \ 30 \ 12 -42 \ 150 \end{array}$$

$$\begin{array}{r} 0 \ 0 22 -22 -50 \\ 1 \ 0 \frac{2}{3} \frac{1}{3} -\frac{50}{3} \\ 0 \ 1 -\frac{1}{3} -\frac{2}{3} \frac{10}{3} \\ 0 \ 0 -1 -1 -\frac{25}{11} \end{array}$$

$$a-d = -\frac{200}{11}$$

$$b-d = \frac{85}{33}$$

$$c-d = -\frac{25}{11}$$

$I_{R4}$

$$a-d = -\frac{200}{11}$$

$\downarrow d$

$$d-a = \frac{200}{11}$$

$\begin{cases} \uparrow 10k \\ \downarrow a \end{cases}$

$$I_{R4} = \frac{200}{11 \cdot 10k} = 1,82 \text{ mA}$$

$I_{R3}$

$$a-d = -\frac{200}{11}$$

$\begin{cases} \uparrow c \\ \downarrow 5k \end{cases}$

$$c-d = -\frac{25}{11}$$

$\downarrow a$

$$c-a = -\frac{25}{11} + \frac{200}{11} = \frac{175}{11}$$

$$I_{R3} = \frac{175}{11 \cdot 5k} = 3,18 \text{ mA}$$

$I_{R2}$

$\begin{cases} \uparrow b \\ \downarrow 2k \end{cases}$

$$b-d = \frac{85}{33}$$

$$b-c = \frac{160}{33}$$

$\begin{cases} \uparrow c \\ \downarrow b \end{cases}$

$$c-d = -\frac{25}{33}$$

$$I_{R2} = \frac{160}{33 \cdot 2k} = \frac{1,67 \text{ mA}}{2,42 \text{ mA}}$$

$I_{R1}$

$\begin{cases} \uparrow b \\ \downarrow 1k \end{cases}$

$$b-d = \frac{85}{33}$$

$\downarrow d$

$$I_{R1} = \frac{85}{33 \cdot 1k} = 2,57 \text{ mA}$$

$$I_{R_5} =$$

$$\left| \begin{array}{l} a \\ b \\ c \end{array} \right| 3k$$

$$d - c = \frac{25}{11}$$

$$I_{R_5} = \frac{25}{11 \cdot 3k} = 0,757 \text{ mA}$$

IV) Superposition principle.

$$I_{R_4} = 1,82 \text{ mA} + 0,606 \text{ mA}$$

$$- 0,364 \text{ mA}$$

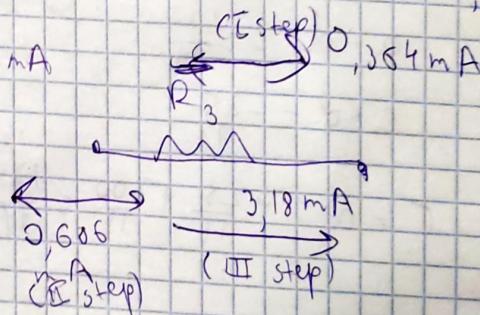
$$2,062 \text{ mA}$$



$$I_{R_3} = 3,18 \text{ mA} - 0,606 \text{ mA}$$

$$+ 0,364 \text{ mA} =$$

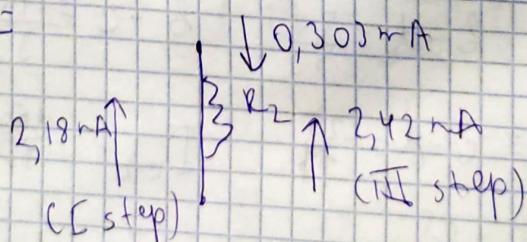
$$2,938 \text{ mA}$$



$$I_{R_2} =$$

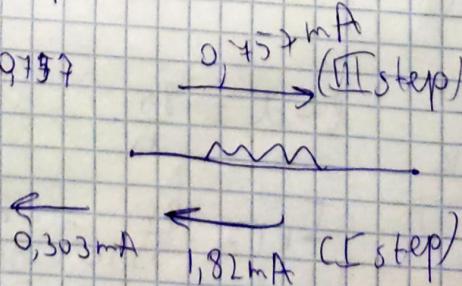
$$2,42 + 2,18 - 0,303 =$$

$$4,297 \text{ mA}$$



$$I_{R_5} = 1,82 \text{ mA} + 0,303 - 0,757$$

$$= 1,366 \text{ mA}$$



$$I_{e1} = 2.57 + 0.303 - 2.18 = 0.693 \text{ mA}$$

(III step)

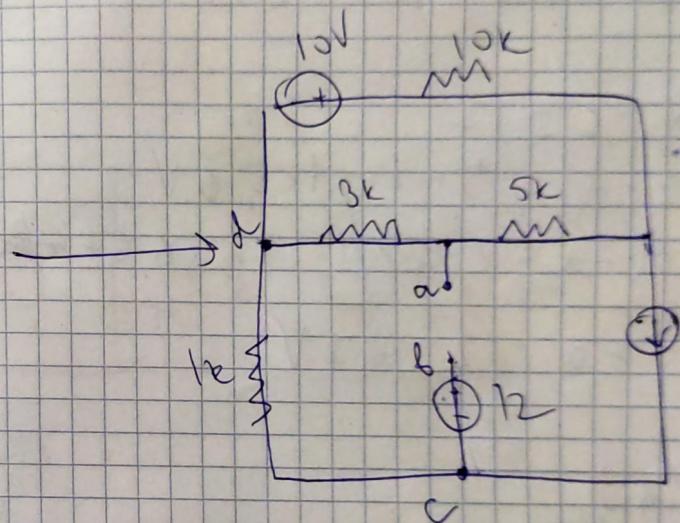
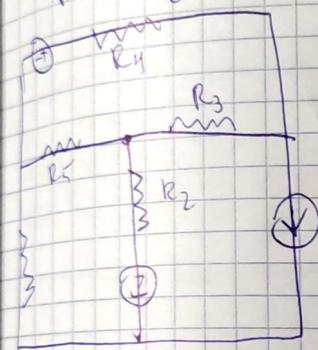
$2.57 \text{ mA} \uparrow$   
 $(\text{III step})$

$\left\{ \begin{array}{l} 1\text{k} \\ 1\text{k} \end{array} \right\} \downarrow 2.18 \text{ mA}$

$\uparrow 0.303 \text{ mA}$

5. Thevenin method

finding  $I_{e2}$

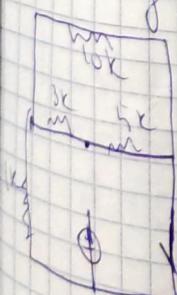


i) finding  $V_{th}$

ii) finding  $V_{d-c}$

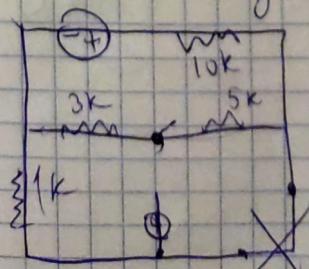
by super position

Turning off  $V_2$

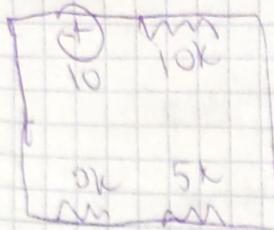


As we can observe,  
 $I_{R_1} = 5 \text{ mA}$      $I_{R_{10}} = \frac{10}{18} \cdot 5 \text{ mA} = 2.78 \text{ mA}$

Turning off current source



$I_{R_1} = 0 \text{ mA}$

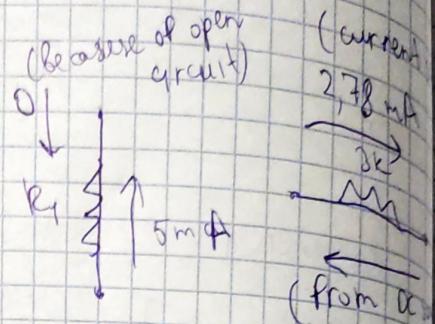


$$I_{R5} = \frac{10}{18} = 0,56 \text{ mA}$$

By Superposition,

$$I_{R1} = 5 \text{ mA} - 0 = 5 \text{ mA}$$

$$I_{R5} = 2,78 - 0,56 = 2,22 \text{ mA}$$

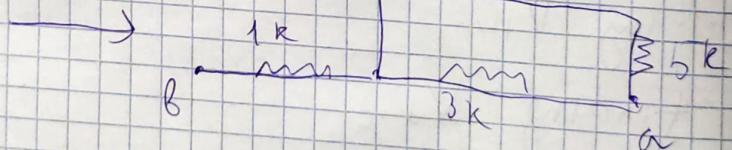
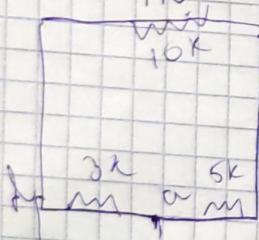


$$+ c - d = 5 \text{ mA} \cdot 1k = 5 \text{ V}$$

$$+ d - a = 2,22 \text{ mA} \cdot 3k = 6,67 \text{ mA} \checkmark$$

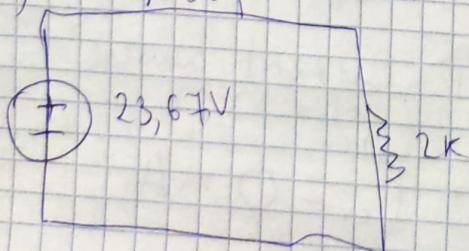
$$V_u = b - a = 23,67 \text{ V}$$

2)  $R_{th}$



$$R_{th} = 1k + \frac{15k \cdot 3k}{18k} = 3,5k$$

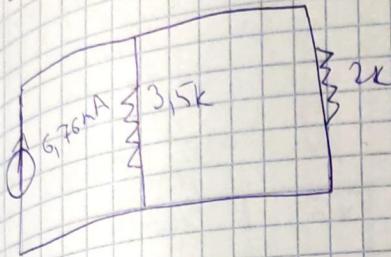
3)



$$I_{R2} = \frac{23,67}{5,5k} = 4,303 \text{ mA}$$

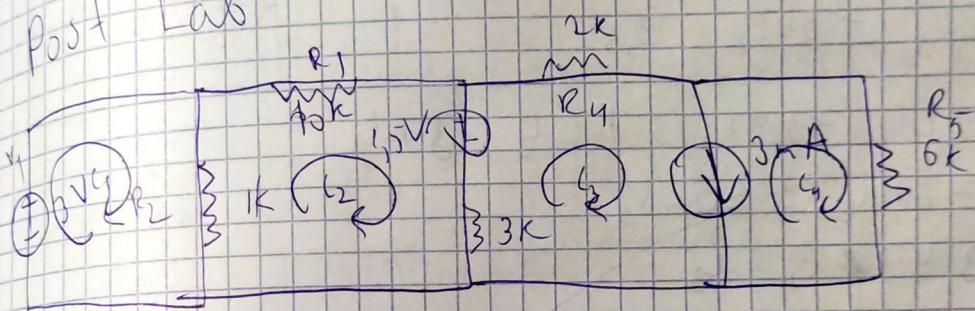
## 6. Norton's theorem

$$I_N = \frac{V_L}{R_L} = \frac{23,67}{3,5k} = 6,76mA$$



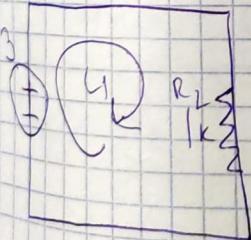
$$I_{R_2} = \frac{3,5}{5,5} \cdot 6,76mA = 4,302mA$$

Post Lab



i) Mesh Analysis

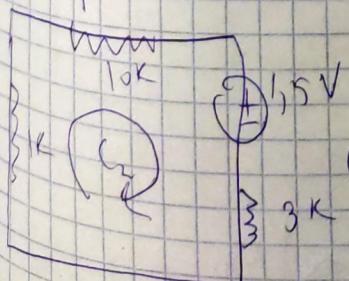
loop 1



$$-3 + 1k(C_1 - C_2) = 0$$

$$C_1 - C_2 = 3mA$$

loop 2

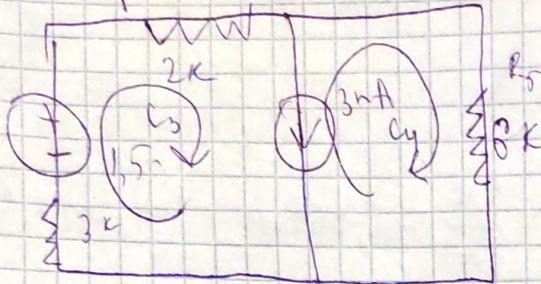


$$10k(C_2 + 1,5 + 3k(C_2 - C_3) + 1k(C_2 - C_1)) = 0$$

$$13k(C_2 + 1,5 - 3kC_3 + 1k(-3mA)) = 0$$

$$13kC_2 - 3kC_3 = 1,5$$

Loop 3



$$3k(l_3 - l_2) - 1,5 + 2k l_3 + 6k l_4 = 0$$

$$R_5 \quad 11k l_3 - 3k l_2 - 19,5 = 0$$

$$3k l_4 = l_2$$

$$l_4 = l_3 - 3\text{mA}$$

$$13k l_2 - 3k l_3 = 1,5 \quad | \cdot 13$$

$$11k l_3 - 3k l_2 = 19,5$$

$$169k l_2 - 39k l_3 = 11k l_3 - 3k l_2$$

$$172k l_2 = 50k l_3$$

$$3,44 l_2 = l_3$$

$$13k l_2 - 3k \cdot 3,44 l_2 = 1,5$$

$$l_2 = \frac{1,5}{13k - 3k \cdot 3,44} = 0,559 \text{ mA}$$

$$l_3 = 3,44 \cdot 0,559 = 1,925 \text{ mA}$$

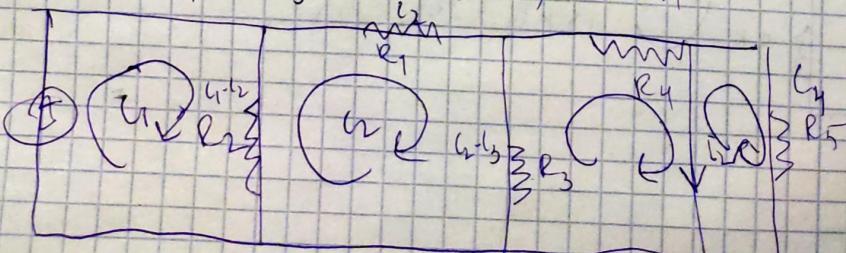
$$I_{R1} = l_2 = 0,559 \text{ mA}$$

$$I_{R4} = l_3 = 1,925 \text{ mA}$$

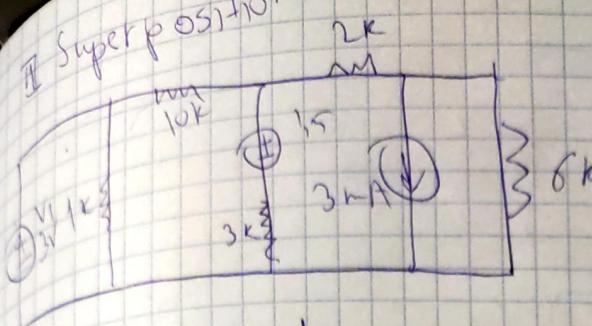
$$I_{R3} = l_2 - l_3 = -1,366 \text{ mA}$$

$$I_{R2} = l_1 - l_2 = 3 \text{ mA}$$

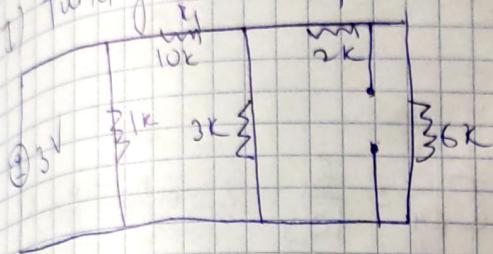
$$I_{R5} = l_4 = l_3 - 3\text{mA} = -1,075 \text{ mA}$$



II Superposition



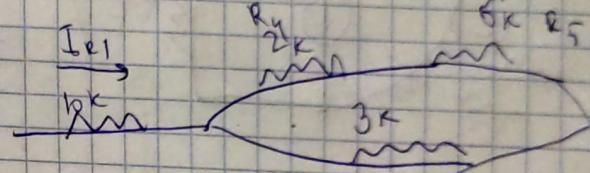
I) turning on  $V_1$



$$R_{eq}(\text{right side}) = 10k + \frac{8k \cdot 3k}{11k} = 12,18k$$

$$I_{R1} = \frac{3}{12,18k} = 0,246 \text{ mA}$$

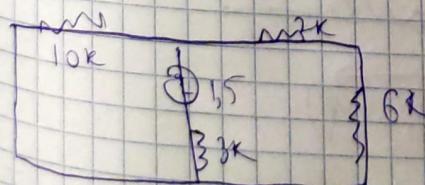
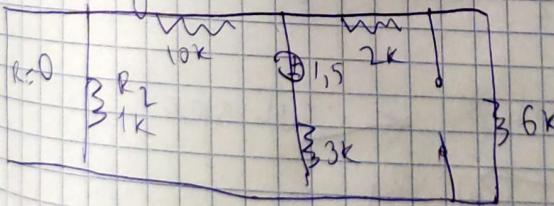
$$I_{R4} = I_{R5} = \frac{3}{11} \cdot 0,246 = 0,067 \text{ mA}$$



$$I_{R3} = 0,179 \text{ mA}$$

$$I_{R2} = \frac{3}{1k} = 3 \text{ mA}$$

II Turning on  $V_2$



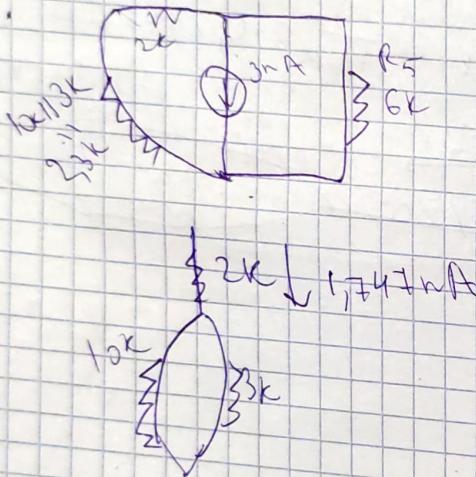
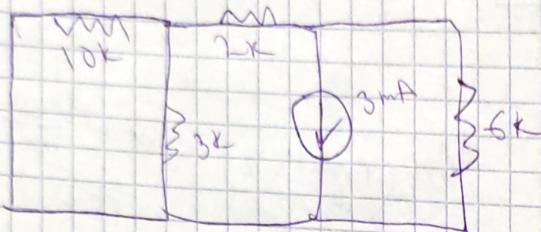
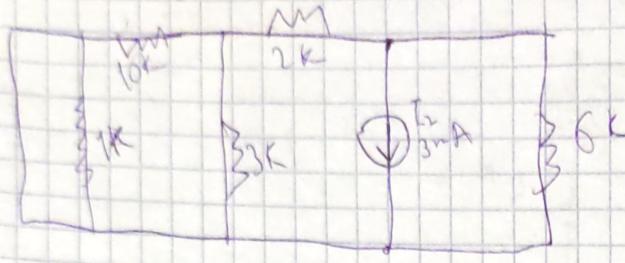
$$R_{eq} = 3 \cdot \frac{10k \cdot 8k}{18k} = 4,44k + 3k = 7,44k$$

$$I_{R3} = \frac{1,5 \text{ V}}{7,44k} = 0,2 \cdot 10^{-3} \text{ A}$$

$$V = 0,9 \text{ V} = 1,5 - 0,2 \text{ mA} \cdot 3 \text{ k}$$

$$I_{R4} = I_{R5} = \frac{0,9 \text{ m}}{8k} = 0,1125 \text{ mA} \quad I_{R1} = \frac{0,9}{10k} = 0,09 \text{ mA}$$

### III. Turning on $I_2$



$$I_{R4} = \frac{6}{10k} \cdot 2,3 \text{ mA} = 1,344 \text{ mA}$$

$$I_{R5} = \frac{4,2}{10k} \cdot 2,3 \text{ mA} = 1,25 \text{ mA}$$

$$I_{R3} = 1,344 \text{ mA}$$

$$I_{R1} = 0,403 \text{ mA}$$

$$I_{R2} = 0$$

IV) Applying Superposition

$$I_{R1} = 0,403 + 0,246 \xrightarrow{\text{(II step)}} R_1 \xrightarrow{\text{(III step)}} R_1$$

$$- 0,09 = 0,559 \text{ mA} \xrightarrow{\text{(IV step)}} R_2$$

$$I_{R2} = 3 \text{ mA}$$

$$(E \text{ step}) \xrightarrow{\sum R^2} \text{II step, III step} = I = 0$$

$$I_{C3} = 1,344 + 0,2 - 0,1793 = 1,365 \text{ mA}$$

↓ 0,1793  
 ↑ 0,2 mA  
 } R\_3 \uparrow 1,344 \text{ mA}

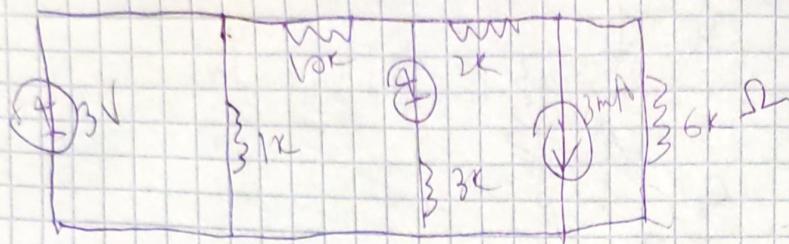
$$I_{R4} = 1,747 + 0,1125 + 0,067 = 1,939 \text{ mA}$$

→ 1,747 mA  
 ← 0,067 → 0,1125 mA

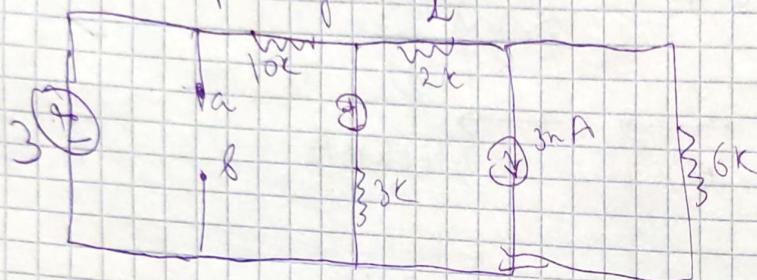
$$I_{R5} = 1,25 - 0,1125 - 0,067 = 1,061 \text{ mA}$$

↓ 0,067 mA  
 } R\_5 \downarrow 0,1125 mA  
 ↑ 1,25 mA

# Norton's Theorem

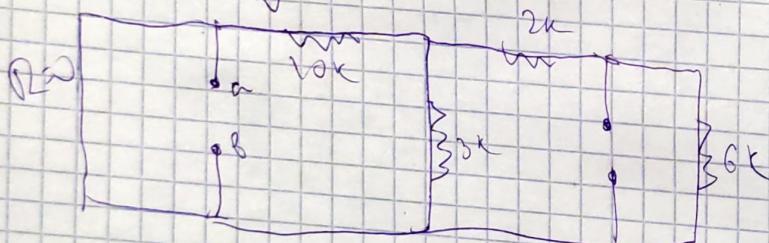


II) Opening  $R_2$



$$V_{th} = a - b \leq 3V$$

Finding  $R_{th}$



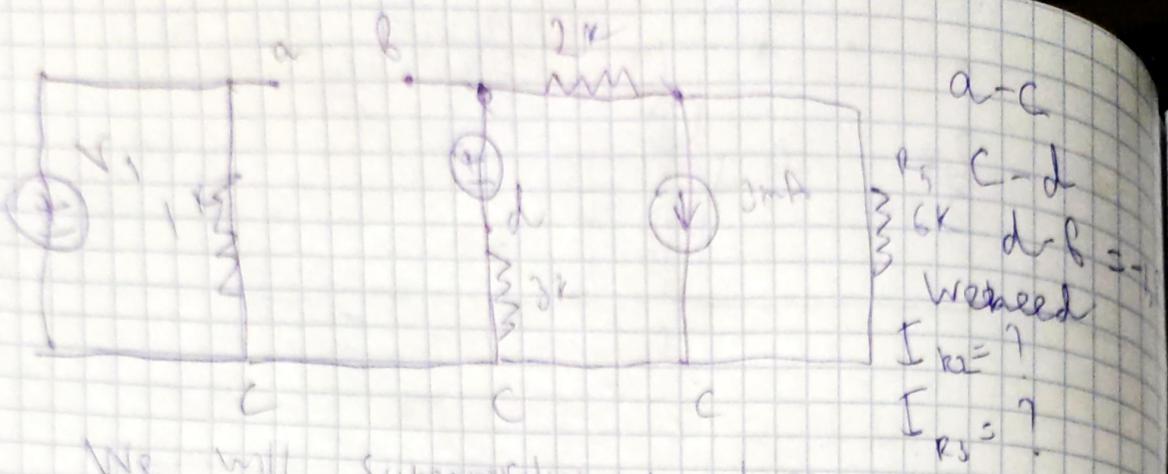
Since  $R_{left} > 0$

$R_{eq} = 0$



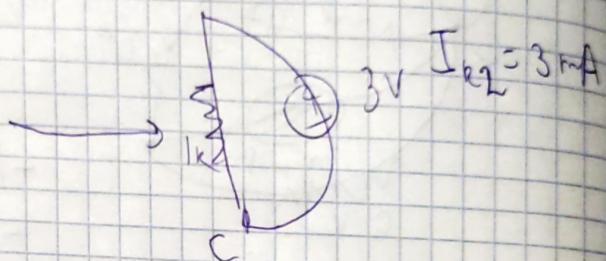
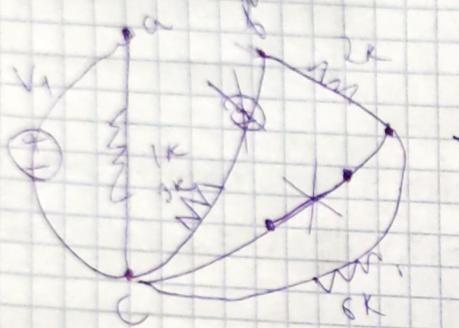
$$I_{R1} = 3mA$$

II) Opening  $R_1$  and finding current  $I_{R1}$



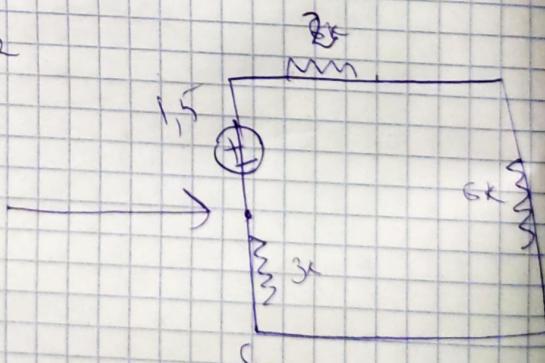
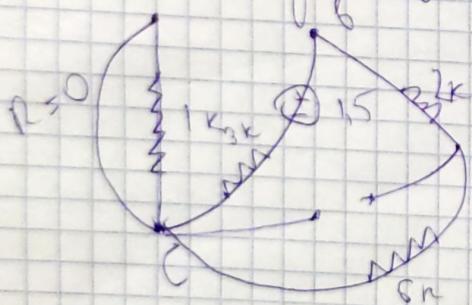
We will Superposition pr. here

I) Looking  $V_1$  turned on



Other current values 0

II) Turning on  $V_2$



$$I_{R2} = 0 \quad I_{R3} = \frac{1.5}{11\text{k}} = 0.136\text{mA}$$

III) Turning on  $I_2$



$$I_{R3} = \frac{6}{11} \cdot 3\text{mA} = 1.636\text{mA}$$



$$I_{R2} = 3 \text{ mA}$$

$$I_{R3} = 1,636 \text{ mA} + 0,130 \text{ mA} = 1,772 \text{ mA}$$

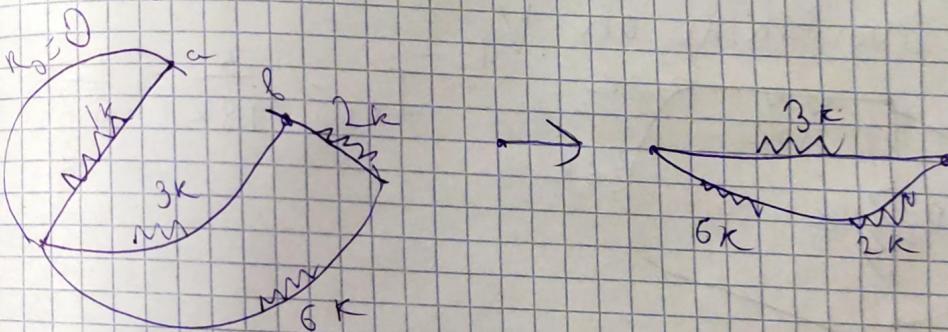
$$a-c = I_{R2} \cdot R_2 = 3 \text{ V}$$

$$+c-d = I_{R3} \cdot R_3 = 1,772 \text{ mA} \cdot 3 \text{ k} = 5,316 \text{ V}$$

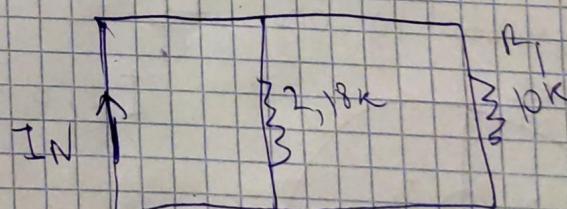
$$+d-f = -1,5$$

$$v_{ea-b} = 8,316 - 1,5 = 6,816 \text{ V}$$

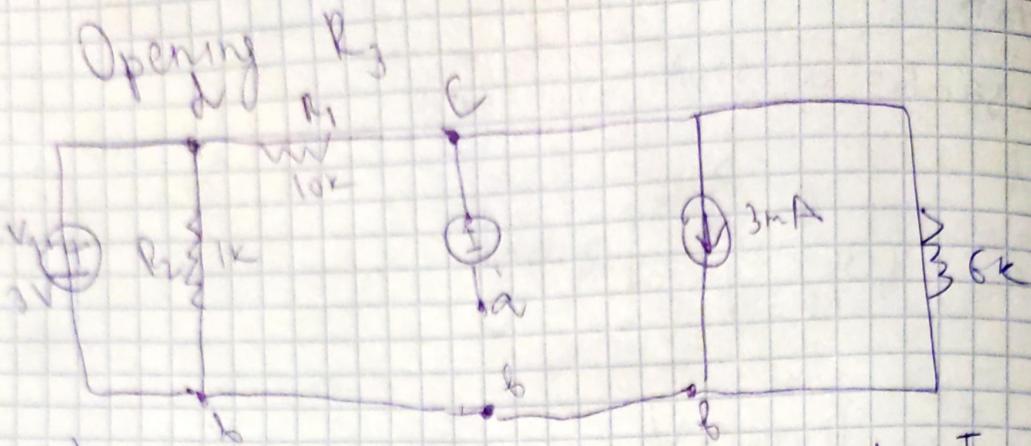
$$R_{th} = \frac{3 \text{ k} \cdot 8 \text{ k}}{11 \text{ k}} = 2,18 \text{ k}$$



$$I_N = 3,127 \text{ mA}$$



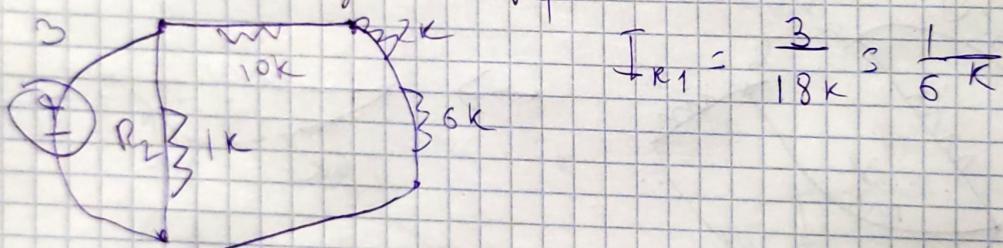
$$I_R = \frac{2,18 \text{ k}}{12,18 \text{ k}} \cdot 3,127 \text{ mA} = 0,559 \text{ mA}$$



I)  $V_{th}$ , so we need to find  $I_{R2}$  and  $I_{R1}$   
 $C-a \approx 1.5V$   
 $d-c \approx$   
 $d-f = 3V$        $I_{R2} = 3mA$

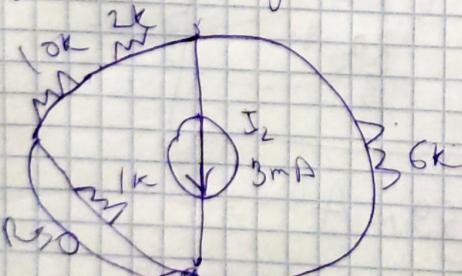
Applying Superposition pr.

1) Switching on  $V_1$

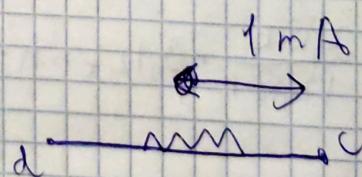


$$I_{R1} = \frac{3}{18k} = \frac{1}{6}mA$$

2) Switching on  $I_2$



$$I_{R1} = \frac{6}{18k} \cdot 3mA = 1mA$$



$$I_{R1} = \frac{1}{6}mA$$

$$d-c = 10k \cdot \frac{7}{6} mA = \frac{70}{6} mA \cdot V$$

$$+c-a = 1,5 V$$

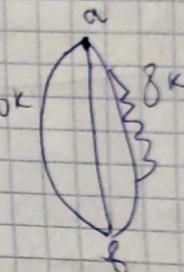
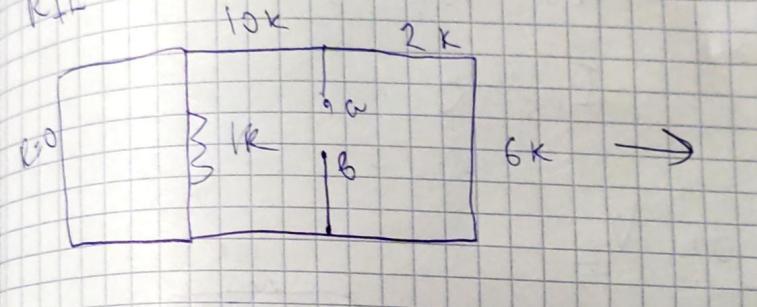
$$d-f = 3$$

$$d-a = 13,167 V$$

$$-d-f = 3 V$$

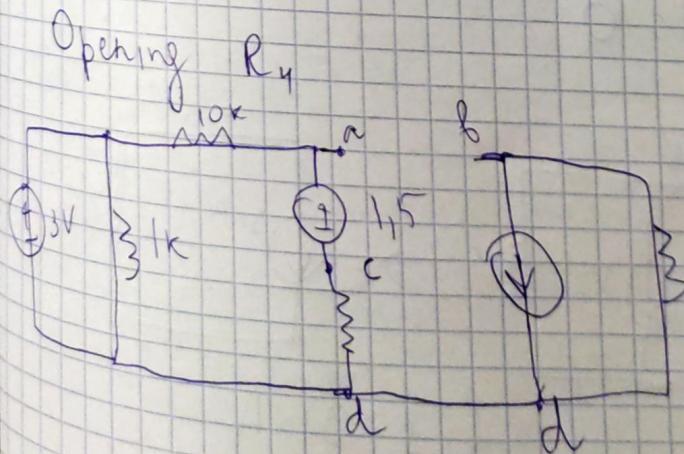
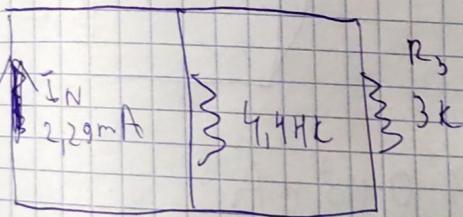
$$V_{af} = b-a = 10,167 V$$

$$R_{TH} = \frac{10k \cdot 8k}{18k} = \frac{80k^2}{18k} = 4,44k$$



$$I_N = \frac{10,167V}{4,44k} = 2,29 mA$$

$$I_{R3} = \frac{4,44}{7,44} \cdot 2,29 = 1,366 mA$$



To find

$$V_{+L}$$

$$a-c = 1,5 V$$

$$c-d =$$

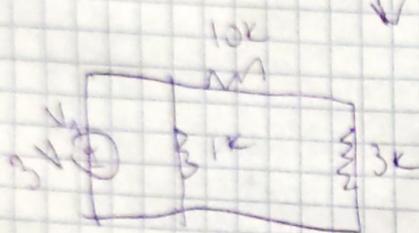
$$d-b =$$

$$I_{R3} =$$

$$I_{R5} = \dots$$

Again, Applying superposition

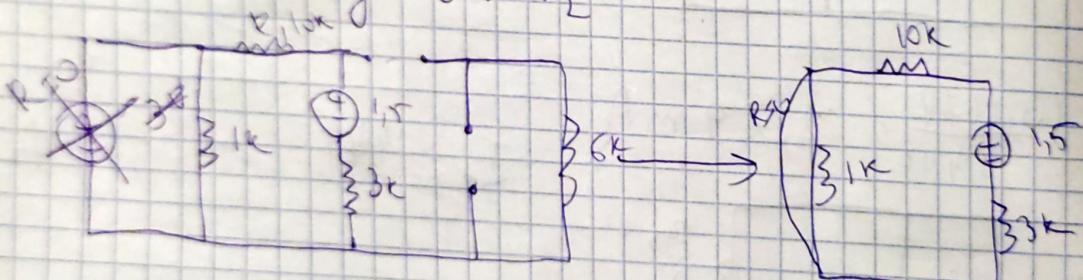
1) Switching on  $V_1$



$$I_{R3} = \frac{3}{13k} = 0,23 \text{ mA}$$

$$I_{R5} = 0$$

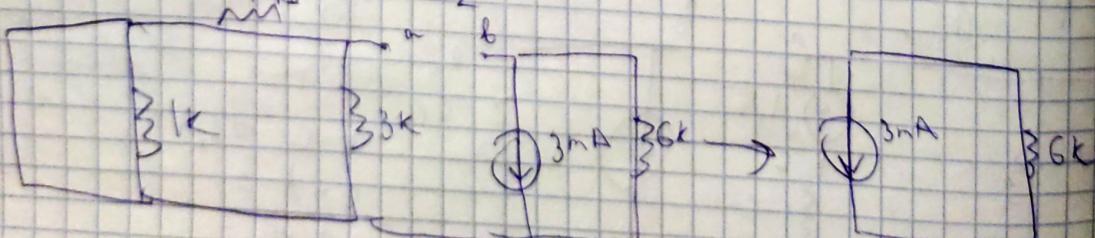
2) Switching on  $V_2$



$$I_{R3} = \frac{1.5}{13k} = 0,115 \text{ mA}$$

$$I_{R5} = 0$$

3) Switching on  $I_2$

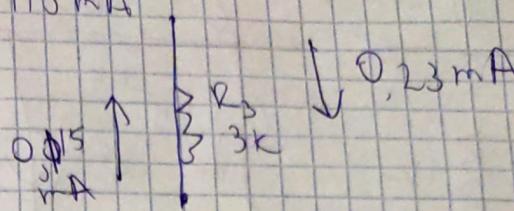


$$I_{R5} = 3 \text{ mA}$$

$$I_{R3} = 0$$

$$I_{B3} = 0,23 - 0,115 = 0,115 \text{ mA}$$

$$I_{es} = 3 \text{ mA}$$



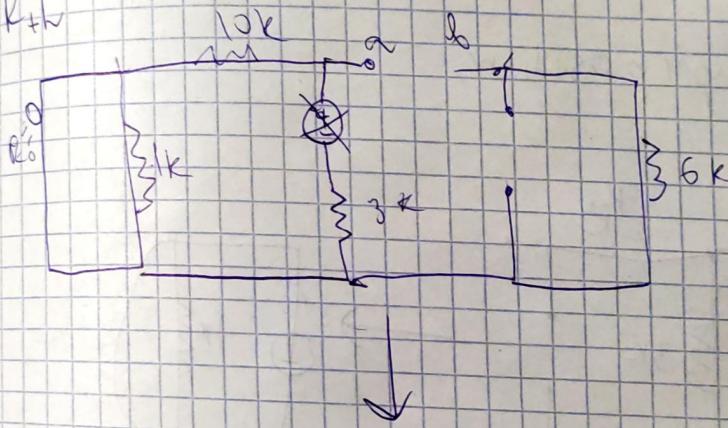
$$a - c = 15$$

$$+c - d = 0,115 \text{ mA} \cdot 3k = 0,345 \text{ V}$$

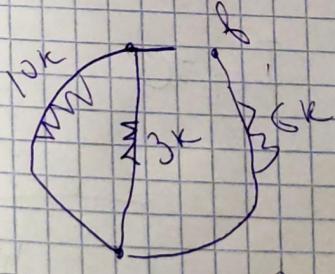
$$+d - b = 3 \text{ mA} \cdot 6k = 18 \text{ V}$$

$$V_H = a - b = 19,845 \text{ V}$$

$R_H$

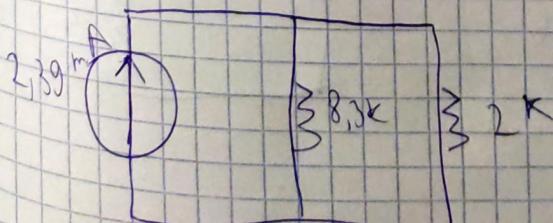


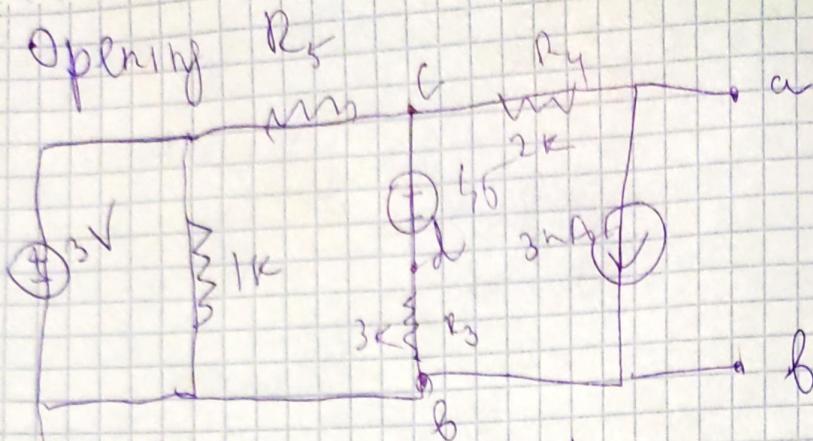
$$R_{eq} = \frac{10 \cdot 3k}{13k} + 6k = 8,3k$$



$$I_N = \frac{19,845}{8,3k} = 2,39 \text{ mA}$$

$$I_{B4} = \frac{8,3k}{10,3k} \cdot 2,39 \text{ mA} = 1,926 \text{ mA}$$

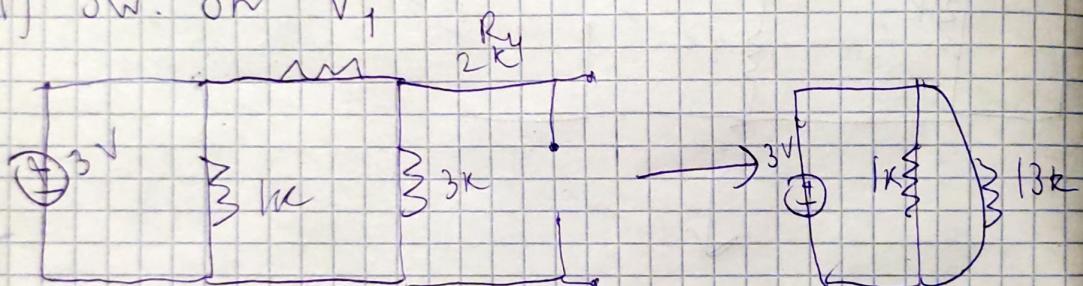




To find  $V_{th}$  and we need  
 $a - c =$   
 $c - d = 1,5$   
 $d - b =$

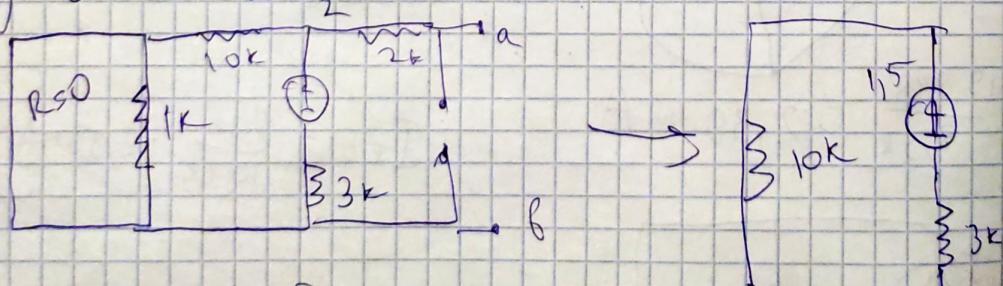
Applying Superposition

1) SW. on  $V_1$



$$I_{R3} = \frac{3}{13k} = 0,23 \text{ mA} \quad I_{R4} = 0$$

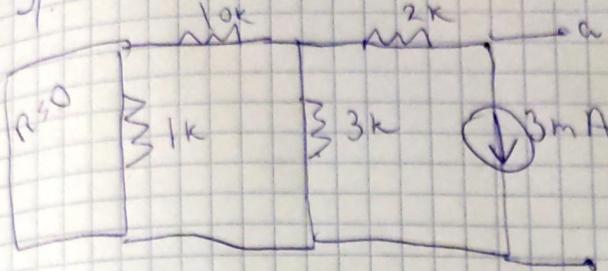
2) SW. on  $V_2$



$$I_{R3} = \frac{15}{13k} = 0,115 \text{ mA}$$

$$I_{R4} = 0$$

3) Sw. on  $I_2$

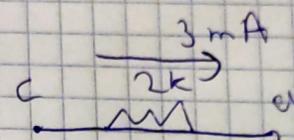


$$I_{R_4} = 3 \text{ mA}$$

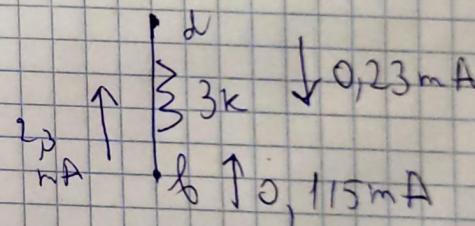
$$I_{R_3} = \frac{10}{13} \cdot 3 \text{ mA} = 2,3 \text{ mA}$$

App. Superp.

$$I_{R_4} = 3 \text{ mA}$$



$$I_{R_3} = 2,3 + 0,115 - 0,23 = 2,185 \text{ mA}$$



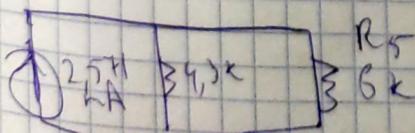
$$a - c = -2 \text{ k} \cdot 3 \text{ mA} = -6 \text{ V}$$

$$d - b = -2,185 \text{ mA} \cdot 3 \text{ k} = -6,555 \text{ mV}$$

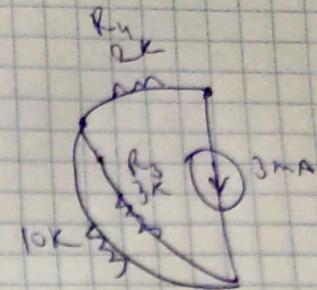
$$c - d = 1,5 \text{ V}$$

$$V_{ab} = a - b = -11,055 \text{ V}$$

$$I_N = \frac{-11,055}{2,3 \text{ k}} \approx 2,571 \text{ mA}$$



$$I_{R_4} = \frac{4,3}{10,3} \cdot 2,571 = 1,073 \text{ mA}$$



$$R_{th} = \frac{10 \cdot 3 \text{ k}}{10 \text{ k} + 3 \text{ k}} = 2,3 \text{ k} \approx 2,3 \text{ k}$$

