

Write a program that, prints a 'pine tree' consisting of triangles of increasing sizes, filled with a character (eg. '*' or '+' or '\$' etc).

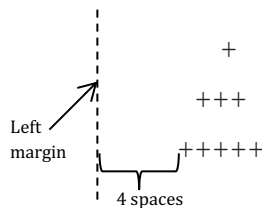
Your program should interact with the user to read the number of triangles in the tree and the character filling the tree.

Your implementation should include the following functions:

- ```
a. void printShiftedTriangle(int n, int m, char symbol)
```

It prints an `n`-line triangle, filled with `symbol` characters, shifted `m` spaces from the left margin.

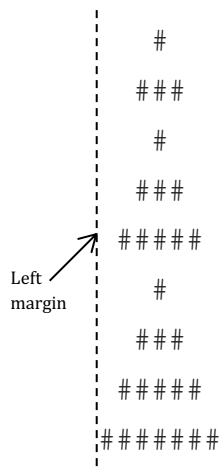
For example, if we call `printShiftedTriangle(3, 4, `+`)`, the expected output is:



- b. `void printPineTree(int n, char symbol)`

It prints a sequence of `n` triangles of increasing sizes (the smallest triangle is a 2-line triangle), which form the shape of a pine tree. The triangles are filled with the `symbol` character.

For example, if we call `printPineTree(3, `#`)`, the expected output is:



### Question 3:

The number  $e$  is an important mathematical constant that is the base of the natural logarithm.  $e$  also arises in the study of compound interest, and in many other applications.

Background of  $e$ : [https://en.wikipedia.org/wiki/E\\_\(mathematical\\_constant\)](https://en.wikipedia.org/wiki/E_(mathematical_constant))

$e$  can be calculated as the sum of the infinite series:

$$e = 1 + \frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \frac{1}{4!} + \dots$$

The value of  $e$  is approximately equal to 2.71828. We can get an approximate value of  $e$ , by calculating only a partial sum of the infinite sum above (the more addends we add, the better approximation we get).

Implement the function:

```
double eApprox(int n)
```

This function is given a positive integer  $n$ , and returns an approximation of  $e$ , calculated by the sum of the first  $(n+1)$  addends of the infinite sum above.

To test your function use the following main:

```
int main() {
 cout.precision(30);

 for (int n = 1; n <= 15; n++) {
 cout<<"n = "<<n<<"\t"<<eApprox(n)<<endl;
 }

 return 0;
}
```

### Notes:

1. Pay attention to the running time of `eApprox`. An efficient implementation would run in  $\Theta(n)$ .
2. Since the values of the factorials will grow to be very large, use a variable of type `double` to store them.

**Question 4:**

- a. Implement a function:

```
void printDivisors(int num)
```

This function is given a positive integer `num`, and prints all of `num`'s divisors in an **ascending order**, separated by a space.

For Example, if we call `printDivisors(100)`, the expected output is:

1 2 4 5 10 20 25 50 100

Implementation requirement: Pay attention to the running time of your function. An efficient implementation would run in  $\Theta(\sqrt{num})$ .

- b. Use the function above when implementing a program that reads from the user a positive integer ( $\geq 2$ ), and prints all its divisors.

Your program should interact with the user **exactly** as it shows in the following example:

Please enter a positive integer  $\geq 2$ : 100

1 2 4 5 10 20 25 50 100

**Question 5:**

Use the definition of  $\Theta$  in order to show the following:

a.  $5n^3 + 2n^2 + 3n = \Theta(n^3)$

b.  $\sqrt{7n^2 + 2n - 8} = \Theta(n)$