1. $C = \{0.9\} \cup \{1.8\} \cup \{2.7\} \cup \{3.6\} \cup \{4.5\}$

Since you have to pick 6 integers, and there are 5 "pigeonholes" (pairs of numbers that sum to 9), at least one pair of numbers in the 6 chasen has to sum to 9.

If f is Ital, Suppose f is not onto, then there exists a $b \in B$ s.t. $f(x) \neq b$ for any $x \in A$. Since |A| = |B|, $\longrightarrow \longleftarrow$, thus f is onto.

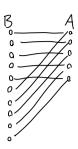
3a. $|B| = {5 \choose 3} = 10$ |A| = 5 A = B, # eF Functions $= |B|^{|A|}$ $10^5 = 100,000$

3b.
$$P(10,5) = \frac{10!}{(10-5)!} = \frac{10!}{5!} = \frac{30,240}{5!}$$

3c. There are none, because since $|A| \angle |B|$, once all elements in A have a arresponding element in B, there are still 5 elements in B left unbit, no matter the function from A = B.

3d. $B \longrightarrow A$, $|A|^{1B1} = 5^{10} = 9,765,625$

3e.



There are no Ital Gundians Grom $B \longrightarrow A$, blc There has to be at least one element in the codomain (A) that gets hit more than once it $|A| \angle |B|$.

3f.
$$9 765 625 - {5 \choose 1}4^{10} + {5 \choose 2}3^{10} - {5 \choose 3}2^{10} + {5 \choose 4}1^{10} - {5 \choose 5}0^{10}$$
$$= 5,103,000$$

3g.
$$\frac{n!}{(n-n)!} \qquad \frac{5!}{0!} = 5! = 120$$

4.

A: 1999

B:
$$(\frac{4}{7})(\frac{4}{7})(\frac{4}{7})(\frac{4}{7}) = 256$$

$$(: (\frac{9}{1})(\frac{9}{1})(\frac{7}{1})(\frac{6}{1}) = 3,024$$

1A(+1B1+1C1- | AMB1-1AMC1-1BMC1+ | AMBMC1

$$(1999 + 256 + 3024) - 64 - 1008, - 96 + 24 = 4135$$

$$(2)(9)(8)(4)$$

$$(4)(4)(3)(2)$$

$$(4)(4)(3)(2)$$

5.
$$f: S \longrightarrow \mathbb{Z}$$
 , $f(x) = - \int x$

Ital: Let
$$x,y \in S$$

$$f(x) = f(y)$$

$$-\sqrt{x} = -\sqrt{y}$$

$$x = y \checkmark$$

$$y = -\int x$$

$$-y = \int x$$

$$x = (-y)^{2}$$

for
$$\forall y \in \mathbb{Z}^-$$
, there exists an $x \in S$.

$$f(x) = -Jx$$
 is a bijection, $f:S \longrightarrow Z$