```
- MODULE optishopylist -
EXTENDS TLC, Integers, FiniteSets, Sequences
CONSTANTS PRODUCTS, APPS, IDs, GATEAPP
PT \stackrel{\triangle}{=} \text{INSTANCE } PT
set ++ item \stackrel{\triangle}{=} set \cup \{item\}
set -- item \stackrel{\triangle}{=} set \setminus \{item\}
In shoppying list, the product is in fact the identifier. Any item could have an information for
how much of a product one wants to buy (not relevant in this specification).
                   \stackrel{\Delta}{=} [id: PRODUCTS, bought: BOOLEAN]
ShopyItems
ADD\_ACTION \triangleq  "add"
RM\_ACTION \triangleq "rm"
SET\_BOUGHT\_ACTION \triangleq  "set_bought"
REQ\_SYNC\_ACTION \triangleq "req\_sync"
RESP\_SYNC\_ACTION \triangleq "resp\_sync"
END\_SYNC\_ACTION \triangleq "end\_sync"
Actions is the set of all possible actions in the system.
Actions \triangleq \{
    ADD_ACTION,
    RM\_ACTION.
    SET\_BOUGHT\_ACTION,
    REQ\_SYNC\_ACTION,
    RESP_SYNC_ACTION,
    END\_SYNC\_ACTION
SyncActions \triangleq \{REQ\_SYNC\_ACTION, RESP\_SYNC\_ACTION\}
SyncMsgs is the set of all possible messages sent for synchronisation of shopy lists.
SyncMsqs \triangleq
    [id:IDs,
```

The spec now depicts a shopping-list app where the server app manages several users and hence multiple lists of items that synch eventually.

The list contains unique items, thus we use a set.

mergedList: Subset ShopyItems,

 $\textbf{--algorithm} \ \textit{OptiShopyList}$

list: Subset ShopyItems,

type: SyncActions

app: APPS,

variable

```
one shopping list for all APPS
    shopyList = [a \in APPS \mapsto \{\}],
     sync requests for all APPS
    syncReqQueue = [a \in APPS \mapsto \langle \rangle],
      sync responses for all APPS
    syncRespQueue = [a \in APPS \mapsto \langle \rangle],
      set of taken IDs
    takenIDs = \{\};
define
    A couple of helpers for shopy-list items
    NewShopyItem(list) \triangleq
                  \mapsto (CHOOSE x \in PRODUCTS : \neg \exists i \in list : x = i.id),
          bought \mapsto \text{FALSE}
    ExistingShopyItem(list) \stackrel{\Delta}{=} CHOOSE \ x \in list : TRUE
    ExistingNotBoughtShopyItem(list) \triangleq CHOOSE \ x \in list : x.bought = FALSE
    Helpers for Sync messages request/response.
    NewSyncMsg(id, a, l, ml, t) \stackrel{\Delta}{=}
         [id \mapsto id,
          app \mapsto a,
          list \mapsto l,
          mergedList \mapsto ml,
          type \mapsto t
    NewSyncReqMsg(a, l, ml, t) \stackrel{\triangle}{=}
         NewSyncMsg(
             (CHOOSE i \in IDs : \forall ti \in takenIDs : i = ti),
             a, l, ml, t
         )
    NewSyncReq(app) \triangleq
         NewSyncReqMsg(app, shopyList[app], \{\}, REQ\_SYNC\_ACTION)
    NewSyncResp(app, mergeResult, id) \stackrel{\triangle}{=}
         NewSyncMsg(id, app, shopyList[app], mergeResult, RESP\_SYNC\_ACTION)
    Helpers for the decentralized network features.
    IsGate(app) \triangleq app = GATEAPP
```

end define;

This process represents a shopy-list running in one of the several offline clients. Several shopy-lists are running on various app processes. Actually, we specify what happens in the system when 2 client apps want to synch their shopy-list. We assume that every client app has only one such list since the user is able to synch any 2 lists together.

```
fair process ClientApp \in APPS
variables gossipFriends;
begin AppLoop:
   while TRUE do
       either
           await Cardinality(shopyList[self]) < Cardinality(PRODUCTS);
            shopyList[self] := shopyList[self] ++ NewShopyItem(shopyList[self]);
       \mathbf{or}
            REMOVE
           await shopyList[self] \neq \{\};
           shopyList[self] := shopyList[self] -- ExistingShopyItem(shopyList[self]);
       \mathbf{or}
            set to BOUGHT
           await shopyList[self] \neq \{\};
           await \exists item \in shopyList[self] : \neg item.bought;
           with modifiedItem = ExistingNotBoughtShopyItem(shopyList[self]) do
               shopyList[self] := shopyList[self] -- modifiedItem ++ [modifiedItem except !.bought = true ]
           end with;
       \mathbf{or}
            request a sync with another app
           with a \in (APPS -- self),
                 newRequest = NewSyncReq(self) do
               syncReqQueue[a] := Append(syncReqQueue[a], newRequest);
           end with;
       \mathbf{or}
            receive a sync request from another app
           await syncReqQueue[self] \neq \langle \rangle;
           with syncRequest = Head(syncReqQueue[self]),
                 mergeResult = shopyList[self] \cup syncRequest.list,
                 newResp = NewSyncResp(self, mergeResult, syncRequest.id) do
               syncReqQueue[self] := Tail(syncReqQueue[self]);
                merge from request app
               shopyList[self] := mergeResult;
               syncRespQueue[syncRequest.app] := Append(syncRespQueue[syncRequest.app], newResp);
           end with;
       \mathbf{or}
            receive a sync response
           await syncRespQueue[self] \neq \langle \rangle;
```

```
with syncResponse = Head(syncRespQueue[self]),
                  mergeResult = shopyList[self] \cup syncResponse.list do
                shopyList[self] := mergeResult;
                syncRespQueue[self] := Tail(syncRespQueue[self]);
            end with;
        end either;
   end while;
end process;
end algorithm;
 BEGIN TRANSLATION (chksum(pcal) = "f4ae31c" \land chksum(tla) = "894de1a")
CONSTANT defaultInitValue
{\tt VARIABLES}\ shopyList,\ syncReqQueue,\ syncRespQueue,\ takenIDs
 define statement
NewShopyItem(list) \triangleq
            \mapsto (CHOOSE x \in PRODUCTS : \neg \exists i \in list : x = i.id),
    bought \mapsto \text{FALSE}
ExistingShopyItem(list) \triangleq CHOOSE \ x \in list : TRUE
ExistingNotBoughtShopyItem(list) \triangleq CHOOSE \ x \in list : x.bought = FALSE
NewSyncMsg(id, a, l, ml, t) \triangleq
    [id \mapsto id,
    app \mapsto a,
    list \mapsto l,
    mergedList \mapsto ml,
    type \mapsto t
NewSyncReqMsg(a, l, ml, t) \triangleq
    NewSyncMsq(
        (CHOOSE i \in IDs : \forall ti \in takenIDs : i = ti),
        a, l, ml, t
NewSyncReq(app) \triangleq
    NewSyncReqMsg(app, shopyList[app], \{\}, REQ\_SYNC\_ACTION)
NewSyncResp(app, mergeResult, id) \stackrel{\triangle}{=}
    NewSyncMsg(id, app, shopyList[app], mergeResult, RESP\_SYNC\_ACTION)
```

```
IsGate(app) \stackrel{\triangle}{=} app = GATEAPP
VARIABLE gossipFriends
vars \triangleq \langle shopyList, syncReqQueue, syncRespQueue, takenIDs, gossipFriends \rangle
ProcSet \triangleq (APPS)
Init \stackrel{\Delta}{=} Global variables
                            \land shopyList = [a \in APPS \mapsto \{\}]
                            \land syncReqQueue = [a \in APPS \mapsto \langle \rangle]
                            \land syncRespQueue = [a \in APPS \mapsto \langle \rangle]
                            \land takenIDs = \{\}
                              Process ClientApp
                            \land gossipFriends = [self \in APPS \mapsto defaultInitValue]
 ClientApp(self) \triangleq \land \lor \land Cardinality(shopyList[self]) < Cardinality(PRODUCTS)
                                                                                   \land shopyList' = [shopyList \ EXCEPT \ ![self] = shopyList[self] ++ NewShopyItem(shop)]
                                                                                   \land UNCHANGED \langle syncReqQueue, syncRespQueue \rangle
                                                                           \lor \land shopyList[self] \neq \{\}
                                                                                    \land shopyList' = [shopyList \ EXCEPT \ ![self] = shopyList[self] -- ExistingShopyItem(shopyList)]
                                                                                    \land UNCHANGED \langle syncReqQueue, syncRespQueue \rangle
                                                                           \lor \land shopyList[self] \neq \{\}
                                                                                   \land \exists item \in shopyList[self] : \neg item.bought
                                                                                    \land LET modifiedItem \stackrel{\triangle}{=} ExistingNotBoughtShopyItem(shopyList[self])IN
                                                                                                 shopyList' = [shopyList \ EXCEPT \ ![self] = shopyList[self] -- modifiedItem ++ [shopyList] ]
                                                                                   \land UNCHANGED \langle syncReqQueue, syncRespQueue \rangle
                                                                           \lor \land \exists a \in (APPS -- self) :
                                                                                                LET newRequest \stackrel{\triangle}{=} NewSyncReq(self)IN
                                                                                                       syncReqQueue' = [syncReqQueue \ EXCEPT \ ![a] = Append(syncReqQueue[a], new \ extra property \ extra prope
                                                                                   \land UNCHANGED \langle shopyList, syncRespQueue \rangle
                                                                           \begin{array}{l} \lor \ \land \ syncReqQueue[self] \neq \langle \rangle \\ \land \ \texttt{LET} \ \ syncRequest \ \stackrel{\triangle}{=} \ \ Head(syncReqQueue[self]) \texttt{in} \end{array} 
                                                                                               Let mergeResult \triangleq shopyList[self] \cup syncRequest.listIn
                                                                                                      LET newResp \triangleq NewSyncResp(self, mergeResult, syncRequest.id)IN
                                                                                                              \land syncRegQueue' = [syncRegQueue \ EXCEPT \ ! [self] = Tail(syncRegQueue[see])
                                                                                                             \land shopyList' = [shopyList \ EXCEPT \ ![self] = mergeResult]
                                                                                                              \land syncRespQueue' = [syncRespQueue \ EXCEPT \ ! [syncRequest.app] = Appendential Appendix of the property of 
                                                                           \lor \land syncRespQueue[self] \neq \langle \rangle
                                                                                    \land LET syncResponse \stackrel{\triangle}{=} Head(syncRespQueue[self])IN
                                                                                                Let mergeResult \triangleq shopyList[self] \cup syncResponse.listIn
                                                                                                        \land shopyList' = [shopyList \ EXCEPT \ ! [self] = mergeResult]
                                                                                                        \land syncRespQueue' = [syncRespQueue \ Except \ ![self] = Tail(syncRespQueue] 
                                                                                   \land UNCHANGED syncReqQueue
                                                                  \land UNCHANGED \langle takenIDs, gossipFriends \rangle
Next \triangleq (\exists self \in APPS : ClientApp(self))
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