# INFSCI 2595: Homework 10

Assigned: November 17, 2019, Due: November 26, 2019

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Submission time: 11/26/2019 at 9:00PM

#### Collaborators

Include the names of your collaborators here.

# Overview

In this assignment you will focus on tuning machine learning algorithms using the caret package. You will practice most of the models we have discussed in this course. You will also get experience working with and interpreting ROC curves. At the conclusion of this assignment you will have completed a small binary classification modeling project from start to finish.

You will notice that when you run the code chunks warnings might be displayed. Usually the warning messages are disabled, but they are allowed to appear to help with installing packages required by caret.

# Load packages

The code chunk below loads in the following packages. If you do not have caret or plotROC installed, please do so before starting this assignment. caret will you prompt you to download and install all other necessary packages, as required.

```
#install.packages("caret")
#install.packages("plotROC")
```

```
library(dplyr)
```

```
##
## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':
##
## filter, lag

## The following objects are masked from 'package:base':
##
## intersect, setdiff, setequal, union

library(ggplot2)

library(caret)
```

```
## Loading required package: lattice
```

# Read in training data

All problems in this assignment use the same training data set. That data set is loaded in the code chunk below. As shown by the glimpse() call, there are 1500 rows with 8 variables. The first 7 variables, x1 through x7 are inputs. Five of the 7 inputs are continuous. One input, x3 is a categorical variable with 5 levels, while x7 is a binary variable. The last variable, output, is the binary response consisting of two levels "event" and "non\_event". In this assignment you will try and predict the "event" class.

### Problem 1

As with any data analysis project, it's best to start out exploring the data before jumping into building models. You will begin by getting a high level overview of summary statistics through a simple exploratory data analysis.

1a)

A quick way to get important summary statistics is to call the summary() function. For continuous variables, summary() displays important statistics about the central tendancy with the mean and median. summary() also gives an idea about the spread in the data by displaying the first and third quartiles, as well as the absolute min and max values observed in the data set. For discrete factor variables, summary() provides the number of observations for each unique level.

## **PROBLEM**

Call the summary() function on the training data set, train\_df. Based on the counts for the discrete variables x3 and x7, are there particular levels that dominate the observations? Based

on the counts alone, would you say the binary response, output, is a balanced or imbalanced data set?

### SOLUTION

```
### your code here
summary(train_df)
```

```
##
                             x^2
                                           xЗ
                                                          x4
          x1
##
           :-4.00000
                               :-4.00000
                                           A:297
                                                           :-4.00000
   Min.
                       Min.
                                                   Min.
                       1st Qu.:-2.33333
##
   1st Qu.:-2.00000
                                           B:305
                                                   1st Qu.:-2.00000
   Median : 0.00000
                       Median : 0.00000
                                                   Median : 0.00000
##
                                           C:291
##
   Mean
          : 0.04844
                       Mean
                              :-0.05333
                                           D:303
                                                   Mean
                                                          :-0.04756
##
   3rd Qu.: 2.00000
                       3rd Qu.: 2.00000
                                           E:304
                                                   3rd Qu.: 2.00000
##
   Max.
           : 4.00000
                       Max.
                              : 4.00000
                                                   Max.
                                                          : 4.00000
##
          x5
                            x6
                                                       output
                                         x7
           :-4.0000
##
  Min.
                             :-4.000
                      Min.
                                        aa:753
                                                           :585
                                                 event
##
   1st Qu.:-2.3333
                      1st Qu.:-2.000
                                        bb:747
                                                 non_event:915
  Median :-0.3333
                      Median : 0.000
##
   Mean
           :-0.1320
                      Mean
                              :-0.006
##
##
    3rd Qu.: 2.0000
                      3rd Qu.: 2.000
           : 4.0000
                              : 4.000
   Max.
                      Max.
```

There appear to be no particular levels for x3 and x7 that dominate as the levels are all within 5% of each other. Based on the counts, the response appears to be an imbalanced set.

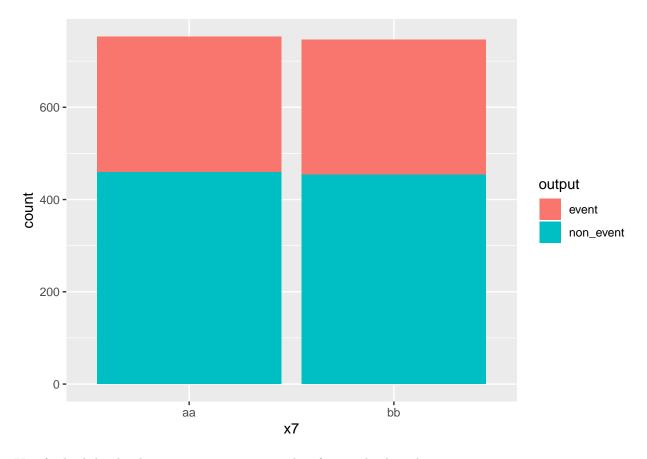
# 1b)

Let's now visualize the binary response for each of the two discrete factors, starting with the binary variable  $\mathbf{z}^7$ 

#### **PROBLEM**

Use ggplot2 to create a bar chart with geom\_bar(). Set the x aesthetic equal to x7 in the parent ggplot() call. In the geom\_bar() call set the fill aesthetic equal to output. Can you tell if the "event" occurs more frequently for either of the levels of x7?

```
### your code here
ggplot(data=train_df, mapping=aes(x=x7)) + geom_bar(mapping = aes(fill=output))
```



Yes, for both levels, the event appears to occur less frequently than the non-event.

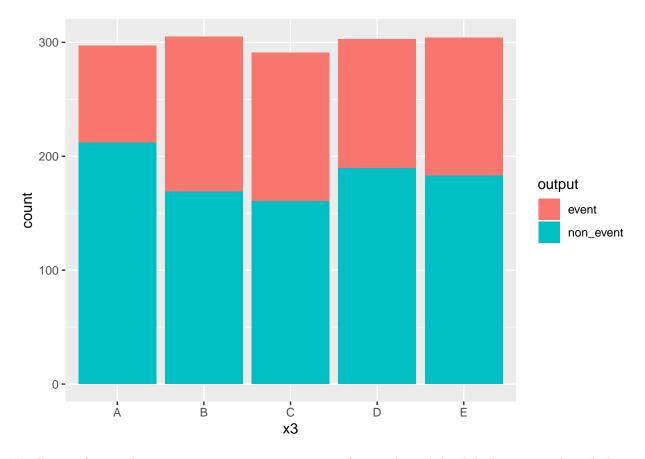
1c)

Now consider the  ${\tt x3}$  factor which has 5 unique levels.

# **PROBLEM**

Use ggplot2 to create a bar chart with geom\_bar(). Set the x aesthetic equal to x3 in the parent ggplot() call. In the geom\_bar() call set the fill aesthetic equal to output. Can you tell if the "event" occurs more frequently for either of the levels of x3?

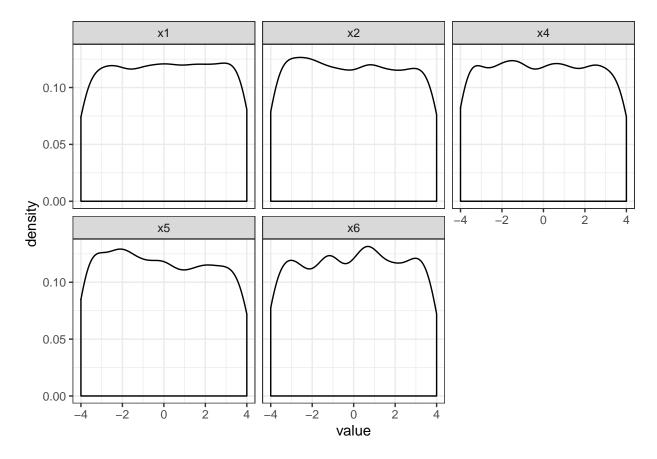
```
### your code here
ggplot(data=train_df, mapping=aes(x=x3)) + geom_bar(mapping = aes(fill=output))
```



In all cases for x3, the non-event appears to occur more frequently with level A showing a relatively lower occurence of the event and levels B, and C showing a relatively higher occurence of the event.

# 1d)

Let's now look at the distributions associated with each continuous input. We will first consider the distributions irrespective of the response and the other discrete inputs. The code chunk below reshapes train\_df to allow visualizing the individual continuous inputs within separate facets. The *marginal* distributions are visualized using the geom\_density() function. As shown by the figure below, the distributions are essentially uniform.



You will now break up each distribution based on the the discrete variable **x3** and the response, output. To help understand the structure of the reshaped data set, the code chunk below prints the first 9 rows to the screen.

Map the values of the continuous inputs with respect to 'x3', 'x7' and 'output'?

```
##
   # A tibble: 100 x 6
##
      obs_id x3
                     x7
                           output
                                       input_name
                                                    value
##
       <int> <fct> <fct>
                           <fct>
                                       <chr>
                                                    <dbl>
##
    1
            1 D
                     bb
                           non_event x1
                                                   -3
##
    2
            2 A
                           non_event x1
                                                    2.67
                     aa
    3
            3 B
                                                   -4
##
                           non_event x1
                     aa
    4
            4 D
                                                   -3.33
##
                     aa
                           non_event x1
            5 E
##
    5
                                                    3.33
                     aa
                           non_event x1
##
    6
            6 A
                           non_event x1
                                                   -3.33
                     aa
    7
            7 D
                                                    2.67
##
                           event
                                       x1
                     aa
##
    8
            8 B
                                       x1
                                                    3.67
                     aa
                            event
    9
            9 E
                                                    0.667
##
                           non_event x1
                     aa
## 10
           10 E
                            event
                                      x1
                                                   -3
                     aa
## # ... with 90 more rows
```

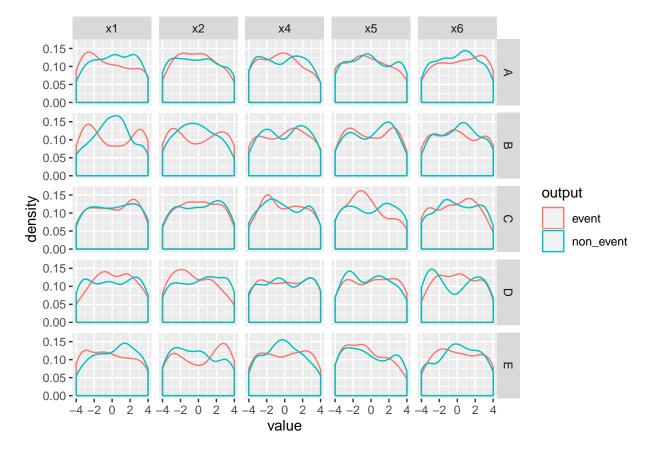
#### **PROBLEM**

You must modify the code which creates the separate distributions by setting the color aesthetic in the geom\_density() call to be equal to output. You must also modify the facet\_wrap() call to be facet\_grid(). The horizontal facets should be based on the input\_name variable while x3 controls the vertical facets.

Based on the visualizations, are there any values of the continuous inputs that seem to be more associated with the "event" occurring? Does the x3 discrete factor influence behavior?

HINT: The R for Data Science book discusses how to create facets if you need a refresher.

#### **SOLUTION**



Based on the visualizations, are there any values of the continuous inputs that seem to be more associated with the "event" occuring? Does the x3 discrete factor influence behavior?

x1 with respect to A, x4 with respect to E, and x5 with respect to C appear to show more non-uniform behavior but, overall, none of the inputs appear to be strongly correlated with the event. Yes, the discrete factor x3 appears to skew the behavior of the event and non-event in a seemingly random manner.

1e)

Exploratory Data Analysis (EDA) helps us get famaliar with a data set and observe high level trends. EDA can help us make an informed decision about what modeling practices are appropriate to consider.

### **PROBLEM**

Based on your visualizations, would you feel it is safe to say interactions are not relevant for this problem?

#### SOLUTION

No, all possible interactions of the inputs have not been explored.

# Problem 2

You will now begin to model the binary outcome, output, based on the inputs. You will use caret to manage the cross-validation data splits and calculate the performance metrics. In this assignment, you will focus on the area under the ROC curve (AUC) as the primary metric of interest for assess model performance. In caret, the area under the ROC curve is referred to as ROC.

#### 2a)

As discussed in lecture, the trainControl() function is used to tell caret how to manage the training and performance assessment. You will specify the arguments of the trainControl() function and also specify the primary metric of interest.

# PROBLEM

Specify the trainControl() to use 5-fold cross validation. You must specify the summaryFunction, classProbs, and savePredictions appropriately in order to allow creating the ROC curves. You must also set the variable metric\_use equal to "ROC".

### 2b)

As we have discussed multiple times this semester, it is always important to consider a simple model before building complex ones. So you will begin by fitting a logistic regression model. Your job will be to complete the train() function call to fit the logistic regression model.

The set.seed() function is set for you, and is set before all models in this assignment. Using the same random seed forces the random data splits to be the same across all models.

#### **PROBLEM**

Complete the code chunk below by specifying the formula to correctly model the binary outcome, output, as a function of all other variables in the data set. Set the data argument equal to train\_df. Set the method argument equal to "glm", and the metric argument equal to the metric\_use variable defined in Problem 2a). Finally, specify the trControl argument equal to the ctrl\_k05 variable you defined in Problem 2a).

Once the code chunk below completes, print the caret object fit\_glm to the screen. What is the area under the ROC curve value (which caret calls ROC) for your logistic regression model? Is this value associated with the training set or holdout set error?

#### SOLUTION

```
fit_glm
```

```
## Generalized Linear Model
##
## 1500 samples
      7 predictor
##
      2 classes: 'event', 'non event'
##
## No pre-processing
## Resampling: Cross-Validated (5 fold, repeated 3 times)
## Summary of sample sizes: 1200, 1200, 1200, 1200, 1200, 1200, ...
## Resampling results:
##
##
     ROC
                Sens
                             Spec
               0.01937322
                            0.9763206
##
     0.5288808
```

What is the area under the ROC curve value (which caret calls ROC) for your logistic regression model? Is this value associated with the training set or holdout set error?\*\*?

The area is approx. 0.529. Since we used the train\_df set, the area appears to be associated with the training set.

2c)

This problem consists of 7 inputs. But, how many parameters were learned in the logistic regression model? A simple way to find out is to use the coef() function, which extracts the coefficients (parameter) values associated with the model object. You can access the logistic regression model within the caret object by calling fit\_glm\$finalModel.

### **PROBLEM**

Call the coef() function on the logistic regression model. How many parameters were learned? Why are the parameters named the way they are?

### SOLUTION

```
### your code here
coef(fit_glm$finalModel)
```

```
##
     (Intercept)
                             x1
                                            x2
                                                         x3B
                                                                        x3C
                                 0.0013738964 -0.7015426126 -0.7053128092
##
    0.9257183054
                  0.0269253125
##
             x3D
                            x3E
                                           x4
                                                          x5
##
  -0.4006518286 -0.4962845183 -0.0006240123 0.0278721689 -0.0100927137
            x7bb
## -0.0119654125
```

How many parameters were learned? Why are the parameters named the way they are?\*? 11 parameters appear to have been learned. They are named, it seems, after the inputs they represent, e.g. "x3C" for input x3 level C.

# **2**d)

You will now use regularization with elastic net through the glmnet package. We discussed how the penalty or regularization factor for lasso and ridge regression can be tuned via cross-validation. The elastic net uses the same regularization parameter, lambda, but also includes a second tuning parameter, alpha. The additional parameter is a weighting or mixing parameter which controls which of the two penalty terms, lasso or ridge, is more prevelant.

You will use the elastic net to a fit a model accounting for interactions between the inputs. Before fitting the model you must determine how many parameters are in a model with all pair-wise and all 3-way interactions.

### **PROBLEM**

How many parameters must be learned in a generalized linear model with all pair-wise interactions? How many parameters must be learned in a generalized linear model with all 3-way interactions? Why would a model like elastic net be an appropriate choice over a conventional generalized model when considering the interactions in this case?

```
### your code here
choose(7, 2)
```

```
## [1] 21
```

```
choose(7, 3)
```

```
## [1] 35
```

How many parameters must be learned in a generalized linear model with all pair-wise interactions? How many parameters must be learned in a generalized linear model with all 3-way interactions? Why would a model like elastic net be an appropriate choice over a conventional generalized model when considering the interactions in this case? ?

Since there 7 inputs, there would be 21 pairwise interactions, and 35 3-way interactions. Because elastic net considers the combined penalties of lasso and ridge regresion, it would likely better suited for multi-interaction parameters.

**2e**)

You will now fit the elastic net model with all pair-wise interactions. You will use the default caret search grid for the alpha and lambda tuning parameters, so you do not need to additional arguments in the call to the train() function just yet.

#### **PROBLEM**

Fit an elastic net model with all pair-wise interactions. You must specify the formula correctly and set the method argument equal to "glmnet". All other arguments can be the same as the call in Problem 2b). After the code chunk completes, print the caret object to the screen.

# SOLUTION

```
fit_glmnet_2
```

```
## glmnet
##
## 1500 samples
##
      7 predictor
##
      2 classes: 'event', 'non_event'
##
## No pre-processing
## Resampling: Cross-Validated (5 fold, repeated 3 times)
## Summary of sample sizes: 1200, 1200, 1200, 1200, 1200, 1200, ...
## Resampling results across tuning parameters:
##
     alpha lambda
##
                          ROC
                                      Sens
                                                  Spec
```

metric = metric\_used, trControl = ctrl\_k05)

```
##
    0.10
           0.0001359713  0.5619292  0.23361823  0.8298725
##
    0.10
          0.0013597126  0.5618732  0.23247863  0.8320583
##
    0.10
          0.0135971264 0.5590771 0.20113960 0.8684882
##
    0.55
          ##
    0.55
          0.0013597126  0.5617829  0.22450142  0.8364299
##
    0.55
          0.0135971264 0.5572276 0.15441595 0.9234973
    1.00
##
          0.0001359713  0.5620880  0.23247863  0.8309654
##
    1.00
          0.0013597126  0.5617113  0.21880342  0.8466302
##
    1.00
           0.0135971264 0.5607367 0.09059829 0.9511840
##
## ROC was used to select the optimal model using the largest value.
## The final values used for the model were alpha = 0.55 and lambda
  = 0.0001359713.
```

2f)

#### **PROBLEM**

Fit another elastic net model using the caret default tuning grid. This time however, fit the model allowing for all 3-way interactions. How does the best tuned elastic net with 3-way interactions compare to the best tuned elastic net with pair-wise interactions, based on the area under the ROC curve? Which model type appears to be better?

```
fit_glmnet_3
```

```
## glmnet
##
## 1500 samples
##
   7 predictor
##
   2 classes: 'event', 'non_event'
##
## No pre-processing
## Resampling: Cross-Validated (5 fold, repeated 3 times)
## Summary of sample sizes: 1200, 1200, 1200, 1200, 1200, 1200, ...
## Resampling results across tuning parameters:
##
##
   alpha lambda
               ROC
                      Sens
                             Spec
##
   0.10
       ##
   0.10
       0.0026652066 0.6177541 0.3669516 0.7934426
##
   0.10
       0.55
##
       ##
   0.55
       ##
   0.55
       ##
   1.00
```

```
## 1.00 0.0026652066 0.6289695 0.3327635 0.8327869

## 1.00 0.0266520660 0.6319960 0.1441595 0.9795993

##

## ROC was used to select the optimal model using the largest value.

## The final values used for the model were alpha = 0.55 and lambda

## = 0.02665207.
```

How does the best tuned elastic net with 3-way interactions compare to the best tuned elastic net with pair-wise interactions, based on the area under the ROC curve? Which model type appears to be better?\*\*\*

The elastic net with 3-way interactions appears to be better with a best tuned ROC value of appox. 0.64 while the pairwise interaction case had a best ROC value of approx. 0.562.

# **2g**)

The caret object print outs display the default grid search values used to try and identify the "best" values of alpha and lambda. This default grid is a great starting point, but let's try and refine it further. You will use the expand.grid() function to define a custom grid search over the alpha and lambda tuning parameters.

### **PROBLEM**

Complete the code chunk below which creates the grid search glmnet\_grid over alpha and lambda, and then executes the training. You must specify alpha to be a vector of 4 values: 0.25, 0.55, 0.85, and 1.0. You must specify lambda to be a vector from -8 and 0.5 in log-lambda space. Each point is spaced by 0.25 log-lambda units.

WHY NOT JUST GIVE THE PARAMETERS OF THE SEQENCE? WHAT DOES SOLVING THIS (IN GARBAGE R) HAVE TO DO WITH MACHINE LEARNING??

You must then perform the training on the elastic net model with all 3-way interactions. In order to use your custom search grid, you must specify tuneGrid to be equal to glmnet\_grid.

After the code chunk completes, rather than printing the results to screen, you will plot the results by calling the plot() function on the caret object fit\_glmnet\_3\_b. Call the plot() function two times. In the first call, just plot the results. In the second call set the xTrans argument equal to log in the plot() call. This converts the x-axis to be log-lambda, rather than lambda directly.

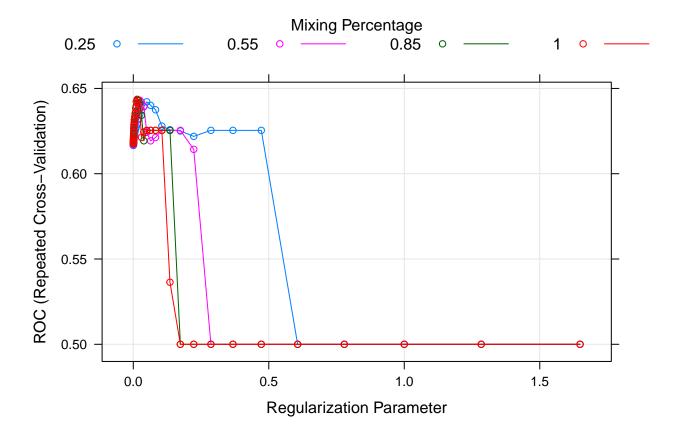
Which values of the regularization parameter, lambda, appear to yield the highest area under the ROC curve? Are there lambda values that clearly yield worse results? What did you use to make that judgement?

HINT: caret requires the tuning parameter to correspond to lambda not log-lambda. By setting the values to be evenly spaced in log-lambda, you must transform the vector appropriately in order to create the lambda value required by caret.

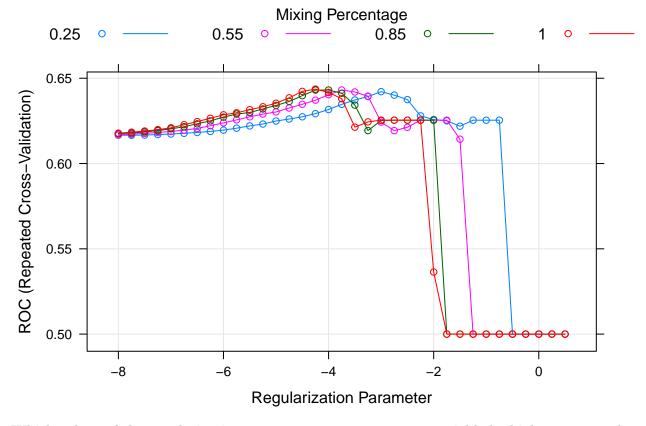
```
alpha = c(0.25, 0.55, 0.85, 1)
lambda = exp(seq(-8, 0.5, by=0.25))
```

Plot the results.

```
### your code here
plot(fit_glmnet_3_b)
```



```
### your code here
plot(fit_glmnet_3_b, xTrans=log)
```



Which values of the regularization parameter, lambda, appear to yield the highest area under the ROC curve? Are there lambda values that clearly yield worse results? What did you use to make that judgement?

Values of lambda near 0 appear to yield the highest area. Yes, lambda values greater than approx. 0.55 appear to yield the worst area. The area under the ROC curve was used.

### 2h)

You could print the fit\_glmnet\_3\_b object to screen, but the print out will be very large. After all, you just trained elastic net models for 140 combinations of lambda and alpha! So rather than reading through the complete print out, you can access the tuned parameter values directly with the \$bestTune variable within the caret model object. Furthermore, you can the access the different tuning parameters with the \$ operator. For example, to access the best tuned value for alpha, you would use \$bestTune\$alpha.

# PROBLEM

Print the best tuning parameters values to screen and calculate the log of the best tuned lambda value and print it to screen. Are these values in line with your interretation of the figures in the previous problem?

```
### your code here
fit_glmnet_3_b$bestTune
```

```
## alpha lambda
## 121 1 0.01426423
```

```
log(fit_glmnet_3_b$bestTune$lambda)
```

```
## [1] -4.25
```

Are these values in line with your interretation of the figures in the previous problem?\*\* ?

Yes. The curve corresponding to alpha=1 near lambda=0.014 appears to have the highest area under the curve.

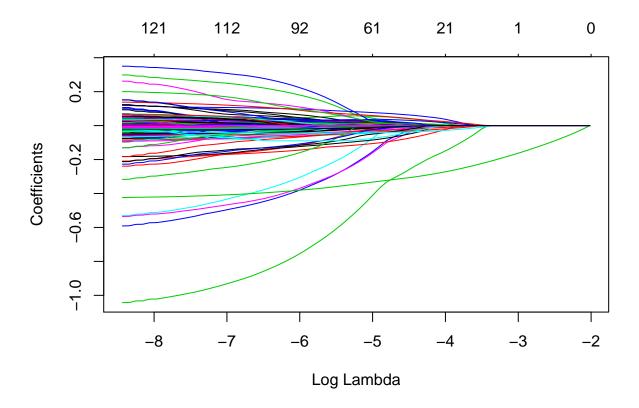
2i)

Just as with the logistic regression model, you can access the final elastic net model object by \$finalModel. Let's check that the behavior of the elastic net model directly, by calling plot() on the final model object. This model object is the result from the glmnet package directly, and so provides the same functionality as when we discussed interpreting glmnet for lasso regression in lecture.

### **PROBLEM**

Call plot() on the final model object associated with the fit\_glmnet\_3\_b caret object. Set the xvar argument to "lambda". How many parameters are "active" around the lambda value you identified as optimal for the 3-way interaction model?

```
### your code here
plot(fit_glmnet_3_b$finalModel, xvar="lambda")
```



How many parameters are "active" around the lambda value you identified as optimal for the 3-way interaction model?\*\*?

At least 2 parameters apprear to be active around log(lambda)=-4.25.

# **2**j)

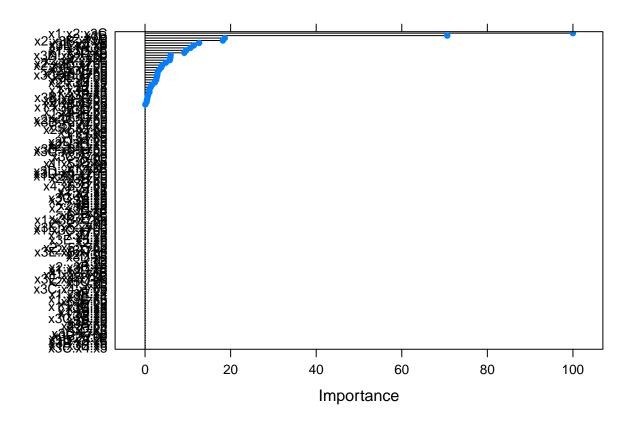
By turning off in-active or unimportant inputs, the elastic net is giving us an idea about what variables matter. We discussed in lecture how the varImp() function can be used to display the variable importance rankings for the random forest model. The function can also be used for glmnet.

# **PROBLEM**

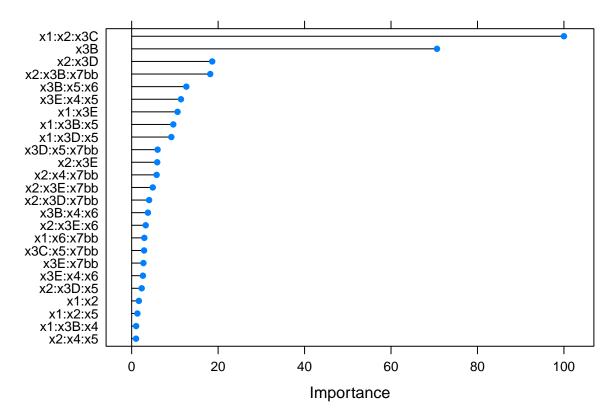
Call plot() on the varImp() function applied to the elastic net model with all 3-way interactions. Then call it again with the top argument in the plot() call set to 25.

Why does the first plot, which includes all variables, look the way it does? What are the top two important variables according to the elastic net?

```
### your code here
plot(varImp(fit_glmnet_3))
```



### your code here
plot(varImp(fit\_glmnet\_3), top=25)



Why does the first plot, which includes all variables, look the way it does? What are the top two important variables according to the elastic net??

The first plot looks congested because it contains all interactions. The two most important variables appear to be x1:x2:x3C and x3B.

# Problem 3

Let's start to consider more complex models. You will fit a Support Vector Machine (SVM) with a linear kernel. If you have not used a SVM in R before, caret will if it can download and install the necessary packages. Follow the instructions within the R console and the packages will be installed correctly.

# 3a)

The linear kernel SVM has a single tuning parameter, the cost C. We discussed this parameter in lecture.

### **PROBLEM**

What does the C parameter control within the SVM? Also, how many unknown parameters are there for the SVM in this specific problem?

### **SOLUTION**

The C parameter controls the size of the margin surrounding the hyperplane. There are appear to be 7 unknown parameters.

3b)

You will fit the SVM with a linear kernel. You will use a custom tuning grid for the C parameter. Even though it's a single variable you must still "wrap" the grid values within the expand.grid() call. There are several different SVM's with linear kernals available within the R ecosystem. However, you will use the library associated with setting the method argument equal to svmLinear.

### **PROBLEM**

Specify the grid of possible C values to be a regular vector containing 0.25, 0.5, 1.0, and 2.0. Train the SVM with a linear kernel. Set the formula to be the response, output, as a function of all other variables in the data set. Set the method argument equal to "svmLinear". Set the tuneGrid argument equal to the svm\_lin\_grid object. The other arguments should be the same as you used for the logistic regression and elastic net models.

Once the code chunk completes, and it MIGHT TAKE A FEW MINUTES, print the caret object to screen. How does the SVM with a linear kernel compare to the best tuned elastic net with all 3-way interactions?

#### SOLUTION

```
#install.packages("e1071")
```

```
#ctrl <- trainControl(method="repeatedcv",</pre>
#
                        number = 10,
#
                        repeats = 2,
#
                        classProbs = TRUE
#
svm_lin_grid <- expand.grid(</pre>
                 C= c(0.25, 0.5, 1.0, 2.0)
set.seed(98131)
fit_svm_lin <- train(output ~ ., data = train_df,</pre>
                  method = "svmLinear",
                  metric = metric used,
                  tuneGrid = svm lin grid,
                  trControl = ctrl_k05)
```

## maximum number of iterations reached 0.0005448217 -0.0005439533maximum number of iterations reached

```
fit_svm_lin
```

```
## Support Vector Machines with Linear Kernel
##
## 1500 samples
## 7 predictor
## 2 classes: 'event', 'non_event'
##
## No pre-processing
## Resampling: Cross-Validated (5 fold, repeated 3 times)
```

```
## Summary of sample sizes: 1200, 1200, 1200, 1200, 1200, 1200, ...
## Resampling results across tuning parameters:
##
##
     С
                      Sens Spec
           ROC
##
     0.25
           0.4907664
                            1
     0.50 0.4860835 0
##
                            1
     1.00
          0.5041490 0
##
     2.00 0.5038874 0
##
                            1
##
## ROC was used to select the optimal model using the largest value.
## The final value used for the model was C = 1.
```

How does the SVM with a linear kernel compare to the best tuned elastic net with all 3-way interactions?\*\*

The SVM appears to yield worse ROC values than the elastic net.

## 3c)

To move beyond linearity, we will use the SVM with a radial basis function. As with the linear kernel, there are multiple libraries to choose from to build this model. You will however use the library associated with the method argument equal to "svmRadial". Compared with the linear kernel, the radial basis function kernel has an additional tuning parameter, sigma, which controls the behavior of the radial basis or Gaussian kernel.

You will first use the default caret search grid. This will allow the underlying package, kernlab, to estimate sigma, which serves as a useful starting point for refining the grid later.

#### **PROBLEM**

Train a SVM with a radial basis function. Use the default caret search grid by NOT including the tuneGrid argument in the train() call. Set the remaining arguments to be the same as what you used in Problem 3b), except set the method equal to "svmRadial".

After the training completes, print the caret object to the screen. What value of sigma was used and what was the optimally identified C value?

```
fit_svm_rbf
```

```
## Support Vector Machines with Radial Basis Function Kernel
##
## 1500 samples
## 7 predictor
## 2 classes: 'event', 'non_event'
##
## No pre-processing
```

```
## Resampling: Cross-Validated (5 fold, repeated 3 times)
## Summary of sample sizes: 1200, 1200, 1200, 1200, 1200, 1200, ...
## Resampling results across tuning parameters:
##
##
                      Sens
                                 Spec
##
     0.25 0.5949714 0.1339031 0.9409836
     0.50 0.5951832 0.1396011 0.9406193
     1.00 0.6017997 0.1527066 0.9329690
##
##
## Tuning parameter 'sigma' was held constant at a value of 0.06695495
## ROC was used to select the optimal model using the largest value.
## The final values used for the model were sigma = 0.06695495 and C = 1.
What value of sigma was used and what was the optimally identified C value?**
A sigmna value of approx. 0.067 was used along with a C value of 1.
```

**3**d)

You will now use a refined grid based on the results from Problem 3c). You will create a search grid that varies sigma as being equal to, double that, four times that, and 8 times the value identified within fit\_svm\_rbf. Can you think of how you can access the best tuned value of sigma from the fit\_svm\_rbf object?

### **PROBLEM**

Define the search grid with with the expand.grid() function. Set sigma to be a vector equal to 1x, 2x, 4x, and 8x times the value identified in Problem 3c). Set the C parameter to a vector with elements equal to 0.5, 1, 2, 4, 8, 16, and 32.

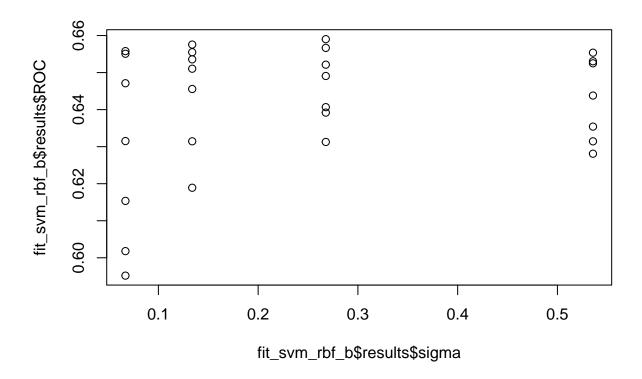
Train a new SVM with radial basis function but now use your custom grid search defined in rbf\_grid. The other arguments should be the same as what you used in Problem 3c).

Once the model training completes, WHICH MIGHT TAKE A FEW MINUTES, print the results to screen and plot the results.

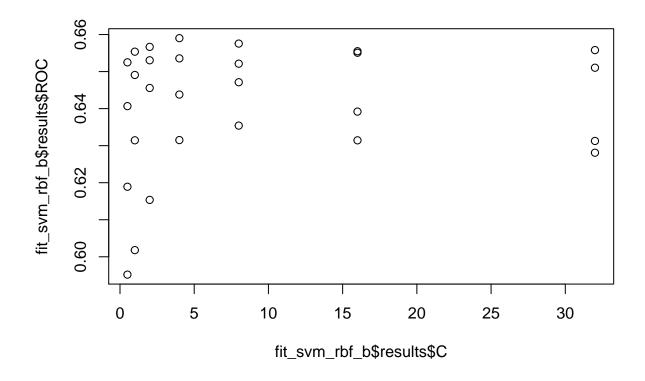
Would continuing to increase the sigma or C parameters relative to the values from Problem 3c) continue to improve the area under the ROC curve?

```
fit_svm_rbf_b
```

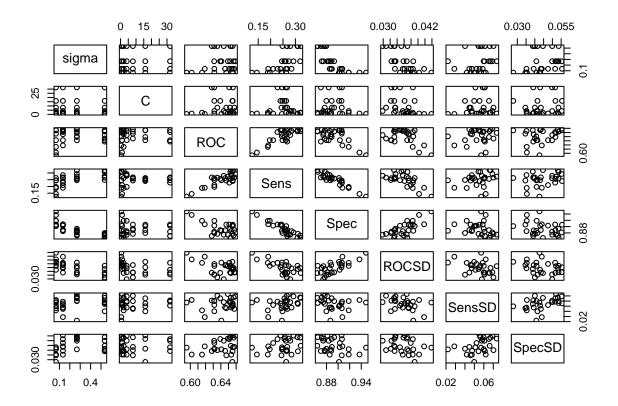
```
## Support Vector Machines with Radial Basis Function Kernel
##
## 1500 samples
##
     7 predictor
##
     2 classes: 'event', 'non_event'
##
## No pre-processing
## Resampling: Cross-Validated (5 fold, repeated 3 times)
## Summary of sample sizes: 1200, 1200, 1200, 1200, 1200, 1200, ...
## Resampling results across tuning parameters:
##
##
    sigma
                С
                      ROC
                                Sens
                                           Spec
##
    0.06695495
                 0.5 0.5951832 0.1247863 0.9482696
##
    0.06695495
                 1.0 0.6017997 0.1447293 0.9369763
##
    0.06695495
                 2.0 0.6153535 0.1886040 0.9183971
##
                 4.0 0.6315072 0.1965812 0.9183971
    0.06695495
##
    0.06695495
                 8.0 0.6471222 0.2438746 0.9063752
##
    0.06695495 16.0 0.6550869 0.2626781 0.9016393
##
    0.06695495 32.0 0.6557938 0.2461538 0.9027322
##
    0.13390990
                 0.5 0.6189093 0.1903134 0.9074681
##
    0.13390990
                 1.0 0.6314480 0.2102564
                                           0.9030965
##
                 2.0 0.6455716 0.2621083 0.8881603
    0.13390990
##
    0.13390990
                 4.0 0.6535675 0.2843305 0.8856102
##
    0.13390990
                 8.0 0.6575592 0.2672365 0.8892532
##
    0.13390990 16.0 0.6555011 0.2398860 0.9060109
##
    0.13390990 32.0 0.6510423 0.2279202 0.9067395
##
    0.26781981
                 0.5 0.6406707 0.2455840 0.8867031
##
    0.26781981
                 1.0 0.6490838 0.2729345 0.8746812
##
    0.26781981
                 2.0 0.6566687 0.3190883
                                           0.8717668
##
    0.26781981
                 4.0 0.6590195 0.2923077
                                           0.8816029
##
    0.26781981
                 8.0 0.6521290 0.2581197 0.8932605
##
    0.26781981 16.0 0.6391917 0.2558405
                                          0.8888889
##
    0.26781981 32.0 0.6312705 0.2609687 0.8837887
##
    0.53563961
                 0.5 0.6524995 0.3082621 0.8648452
##
    0.53563961
                 1.0 0.6553734 0.3099715 0.8772313
##
    0.53563961
                 2.0 0.6530506 0.3213675
                                           0.8641166
##
    0.53563961
                 4.0 0.6437999 0.2792023
                                           0.8743169
##
    0.53563961
                 8.0 0.6354148 0.2655271
                                           0.8768670
##
    0.53563961 16.0 0.6314387
                                0.2478632
                                           0.8797814
##
                32.0 0.6280946 0.2666667 0.8703097
    0.53563961
##
## ROC was used to select the optimal model using the largest value.
## The final values used for the model were sigma = 0.2678198 and C = 4.
### your code here
plot(x=fit_svm_rbf_b$results$sigma, y=fit_svm_rbf_b$results$ROC)
```



plot(x=fit\_svm\_rbf\_b\$results\$C, y=fit\_svm\_rbf\_b\$results\$ROC)



plot(fit\_svm\_rbf\_b\$results)



<sup>\*</sup>Would continuing to increase the sigma or C parameters relative to the values from Problem 3c) continue to improve the area under the ROC curve? ?

It appears that increasing the sigma parameter would improve the area under the ROC curve more than increasing the C parameter. ## Problem 4

# 4a)

Up to this point, we have only focused on the area under the ROC curve. However, there are multiple other metrics to consider. You can easily see the confusion matrix performance assessed on the hold-out sets by calling the confusionMatrix.train() function on a caret model object.

#### **PROBLEM**

Call confusionMatrix.train() on the custom search grid elastic net model with all 3-way interactions and the custom search grid SVM with radial basis function. Which model has the higher hold-out average accuracy? Which model is better at predicting the "event" when the "event" actually occurs?

# SOLUTION

```
### your code here
confusionMatrix.train(fit_glmnet_3)
```

## Cross-Validated (5 fold, repeated 3 times) Confusion Matrix
##

```
(entries are percentual average cell counts across resamples)
##
              Reference
##
## Prediction
               event non_event
##
     event
                 7.1
                            2.6
               31.9
                           58.4
##
     non event
##
##
    Accuracy (average): 0.6551
### your code here
confusionMatrix.train(fit svm rbf)
  Cross-Validated (5 fold, repeated 3 times) Confusion Matrix
##
   (entries are percentual average cell counts across resamples)
##
##
##
              Reference
## Prediction
               event non_event
##
     event
                 6.0
##
     non event 33.0
                           56.9
```

Which model has the higher hold-out average accuracy? Which model is better at predicting the "event" when the "event" actually occurs? \*\*?

The elastic-net model appears to have higher average accuracy than the sym-rbf. The elastic-net model appears to also be better at predicting the event when it occurs (corresponding to higher sensitivity).

## 4b)

## ##

Accuracy (average): 0.6287

The previous question was alluding to the Sensitivity or True Positive (TP) rate of the models. You might have noticed that in the caret model object print outs, there are two other columns next to ROC: Sens, and Spec. Sens is the Sensitivity, or TP rate, and Spec is the Specificity which is related to the False Positive (FP) rate. We will now go through understanding the Sensitivity and Specificity in relationship to the ROC curve itself.

You will need to work with the hold-out set predictions directly to accomplish this. As discussed in lecture, the predictions are contained within the \$pred data.frame within thecaret model object. The first 11 rows associated with the hold-out set predictions for the fit\_svm\_rbf\_b object are printed to screen for you in the code chunk below.

```
fit_svm_rbf_b$pred %>% tbl_df() %>% head(11)
```

```
## # A tibble: 11 x 8
##
                                                                 C Resample
      pred
                obs
                           event non event rowIndex
                                                      sigma
##
      <fct>
                <fct>
                           <dbl>
                                     <dbl>
                                               <int>
                                                      <dbl> <dbl> <chr>
                                                              0.5 Fold1.Rep1
##
   1 non_event non_event 0.345
                                     0.655
                                                   4 0.0670
##
                           0.360
                                     0.640
                                                   7 0.0670
                                                              0.5 Fold1.Rep1
    2 non_event event
##
   3 non event event
                           0.383
                                     0.617
                                                  10 0.0670
                                                              0.5 Fold1.Rep1
   4 non_event non_event 0.352
                                                              0.5 Fold1.Rep1
##
                                     0.648
                                                  11 0.0670
##
    5 non event event
                           0.418
                                     0.582
                                                  23 0.0670
                                                              0.5 Fold1.Rep1
   6 non_event non_event 0.356
                                     0.644
                                                  27 0.0670
                                                              0.5 Fold1.Rep1
```

```
## 7 non_event non_event 0.381
                                    0.619
                                                29 0.0670
                                                            0.5 Fold1.Rep1
                                                31 0.0670
                                                            0.5 Fold1.Rep1
## 8 non_event event
                          0.334
                                    0.666
                                                            0.5 Fold1.Rep1
## 9 non event event
                          0.393
                                    0.607
                                                33 0.0670
                                                            0.5 Fold1.Rep1
## 10 non_event event
                          0.422
                                    0.578
                                                34 0.0670
## 11 non event event
                          0.389
                                    0.611
                                                41 0.0670
                                                            0.5 Fold1.Rep1
```

The last column Resample is an identifer for the resample Fold ID (in this case). The code chunk below counts the number of rows in the hold-out prediction object associated with each Fold.

```
fit_svm_rbf_b$pred %>% tbl_df() %>%
count(Resample)
```

```
## # A tibble: 15 x 2
##
     Resample
##
      <chr>
                <int>
  1 Fold1.Rep1 8400
##
## 2 Fold1.Rep2 8400
## 3 Fold1.Rep3
                 8400
## 4 Fold2.Rep1
                 8400
## 5 Fold2.Rep2
                 8400
## 6 Fold2.Rep3
                 8400
## 7 Fold3.Rep1
                 8400
## 8 Fold3.Rep2
                 8400
## 9 Fold3.Rep3
                 8400
## 10 Fold4.Rep1
                 8400
## 11 Fold4.Rep2
                 8400
## 12 Fold4.Rep3
                 8400
## 13 Fold5.Rep1
                 8400
## 14 Fold5.Rep2
                 8400
## 15 Fold5.Rep3 8400
```

The reason why it seems like there are so many predictions, is because of all of the C and sigma combinations that were tried! To simplify things, you will focus just on the best tuned case when creating the ROC curves.

## **PROBLEM**

Complete the code chunk below which filters the hold-out prediction object for the SVM radial basis kernel to focus just on the best tuned C and sigma values. In addition, you must focus just on "Fold1". The result is stored to the best\_svm\_rbf\_F1\_pred object.

How can you check if the resulting object has the correct number of rows?

HINT: How can you access the best tuned C and sigma values?

```
## # A tibble: 300 x 8
##
                obs
                                                                 C Resample
      pred
                           event non_event rowIndex sigma
      <fct>
##
                <fct>
                           <dbl>
                                     <dbl>
                                               <int>
                                                      <dbl> <dbl> <chr>
                                     0.681
                                                   4 0.0670
                                                                 1 Fold1.Rep1
##
    1 non_event non_event 0.319
##
    2 non event event
                           0.343
                                     0.657
                                                   7 0.0670
                                                                 1 Fold1.Rep1
##
    3 non event event
                           0.378
                                     0.622
                                                  10 0.0670
                                                                 1 Fold1.Rep1
##
   4 non event non event 0.330
                                     0.670
                                                  11 0.0670
                                                                 1 Fold1.Rep1
##
    5 non event event
                           0.436
                                     0.564
                                                  23 0.0670
                                                                 1 Fold1.Rep1
##
    6 non_event non_event 0.336
                                     0.664
                                                  27 0.0670
                                                                 1 Fold1.Rep1
##
   7 non_event non_event 0.376
                                     0.624
                                                  29 0.0670
                                                                 1 Fold1.Rep1
   8 non_event event
                           0.304
                                     0.696
                                                  31 0.0670
                                                                 1 Fold1.Rep1
                                                                 1 Fold1.Rep1
   9 non_event event
                           0.394
                                     0.606
                                                  33 0.0670
## 10 non_event event
                           0.441
                                     0.559
                                                  34 0.0670
                                                                 1 Fold1.Rep1
## # ... with 290 more rows
```

```
count(tbl_df(best_svm_rbf_F1_pred$Resample))
```

```
## # A tibble: 1 x 1
## n
## <int>
## 1 300
```

```
best_svm_rbf_F1_pred %>% tbl_df() %>%
count(Resample)
```

# How can you check if the resulting object has the correct number of rows?

By counting the Resample rows and comparing with the filter results. Since there are 1500 observations and we used 5 folds, each should contain 300 observations.

### 4c)

The confusionMatrix.train() function is specific to caret trained model objects. However, caret includes a more general function confusionMatrix() which requires at minimum two input arguments, the predicted class and the observed/target/reference class. The generic syntax is shown below:

```
confusionMatrix(<predicted class vector>, <observed/target/refernce class vector>)
```

This call produces a confusion matrix that returns counts rather than percentages. Substantial more information is printed to screen as well, including the 95% confidence interval on the Accuracy, the Senstivity, and the Specificity. The function also tells you which class label ("event" or "non\_event" in this problem) is considered to be the "Positive" class within the confusion matrix.

## **PROBLEM**

Call the confusionMatrix() function on the radial basis kernel SVM by passing in the predicted class and observed class correctly. How many False-Positive counts were observed in this fold?

After calling the function and printing the results to screen, call the confusionMatrix() function a second time, but this time save the results to the variable best\_svm\_rbf\_F1\_cm. Doing this allows you to access the confusion matrix results programmatically. To access the Sensitivity, you would use best\_svm\_rbf\_F1\_cm\$byClass["Sensitivity"]. Print the Sensitivity to the screen and check it is the same as what was displayed when you called the confusionMatrix() function directly.

### SOLUTION

### your code here

```
confusionMatrix(best svm rbf F1 pred$pred, best svm rbf F1 pred$obs)
## Confusion Matrix and Statistics
##
##
              Reference
## Prediction event non event
##
     event
                  20
                             7
                  97
                           176
##
     non_event
##
##
                  Accuracy : 0.6533
##
                    95% CI: (0.5965, 0.7071)
       No Information Rate: 0.61
##
       P-Value [Acc > NIR] : 0.06872
##
##
##
                     Kappa: 0.1541
##
##
    Mcnemar's Test P-Value : < 2e-16
##
##
               Sensitivity: 0.17094
##
               Specificity: 0.96175
##
            Pos Pred Value: 0.74074
            Neg Pred Value: 0.64469
##
##
                Prevalence: 0.39000
            Detection Rate: 0.06667
##
##
      Detection Prevalence: 0.09000
##
         Balanced Accuracy: 0.56634
##
##
          'Positive' Class : event
##
```

```
best_svm_rbf_F1_pred
```

```
## # A tibble: 300 x 8
                           event non_event rowIndex
##
      pred
                obs
                                                      sigma
                                                                 C Resample
##
      <fct>
                <fct>
                           <dbl>
                                      <dbl>
                                               <int>
                                                      <dbl> <dbl> <chr>
##
    1 non_event non_event 0.319
                                     0.681
                                                   4 0.0670
                                                                 1 Fold1.Rep1
##
    2 non_event event
                           0.343
                                     0.657
                                                   7 0.0670
                                                                 1 Fold1.Rep1
                                     0.622
##
    3 non_event event
                           0.378
                                                  10 0.0670
                                                                 1 Fold1.Rep1
    4 non_event non_event 0.330
                                     0.670
                                                  11 0.0670
                                                                 1 Fold1.Rep1
##
##
    5 non_event event
                           0.436
                                     0.564
                                                  23 0.0670
                                                                 1 Fold1.Rep1
##
                                     0.664
                                                  27 0.0670
                                                                 1 Fold1.Rep1
    6 non_event non_event 0.336
   7 non_event non_event 0.376
                                     0.624
                                                  29 0.0670
                                                                 1 Fold1.Rep1
```

```
8 non event event
                           0.304
                                     0.696
                                                  31 0.0670
                                                                1 Fold1.Rep1
## 9 non_event event
                           0.394
                                     0.606
                                                  33 0.0670
                                                                1 Fold1.Rep1
                                                                1 Fold1.Rep1
## 10 non event event
                           0.441
                                     0.559
                                                  34 0.0670
## # ... with 290 more rows
```

```
best_svm_rbf_F1_cm = confusionMatrix(best_svm_rbf_F1_pred$pred, best_svm_rbf_F1_pred$obs)
best_svm_rbf_F1_cm$byClass["Sensitivity"]
```

```
## Sensitivity
## 0.1709402
```

How many False-Positive counts were observed in this fold?\*\*? There were 7 false positives.

### 4d)

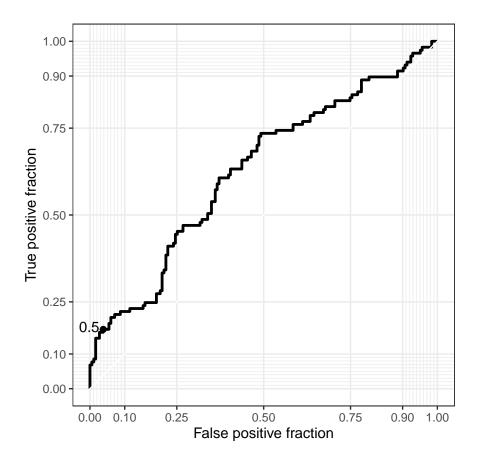
You will now plot the ROC curve associated with Fold 1 and the best tuned radial basis function SVM. You will use the plotROC package set of functions discussed in lecture to generate the ROC curve. Remember that within the plotROC syntax, you must set the probability of the EVENT of interest to the m aesthetic within the parent ggplot() call. You must also set the observed EVENT of interest as a 1 (if it occurred) and a 0 if it did not occur to the d aesthetic within the parent ggplot() call. The ROC curve itself is created by the geom\_roc() function, where you can specify other grouping variables (such as through the color aesthetic) and the number of "cuts" or specific "cut" values to display. The "cut" corresponds to the probability threshold value used to classify the EVENT.

### **PROBLEM**

Create the ROC curve using the variables contained within best\_svm\_rbf\_F1\_pred object. Specify the m and d aesthetics within the parent ggplot() call correctly. Specify the cutoffs.at argument within the geom\_roc() call to be equal to 0.5. After the geom\_roc() call, use the coord\_equal() and style\_roc() function calls.

```
best_svm_rbf_F1_pred %>% tbl_df()
```

```
## # A tibble: 300 x 8
##
                                                                C Resample
      pred
                obs
                           event non_event rowIndex
                                                      sigma
##
      <fct>
                <fct>
                           <dbl>
                                     <dbl>
                                               <int>
                                                      <dbl> <dbl> <chr>
                                     0.681
                                                   4 0.0670
                                                                1 Fold1.Rep1
##
   1 non_event non_event 0.319
                                                   7 0.0670
                                                                1 Fold1.Rep1
##
    2 non_event event
                           0.343
                                     0.657
    3 non_event event
                                                                1 Fold1.Rep1
##
                           0.378
                                     0.622
                                                  10 0.0670
##
    4 non_event non_event 0.330
                                     0.670
                                                  11 0.0670
                                                                1 Fold1.Rep1
                                                                1 Fold1.Rep1
##
   5 non_event event
                           0.436
                                     0.564
                                                  23 0.0670
  6 non_event non_event 0.336
                                     0.664
                                                  27 0.0670
                                                                1 Fold1.Rep1
                                                                1 Fold1.Rep1
##
   7 non_event non_event 0.376
                                     0.624
                                                  29 0.0670
                                                                1 Fold1.Rep1
##
  8 non_event event
                           0.304
                                     0.696
                                                  31 0.0670
  9 non event event
                           0.394
                                     0.606
                                                  33 0.0670
                                                                1 Fold1.Rep1
## 10 non event event
                           0.441
                                     0.559
                                                  34 0.0670
                                                                1 Fold1.Rep1
## # ... with 290 more rows
```



4e)

In Problem 4c) you saved the confusion matrix calculations to an object, best\_svm\_rbf\_F1\_cm. This allows you to programmatically access the Sensitivity and Specificity associated with the results. To help interpret the ROC curve, you will now plot the Sensitivity as a red dashed horizontal line, and 1 - Specificity as a red dashed vertical line.

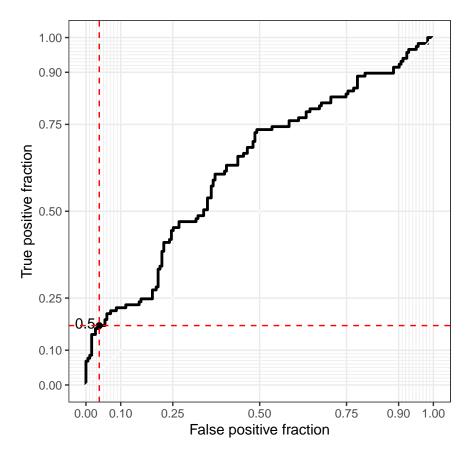
# **PROBLEM**

Remake the ROC curve from Problem 4d). This time include the geom\_hline() and geom\_vline() before the coord\_equal() "layer". Within geom\_hline() set the yintercept argument equal to the Sensitivity. Within geom\_vline() set the xintercept argument equal to 1 - Specificity. Within both geom\_hlin() and geom\_vline() set the color argument to "red" and the linetype argument to "dashed".

Based on the resulting figure, what threshold value do you think is used to calculate the reported Sensitivity and Specificity values in the confusionMatrix() function?

HINT: Look back at how to access the Sensitivity from the saved confusion matrix object.

#### SOLUTION



Based on the resulting figure, what threshold value do you think is used to calculate the reported Sensitivity and Specificity values in the confusionMatrix() function? ? 0.5 appears to be the threshold value used to calculate the Sensitivity and Specificity.

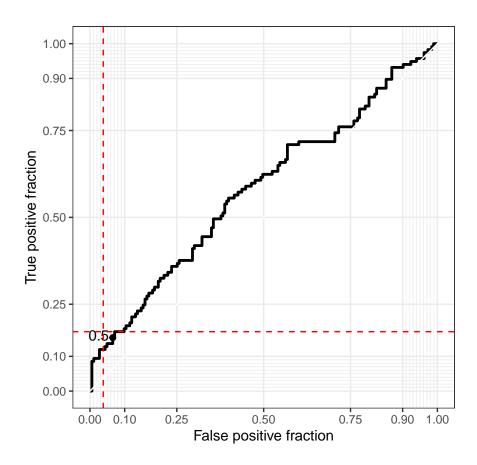
4f)

The ROC curve you created in the previous problems corresponds to just a single Fold. In this problem, you will repeat the previous set of actions, but this time for fold 4.

### **PROBLEM**

Create the best\_svm\_rbf\_F4\_pred object by filtering to just the fourth fold associated with the best tuning parameter values. Calculate the confusion matrix and store to best\_svm\_rbf\_F4\_cm. Generate the ROC curve and include the Sensitivity and 1 - Specificity as horizontal and vertical dashed lines, respectively.

How does the fourth fold compare to the performance of the first fold you visualized previously?



? The 4th fold appears to be straighter than the previous.

### **4g**)

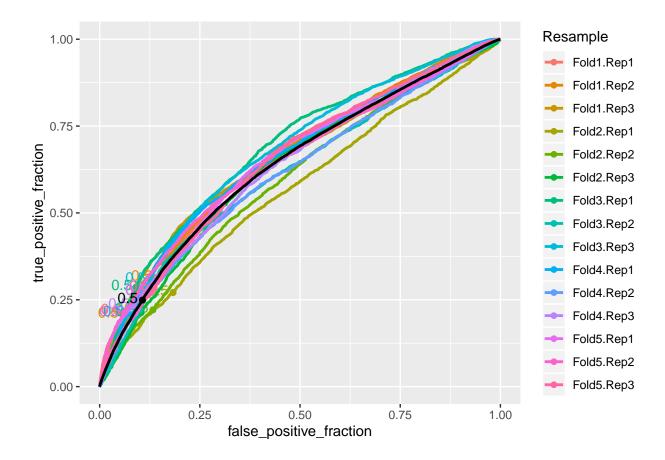
Let's now compare the variability in the ROC curves across the folds to the overall averaged ROC curve for the best tuning parameter values. To create this figure, you will need to make use of the color aesthetic within the <code>geom\_roc()</code> call.

# **PROBLEM**

Create the best\_svm\_rbf\_pred object which filters the tuning parameters to equal their best identified values. You will not filter any of the Resample folds. Use best\_svm\_rbf\_pred with two different geom\_roc() calls. In the first call, set the color aesthetic equal to Resample. In the second geom\_roc() do not use any additional aesthetics. In both geom\_roc() calls set the cutoff.at argument equal to 0.5. Do not include any additional reference lines.

The colored ROC curves correspond to the separate Resample folds. How does the overall average ROC curve compare to the fold-to-fold variability? Which fold appears to have the worse performance?

```
best_svm_rbf_pred <- fit_svm_rbf_b$pred %>% tbl_df() %>%
filter()
```



How does the overall average ROC curve compare to the fold-to-fold variability? Which fold appears to have the worse performance?\*\*

The overall ROC curve appears to be thicker than those with fold-to-fold variability. The green colored fold (2) appears to have the best performance since it's area is greatest.

# 4h)

Let's now compare the ROC curves between logistic regression, elastic net, SVM with linear kernel, and SVM with radial basis kernel. You have the required information contained within best\_svm\_rbf\_pred object to create the figure, but not all caret \$pred objects will be the same. The number of columns will vary based upon the number of tuning parameters. Therefore you need to take a few additional steps to enable merging together the results.

The code chunk below demonstrates how to do that with the results from the logistic regression model. The logistic regression model does not include any tuning parameters, and so it coincides with the "best" tuned model without requiring additional filtering steps. The code chunk uses the dplyr::select() function to grab the minimum set of columns needed to make the ROC curve. It then uses the mutate() function to create a new column model\_name which is set to "GLM". The result is saved to the best\_glm\_cv\_pred.

```
best_glm_cv_pred <- fit_glm$pred %>% tbl_df() %>%
  dplyr::select(pred, obs, event, non_event, rowIndex, Resample) %>%
  mutate(model_name = "GLM")
```

### **PROBLEM**

You will follow the logistic regression example and isolate the best tuning parameter values and put the results into the correct format for the elastic net with all 3-way interactions, the SVM with linear kernel, and the SVM with radial basis kernel.

Name the elastic net model "GLMNET-3". Name the SVM with linear kernel "SVM-LIN". Name the SVM with radial basis kernel "SVM-RBF".

### **SOLUTION**

4i)

The code chunk below combines all of the best tuning parameter hold-out set predictions together.

```
best_mod_cv_pred_a <- best_glm_cv_pred %>%
bind_rows(best_glmnet_3_cv_pred) %>%
bind_rows(best_svm_lin_cv_pred) %>%
bind_rows(best_svm_rbf_cv_pred)
```

The best\_mod\_cv\_pred\_a object is now in a format suitable for generating separate resample averaged ROC curves for the different models.

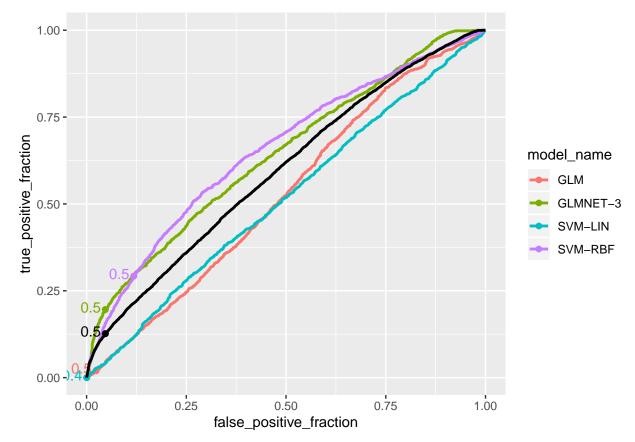
### **PROBLEM**

Create the ROC curves for each model by correctly specifying the m and d aesthetics within the parent ggplot() call. Set the color aesthetic within geom\_roc() equal to model\_name, and set the cutoff.at argument equal to 0.5.

Which model appears the best, based on the Resample averaged ROC curves?

### SOLUTION

```
### compare the models by comparing their resample
### averaged ROC curves!!!
best_mod_cv_pred_a %>%
    ggplot(mapping = aes(m = event, d = ifelse(obs == 'event',1,0))) +
    geom_roc(mapping = aes(color = model_name), cutoffs.at = 0.5) +
    geom_roc(cutoffs.at = 0.5)
```



Which model appears the best, based on the Resample averaged ROC curves?

. The SVM-RBF model appears to be best.

# Problem 5

You will now train several more complex models. Let's first start with a neural network to predict the binary outcome. You will set the method argument equal to "nnet" in the call to train(). If this is the first you have used nnet caret will ask if the necessary packages can be downloaded. Check the R console for the prompting questions.

5a)

## **PROBLEM**

Use the caret default grid search to tune a neural network model. Besides changing the method argument to "nnet", the other arguments should be consistent with the other problems.

However, it is recommended that you set the trace argument to FALSE. If you do not all of the iterations will be printed to screen and therefore to your rendered PDF file. SET trace to FALSE.

After training is complete, WHICH MIGHT TAKE SEVERAL MINUTES, print the caret object to screen. Which set of tuning parameters produce the best performing model?

### SOLUTION

fit\_nnet\_a

```
## Neural Network
##
## 1500 samples
##
     7 predictor
##
     2 classes: 'event', 'non_event'
##
## No pre-processing
## Resampling: Cross-Validated (5 fold, repeated 3 times)
## Summary of sample sizes: 1200, 1200, 1200, 1200, 1200, 1200, ...
## Resampling results across tuning parameters:
##
##
    size decay ROC
                            Sens
                                        Spec
##
          0e+00 0.5364890 0.22336182 0.8313297
##
    1
          1e-04 0.5477512 0.17834758 0.8732240
##
          1e-01 0.5137515 0.08205128 0.9362477
          0e+00 0.5772500 0.33105413 0.7715847
##
    3
    3
          1e-04 0.5961468 0.33675214 0.7970856
##
##
    3
          1e-01 0.6823471 0.41595442 0.8269581
##
    5
          0e+00 0.6298289 0.40740741 0.7730419
##
    5
          1e-04 0.6251989 0.42621083 0.7519126
##
    5
          1e-01 0.7146451 0.47806268 0.8069217
##
## ROC was used to select the optimal model using the largest value.
## The final values used for the model were size = 5 and decay = 0.1.
```

The parameters with size = 5 appear to produce the best result with ROC = 0.715.

5b)

As you should see from Problem 5a), the tuning parameters to a neural network from nnet are size and decay. size is the number of hidden units within the hidden layer, and decay is the weight decay of

the parameters. Weight decay provides regularization effects to the parameters. The larger the decay the stronger a regularizing effect.

You will now try a custom grid search to study what happens if more hidden units are used within the model.

### **PROBLEM**

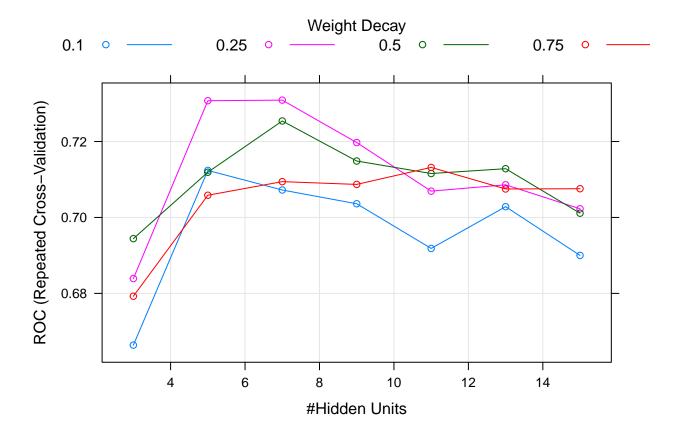
Create a grid, nnet\_grid, with the expand.grid() function. Set the size variable to a vector with values of 3, 5, 7, 9, 11, 13, 15. Set the decay variable within the grid to be a vector with values 0.1, 0.25, 0.5, and 0.75 Train the neural network model by setting the tuneGrid argument equal to nnet\_grid. BE SURE TO SET trace equal to FALSE.

Once the training completes, WHICH MIGHT TAKE SEVERAL MINUTES, plot the results using the plot() function and print the best tuning values to screen.

```
### print out the best tuning parameters
### and plot the results
fit_nnet_b$bestTune
```

```
## size decay
## 10    7    0.25

plot(fit_nnet_b)
```



**5c**)

### **PROBLEM**

Display the confusion matrix percentages associated with the training results. How does the neural network model compare in accuracy with the other models you have built so far?

# SOLUTION

```
### your code here
confusionMatrix(fit_nnet_b)
## Cross-Validated (5 fold, repeated 3 times) Confusion Matrix
##
##
   (entries are percentual average cell counts across resamples)
##
##
              Reference
## Prediction
               event non_event
                19.6
##
     event
                           11.6
##
     non_event
               19.4
                           49.4
##
    Accuracy (average) : 0.6902
```

How does the neural network model compare in accuracy with the other models you have built so far?\*\*? The neural net model appears to be slightly better in accuracy than the rest but, in general, as good the other models.

5d)

Next, you will visualize the ROC curve associated with the best neural network model.

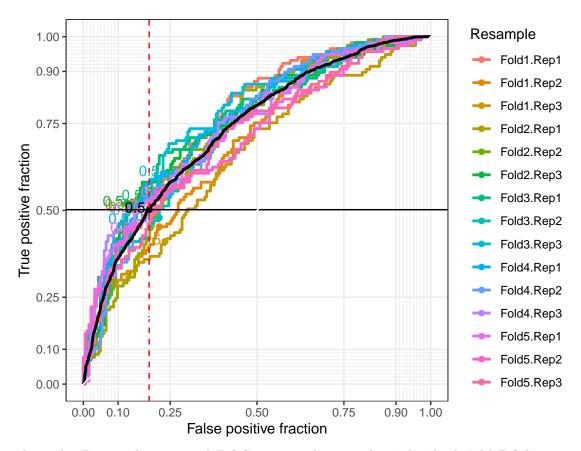
#### **PROBLEM**

Filter the hold-out set predictions for the best neural network model. Do not filter based on the Resample. Store the results to best\_nnet\_cv\_pred. Follow the same format as the best\_glm\_cv\_pred object, by selecting a specific set of the variables and create a new column, model\_name = "NNET". Use the variables within best\_nnet\_cv\_pred with the confusionMatrix() function and store the results to best\_nnet\_cm. Create the Resample averaged ROC curve and compare to the individual Resample Folds ROC curves. For reference, plot the Sensitivity and 1 - Specificity as horizontal and vertical red dashed lines.

How does the Resample averaged ROC curve relate to the individual Fold ROC curves for the neural network model?

How does the location of the 50% threshold compare to that for the other models?

```
best_nnet_cv_pred <- fit_nnet_b$pred %>% tbl_df() %>%
  filter(size == fit_nnet_b$bestTune$size,
         decay == fit_nnet_b$bestTune$decay)%>% mutate(model_name = "NNET")
best_nnet_cm <- confusionMatrix(best_nnet_cv_pred$pred, best_nnet_cv_pred$obs)</pre>
### ROC curves for the NNET model
best_nnet_cv_pred %>%
     ggplot(mapping = aes(m = event,
                         d = ifelse(obs == 'event',1,0))) +
    geom_roc(mapping = aes(color = Resample), cutoffs.at = 0.5) +
    geom\ roc(cutoffs.at = 0.5) +
  geom_hline(yintercept = best_nnet_cm$byClass["Sensitivity"]) +
  geom vline(xintercept = 1 - best nnet cm$byClass["Specificity"],
             color ='red',
             linetype ="dashed")+
    coord_equal() +
    style roc()
```



How does the Resample averaged ROC curve relate to the individual Fold ROC curves for the neural network model?

How does the location of the 50% threshold compare to that for the other models? ?

For the nnet model, the resample avg ROC curve appears to be in the middle of the individual curves. The location of the 50% threshold appears higher than that for other models.

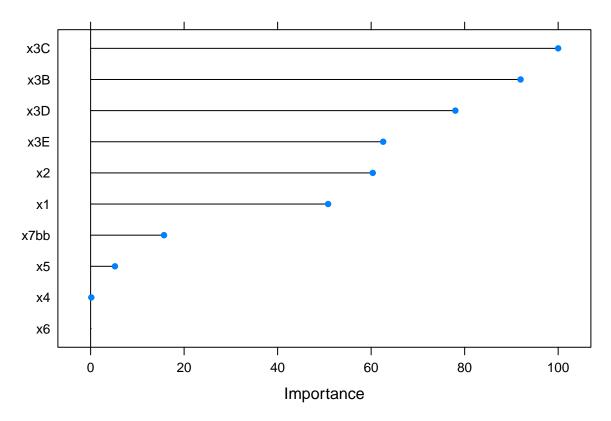
**5e**)

We discussed how individual hidden unit parameters cannot be used to interpret input importance with neural networks. We discussed that all of the hidden units and output layer parameters would need to be considered. Although this sounds challenging, methods exist for analyzing such variable importances with neural networks. In caret, all you have to do is call the varImp() function on the nnet associated caret model object.

### **PROBLEM**

Use the plot() function to plot the variable importances as viewed by the neural network model. Which inputs are considered to be 20% or less of the importance of the top predictor (feature)?

```
### your code here
plot(varImp(fit_nnet_b))
```



Which inputs are considered to be 20% or less of the importance of the top predictor (feature)?\*\*? Inputs x7bb, x5, and x6 appear to be of 20% or less importance than the top.

# Save memory

NOTE: To save RAM the code chunk below deletes objects that we will no longer use.

```
rm(fit_glmnet_2, fit_glmnet_3, fit_nnet_a, fit_svm_rbf)
rm(best_svm_rbf_F1_cm, best_svm_rbf_F4_cm, best_svm_rbf_F1_pred, best_svm_rbf_F4_pred)
rm(best_nnet_cm)
rm(best_glm_cv_pred, best_glmnet_3_cv_pred, best_svm_lin_cv_pred, best_svm_rbf_cv_pred)
```

# Problem 6

You will now build a random forest model using caret. The method argument within train() will be set to "rf". If this is your first time building a random forest model in R, caret will ask if it can download and install the necessary packages. Please look at the R console for the prompt. There are other random forest implementations in R, but the one associated with the "rf" method is the original.

6a)

As discussed in lecture, the main tuning parameter for a random forest is the number of randomly selected predictors (features) to try at a split, mtry. You will use the default number of trees.

### **PROBLEM**

In the code chunk below create a grid of possible mtry values to consider. Set the mtry variable within the expand.grid() call to be a vector with elements equal to 2, 3, 5, 7. Train the model using arguments consistent with the previous training calls, but set the rf\_grid equal to the tuneGrid argument, and set method equal to "rf". Also, include the importance = TRUE within the train() call.

After training completes, WHICH MIGHT TAKE A FEW MINUTES, print the result to screen. Which value of mtry provides the best performing model? Which mtry corresponds to a bagged tree model?

### SOLUTION

```
rf_grid <- expand.grid(mtry=c(2,3,5,7))</pre>
```

## fit\_rf

```
## Random Forest
##
## 1500 samples
##
      7 predictor
##
      2 classes: 'event', 'non_event'
##
## No pre-processing
## Resampling: Cross-Validated (5 fold, repeated 3 times)
## Summary of sample sizes: 1200, 1200, 1200, 1200, 1200, 1200, ...
## Resampling results across tuning parameters:
##
##
          ROC
     mtry
                      Sens
                                 Spec
##
     2
           0.6356779 0.1680912 0.9486339
##
     3
           0.6638005 0.3168091 0.8899818
##
     5
           0.6776672  0.3612536  0.8695811
##
    7
           0.6858593 0.3908832 0.8663024
## ROC was used to select the optimal model using the largest value.
## The final value used for the model was mtry = 7.
```

Which value of mtry provides the best performing model? Which mtry corresponds to a bagged tree model?\*\*\*

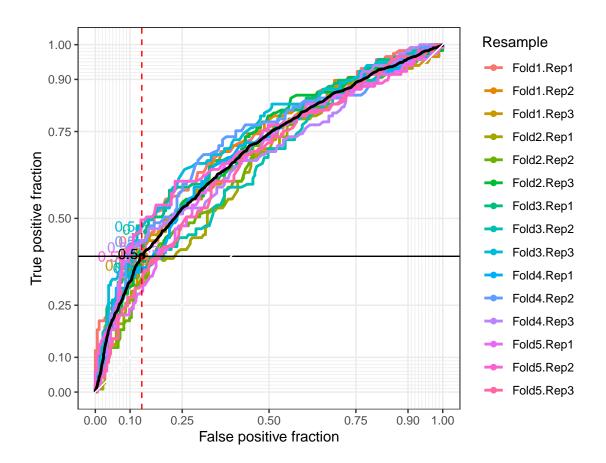
mtry = 7 appars to provide the best performance. The final mtry value of 7 corresponds to a bagged tree. ### 6b)

Let's now look at the ROC curve for the best performing random forest model.

### **PROBLEM**

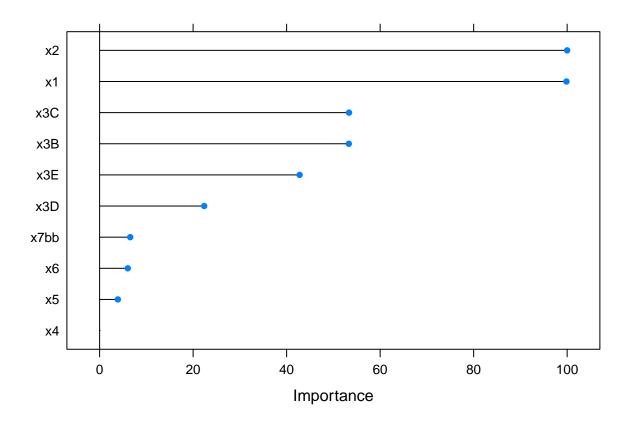
Extract the hold-out set predictions for the best tuned random forest model and store the result to best\_rf\_cv\_pred. Do not filter by Resample. Follow the example with best\_glm\_cv\_pred by selecting a specific subset of the variables. Create a new column with mutate() with model\_name = "RF". Use the variables within best\_rf\_cv\_pred and the confusionMatrix() function to calculate the confusion matrix, and store the result to best\_rf\_cm. Create the ROC curve similar to that for the neural network model where you compared the resample averaged ROC curve to the ROC curves associated with each resample fold. Include the Sensitivity and 1 - Specificity as reference lines.

```
best_rf_cv_pred <- fit_rf$pred %>% tbl_df() %>%
  filter(mtry == fit_rf$bestTune$mtry)%>%
  mutate(model name = "RF")
best rf cm <- confusionMatrix(best rf cv pred$pred, best rf cv pred$obs)
### create the ROC curve for the random forest model
best_rf_cv_pred %>%
     ggplot(mapping = aes(m = event,
                         d = ifelse(obs == 'event',1,0))) +
    geom_roc(mapping = aes(color = Resample), cutoffs.at = 0.5) +
    geom_roc(cutoffs.at = 0.5) +
    geom_hline(yintercept = best_rf_cm$byClass["Sensitivity"]) +
    geom_vline(xintercept = 1 - best_rf_cm$byClass["Specificity"],
             color ='red',
             linetype ="dashed")+
    coord_equal() +
    style_roc()
```



6c

plot(varImp(fit\_rf))



# **PROBLEM**

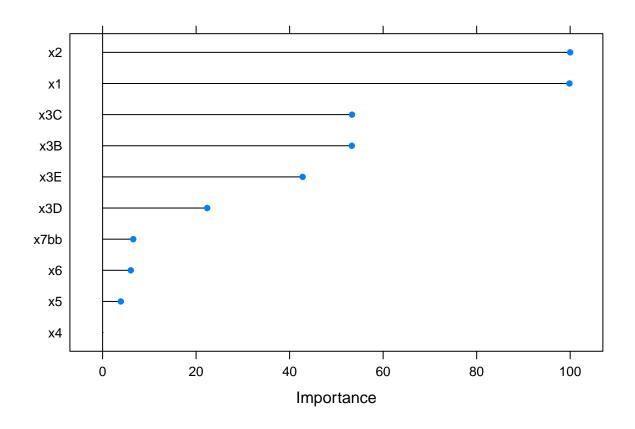
Plot the variable importances as viewed by the random forest model. Do any inputs have a relative importance of less than 20% of the top input? If so, which ones?

How do the variable importances compare between the random forest and neural network models?

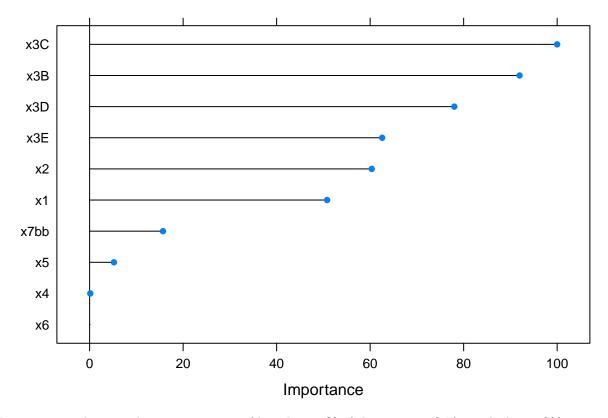
Yes. x7bb, x6, and x5 have relative importance less than 20%. The variable importances are similar to that of the neural network in terms of the unimportant variables but different in terms of the important ones.

# SOLUTION

### your code here
plot(varImp(fit\_rf))



plot(varImp(fit\_nnet\_b))



Do any inputs have a relative importance of less than 20% of the top input? If so, which ones?\*\*

# How do the variable importances compare between the random forest and neural network models?

?

Yes. x7bb, x6, and x5 have relative importance less than 20%. The variable importances are similar to that of the neural network in terms of the unimportant variables but different in terms of the important ones.

# Problem 7

You will now build a boosted tree model using the method equal to "gbm". If this is the first time using a "gbm" in R follow the R console prompts to install and download the package.

### 7a)

As discussed in lecture boosted trees have more tuning parameters compared to the random forest. You will start out considering a default value for the learning rate (the shrinkage) of 0.1, while varying the number of trees, n.trees, and the interaction depth, interaction.depth. You try out two different n.minobsinnode values as well.

# PROBLEM

Create a grid of tuning parameter values, gbm\_grid\_a, with the expand.grid() function. Set the variable n.trees to a vector from 50 to 1050 by 100. Set interaction.depth to a vector with values of 1, 9, and 18. Set n.minobsinnode to be 5 and 10. Use the default shrinkage.

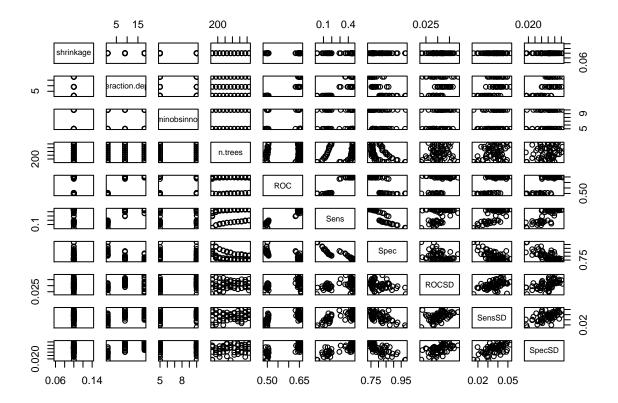
Train the boosted model using arguments consistent with the previous models, except set the method to "gbm" and tuneGrid to gbm\_grid\_a. Set verbose to FALSE to prevent each iteration from being printed to the screen.

After training is complete, WHICH WILL TAKE A FEW MINUTES, use the plot() function to plot the results and print the best tuning parameter values to the screen.

```
### print out the best tuning parameters and plot
### the results
fit_gbm_a$bestTune
```

```
## n.trees interaction.depth shrinkage n.minobsinnode
## 46   150     18     0.1     5

plot(fit_gbm_a$results)
```



# 7b)

### **PROBLEM**

Which interaction.depth yielded the best results? What do you think that represents about the model behavior?

# SOLUTION

?

An interaction depth of 18 appears to have yielded the best result. This suggests the model converges relatively quickly.

7c)

Now let's try lowering the learning rate. You will keep the interaction.depth fixed to 18 and the n.minobsinnode fixed at 5 for this problem.

### **PROBLEM**

Specify a new grid with expand.grid(). Set the variable n.trees to be a vector from 250 to 2250 by increments of 500. Set the shrinkage to 0.005 and 0.01. Set the interaction.depth to 18 and the n.minobsinnode equal to 5.

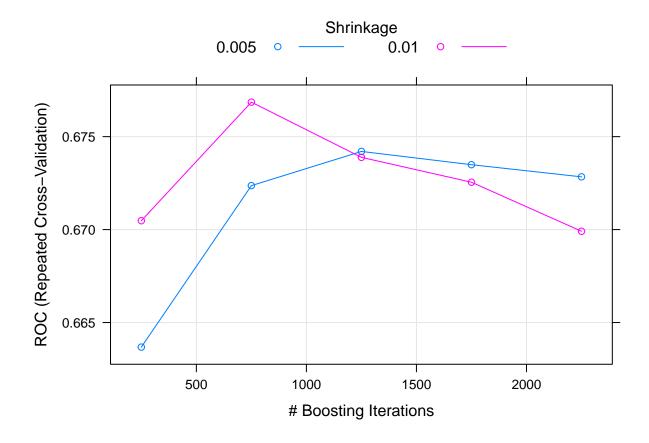
Train the boosted tree, using arguments similar to that in Problem 7a). Be sure to set verbose to FALSE. After training is complete, print results to screen and plot the results.

### THE MODEL WILL TAKE SEVERAL MINUTES TO TRAIN.

# SOLUTION

plot(fit\_gbm\_b)

```
gbm grid b <- expand.grid(n.trees=seq(250, 2250, by=500),
                         interaction.depth = 18,
                         shrinkage=c(0.005,0.01),
                         n.minobsinnode=5)
set.seed(98131)
fit_gbm_b <- train(output ~ . ,</pre>
               method = "gbm",
               data = train_df,
               metric = metric used,
               trControl = ctrl_k05,
               tuneGrid = gbm_grid_b,
               verbose = FALSE)
fit_gbm_b
## Stochastic Gradient Boosting
##
## 1500 samples
##
     7 predictor
     2 classes: 'event', 'non_event'
##
##
## No pre-processing
## Resampling: Cross-Validated (5 fold, repeated 3 times)
## Summary of sample sizes: 1200, 1200, 1200, 1200, 1200, 1200, ...
## Resampling results across tuning parameters:
##
##
    shrinkage n.trees ROC
                                  Sens
                                            Spec
##
    0.005
              250
                       0.6636775 0.1487179 0.9650273
                       0.6723647 0.3213675 0.8950820
    0.005
               750
##
    0.005
##
             1250 0.6742048 0.3658120 0.8586521
##
    0.005
             1750 0.6734918 0.3903134 0.8397086
##
    0.005
             2250 0.6728379 0.4091168 0.8240437
             250
##
    0.010
                       0.6704778 0.2638177 0.9198543
##
    0.010
              750 0.6768577 0.3874644 0.8444444
##
    0.010
             1250
                       0.6725484 0.4273504 0.7996357
              1750
##
    0.010
##
    0.010
               2250
                       0.6699111 0.4358974 0.7938069
##
## Tuning parameter 'interaction.depth' was held constant at a value of
## Tuning parameter 'n.minobsinnode' was held constant at a value of 5
## ROC was used to select the optimal model using the largest value.
## The final values used for the model were n.trees = 750,
   interaction.depth = 18, shrinkage = 0.01 and n.minobsinnode = 5.
### plot the results
```



7d)

Let's now assemble the two different boosted tree model results into the format to create the ROC curve. You must filter the hold-out set predictions to just the best tuned models, but you do not need to filter by Resample.

### **PROBLEM**

Create the best\_gbm\_cv\_pred\_a and best\_gbm\_cv\_pred\_b objects by filtering the best tuned parameter values. Do not filter by the Resample. Follow the best\_glm\_cv\_pred format and select a specific subset of the variables, and mutate() a new column. Set the model\_name = "GBM-A" for best\_gbm\_cv\_pred\_a and model\_name = "GBM-B" for best\_gbm\_cv\_pred\_b.

The second code chunk is completed for you. It merges the two GBM results together into a single object. You must use this new object, best\_gbm\_cv\_preds, to compare the two different boosted tree models through ROC curves.

Create the ROC curve by specifying the m and d aesthetics in the parent ggplot() call correctly. Use two geom\_roc() calls, where the first one sets the color aesthetic equal to Resample and the second geom\_roc() call does not specify other additional aesthetics. In each geom\_roc() call set cutoff.at equal to 0.5. This time you must use the facet\_wrap() function to create a facet based on model\_name.

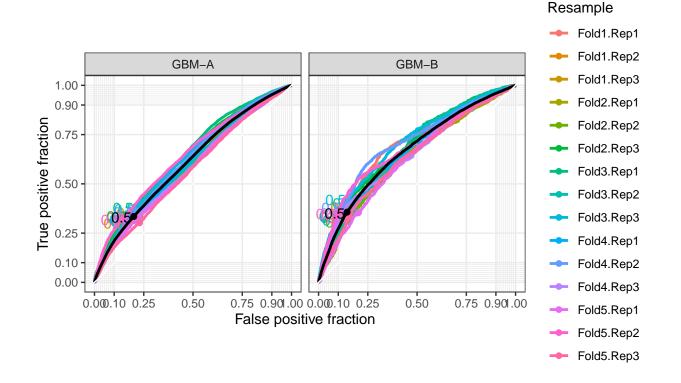
```
best_gbm_cv_pred_a <- fit_gbm_a$pred %>% tbl_df() %>%
  filter(n.trees, interaction.depth, shrinkage, n.minobsinnode)%>%
  mutate(model_name = "GBM-A")

best_gbm_cv_pred_b <- fit_gbm_b$pred %>% tbl_df() %>%
  filter(n.trees, interaction.depth, shrinkage, n.minobsinnode)%>%
  mutate(model_name = "GBM-B")

### requires the code chunk above, solution 07d, to
```

```
### requires the code chunk above, solution_07d, to
### be completed properly
best_gbm_cv_preds <- best_gbm_cv_pred_a %>%
bind_rows(best_gbm_cv_pred_b)
```

Compare the two boosted trees through their ROC curves.



It's time to compare the different models based on their ROC curves. The code chunk below merges the neural net, random forest, and the boosted tree model hold-out predictions with the previously compiled model results best\_mod\_cv\_pred\_a. The new object is named best\_mod\_cv\_pred\_b, and as a check the the count() function is applied to model\_name to show all of the models of interest are assembled.

```
best_mod_cv_pred_b <- best_mod_cv_pred_a %>%
bind_rows(best_nnet_cv_pred) %>%
bind_rows(best_rf_cv_pred) %>%
bind_rows(best_gbm_cv_preds)

best_mod_cv_pred_b %>%
count(model_name)
```

```
## # A tibble: 8 x 2
##
     model_name
                      n
##
     <chr>>
                  <int>
## 1 GBM-A
                297000
## 2 GBM-B
                  45000
## 3 GLM
                   4500
## 4 GLMNET-3
                   4500
## 5 NNET
                   4500
## 6 RF
                   4500
## 7 SVM-LIN
                   4500
## 8 SVM-RBF
                   4500
```

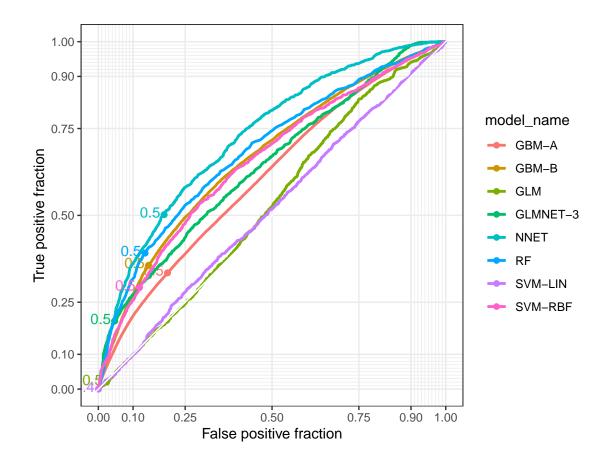
### **PROBLEM**

Create the ROC curves for each model by correctly specifying the m and d aesthetics within the parent ggplot() call. Set the color aesthetic within geom\_roc() equal to model\_name, and set the cutoff.at argument equal to 0.5.

Which model appears the best, based on the Resample averaged ROC curves?

## SOLUTION

Based on the resampled avg ROC curves, the GBM-B model appears to be best.



**7f**)

### **PROBLEM**

Based on the ROC curves in Problem 7d), which is the best performing model?

Which model has the highest Sensitivity at the 50% threshold value?

We have discussed several times in lecture the shape of the "ideal" ROC curve. Based on all of the ROC curves you have generated, can you describe why the "ideal" ROC curve looks the way it does?

### **SOLUTION**

?

Based on the ROC curves in 7d, the NNET model appears to be the best performing. The NNET model appears to have the highest Sensitivity at 50% threshold.

# **7g**)

The resamples() function in caret allows compiling all of the resample fold results and extracting the best tuned parameter values. It essentially provides a short cut to comparing models, without having to resort to working with the hold-out predictions directly. We needed those predictions in the assignment in order to generate the ROC curves. However, the resamples() function allows comparing models even when the predictions were not saved.

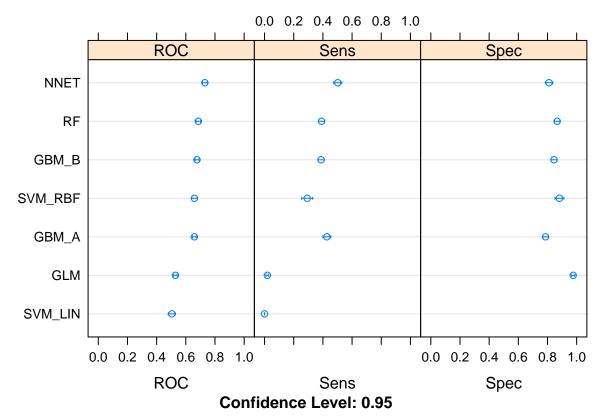
To use the resamples() function, each caret model object must be assigned to a variable in a list. The code chunk below is started for you for the logistic regression model fit. You will complete the list by assigning the models as specified by the names in the list.

### **PROBLEM**

Complete the list in the first code chunk below. Once completed, use the dotplot() function to summarize the performance metrics across the resample folds for each model. Are the results consistent with your conclusions based on the ROC curves directly?

### SOLUTION

```
### call the dotplot function to compare the models
dotplot(mod_results)
```



Are the results consistent with your conclusions based on the ROC curves directly?\*\*\*  $^{2}$ 

Yes, the results are consistent with conclusions.