

# Search in AI + Production Systems

Note Title

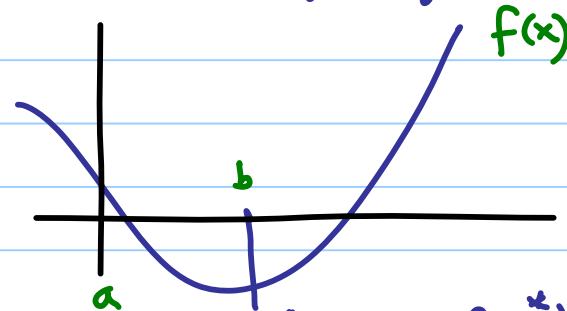
## Classical Search

Linear Search  
Binary Search

"Root-Finding Methods"

Given  $x_0, x_1, \dots, x_{N-1}$

Find  $i$  s.t.  $x_i = \text{key}$  or  $-1$  if not found



Find  $x^*$  s.t.  $f(x^*) = 0$

a method:

Bisection  $\rightarrow$  given  $[a, b] \in \mathbb{R}$

where it is known that  $f(x) = 0$  for some

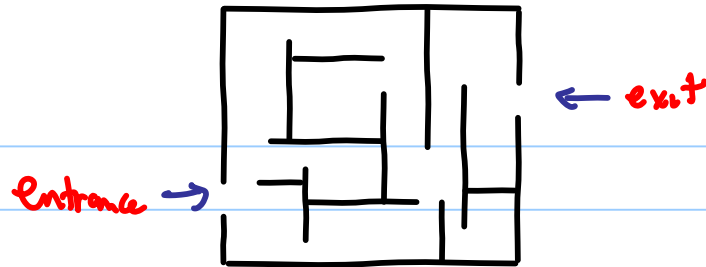
$x \in [a, b]$  [ $f(a)$  and  $f(b)$  have opposite signs]

.....  $\rightarrow$  compute  $m \leftarrow (a+b)/2$

if  $f(a)$  and  $f(m)$  have same sign,  $a \leftarrow m$   
else  $b \leftarrow m$

## Problem Solving

- (a) Given a maze  
Entrance, exit, walls

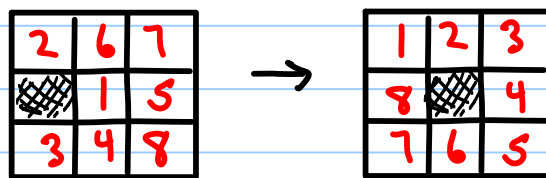


Find a sequence of moves that can get you from entrance to exit.

- (b) A farmer is taking a fox, goose, and bag of corn to market. He must cross a river and the boat is only large enough to transport himself + one item at a time. If left unattended, the fox will eat the goose and/or goose will eat the corn. Plan a way for the farmer to get them across -

- (c) Given two jugs - one w/ 5 quart capacity, another with 2-qt capacity. The 5 quart jug is full. Find a way of pouring water from jug to jug (or to ground) which leaves 1 qt. in the 2qt. jug -

(d) "8-puzzle" - given a sliding-block puzzle in an initial configuration,  
find a sequence of moves that yields another desired configuration



What is a "problem" of this nature?

- Knowledge Base = some set of information that completely describes the problem

State = particular current configuration of the system

goal condition = true if state satisfies desired configuration

- Actions / Moves / Rules =  
"legal moves"

|| We want to find a way  
of choosing the best move

rule = (precondition, action)

↓  
is the move  
applicable  
to current state?

↓  
"move to be applied"  
applying action to  
current state produces  
new state

When several are  
applicable

• "Search strategy"

---

A very simple (not very intelligent) search strategy —

given state,

While not goal (state)

Find all applicable rules  
Try one at random  
update state

"FLAIL WILDLY"  
strategy

note: doesn't always work  
e.g. pour all water out of  
5 qt. jug  
or take corn across river  
first

	Maze	Water Jugs	Fox - Goose - Corn																																		
<u>Knowledge Base</u>	Maze configuration : positions of walls, Entrance, exit	# of jugs capacities of jugs	<ul style="list-style-type: none"><li>• position of boat/farmer</li><li>• contents of left bank</li><li>• contents of right bank</li></ul>																																		
<u>State</u>	where the user is	contents of each jug																																			
<u>rules/ moves</u>	<table><tr><th><u>action</u></th><th><u>precond</u></th></tr><tr><td>↑</td><td>not blocked + on board</td></tr><tr><td>↓</td><td>not blocked</td></tr><tr><td>←</td><td>not blocked "</td></tr><tr><td>→</td><td>not blocked "</td></tr></table>	<u>action</u>	<u>precond</u>	↑	not blocked + on board	↓	not blocked	←	not blocked "	→	not blocked "	<table><tr><th><u>action</u></th><th><u>precond</u></th></tr><tr><td>pour all water out of jug i</td><td>jug i not empty</td></tr><tr><td>pour enough water from jug i to fill jug j</td><td><math>\text{amt}(i) + \text{amt}(j) \geq \text{capacity}(j)</math></td></tr><tr><td>pour all water from jug i to jug j</td><td><math>\text{amt}(i) + \text{amt}(j) \leq \text{capacity}(j)</math></td></tr></table>	<u>action</u>	<u>precond</u>	pour all water out of jug i	jug i not empty	pour enough water from jug i to fill jug j	$\text{amt}(i) + \text{amt}(j) \geq \text{capacity}(j)$	pour all water from jug i to jug j	$\text{amt}(i) + \text{amt}(j) \leq \text{capacity}(j)$	<table><tr><td>Farmer</td><td>→</td></tr><tr><td>Farmer, Goose</td><td>→</td></tr><tr><td>Farmer, Fox</td><td>→</td></tr><tr><td>Farmer, Corn</td><td>→</td></tr><tr><td>Farmer</td><td>←</td></tr><tr><td>Farmer, Goose</td><td>←</td></tr><tr><td>Farmer, Fox</td><td>←</td></tr><tr><td>Farmer, Corn</td><td>←</td></tr></table> <u>Feast condition</u>	Farmer	→	Farmer, Goose	→	Farmer, Fox	→	Farmer, Corn	→	Farmer	←	Farmer, Goose	←	Farmer, Fox	←	Farmer, Corn	←
<u>action</u>	<u>precond</u>																																				
↑	not blocked + on board																																				
↓	not blocked																																				
←	not blocked "																																				
→	not blocked "																																				
<u>action</u>	<u>precond</u>																																				
pour all water out of jug i	jug i not empty																																				
pour enough water from jug i to fill jug j	$\text{amt}(i) + \text{amt}(j) \geq \text{capacity}(j)$																																				
pour all water from jug i to jug j	$\text{amt}(i) + \text{amt}(j) \leq \text{capacity}(j)$																																				
Farmer	→																																				
Farmer, Goose	→																																				
Farmer, Fox	→																																				
Farmer, Corn	→																																				
Farmer	←																																				
Farmer, Goose	←																																				
Farmer, Fox	←																																				
Farmer, Corn	←																																				
<u>goal</u>	state == exit	amt(2) == 1	all occupants on right																																		

## A CLOSER LOOK:

action

pour all water  
out of jug i

pour enough  
water from  
jug i to fill  
jug j

pour all water  
from jug i  $\rightarrow$   
jug j

precond

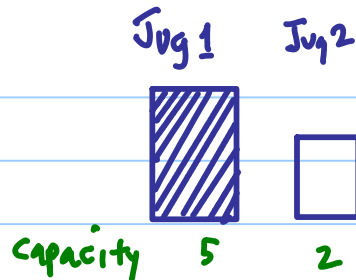
jug i  
not empty

$\text{amt}(i) +$   
 $\text{amt}(j) \geq$   
 $\text{capacity}(j)$

$\text{amt}(i) +$   
 $\text{amt}(j)$   
 $\leq \text{capacity}(j)$

} Jug i not empty  
Jug j not full

} Jug i not empty  
Jug j not full



state  
(5, 0)

$\text{amt}(1) = 5$   
 $\text{amt}(2) = 0$

Pour all water out of Jug 1  
 $(-5, 0) \rightarrow (0, 0)$

Pour all water out of Jug 2  
 $\times$  not applicable

Pour enough water from  
Jug 1 to Jug 2 to fill Jug 2  
precond OK:  $(-2, 2) \rightarrow (3, 2)$

Pour enough water from Jug 2,  
 $\times$  not applicable

Pour all from 1 to 2  $\times$   
Pour all from 2 to 1  $\times$

state = initialstate  
while not goal (state)

Rules  $\leftarrow$  ApplicableRules(state)

choose  $r \in$  Rules

state = ApplyRule(r, state)

result = null  
for each rule

if precondition(rule, state)  
add rule to result

return result

"FLAUNGS"  
Strategy

Finding a valid sequence of rules efficiently is the "intelligent" part.

"GPS" — Generalized Problem Solver  
(Newell & Simon, late 1950's)