

Affordance-Aware Planning

Paper-ID: 5

Abstract—Planning algorithms for non-deterministic domains are often intractable in large state spaces due to the well-known “curse of dimensionality.” Existing approaches to address this problem fail to prevent the planner from considering many actions which would be obviously irrelevant to a human solving the same problem. We formalize the notion of affordances [7] as knowledge added to an MDP that prunes actions in a state- and reward- general way. This pruning significantly reduces the number of state-action pairs the agent needs to evaluate in order to act optimally. We demonstrate our approach in the Minecraft domain, showing significant increase in speed and reduction in state-space exploration during planning. Further, we provide a learning framework that enables an agent to learn affordances through experience, removing the agent’s dependence on the expert. We provide preliminary results indicating that the learning process effectively produces affordances that help solve an MDP faster.

I. INTRODUCTION

As robots move out of the lab and into the real world, planning algorithms need to scale to domains of increased noise, size, and complexity. A classic formalization of this problem is a stochastic sequential decision making problem in which the agent must find a policy (a mapping from states to actions) for some subset of the state space that enables the agent to achieve a goal from some initial state, while minimizing any costs along the way. Increases in planning problem size and complexity directly correspond to an explosion in the state-action space. Current approaches to solving sequential decision making problems in the face of uncertainty cannot tackle these problems as the state-action space becomes too large [8].

To address this state-space explosion, prior work has explored adding knowledge to the planner to solve problems in these massive domains, such as options [20] and macroactions [4, 15]. However, these approaches add knowledge in the form of additional high-level actions to the agent, which *increases* the size of the state-action space (while also allowing the agent to search more deeply within the space). The resulting augmented space is even larger, which can have the paradoxical effect of increasing the search time for a good policy [11]. Further, other approaches fall short of learning useful, transferable knowledge, either due to complexity or lack of generalizability.

Instead, we propose a formalization of *affordances* [7] for Markov Decision Processes (MDPs) that specifies which actions an agent should consider in different kinds of states to achieve a certain kind of goal. Our approach enables an agent to focus on aspects of the environment that are most relevant toward solving its current goal and avoids exploration of irrelevant parts of the state-action space, which leads to dramatic speedups in planning.

Further, we propose a learning process that enables agents to autonomously learn affordances through experience, lessening the agent’s dependence on expert knowledge. Affordances are not specific to a particular reward function or state space, and provide the agent with transferable knowledge that is effective in a wide variety of problems. We call any planner that uses affordances an *affordance-aware* planner.

Because affordances define the *kind* of goals for which actions are useful, affordances also enable high-level reasoning that can be combined with approaches like high-level subgoal planning for even greater performance gains. For now, we chose to ignore approaches to affordances that emphasize direct perception of affordances in the environment, and instead emphasize an affordance’s role as a means of guiding a planning agent through large stochastic state spaces. We foresee future methods that bring together affordance-aware planners with these approaches to affordances in the perception and sensing pipeline to create robust, near-autonomous robotic agents.

II. BACKGROUND

We use Minecraft as our planning and evaluation domain. Minecraft is a 3-D blocks world game in which the user can place and destroy blocks of different types. Minecraft’s physics and action space is expressive enough to allow very complex worlds to be created by users, such as a functional scientific graphing calculator¹; simple scenes from a Minecraft world appear in Figure 1 - a video demonstration of an affordance-aware planner solving this task may be seen online². Minecraft serves as a model for robotic tasks such as cooking assistance, assembling items in a factory, and object retrieval. As in these tasks, the agent operates in a very large state-action space in an uncertain environment.

Minecraft is also an effective parallel for the actual world, both in terms of approximating the complexity and scope of planning problems, as well as modeling the uncertainty and noise presented to a real world agent. For instance, robotic agents are prone to uncertainty throughout their system, including noise in their sensors (cameras, LIDAR, microphones, etc.), odometry, control, and actuation. In order to accurately capture some of the inherent difficulties of planning under uncertainty, the Minecraft agent’s actions were modified to have stochastic outcomes. These stochastic outcomes may require important changes in the optimal policy in contrast to deterministic actions, such as keeping the agent’s distance from high cost areas of the state-space, such as lava. We

¹<https://www.youtube.com/watch?v=wgJfVRhotlQ>

²Watch at: <https://vimeo.com/88689171>

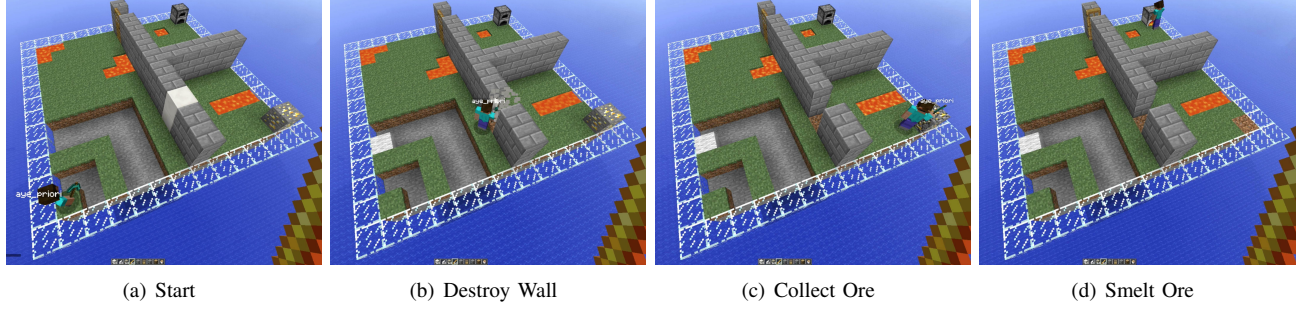


Fig. 1. Affordance-aware RTDP tasked with a gold-smelting task with a variety of obstacles (only solved by an affordance-aware planner)

chose to give the Minecraft agent perfect sensor data about the Minecraft world.

A. OO-MDPs

We define affordances in terms of propositional functions on states. Our definition builds on the Object-Oriented Markov Decision Process (OO-MDP) [6]. OO-MDPs are an extension of the classic Markov Decision Process (MDP). A classic MDP is a five-tuple: $\langle \mathcal{S}, \mathcal{A}, \mathcal{T}, \mathcal{R}, \gamma \rangle$, where \mathcal{S} is a state-space; \mathcal{A} is the agent’s set of actions; \mathcal{T} denotes $\mathcal{T}(s' | s, a)$, the transition probability of an agent applying action $a \in \mathcal{A}$ in state $s \in \mathcal{S}$ and arriving in $s' \in \mathcal{S}$; $\mathcal{R}(s, a, s')$ denotes the reward received by the agent for applying action a in state s and transitioning to state s' ; and $\gamma \in [0, 1)$ is a discount factor that defines how much the agent prefers immediate rewards over distant rewards (the agent more greatly prefers to maximize more immediate rewards as γ decreases).

A classic way to provide a factored representation of an MDP state is to represent each MDP state as a single feature vector. By contrast, an OO-MDP represents the state space as a collection of objects, $O = \{o_1, \dots, o_o\}$. Each object o_i belongs to a class $c_j \in \{c_1, \dots, c_c\}$. Every class has a set of attributes $Att(c) = \{c.a_1, \dots, c.a_a\}$, each of which has a domain $Dom(c.a)$ of possible values. Upon instantiation of an object class, its attributes are given a state $o.state$ (an assignment of values to its attributes). The underlying MDP state is the set of all the object states: $s \in \mathcal{S} = \cup_{i=1}^o \{o_i.state\}$.

There are two advantages to using an object-oriented factored state representation instead of a single feature vector. First, different states in the same state space may contain different numbers of objects of varying classes, which is useful in domains like Minecraft in which the agent can dynamically add and remove blocks to the world. Second, MDP states can be defined invariantly to the specific object references. For instance, consider a Minecraft world with two block objects, b_1 and b_2 . If the agent picked up and swapped the position of b_1 and b_2 , the MDP state before the swap and after the swap would be the same, because the MDP state definition is invariant to which object holds which object state.

While the OO-MDP state definition is a good fit for the Minecraft domain, our motivation for using an OO-MDP lies in the ability to formulate predicates over classes of objects. That is, the OO-MDP definition also includes a set

of predicates \mathcal{P} that operate on the state of objects to provide additional high-level information about the MDP state. In the original OO-MDP work, these predicates were used to model and learn an MDP’s transition dynamics.

While an OO-MDP reduces the size of the Minecraft state space by a significant factor, the resulting state space is still far too large to solve with any existing (OO)-MDP solver. This is the primary motivator for incorporating affordances - to reduce the amount of the state space that an OO-MDP agent will have to explore.

III. AFFORDANCES

We define an affordance Δ as the mapping $\langle p, g \rangle \mapsto \mathcal{A}'$, where:

$\mathcal{A}' \subseteq \mathcal{A}$, a subset of the action space, representing the relevant *action-possibilities* of the environment.

p is a predicate on states, $s \rightarrow \{0, 1\}$ representing the *precondition* for the affordance.

g is an ungrounded predicate on states representing a *lifted goal description*.

The precondition and goal description refer to predicates that are defined in the OO-MDP definition. We call an affordance *activated* when its predicate is true and its lifted goal description g matches the agent’s current goal. Using OO-MDP predicates for affordance preconditions and goal descriptions allows for state space independence. Thus, a planner equipped with affordances can be used in any number of different environments. For instance, the affordances defined for Minecraft navigation problems can be used in any task regardless of the spatial size of the world, number of blocks in the world, and specific goal location that needs to be reached.

A. Affordance Aware Planning

We call any planner that uses affordances an *affordance-aware* planner. For a given state, our goal is to solve for the probability of getting a particular action set \mathcal{A}^* , and approximate sampling from this distribution. This ensures that in the limit, it is possible to apply each action in each state. \mathcal{A}^* represents a drawn action subset from the OO-MDP action set \mathcal{A} that is likely to contain the optimal action(s) for a given state, but not suboptimal actions.

$$\Pr(\mathcal{A}^* | s, \Delta_0 \dots \Delta_N) \quad (1)$$

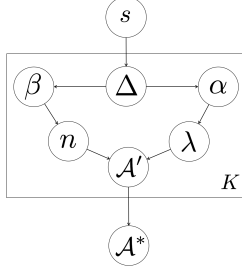


Fig. 2. The full graphical model approximating a distribution over \mathcal{A}^* , the pruned action set for a given state s

We let each affordance contribute a set $\mathcal{A}' \subseteq \mathcal{A}^*$ in each state:

$$\Pr(\mathcal{A}'_0 \cup \dots \cup \mathcal{A}'_N \mid s, \Delta_0 \dots \Delta_N) \quad (2)$$

We approximate this term assuming the sets \mathcal{A}'_i are disjoint:

$$\sum_i^K \Pr(\mathcal{A}'_i \mid s, \Delta_i) \quad (3)$$

Given a set of K domain affordances $Z = \{\Delta_1, \dots, \Delta_K\}$ and a current agent goal condition defined with an OO-MDP predicate G , the action set that a planning algorithm considers is pruned on a state by state basis as shown in Algorithm 1. Each activated affordance contributes a suggested action set, determined by Algorithm 2.

Algorithm 1 `getActionsForState(state, Z, G)`

```

1:  $\mathcal{A}^* \leftarrow \{\}$ 
2: for  $\Delta \in Z$  do
3:   if  $\Delta.p(\text{state})$  and  $\Delta.g = G$  then
4:      $\mathcal{A}^* \leftarrow \mathcal{A}^* \cup \Delta.getActions(s)$ 
5:   end if
6: end for
7: return  $\mathcal{A}^*$ 

```

Specifically, we prune actions on a state by state basis by initializing an empty set of actions \mathcal{A}^* (line 1). The algorithm then iterates through each of the domain affordances (lines 2-6). If the affordance precondition ($\Delta.p$) is satisfied by some set of objects in the current state and the affordance goal condition ($\Delta.g$) is defined with the same predicate as the current goal (line 3), then the actions associated with the affordance ($\Delta.\mathcal{A}' = \Delta.getActions(s)$) are added to the action set \mathcal{A}^* (line 4). Finally, \mathcal{A}^* is returned (line 7).

For each affordance, we get an action set \mathcal{A}' . This process is outlined by Algorithm 2. To compute \mathcal{A}' , we form a Dirichlet-multinomial distribution over actions (λ), and a Dirichlet distribution over the size (N) of each action set. Therefore, the probability of getting an action set from affordance i in state s is:

$$\Pr(\mathcal{A}'_i \mid s, \Delta_i) = \Pr(\mathcal{A}'_i \mid N, \lambda) = \Pr(\lambda \mid \alpha) \cdot \Pr(N \mid \beta) \quad (4)$$

For a given affordance Δ_i , first we sample from our distribution over action set size to get a candidate action set size (lines

1-2). We then take that many samples from our distribution over actions to get a candidate action set \mathcal{A}' (lines 3-5).

$$\Pr(\lambda \mid \alpha) = \text{DirMult}(\alpha) \quad (5)$$

$$\Pr(N \mid \beta) = \text{Dir}(\beta) \quad (6)$$

Algorithm 2 `$\Delta_i.getActions(s)$`

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1:  $\lambda \leftarrow \text{DirMult}(\Delta_i.\alpha)$ 
2:  $N \leftarrow \text{Dir}(\Delta_i.\beta)$ 
3: for 1 to  $N$  do
4:    $\Delta_i.\mathcal{A}' \leftarrow \lambda$ 
5: end for
6: return  $\Delta_i.\mathcal{A}'$ 

```

Through the use of Algorithms 1 & 2, any OO-MDP solver can be made *affordance aware*. For a planner to be made affordance-aware, we require that an expert provide a set \mathcal{P} of predicates for the domain of relevance (i.e. Minecraft). Additionally, the expert must specify a set $\mathcal{G} \subset \mathcal{P}$ that indicates which predicates may serve as goal conditions. If the expert wishes to provide the affordances directly, they must specify the Dirichlet parameters α and β . Note that in the limit, the expert may fix α and β in a way that forces a given affordance to always suggest a specific set of actions - this type of expert affordances was given for all experiments.

B. Learning Affordances

A strength of our affordance formalism is that it is simple to learn useful affordances directly. Given the set of predicates \mathcal{P} and possible goals $\mathcal{G} \subset \mathcal{P}$, we form a set of candidate affordances Δ with every combination of $\langle p, g \rangle$, for $p \in \mathcal{P}$ and $g \in \mathcal{G}$. To learn the action set for each of these candidate affordances, we propose a scaffolded learning process that computes α and β from the solved policy of m goal-annotated OO-MDPs that have small state spaces, but still present similar sorts of features to the state spaces the agent might expect to see in more complex environments.

For each optimal policy, we count the number of policies that used each action when each affordance was activated. α is set to this count. Additionally, we define β as a vector of the integers 1 to $|\mathcal{A}|$. Then, for each optimal policy, we count the number of different actions that were optimal for each activated affordance Δ_i , and increment that value for $\Delta_i.\beta$. This captures how large or small optimal action sets are expected to be.

IV. EXPERIMENTS

We conducted a series of experiments in the Minecraft domain that compared the performance of several OO-MDP solvers without affordances to their affordance-aware counterparts. We selected the expert affordances from our background knowledge of the domain and specified them so that each affordance always mapped to the same set of actions.

For the expert affordances, we gave the agent a knowledge base of 5 types of affordances, which are listed in Figure 3. Our experiments consisted of a variety of common tasks (state

spaces 1-7 in Table I) in Minecraft, ranging from basic path planning, to smelting gold, to opening doors and tunneling through walls. We also tested each planner on worlds of varying size and difficulty to demonstrate the scalability and flexibility of the affordance formalism.

Additionally, we tested our learning procedure and compared the performance of RTDP solving the OO-MDP with (1) No affordances, (2) Learned affordances, and (3) Expert provided affordances. The training data consisted of 1000 simple state spaces, each a $3 \times 3 \times 3$ world with randomized features that mirrored the agent’s actual state space. The same training data was used for each test state space.

The evaluation metric for each trial was the number of Bellman updates that were executed by each planning algorithm. Value Iteration was terminated when the maximum change in the value function was less than 0.01. RTDP terminated when the maximum change in the value function was less than 0.01 for five consecutive policy rollouts. In subgoal planning, the high-level subgoal plan was solved using breadth-first search, which only took a small fraction of the time compared to the total low-level planning and therefore is not reported. We set the reward function to -1 for all transitions, except transitions to states in which the agent was on lava, which returned -200 . The goal was set to be terminal. The discount factor was set to $\lambda = 0.99$. For all experiments, actions associated with a direction (e.g. movement, block placement, jumping, etc.), had a small probability (0.3) of moving in another random direction.

Lastly, we conducted experiments in which we varied the number of training worlds used in the learning process from 0-1000 to demonstrate that planning performance improves with more training data. As in Table II, we generated 0 to 1000 simple state spaces, each a $3 \times 3 \times 3$ world with randomized features that mirrored the agent’s actual state space. We then solved the OO-MDP with training data of 0 up to 1000 simple state spaces to demonstrate the effectiveness of added training data.

V. RESULTS

Table I shows the number of Bellman updates required when solving the OO-MDP with conventional methods (left column) compared to solving the OO-MDP with an affordance-aware method (right column). The affordance-aware methods significantly outperformed their unaugmented counterparts in all of these experiments. These results, while unsurprising, concretely demonstrate that a small set of affordances prune

$$\begin{aligned}\Delta_1 &= \langle \text{nearTrench}, \text{reachGoal} \rangle \mapsto \{\text{place}, \text{jump}\} \\ \Delta_2 &= \langle \text{onPlane}, \text{reachGoal} \rangle \mapsto \{\text{move}\} \\ \Delta_3 &= \langle \text{nearWall}, \text{reachGoal} \rangle \mapsto \{\text{destroy}\} \\ \Delta_4 &= \langle \text{nearFurnace}, \text{makeGold} \rangle \mapsto \{\text{place}\} \\ \Delta_5 &= \langle \text{nearOre}, \text{makeGold} \rangle \mapsto \{\text{destroy}\}\end{aligned}$$

Fig. 3. The five affordance types used in expert experiments.

TABLE I
EXPERT AFFORDANCE RESULTS: AVG. NUMBER OF BELLMAN UPDATES PER CONVERGED POLICY

State Space	VI	A-VI	RTDP	A-RTDP	SG	A-SG
1	71604	100	836	152	1373	141
2	413559	366	4561	392	28185	547
3	1439883	904	18833	788	15583	1001
4	861084	4368	12207	1945	6368	1381
5	413559	366	4425	993	25792	597
6	203796	105	26624	145	5404	182
7	16406	962	7738	809	7412	578

TABLE II
LEARNED AFFORDANCE RESULTS: AVG. NUMBER OF BELLMAN UPDATES PER CONVERGED POLICY

State Space	No Affordances	Learned	Expert
Tiny	879	414	94
Small	1460	802	321
Medium	3993	2412	693
Large	8344	5100	1458

away many useless actions across many different types of Minecraft tasks.

Table II indicates the average number of Bellman updates required by RTDP to solve the OO-MDP in each of the four candidate worlds. The learned affordances clearly improved on standard RTDP by a significant margin, though there is clearly still room to improve the learning process to learn near-expert level affordances.

Figure 4 demonstrates the added effect of more training data. In these experiments, we tested on map types that mirrored the features of the worlds generated during training, but this process could be extended to allow for scaffolded learning and more complicated maps (such as the gold smelting task in Figure 1). The averages reported are from solving the OO-MDP 20 times for each world, with each knowledge base. There was a negligible difference in the quality of the policies generated.

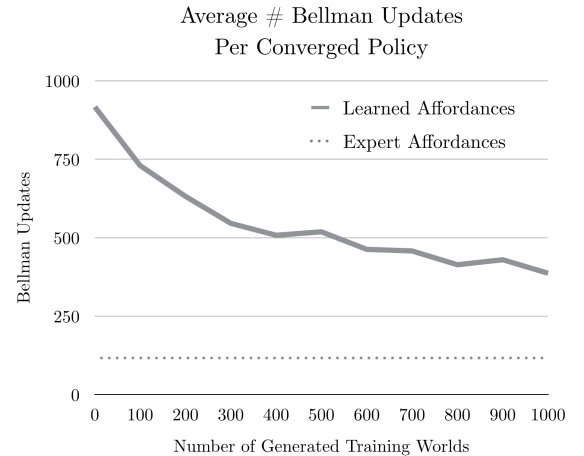


Fig. 4. The effectiveness of added training data on planning performance.

VI. RELATED WORK

In this section, we discuss the differences between affordance-aware planning and other forms of knowledge that have been used to accelerate planning.

A. Temporarily Extended Actions

Temporally extended actions are actions that the agent can select like any other action of the domain, except executing them results in multiple primitive actions being executed in succession. Two common forms of temporally extended actions are *macro-actions* [10] and *options* [20]. Macro-actions are actions that always execute the same sequence of primitive actions. Options are defined with high-level policies that accomplish specific sub tasks. For instance, when an agent is near a door, the agent can engage the ‘door-opening-option-policy’, which switches from the standard high-level planner to running a policy that is hand crafted to open doors. Although the classic options framework is not generalizable to different state spaces, creating *portable* options is a topic of active research [14, 12, 17, 5, 1, 13].

Given the potential for unhelpful temporally extended actions to negatively impact planning time [11], we believe combining affordances with temporally extended actions may be especially valuable because it will restrict the set of temporally extended actions to those useful for a task. In the future, we plan to explore the benefit from combining these approaches.

B. Action Pruning

Sherstov and Stone [19] considered MDPs with a very large action set and for which the action set of the optimal policy of a source task could be transferred to a new, but similar, target task to reduce the learning time required to find the optimal policy in the target task.

The main difference between our affordance-based action set pruning and this action transfer work is that affordances prune away actions on a state by state basis, whereas the learned action pruning is on per task level. Further, with lifted goal descriptions, affordances may be attached to subgoal planning for a significant benefit in planning tasks where complete subgoal knowledge is known.

Rosman and Ramamoorthy [18] provide a method for learning action priors over a set of related tasks. Specifically, they compute a Dirichlet distribution over actions by extracting the frequency that each action was optimal in each state for each previously solved task.

There are a few limitations of the actions priors work that affordance-aware planning does not possess: (1) the action priors can only be used with planning/learning algorithms that work well with an ϵ -greedy rollout policy; (2) the priors are only utilized for fraction ϵ of the time steps, which is typically quite small; and (3) as variance in tasks explored increases, the priors will become more uniform. In contrast, affordance-aware planning can be used in a wide range of planning algorithms, benefits from the pruned action set in every time step, and the affordance defined lifted goal-description enables higher-level reasoning such as subgoal planning.

C. Temporal Logic

Bacchus and Ady [2, 3] provided planners with domain dependent knowledge in the form of a first-order version of linear temporal logic (LTL), which they used for control of a forward-chaining planner. With this methodology, STRIPS style planner may be guided through the search space by checking whether candidate plans do not falsify a given knowledge base of LTL formulas, often achieving polynomial time planning in exponential space.

The primary difference between this body of work and our affordance formalism is that affordances may be learned, increasing autonomy of the agent, while LTL formulas are far too complicated to learn effectively, placing dependence on an expert.

D. Heuristics

Heuristics in MDPs are used to convey information about the value of a given state-action pair with respect to the task being solved and typically take the form of either *value function initialization*, or *reward shaping*. Initializing the value function to an admissible close approximation of the optimal value function has been shown to be effective for LAO* and RTDP [9].

Reward shaping is an alternative approach to providing heuristics. The planning algorithm uses a modified version of the reward function that returns larger rewards for state-action pairs that are expected to be useful, but does not guarantee convergence to an optimal policy unless certain properties of the shaped reward are satisfied [16].

A critical difference between heuristics and affordances is that heuristics are highly dependent on the reward function and state space of the task being solved, whereas affordances are state space independent and transferable between different reward functions. However, if a heuristic can be provided, the combination of heuristics and affordances may even more greatly accelerate planning algorithms than either approach alone.

VII. CONCLUSION

We proposed a novel approach to representing knowledge in terms of *affordances* [7] that allows an agent to efficiently prune its action space based on domain knowledge, providing a significant reduction in the number of state-action pairs the agent needs to evaluate in order to act optimally. We demonstrated the efficacy of the affordance model by comparing standard paradigm planners to their affordance-aware equivalents in a series of challenging planning tasks in the Minecraft domain. Further, we designed a full learning process that allows an agent to autonomously learn useful affordances. We provided preliminary results indicating the effectiveness of the learned affordances, suggesting that the agent may be able to learn to tackle new types of problems on its own.

In the future, we hope to increase our coverage of Minecraft to solve even more difficult planning problems, and apply this approach beyond the Minecraft domain and onto actual robots and other domains of interest.

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