```
- MODULE optishopylist
EXTENDS TLC, Integers, FiniteSets, Sequences, Reals
CONSTANTS PRODUCTS, APPS, IDs, GATEAPPS
Assume Cardinality(APPS) > 0
PT \triangleq \text{Instance } PT
set ++ item \stackrel{\Delta}{=} set \cup \{item\}
set -- item \triangleq set \setminus \{item\}
In shoppying list, the product is in fact the identifier. Any item could have an information for
how much of a product one wants to buy (not relevant in this specification).
                  \triangleq [id : PRODUCTS, bought : BOOLEAN]
ShopyItems
ADD\_ACTION \triangleq  "add"
RM\_ACTION \stackrel{\triangle}{=} "rm"
SET\_BOUGHT\_ACTION \triangleq "set_bought"
REQ\_SYNC\_ACTION \triangleq "req\_sync"
RESP\_SYNC\_ACTION \triangleq "resp\_sync"
END\_SYNC\_ACTION \triangleq "end\_sync"
Actions is the set of all possible actions in the system.
Actions \triangleq \{
    ADD_ACTION,
    RM\_ACTION,
    SET_BOUGHT_ACTION,
    REQ\_SYNC\_ACTION,
    RESP\_SYNC\_ACTION,
    END\_SYNC\_ACTION
}
SyncActions \triangleq \{REQ\_SYNC\_ACTION, RESP\_SYNC\_ACTION\}
SyncMsqs is the set of all possible messages sent for synchronisation of shopy lists.
SyncMsqs \stackrel{\triangle}{=}
   [id:IDs,
    app:APPS,
     list: Subset ShopyItems,
     mergedList: SUBSET ShopyItems,
     type: SyncActions
Messages sent for joining the network.
JoinRespMsgs \triangleq
   [app:APPS,
    knownHosts: PT!SeqOf(APPS, Cardinality(APPS))]
```

```
JoinReqMsgs \triangleq [app : APPS]
```

Messages sent for notifications about new joiners in the network.

```
JoinNotifMsgs \stackrel{\triangle}{=} [app : APPS]
```

The spec now depicts a shopping-list app where the server app manages several users and hence multiple lists of items that synch eventually.

The list contains unique items, thus we use a set.

--algorithm OptiShopyList

variable

```
whether an app is a gate isGate = [a \in APPS \mapsto a \in GATEAPPS], one shopping list for all APPS shopyList = [a \in APPS \mapsto \{\}], sync shopyList requests/responses syncReqQueue = [a \in APPS \mapsto \langle \rangle], syncRespQueue = [a \in APPS \mapsto \langle \rangle], join to network requests/responses joinReqQueue = [a \in APPS \mapsto \langle \rangle], joinRespQueue = [a \in APPS \mapsto \langle \rangle], new joiner notifications newJoinerNotif = [a \in APPS \mapsto \langle \rangle], set of taken IDs takenIDs = \{\};
```

define

A couple of helpers for shopy-list items

```
\begin{aligned} NewShopyItem(list) &\triangleq \\ & [id &\mapsto (\texttt{CHOOSE} \ x \in PRODUCTS : \neg \exists \ i \in list : x = i.id), \\ & bought \mapsto \texttt{FALSE}] \end{aligned} ExistingShopyItem(list) \triangleq \texttt{CHOOSE} \ x \in list : \texttt{TRUE}
```

 $ExistingNotBoughtShopyItem(list) \triangleq CHOOSE \ x \in list : x.bought = FALSE$

Helpers for Sync messages request/response.

```
\begin{aligned} NewSyncMsg(id,\ a,\ l,\ ml,\ t) &\triangleq \\ [id \mapsto id, \\ app \mapsto a, \\ list \mapsto l, \\ mergedList \mapsto ml, \end{aligned}
```

```
type \mapsto t
NewSyncReqMsg(a, l, ml, t) \stackrel{\Delta}{=}
    NewSyncMsq(
        (CHOOSE i \in IDs : \forall ti \in takenIDs : i = ti),
        a, l, ml, t
    )
NewSyncReq(app) \triangleq
    NewSyncReqMsg(app, shopyList[app], \{\}, REQ\_SYNC\_ACTION)
NewSyncResp(app, mergeResult, id) \stackrel{\triangle}{=}
    NewSyncMsg(id, app, shopyList[app], mergeResult, RESP_SYNC_ACTION)
Helpers for the decentralized network features.
NewJoinReqMsq(app) \stackrel{\Delta}{=} [app \mapsto app]
NewJoinRespMsg(app, hosts) \triangleq
    [app \mapsto app,
     knownHosts \mapsto hosts
GateApps \triangleq \{a \in APPS : isGate[a]\}
NewJoinerNotifReq(app) \triangleq [app \mapsto app]
PickGossipFriends(app, knownApps) \stackrel{\Delta}{=}
    Let Opposit \triangleq
             PT!Index(knownApps, app) + (Len(knownApps) \div 2) - (Len(knownApps)\%2)
         PreviousIndex(i) \triangleq
             If Len(knownApps) < 3
              THEN 1
              ELSE IF i = 1 THEN Len(knownApps) ELSE i - 1
         NextIndex(i) \triangleq
             IF Len(knownApps) < 3
              THEN Len(knownApps)
              ELSE IF i = Len(knownApps) THEN 1 ELSE i + 1
         \{knownApps[PreviousIndex(Opposit)], knownApps[NextIndex(Opposit)]\}
Not used, it's an example of how we'd keep the ordering of the responsed knownApps sequence
on joining. If it's used, it should be with small sequences to not generate enormous sets.
MergeKnownApps(apps1, apps2) \triangleq
    LET AppSeq(n) \stackrel{\triangle}{=} PT!SeqOf(APPS, n)
          Contains(appSeq, appItem) \triangleq
              Cardinality(PT!Matching(appSeq, appItem)) > 0
```

```
f[args \in AppSeq(Len(apps1))]
                         \times AppSeq(Len(apps2))
                         \times AppSeq(Len(apps1) + Len(apps2))] \stackrel{\Delta}{=}
                  Let l1 \triangleq args[1]
                        l2 \triangleq args[2]
                        acc \stackrel{\triangle}{=} args[3]
                        \textit{PickFromL}1 \; \stackrel{\Delta}{=} \; f[\langle
                            Tail(l1),
                            l2,
                            Append(acc, Head(l1))\rangle
                        SkipOneL1 \triangleq f[\langle
                            Tail(l1),
                            l2
                            acc\rangle
                        PickFromL2 \triangleq f[\langle
                            l1,
                            Tail(l2),
                            Append(acc, Head(l2))\rangle
                        SkipOneL2 \triangleq f[\langle
                            l1,
                            Tail(l2),
                            acc\rangle
                  IN
                       If Len(l2) = 0
                       THEN IF Len(l1) = 0
                                THEN acc
                                ELSE IF Contains(acc, Head(l1)) THEN SkipOneL1 ELSE PickFromL1
                        ELSE IF Head(l1) \neq Head(l2)
                                THEN IF Contains(acc, Head(l2)) THEN SkipOneL2 ELSE PickFromL2
                                ELSE IF Contains(acc, Head(l1)) THEN SkipOneL1 ELSE PickFromL1
        IN f[\langle apps1, apps2, \langle \rangle \rangle]
end define;
macro Notify(gossipFriends, newJoiner)
begin
    with a \in gossipFriends
         new Joiner Notif[a] := Append(new Joiner Notif[a], New Joiner NotifReq(app));
    end with;
end macro;
```

This process represents a shopy-list running in one of the several network clients.

Since Opti-shopylist is a decentralized program, the user creates a network of connected instances of Opti-shopylist.

We assume that every client app has only one shopy-list.

```
fair process ClientApp \in APPS
variables
   joined = FALSE,
   gossipFriends = \{\},
   knownApps = \langle self \rangle;
begin AppLoop:
   while TRUE do
       Below are actions to manage the connection to the network.
       either
            SEND JOIN REQUEST
           with a \in (GateApps -- self)
              joinReqQueue[a] := Append(joinReqQueue[a], NewJoinReqMsg(self));
           end with;
       \mathbf{or}
            RESPOND TO JOIN REQUEST
           if isGate[self] then
              await joinRegQueue[self] \neq \langle \rangle;
              with joinRequest = Head(joinReqQueue[self]),
                    updatedKnownApps = Append(knownApps, joinRequest.app)
               do
                  joinRespQueue[joinRequest.app] := Append(
                     joinRespQueue[joinRequest.app],
                     New Join Resp Msg(self, Select Seq(known Apps,
                         LAMBDA app: app \neq joinRequest.app)));
                  if joinRequest.app \notin PT!Range(knownApps)
                  then
                      knownApps := updatedKnownApps;
                      gossipFriends := PickGossipFriends(self, Tail(updatedKnownApps));
                  end if;
                  joinReqQueue[self] := Tail(joinReqQueue[self]);
                  joined := TRUE;
              end with;
           end if;
       \mathbf{or}
```

RECEIVE JOIN RESPONSE

```
await joinRespQueue[self] \neq \langle \rangle;
    with joinResponse
                          = Head(joinRespQueue[self]),
          newKnownApps = PT!Range(joinResponse.knownHosts) \setminus PT!Range(knownApps)
    do
        gossipFriends := PickGossipFriends(self, joinResponse.knownHosts);
       knownApps := knownApps \circ PT! OrderSet(newKnownApps);
       joinRespQueue[self] := Tail(joinRespQueue[self]);
       joined := TRUE;
   end with;
Following are the actions applying to the shopy-list managed by the app.
\mathbf{or}
     ADD
    \mathbf{await} \ \ Cardinality(shopyList[self]) < Cardinality(PRODUCTS);
    shopyList[self] := shopyList[self] ++ NewShopyItem(shopyList[self]);
\mathbf{or}
     REMOVE
    await shopyList[self] \neq \{\};
    shopyList[self] := shopyList[self] -- ExistingShopyItem(shopyList[self]);
\mathbf{or}
     ITEM HAS BEEN BOUGHT
    await shopyList[self] \neq \{\};
    await \exists item \in shopyList[self] : \neg item.bought;
    with modifiedItem = ExistingNotBoughtShopyItem(shopyList[self])
        shopyList[self] := shopyList[self] -- modifiedItem ++ [modifiedItem Except !.bought = true]
   end with;
Below actions manage the synchronization of the list.
\mathbf{or}
     SEND SYNC REQUEST
    with a \in (PT!Range(knownApps) -- self)
        syncReqQueue[a] := Append(syncReqQueue[a], NewSyncReq(self));
    end with;
or
     RCV SYNC REQUEST
    await syncRegQueue[self] \neq \langle \rangle;
    with syncRequest = Head(syncReqQueue[self]),
          mergeResult = shopyList[self] \cup syncRequest.list,
          newResp = NewSyncResp(self, mergeResult, syncRequest.id)
    do
```

```
syncReqQueue[self] := Tail(syncReqQueue[self]);
                 merge from request app
                shopyList[self] := mergeResult;
                syncRespQueue[syncRequest.app] := Append(syncRespQueue[syncRequest.app], newResp);
            end with:
        \mathbf{or}
             RCV SYNC RESPONSE
            await syncRespQueue[self] \neq \langle \rangle;
            with syncResponse = Head(syncRespQueue[self]),
                  mergeResult = shopyList[self] \cup syncResponse.list
             do
                shopyList[self] := mergeResult;
                syncRespQueue[self] := Tail(syncRespQueue[self]);
            end with;
        end either;
   end while;
end process;
end algorithm;
 BEGIN TRANSLATION (chksum(pcal) = "a4dd4f8d" \land chksum(tla) = "e6dbda73")
Variables isGate, shopyList, syncReqQueue, syncRespQueue, joinReqQueue,
            joinRespQueue, newJoinerNotif, takenIDs
 define statement
NewShopyItem(list) \triangleq
            \mapsto (CHOOSE x \in PRODUCTS : \neg \exists i \in list : x = i.id),
    bought \mapsto \text{FALSE}
ExistingShopyItem(list) \stackrel{\Delta}{=} CHOOSE \ x \in list : TRUE
ExistingNotBoughtShopyItem(list) \stackrel{\triangle}{=} CHOOSE \ x \in list : x.bought = FALSE
NewSyncMsg(id, a, l, ml, t) \triangleq
    [id \mapsto id,
    app \mapsto a,
    list \mapsto l,
    mergedList \mapsto ml,
    type \mapsto t
NewSyncReqMsg(a, l, ml, t) \triangleq
    NewSyncMsg(
        (CHOOSE i \in IDs : \forall ti \in takenIDs : i = ti),
        a, l, ml, t
```

```
)
NewSyncReq(app) \stackrel{\triangle}{=}
    NewSyncReqMsg(app, shopyList[app], \{\}, REQ\_SYNC\_ACTION)
NewSyncResp(app, mergeResult, id) \stackrel{\triangle}{=}
    NewSyncMsg(id, app, shopyList[app], mergeResult, RESP\_SYNC\_ACTION)
NewJoinRegMsg(app) \stackrel{\triangle}{=} [app \mapsto app]
NewJoinRespMsg(app, hosts) \triangleq
    [app \mapsto app,
    knownHosts \mapsto hosts
GateApps \ \triangleq \ \{a \in APPS : isGate[a]\}
New Joiner NotifReq(app) \stackrel{\Delta}{=} [app \mapsto app]
PickGossipFriends(app, knownApps) \stackrel{\Delta}{=}
    Let Opposit \triangleq
             PT!Index(knownApps, app) + (Len(knownApps) \div 2) - (Len(knownApps)\%2)
         PreviousIndex(i) \triangleq
             IF Len(knownApps) < 3
              THEN 1
              ELSE IF i = 1 THEN Len(knownApps) ELSE i - 1
         NextIndex(i) \stackrel{\triangle}{=}
             IF Len(knownApps) < 3
              THEN Len(knownApps)
              ELSE IF i = Len(knownApps) THEN 1 ELSE i + 1
         \{knownApps[PreviousIndex(Opposit)], knownApps[NextIndex(Opposit)]\}
MergeKnownApps(apps1, apps2) \stackrel{\Delta}{=}
    LET AppSeq(n) \triangleq PT!SeqOf(APPS, n)
         Contains(appSeq, appItem) \triangleq
              Cardinality(PT!Matching(appSeq, appItem)) > 0
         f[args \in AppSeq(Len(apps1))]
                    \times AppSeq(Len(apps2))
                    \times AppSeq(Len(apps1) + Len(apps2))] \stackrel{\Delta}{=}
```

```
Let l1 \triangleq args[1]
                     l2 \stackrel{\triangle}{=} args[2]
                     acc \triangleq args[3]
                     PickFromL1 \triangleq f[\langle
                          Tail(l1),
                         l2,
                         Append(acc, Head(l1))\rangle
                     SkipOneL1 \stackrel{\Delta}{=} f[\langle
                          Tail(l1),
                         l2,
                         acc\rangle
                     PickFromL2 \triangleq f[\langle
                         l1,
                          Tail(l2),
                         Append(acc, Head(l2))\rangle]
                     SkipOneL2 \triangleq f[\langle
                         l1,
                          Tail(l2),
                          acc\rangle
               IN
                   IF Len(l2) = 0
                    THEN IF Len(l1) = 0
                             THEN acc
                             ELSE IF Contains (acc, Head (11)) THEN Skip OneL1 ELSE PickFromL1
                     ELSE IF Head(l1) \neq Head(l2)
                             THEN IF Contains (acc, Head(l2)) THEN SkipOneL2 ELSE PickFromL2
                             ELSE IF Contains (acc, Head(l1)) THEN SkipOneL1 ELSE PickFromL1
         f[\langle apps1, apps2, \langle \rangle \rangle]
VARIABLES joined, gossipFriends, knownApps
vars \stackrel{\Delta}{=} \langle isGate, shopyList, syncReqQueue, syncRespQueue, joinReqQueue,
           joinRespQueue, newJoinerNotif, takenIDs, joined, gossipFriends,
           knownApps\rangle
ProcSet \stackrel{\Delta}{=} (APPS)
Init \stackrel{\triangle}{=} Global variables
           \land isGate = [a \in APPS \mapsto a \in GATEAPPS]
           \land shopyList = [a \in APPS \mapsto \{\}]
           \land syncReqQueue = [a \in APPS \mapsto \langle \rangle]
           \land syncRespQueue = [a \in APPS \mapsto \langle \rangle]
```

```
\land joinRespQueue = [a \in APPS \mapsto \langle \rangle]
          \land newJoinerNotif = [a \in APPS \mapsto \langle \rangle]
          \land takenIDs = \{\}
          Process ClientApp
          \land joined = [self \in APPS \mapsto FALSE]
          \land gossipFriends = [self \in APPS \mapsto \{\}]
          \land knownApps = [self \in APPS \mapsto \langle self \rangle]
ClientApp(self) \triangleq \land \lor \land \exists a \in (GateApps -- self) :
                                   joinReqQueue' = [joinReqQueue \ EXCEPT \ ![a] = Append(joinReqQueue[a], News)
                              \land UNCHANGED \langle shopyList, syncReqQueue, syncRespQueue, joinRespQueue, joined,
                           \vee \wedge \text{IF } isGate[self]
                                     Then \land joinReqQueue[self] \neq \langle \rangle
                                              \land LET joinRequest \stackrel{\triangle}{=} Head(joinReqQueue[self])IN
                                                   LET updatedKnownApps \triangleq Append(knownApps[self], joinRequest.
                                                      \land joinRespQueue' = [joinRespQueue \ EXCEPT \ ! [joinRequest.app] :
                                                     \land IF joinRequest.app \notin PT!Range(knownApps[self])
                                                            THEN \land knownApps' = [knownApps \ \text{EXCEPT} \ ![self] = upda
                                                                     \land gossipFriends' = [gossipFriends \ EXCEPT \ ! [self] = I
                                                            ELSE \land TRUE
                                                                     \land UNCHANGED \langle gossipFriends,
                                                                                         knownApps\rangle
                                                      \land joinReqQueue' = [joinReqQueue \ EXCEPT \ ![self] = Tail(joinReqQueue')
                                                      \land joined' = [joined \ EXCEPT \ ![self] = TRUE]
                                     ELSE ∧ TRUE
                                              \land UNCHANGED \langle joinRegQueue,
                                                                  joinRespQueue, joined,
                                                                  gossipFriends, knownApps\rangle
                              \land UNCHANGED \langle shopyList, syncReqQueue, syncRespQueue \rangle
                            \lor \land joinRespQueue[self] \neq \langle \lor \\ \land \texttt{LET}\ joinResponse \ \stackrel{\triangle}{=}\ Head(joinRespQueue[self]) \texttt{IN} 
                                   LET newKnownApps \triangleq PT!Range(joinResponse.knownHosts) \setminus PT!Range(knownHosts)
                                      \land gossipFriends' = [gossipFriends \ EXCEPT \ ![self] = PickGossipFriends(self, j)]
                                      \land knownApps' = [knownApps \ EXCEPT \ ![self] = knownApps[self] \circ PT ! Orders
                                      \land joinRespQueue' = [joinRespQueue \ Except \ ![self] = Tail(joinRespQueue[see])
                                      \land joined' = [joined \ EXCEPT \ ![self] = TRUE]
                              \land UNCHANGED \langle shopyList, syncReqQueue, syncRespQueue, joinReqQueue \rangle
                           \lor \land Cardinality(shopyList[self]) < Cardinality(PRODUCTS)
                               \land shopyList' = [shopyList \ EXCEPT \ ! [self] = shopyList[self] + NewShopyItem(shop)
                               \land UNCHANGED \langle syncRegQueue, syncRespQueue, joinRegQueue, joinRespQueue, join
                           \lor \land shopyList[self] \neq \{\}
```

 $\land joinReqQueue = [a \in APPS \mapsto \langle \rangle]$

```
\land shopyList' = [shopyList \ Except \ ![self] = shopyList[self] -- ExistingShopyItem(shopyList)]
                                                                                                                                                   \land UNCHANGED \langle syncReqQueue, syncRespQueue, joinReqQueue, joinRespQueue, joinR
                                                                                                                                     \lor \land shopyList[self] \neq \{\}
                                                                                                                                                   \land \exists item \in shopyList[self] : \neg item.bought
                                                                                                                                                    \land Let modifiedItem \triangleq ExistingNotBoughtShopyItem(shopyList[self])in
                                                                                                                                                                           shopyList' = [shopyList \ EXCEPT \ ![self] = shopyList[self] -- modifiedItem ++ [shopyList] ]
                                                                                                                                                   \land UNCHANGED \langle syncReqQueue, syncRespQueue, joinReqQueue, joinRespQueue, joinR
                                                                                                                                    \lor \land \exists a \in (PT!Range(knownApps[self]) -- self):
                                                                                                                                                                            syncReqQueue' = [syncReqQueue \ EXCEPT \ ![a] = Append(syncReqQueue[a], New)
                                                                                                                                                   \land UNCHANGED \langle shopyList, syncRespQueue, joinReqQueue, joinRespQueue, joined, goined, goingle <math>\langle shopyList, syncRespQueue, joinReqQueue, joinRespQueue, j
                                                                                                                                    \begin{array}{l} \lor \land syncReqQueue[self] \neq \langle \rangle \\ \land \texttt{LET} \ syncRequest \stackrel{\triangle}{=} \ Head(syncReqQueue[self]) \texttt{IN} \\ \texttt{LET} \ mergeResult} \stackrel{\triangle}{=} \ shopyList[self] \cup syncRequest.list\texttt{IN} \\ \end{array} 
                                                                                                                                                                                     LET newResp \triangleq NewSyncResp(self, mergeResult, syncRequest.id)IN
                                                                                                                                                                                                    \land syncReqQueue' = [syncReqQueue \ EXCEPT \ ! [self] = Tail(syncReqQueue[self]) = Tail(syncReqQueue[self])
                                                                                                                                                                                                   \land shopyList' = [shopyList \ EXCEPT \ ![self] = mergeResult]
                                                                                                                                                                                                   \land syncRespQueue' = [syncRespQueue \ EXCEPT \ ! [syncRequest.app] = Appendential Appendix of the sync of the sync
                                                                                                                                                   \land UNCHANGED \langle joinReqQueue, joinRespQueue, joined, gossipFriends, knownApps <math>\rangle
                                                                                                                                    \lor \land syncRespQueue[self] \neq \langle \rangle
                                                                                                                                                    \land \text{ LET } syncResponse \stackrel{\triangle}{=} Head(syncRespQueue[self]) \text{IN}    \text{ LET } mergeResult \stackrel{\triangle}{=} shopyList[self] \cup syncResponse.list \text{IN}  
                                                                                                                                                                                         \land shopyList' = [shopyList \ EXCEPT \ ![self] = mergeResult]
                                                                                                                                                                                         \land syncRespQueue' = [syncRespQueue \ Except \ ![self] = Tail(syncRespQueue]
                                                                                                                                                    \land UNCHANGED \langle syncReqQueue, joinReqQueue, joinRespQueue, joined, gossipFriend
                                                                                                                     \land UNCHANGED \langle isGate, newJoinerNotif, takenIDs \rangle
Next \stackrel{\Delta}{=} (\exists self \in APPS : ClientApp(self))
 Spec \stackrel{\triangle}{=} \wedge Init \wedge \Box [Next]_{vars}
                                                        \land \forall self \in APPS : WF_{vars}(ClientApp(self))
       END TRANSLATION
NoDuplicates(seq) \triangleq
                    \forall i, j \in \text{DOMAIN } seq:
                                    i \neq j \Rightarrow seq[i] \neq seq[j]
 CountNumberOfGossips(app) \stackrel{\Delta}{=}
                      PT!ReduceSet(
                                                     LAMBDA a, acc : acc + (IF app \in gossipFriends[a])
                                                                                                                                                                                                     THEN 1 ELSE 0),
```

APPS, 0)

 $ExistsRoute(from, to, _gossipFriends) \stackrel{\Delta}{=}$

 $to \in _gossipFriends[app]$

LET $f[\langle app, visited \rangle \in APPS \times SUBSET APPS] \triangleq$

```
\vee \exists a \in (\_gossipFriends[app] \setminus visited) : f[a, visited ++ app]
         from = to \lor f[\langle from, \{\} \rangle]
TypeOK \triangleq
     \land \quad \forall \ a \in APPS :
            Checking on variables' domains.
             \land shopyList[a] \subseteq ShopyItems
             \land PT!Range(syncReqQueue[a]) \subseteq SyncMsgs
             \land PT!Range(syncRespQueue[a]) \subseteq SyncMsgs
              The queue for join requests is only for gate apps
             \wedge IF isGate[a]
                THEN PT!Range(joinReqQueue[a]) \subseteq JoinReqMsgs
                          \land \forall \mathit{req} \in \mathit{PT!Range}(\mathit{joinReqQueue}[\mathit{a}]) : \mathit{req.app} \neq \mathit{a}
                 ELSE joinReqQueue[a] = \langle \rangle
             \land PT!Range(joinRespQueue[a]) \subseteq JoinRespMsgs
             \land PT! Range(newJoinerNotif[a]) \subseteq JoinNotifMsgs
             knownApps is a collection of unique, ordered apps.
             \land PT!Range(knownApps[a]) \subseteq APPS
             \land NoDuplicates(knownApps[a])
             Apps don't gossip themselves
             \land gossipFriends[a] \subseteq (APPS -- a)
              Invariant when we're connected or not.
             \land gossipFriends[a] \neq \{\}
                \equiv knownApps[a] \neq \langle a \rangle
          takenIDs \subseteq IDs
Liveness \stackrel{\triangle}{=}
     \land \forall a \in APPS:
         joined[a]
          there's a route from every other connected app to a
          \rightsquigarrow \forall a2 \in \{j \in (APPS -- a) : joined[j]\} :
                 ExistsRoute(a2, a, qossipFriends)
```

 $[\]backslash *$ Last modified $\mathit{Tue}\ \mathit{Mar}\ 16\ 19{:}24{:}39\ \mathit{CET}\ 2021$ by davd

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