

Empiracle Assignment

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1)

```
a <- c(0.42, 0.06, 0.88, 0.40, 0.90,  
0.38, 0.78, 0.71, 0.57, 0.66,  
0.48, 0.35, 0.16, 0.22, 0.08,  
0.11, 0.29, 0.79, 0.75, 0.82,  
0.30, 0.23, 0.01, 0.41, 0.09)
```

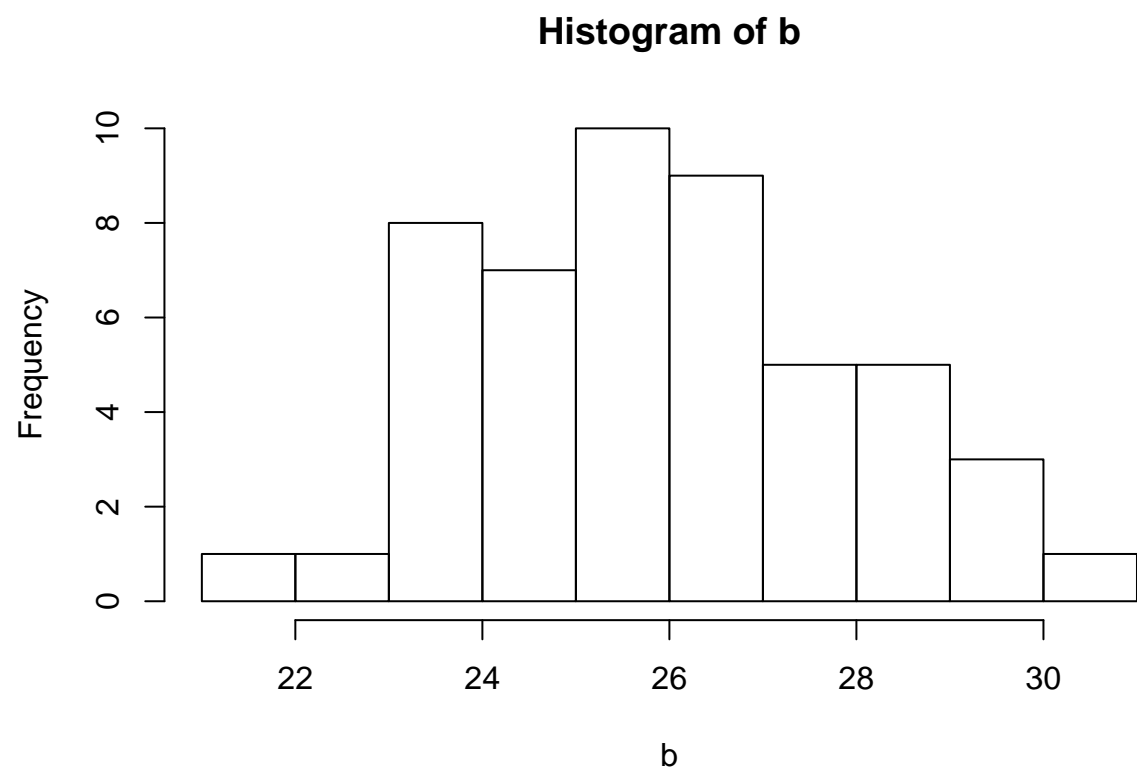
```
ks.test(a,"punif",0,1)
```

```
##  
## One-sample Kolmogorov-Smirnov test  
##  
## data: a  
## D = 0.18, p-value = 0.3501  
## alternative hypothesis: two-sided
```

2)

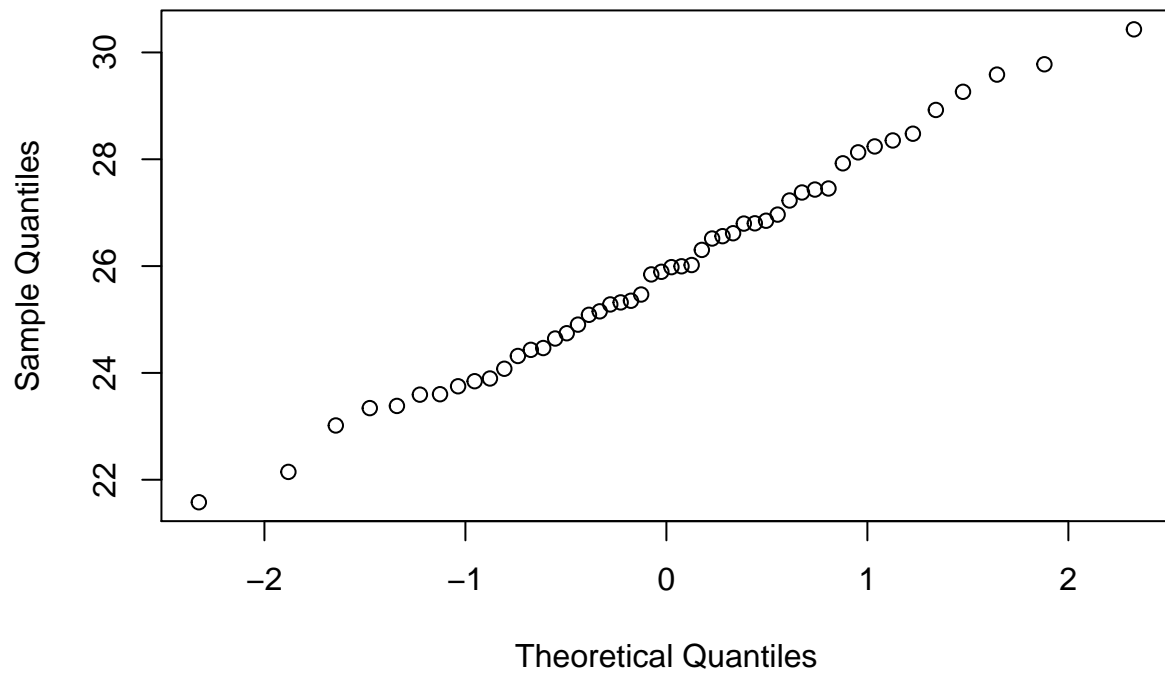
```
b <- c(25.088, 26.615, 25.468, 27.453, 23.845,  
25.996, 26.516, 28.240, 25.980, 30.432,  
26.560, 25.844, 26.964, 23.382, 25.282,  
24.432, 23.593, 24.644, 26.849, 26.801,  
26.303, 23.016, 27.378, 25.351, 23.601,  
24.317, 29.778, 29.585, 22.147, 28.352,  
29.263, 27.924, 21.579, 25.320, 28.129,  
28.478, 23.896, 26.020, 23.750, 24.904,  
24.078, 27.228, 27.433, 23.341, 28.923,  
24.466, 25.153, 25.893, 26.796, 24.743)
```

```
hist(b)
```



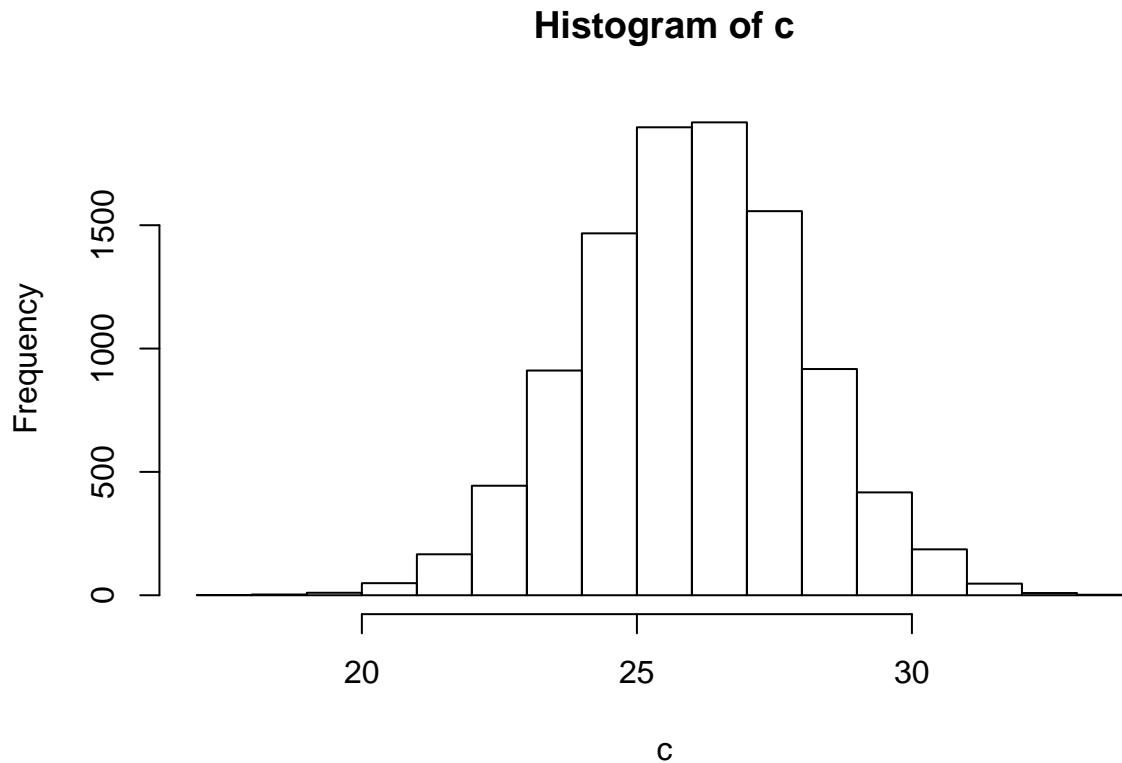
`qqnorm(b)`

Normal Q-Q Plot



```
c <- rnorm(10000,26,2)
```

```
hist(c)
```



```
ks.test(b,pnorm,26,2)
```

```
##
##  One-sample Kolmogorov-Smirnov test
##
## data:  b
## D = 0.06722, p-value = 0.9663
## alternative hypothesis: two-sided
```

```
ks.test(b,c)
```

```
##
##  Two-sample Kolmogorov-Smirnov test
##
## data:  b and c
## D = 0.0715, p-value = 0.9611
## alternative hypothesis: two-sided
```

The data is normally distributed with a mean of 26 and variance of 4. The histogram looks normal, qqplot looks good. I ran a KS test on both the normal distribution, and a simulated dataset. Interestingly, I accidentally included the mean as 28 the first time, and my tests had extremely low p-values. Shows how accurate it is!

3)

```
d <- c(0.61, 0.29, 0.06, 0.59,-1.73,
-0.74, 0.51,-0.56,0.39, 1.64,
```

```
0.05,-0.06, 0.64,-0.82, 0.31,
1.77, 1.09, -1.28, 2.36, 1.31,
1.05,-0.32,0.40, 1.06,-2.47)
```

```
e <- c(2.20, 1.66, 1.38, 0.20,
0.36, 0.00, 0.96, 1.56,
0.44, 1.50,-0.30, 0.66,
2.31, 3.29, -0.27,-0.37,
0.38, 0.70, 0.52,-0.71)
```

```
ks.test(d,e)
```

```
##
## Two-sample Kolmogorov-Smirnov test
##
## data: d and e
## D = 0.23, p-value = 0.5286
## alternative hypothesis: two-sided
```

```
ks.test(d+2,e)
```

```
## Warning in ks.test(d + 2, e): cannot compute exact p-value with ties
```

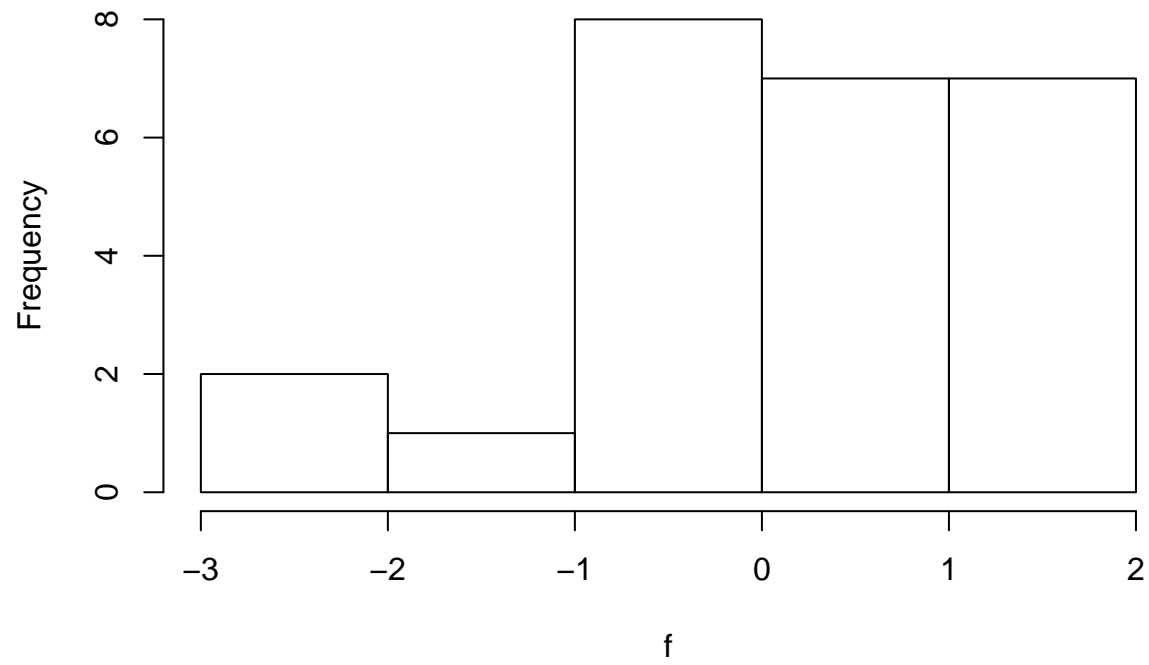
```
##
## Two-sample Kolmogorov-Smirnov test
##
## data: d + 2 and e
## D = 0.61, p-value = 0.0005127
## alternative hypothesis: two-sided
```

It seems like X and Y have the same distribution, and $X+2$ does not have the same distribution as Y .

4)

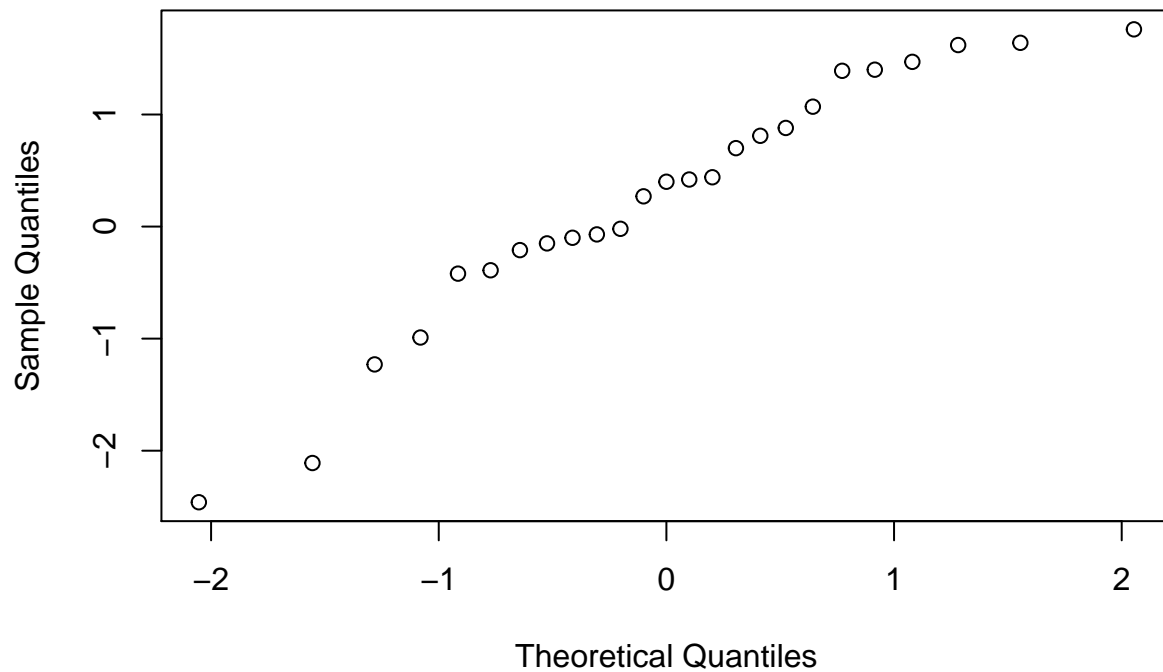
```
f <- readRDS("norm_sample.Rdata")
g <- rnorm(1000,0,1)
hist(f)
```

Histogram of f



`qqnorm(f)`

Normal Q-Q Plot



```
ks.test(f,"pnorm",0,1)
```

```
##  
## One-sample Kolmogorov-Smirnov test  
##  
## data: f  
## D = 0.17724, p-value = 0.3683  
## alternative hypothesis: two-sided
```

```
ks.test(f,g)
```

```
##  
## Two-sample Kolmogorov-Smirnov test  
##  
## data: f and g  
## D = 0.175, p-value = 0.4439  
## alternative hypothesis: two-sided
```

Yes, this data does follow the standard normal distribution, but not extremely well.

```
cdf<- ecdf(f)
```

5)

```
fiji <- read.table("fijiquakes(1).dat",header = TRUE)  
faith <- read.table("faithful(1).dat",header = TRUE)
```

```

ecdf_fiji <- ecdf(fiji$mag)
ecdf_faith <- ecdf(faith$waiting)

e_faith <- sqrt(log(2/.1)/(2*272))
e_fiji <- sqrt(log(2/.05)/(2*1000))

answ <- ecdf_fiji(4.9)-ecdf_fiji(4.3)
answ + e_fiji

## [1] 0.5689469
answ - e_fiji

## [1] 0.4830531
*F(4.9) - F(4.3) 95% confidence interval: [0.48, 0.57]
avg <- mean(faith$waiting)

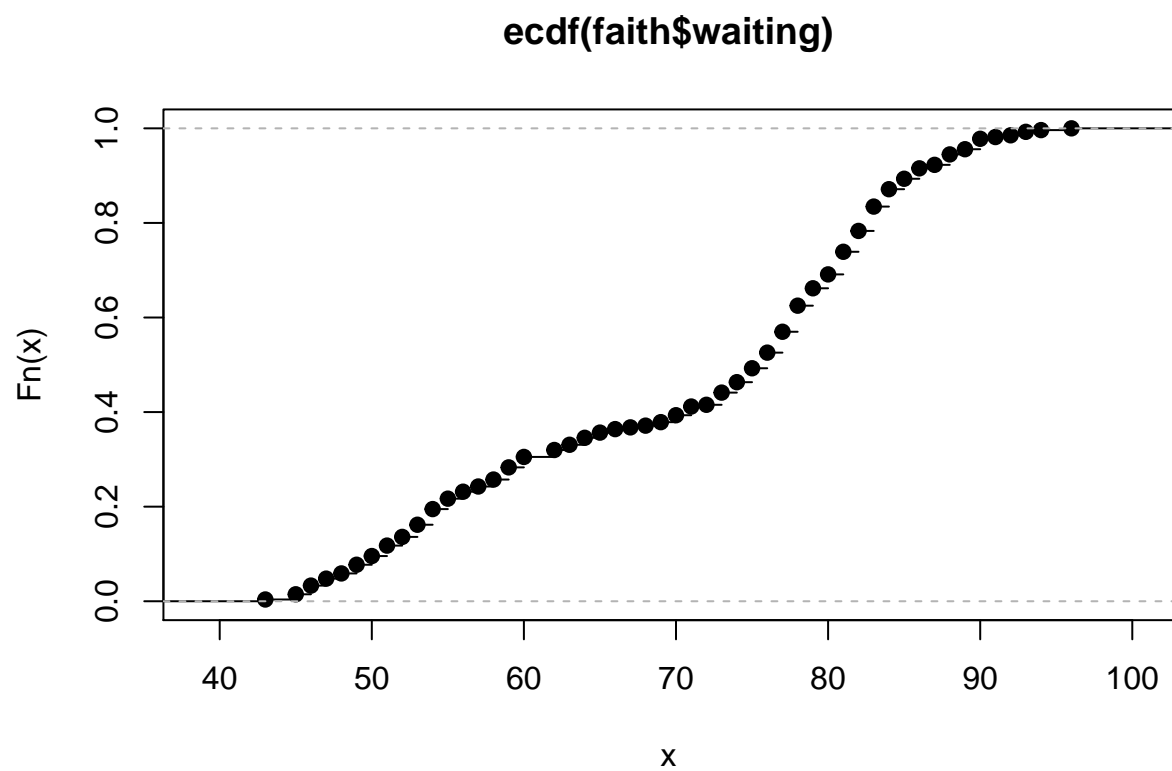
answ2 <- ecdf_faith(mean(avg))

answ2 + e_faith

## [1] 0.4675906
answ2 - e_faith

## [1] 0.3191741
The confidence band for the mean waitig time, F(70.9) is[0.32,0.46].
plot(ecdf_faith)

```

```
quantile(ecdf_faith,probs = .5)
```

```
## 50%  
## 76
```

The median wait time based on our ecdf is 76.