



# Z3 API in Python

1. [Getting Started](#)
2. [Boolean Logic](#)
3. [Solvers](#)
4. [Arithmetic](#)
5. [Machine Arithmetic](#)
6. [Functions](#)
7. [Satisfiability and Validity](#)
8. [List Comprehensions](#)
9. [Kinematic Equations](#)
10. [Bit Tricks](#)
11. [Puzzles](#)
12. [Application: Install Problem](#)
13. [Using Z3Py Locally](#)
14. [tutorials](#)

Z3 is a high performance theorem prover developed at [Microsoft Research](#). Z3 is used in many applications such as: software/hardware verification and testing, constraint solving, analysis of hybrid systems, security, biology (in silico analysis), and geometrical problems.

This tutorial demonstrates the main capabilities of Z3Py: the Z3 API in [Python](#). No Python background is needed to read this tutorial. However, it is useful to learn Python (a fun language!) at some point, and there are many excellent free resources for doing so ([Python Tutorial](#)).

The Z3 distribution also contains the **C**, **.Net** and **OCaml** APIs. The source code of Z3Py is available in the Z3 distribution, feel free to modify it to meet your needs. The source code also demonstrates how to use new features in Z3 4.0. Other cool front-ends for Z3 include [Scala^Z3](#) and [SBV](#).

Be sure to follow along with the examples by clicking the **load in editor** link in the corner. See what Z3Py says, try your own scripts, and experiment!

Please send feedback, comments and/or corrections to [leonardo@microsoft.com](mailto:leonardo@microsoft.com). Your comments are very valuable.

## Getting Started

Let us start with the following simple example:

[load in editor](#)

```
x = Int('x')
y = Int('y')
solve(x > 2, y < 10, x + 2*y == 7)
```

The function `Int('x')` creates an integer variable in Z3 named `x`. The `solve` function solves a system of

constraints. The example above uses two variables  $x$  and  $y$ , and three constraints. Z3Py like Python uses `=` for assignment. The operators `<`, `<=`, `>`, `>=`, `==` and `!=` for comparison. In the example above, the expression  $x + 2*y == 7$  is a Z3 constraint. Z3 can solve and crunch formulas.

The next examples show how to use the Z3 formula/expression simplifier.

[load in editor](#)

```
x = Int('x')
y = Int('y')
print simplify(x + y + 2*x + 3)
print simplify(x < y + x + 2)
print simplify(And(x + 1 >= 3, x**2 + x**2 + y**2 + 2 >= 5))
```

By default, Z3Py (for the web) displays formulas and expressions using mathematical notation. As usual,  $\wedge$  is the logical and,  $\vee$  is the logical or, and so on. The command `set_option(html_mode=False)` makes all formulas and expressions to be displayed in Z3Py notation. This is also the default mode for the offline version of Z3Py that comes with the Z3 distribution.

[load in editor](#)

```
x = Int('x')
y = Int('y')
print x**2 + y**2 >= 1
set_option(html_mode=False)
print x**2 + y**2 >= 1
```

Z3 provides functions for traversing expressions.

[load in editor](#)

```
x = Int('x')
y = Int('y')
n = x + y >= 3
print "num args: ", n.num_args()
print "children: ", n.children()
print "1st child:", n.arg(0)
print "2nd child:", n.arg(1)
print "operator: ", n.decl()
print "op name: ", n.decl().name()
```

Z3 provides all basic mathematical operations. Z3Py uses the same operator precedence of the Python language. Like Python, `**` is the power operator. Z3 can solve nonlinear *polynomial* constraints.

[load in editor](#)

```
x = Real('x')
y = Real('y')
solve(x**2 + y**2 > 3, x**3 + y < 5)
```

The procedure `Real('x')` creates the real variable  $x$ . Z3Py can represent arbitrarily large integers, rational numbers (like in the example above), and irrational algebraic numbers. An irrational algebraic number is a root of a polynomial with integer coefficients. Internally, Z3 represents all these numbers precisely. The irrational numbers are displayed in decimal notation for making it easy to read the results.

[load in editor](#)

```
x = Real('x')
y = Real('y')
solve(x**2 + y**2 == 3, x**3 == 2)

set_option(precision=30)
print "Solving, and displaying result with 30 decimal places"
solve(x**2 + y**2 == 3, x**3 == 2)
```

The procedure `set_option` is used to configure the Z3 environment. It is used to set global configuration options such as how the result is displayed. The option `set_option(precision=30)` sets the number of decimal places used when displaying results. The ? mark in 1.2599210498? indicates the output is truncated.

The following example demonstrates a common mistake. The expression `3/2` is a Python integer and not a Z3 rational number. The example also shows different ways to create rational numbers in Z3Py. The procedure `Q(num, den)` creates a Z3 rational where `num` is the numerator and `den` is the denominator. The `RealVal(1)` creates a Z3 real number representing the number 1.

[load in editor](#)

```
print 1/3
print RealVal(1)/3
print Q(1,3)

x = Real('x')
print x + 1/3
print x + Q(1,3)
print x + "1/3"
print x + 0.25
```

Rational numbers can also be displayed in decimal notation.

[load in editor](#)

```
x = Real('x')
solve(3*x == 1)

set_option(rational_to_decimal=True)
solve(3*x == 1)

set_option(precision=30)
solve(3*x == 1)
```

A system of constraints may not have a solution. In this case, we say the system is **unsatisfiable**.

[load in editor](#)

```
x = Real('x')
solve(x > 4, x < 0)
```

Like in Python, comments begin with the hash character `#` and are terminated by the end of line. Z3Py does not support comments that span more than one line.

[load in editor](#)

```
# This is a comment
x = Real('x') # comment: creating x
```

```
print x**2 + 2*x + 2 # comment: printing polynomial
```

## Boolean Logic

Z3 supports Boolean operators: And, Or, Not, Implies (implication), If (if-then-else). Bi-implications are represented using equality ==. The following example shows how to solve a simple set of Boolean constraints.

[load in editor](#)

```
p = Bool('p')
q = Bool('q')
r = Bool('r')
solve(Implies(p, q), r == Not(q), Or(Not(p), r))
```

The Python Boolean constants True and False can be used to build Z3 Boolean expressions.

[load in editor](#)

```
p = Bool('p')
q = Bool('q')
print And(p, q, True)
print simplify(And(p, q, True))
print simplify(And(p, False))
```

The following example uses a combination of polynomial and Boolean constraints.

[load in editor](#)

```
p = Bool('p')
x = Real('x')
solve(Or(x < 5, x > 10), Or(p, x**2 == 2), Not(p))
```

## Solvers

Z3 provides different solvers. The command solve, used in the previous examples, is implemented using the Z3 solver API. The implementation can be found in the file z3.py in the Z3 distribution. The following example demonstrates the basic Solver API.

[load in editor](#)

```
x = Int('x')
y = Int('y')

s = Solver()
print s

s.add(x > 10, y == x + 2)
print s
print "Solving constraints in the solver s ..."
print s.check()

print "Create a new scope..."
s.push()
```

```

s.add(y < 11)
print s
print "Solving updated set of constraints..."
print s.check()

print "Restoring state..."
s.pop()
print s
print "Solving restored set of constraints..."
print s.check()

```

The command `Solver()` creates a general purpose solver. Constraints can be added using the method `add`. We say the constraints have been **asserted** in the solver. The method `check()` solves the asserted constraints. The result is `sat` (satisfiable) if a solution was found. The result is `unsat` (unsatisfiable) if no solution exists. We may also say the system of asserted constraints is **infeasible**. Finally, a solver may fail to solve a system of constraints and `unknown` is returned.

In some applications, we want to explore several similar problems that share several constraints. We can use the commands `push` and `pop` for doing that. Each solver maintains a stack of assertions. The command `push` creates a new scope by saving the current stack size. The command `pop` removes any assertion performed between it and the matching `push`. The `check` method always operates on the content of solver assertion stack.

The following example shows an example that Z3 cannot solve. The solver returns `unknown` in this case. Recall that Z3 can solve nonlinear polynomial constraints, but  $2^{**}x$  is not a polynomial.

[load in editor](#)

```

x = Real('x')
s = Solver()
s.add(2**x == 3)
print s.check()

```

The following example shows how to traverse the constraints asserted into a solver, and how to collect performance statistics for the `check` method.

[load in editor](#)

```

x = Real('x')
y = Real('y')
s = Solver()
s.add(x > 1, y > 1, Or(x + y > 3, x - y < 2))
print "asserted constraints..."
for c in s.assertions():
    print c

print s.check()
print "statistics for the last check method..."
print s.statistics()
# Traversing statistics
for k, v in s.statistics():
    print "%s : %s" % (k, v)

```

The command `check` returns `sat` when Z3 finds a solution for the set of asserted constraints. We say Z3 **satisfied** the set of constraints. We say the solution is a **model** for the set of asserted constraints. A model is an **interpretation** that makes each asserted constraint **true**. The following example shows the basic

methods for inspecting models.

[load in editor](#)

```
x, y, z = Reals('x y z')
s = Solver()
s.add(x > 1, y > 1, x + y > 3, z - x < 10)
print s.check()

m = s.model()
print "x = %s" % m[x]

print "traversing model..."
for d in m.decls():
    print "%s = %s" % (d.name(), m[d])
```

In the example above, the function `Reals('x y z')` creates the variables `x`, `y` and `z`. It is shorthand for:

```
x = Real('x')
y = Real('y')
z = Real('z')
```

The expression `m[x]` returns the interpretation of `x` in the model `m`. The expression `"%s = %s" % (d.name(), m[d])` returns a string where the first `%s` is replaced with the name of `d` (i.e., `d.name()`), and the second `%s` with a textual representation of the interpretation of `d` (i.e., `m[d]`). Z3Py automatically converts Z3 objects into a textual representation when needed.

## Arithmetic

Z3 supports real and integer variables. They can be mixed in a single problem. Like most programming languages, Z3Py will automatically add coercions converting integer expressions to real ones when needed. The following example demonstrates different ways to declare integer and real variables.

[load in editor](#)

```
x = Real('x')
y = Int('y')
a, b, c = Reals('a b c')
s, r = Ints('s r')
print x + y + 1 + (a + s)
print ToReal(y) + c
```

The function `ToReal` casts an integer expression into a real expression.

Z3Py supports all basic arithmetic operations.

[load in editor](#)

```
a, b, c = Ints('a b c')
d, e = Reals('d e')
solve(a > b + 2,
      a == 2*c + 10,
      c + b <= 1000,
      d >= e)
```

The command `simplify` applies simple transformations on Z3 expressions.



[load in editor](#)

```
x = BitVec('x', 16)
y = BitVec('y', 16)
print x + 2
# Internal representation
print (x + 2).sexpr()

# -1 is equal to 65535 for 16-bit integers
print simplify(x + y - 1)

# Creating bit-vector constants
a = BitVecVal(-1, 16)
b = BitVecVal(65535, 16)
print simplify(a == b)

a = BitVecVal(-1, 32)
b = BitVecVal(65535, 32)
# -1 is not equal to 65535 for 32-bit integers
print simplify(a == b)
```

In contrast to programming languages, such as C, C++, C#, Java, there is no distinction between signed and unsigned bit-vectors as numbers. Instead, Z3 provides special signed versions of arithmetical operations where it makes a difference whether the bit-vector is treated as signed or unsigned. In Z3Py, the operators <, <=, >, >=, /, % and >> correspond to the signed versions. The corresponding unsigned operators are ULT, ULE, UGT, UGE, UDiv, URem and LShR.

[load in editor](#)

```
# Create to bit-vectors of size 32
x, y = BitVecs('x y', 32)

solve(x + y == 2, x > 0, y > 0)

# Bit-wise operators
# & bit-wise and
# | bit-wise or
# ~ bit-wise not
solve(x & y == ~y)

solve(x < 0)

# using unsigned version of <
solve(ULT(x, 0))
```

The operator >> is the arithmetic shift right, and << is the shift left. The logical shift right is the operator LShR.

[load in editor](#)

```
# Create to bit-vectors of size 32
x, y = BitVecs('x y', 32)

solve(x >> 2 == 3)

solve(x << 2 == 3)

solve(x << 2 == 24)
```



# Functions

Unlike programming languages, where functions have side-effects, can throw exceptions, or never return, functions in Z3 have no side-effects and are **total**. That is, they are defined on all input values. This includes functions, such as division. Z3 is based on [first-order logic](#).

Given a constraints such as  $x + y > 3$ , we have been saying that  $x$  and  $y$  are variables. In many textbooks,  $x$  and  $y$  are called uninterpreted constants. That is, they allow any interpretation that is consistent with the constraint  $x + y > 3$ .

More precisely, function and constant symbols in pure first-order logic are *uninterpreted* or *free*, which means that no a priori interpretation is attached. This is in contrast to functions belonging to the signature of theories, such as arithmetic where the function  $+$  has a fixed standard interpretation (it adds two numbers). Uninterpreted functions and constants are maximally flexible; they allow any interpretation that is consistent with the constraints over the function or constant.

To illustrate uninterpreted functions and constants let us the uninterpreted integer constants (aka variables)  $x, y$ . Finally let  $f$  be an uninterpreted function that takes one argument of type (aka sort) integer and results in an integer value. The example illustrates how one can force an interpretation where  $f$  applied twice to  $x$  results in  $x$  again, but  $f$  applied once to  $x$  is different from  $x$ .

[load in editor](#)

```
x = Int('x')
y = Int('y')
f = Function('f', IntSort(), IntSort())
solve(f(f(x)) == x, f(x) == y, x != y)
```

The solution (interpretation) for  $f$  should be read as  $f(0)$  is 1,  $f(1)$  is 0, and  $f(a)$  is 1 for all  $a$  different from 0 and 1.

In Z3, we can also evaluate expressions in the model for a system of constraints. The following example shows how to use the `evaluate` method.

[load in editor](#)

```
x = Int('x')
y = Int('y')
f = Function('f', IntSort(), IntSort())
s = Solver()
s.add(f(f(x)) == x, f(x) == y, x != y)
print s.check()
m = s.model()
print "f(f(x)) =", m.evaluate(f(f(x)))
print "f(x)      =", m.evaluate(f(x))
```

## Satisfiability and Validity

A formula/constraint  $F$  is **valid** if  $F$  always evaluates to true for any assignment of appropriate values to its uninterpreted symbols. A formula/constraint  $F$  is **satisfiable** if there is some assignment of appropriate values to its uninterpreted symbols under which  $F$  evaluates to true. Validity is about finding a proof of a statement; satisfiability is about finding a solution to a set of constraints. Consider a formula  $F$  containing  $a$  and  $b$ . We can ask whether  $F$  is valid, that is whether it is always true for any combination of values for  $a$

and b. If  $F$  is always true, then  $\text{Not}(F)$  is always false, and then  $\text{Not}(F)$  will not have any satisfying assignment (i.e., solution); that is,  $\text{Not}(F)$  is unsatisfiable. That is,  $F$  is valid precisely when  $\text{Not}(F)$  is not satisfiable (is unsatisfiable). Alternately,  $F$  is satisfiable if and only if  $\text{Not}(F)$  is not valid (is invalid). The following example proves the deMorgan's law.

The following example redefines the Z3Py function `prove` that receives a formula as a parameter. This function creates a solver, adds/asserts the negation of the formula, and check if the negation is unsatisfiable. The implementation of this function is a simpler version of the Z3Py command `prove`.

[load in editor](#)

```
p, q = Booleans('p q')
demorgan = And(p, q) == Not(Or(Not(p), Not(q)))
print demorgan

def prove(f):
    s = Solver()
    s.add(Not(f))
    if s.check() == unsat:
        print "proved"
    else:
        print "failed to prove"

print "Proving demorgan..."
prove(demorgan)
```

## List Comprehensions

Python supports [list comprehensions](#). List comprehensions provide a concise way to create lists. They can be used to create Z3 expressions and problems in Z3Py. The following example demonstrates how to use Python list comprehensions in Z3Py.

[load in editor](#)

```
# Create list [1, ..., 5]
print [ x + 1 for x in range(5) ]

# Create two lists containing 5 integer variables
X = [ Int('x%s' % i) for i in range(5) ]
Y = [ Int('y%s' % i) for i in range(5) ]
print X

# Create a list containing X[i]+Y[i]
X_plus_Y = [ X[i] + Y[i] for i in range(5) ]
print X_plus_Y

# Create a list containing X[i] > Y[i]
X_gt_Y = [ X[i] > Y[i] for i in range(5) ]
print X_gt_Y

print And(X_gt_Y)

# Create a 3x3 "matrix" (list of lists) of integer variables
X = [ [ Int("x_%s_%s" % (i+1, j+1)) for j in range(3) ]
       for i in range(3) ]
pp(X)
```

In the example above, the expression "x%s" % i returns a string where %s is replaced with the value of i.

The command pp is similar to print, but it uses Z3Py formatter for lists and tuples instead of Python's formatter.

Z3Py also provides functions for creating vectors of Boolean, Integer and Real variables. These functions are implemented using list comprehensions.

[load in editor](#)

```
X = IntVector('x', 5)
Y = RealVector('y', 5)
P = BoolVector('p', 5)
print X
print Y
print P
print [ y**2 for y in Y ]
print Sum([ y**2 for y in Y ])
```

## Kinematic Equations

In high school, students learn the kinematic equations. These equations describe the mathematical relationship between **displacement** (d), **time** (t), **acceleration** (a), **initial velocity** (v\_i) and **final velocity** (v\_f). In Z3Py notation, we can write these equations as:

```
d == v_i * t + (a*t**2)/2,
v_f == v_i + a*t
```

### Problem 1

Ima Hurryin is approaching a stoplight moving with a velocity of 30.0 m/s. The light turns yellow, and Ima applies the brakes and skids to a stop. If Ima's acceleration is -8.00 m/s<sup>2</sup>, then determine the displacement of the car during the skidding process.

[load in editor](#)

```
d, a, t, v_i, v_f = Reals('d a t v__i v__f')

equations = [
    d == v_i * t + (a*t**2)/2,
    v_f == v_i + a*t,
]
print "Kinematic equations:"
print equations

# Given v_i, v_f and a, find d
problem = [
    v_i == 30,
    v_f == 0,
    a == -8
]
print "Problem:"
print problem

print "Solution:"
```

```
solve(equations + problem)
```

## Problem 2

Ben Rushin is waiting at a stoplight. When it finally turns green, Ben accelerated from rest at a rate of a  $6.00 \text{ m/s}^2$  for a time of  $4.10$  seconds. Determine the displacement of Ben's car during this time period.

[load in editor](#)

```
d, a, t, v_i, v_f = Reals('d a t v__i v__f')
```

```
equations = [  
    d == v_i * t + (a*t**2)/2,  
    v_f == v_i + a*t,  
]
```

```
# Given v_i, t and a, find d
```

```
problem = [  
    v_i == 0,  
    t == 4.10,  
    a == 6  
]
```

```
solve(equations + problem)
```

```
# Display rationals in decimal notation  
set_option(rational_to_decimal=True)
```

```
solve(equations + problem)
```

## Bit Tricks

Some low level [hacks](#) are very popular with C programmers. We use some of these hacks in the Z3 implementation.

### Power of two

This hack is frequently used in C programs (Z3 included) to test whether a machine integer is a power of two. We can use Z3 to prove it really works. The claim is that  $x \neq 0 \ \&\& \ (x \ \& \ (x - 1)) == 0$  is true if and only if  $x$  is a power of two.

[load in editor](#)

```
x      = BitVec('x', 32)  
powers = [ 2**i for i in range(32) ]  
fast   = And(x != 0, x & (x - 1) == 0)  
slow   = Or([ x == p for p in powers ])  
print fast  
prove(fast == slow)  
  
print "trying to prove buggy version..."  
fast   = x & (x - 1) == 0  
prove(fast == slow)
```

## Opposite signs

The following simple hack can be used to test whether two machine integers have opposite signs.

[load in editor](#)

```
x      = BitVec('x', 32)
y      = BitVec('y', 32)

# Claim: (x ^ y) < 0 iff x and y have opposite signs
trick  = (x ^ y) < 0

# Naive way to check if x and y have opposite signs
opposite = Or(And(x < 0, y >= 0),
              And(x >= 0, y < 0))

prove(trick == opposite)
```

## Puzzles

### Dog, Cat and Mouse

Consider the following puzzle. Spend exactly 100 dollars and buy exactly 100 animals. Dogs cost 15 dollars, cats cost 1 dollar, and mice cost 25 cents each. You have to buy at least one of each. How many of each should you buy?

[load in editor](#)

```
# Create 3 integer variables
dog, cat, mouse = Ints('dog cat mouse')
solve(dog >= 1,    # at least one dog
      cat >= 1,    # at least one cat
      mouse >= 1,  # at least one mouse
      # we want to buy 100 animals
      dog + cat + mouse == 100,
      # We have 100 dollars (10000 cents):
      #   dogs cost 15 dollars (1500 cents),
      #   cats cost 1 dollar (100 cents), and
      #   mice cost 25 cents
      1500 * dog + 100 * cat + 25 * mouse == 10000)
```

## Sudoku

[Sudoku](#) is a very popular puzzle. The goal is to insert the numbers in the boxes to satisfy only one condition: each row, column and 3x3 box must contain the digits 1 through 9 exactly once.

				9	4		3	
			5	1				7
	8	9					4	
						2		8
	6		2		1		5	
1		2						
	7					5	2	
9				6	5			
	4		9	7				

The following example encodes the sudoku problem in Z3. Different sudoku instances can be solved by modifying the matrix instance. This example makes heavy use of [list comprehensions](#) available in the Python programming language.

[load in editor](#)

```
# 9x9 matrix of integer variables
X = [ [ Int("x_%s_%s" % (i+1, j+1)) for j in range(9) ]
      for i in range(9) ]

# each cell contains a value in {1, ..., 9}
cells_c = [ And(1 <= X[i][j], X[i][j] <= 9)
            for i in range(9) for j in range(9) ]

# each row contains a digit at most once
rows_c = [ Distinct(X[i]) for i in range(9) ]

# each column contains a digit at most once
cols_c = [ Distinct([ X[i][j] for i in range(9) ])
          for j in range(9) ]

# each 3x3 square contains a digit at most once
sq_c = [ Distinct([ X[3*i0 + i][3*j0 + j]
                   for i in range(3) for j in range(3) ])
        for i0 in range(3) for j0 in range(3) ]

sudoku_c = cells_c + rows_c + cols_c + sq_c

# sudoku instance, we use '0' for empty cells
instance = ((0,0,0,0,9,4,0,3,0),
            (0,0,0,5,1,0,0,0,7),
            (0,8,9,0,0,0,0,4,0),
            (0,0,0,0,0,0,2,0,8),
            (0,6,0,2,0,1,0,5,0),
            (1,0,2,0,0,0,0,0,0),
            (0,7,0,0,0,0,5,2,0),
            (9,0,0,0,6,5,0,0,0),
```

```

(0,4,0,9,7,0,0,0,0))

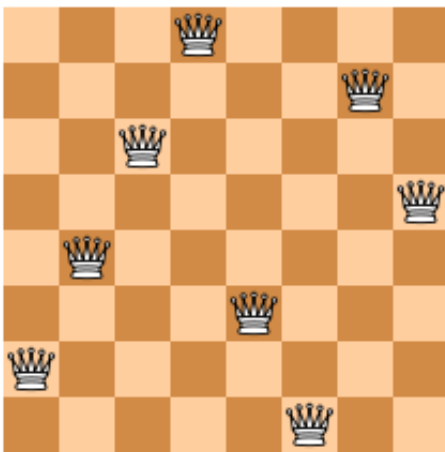
instance_c = [ If(instance[i][j] == 0,
                  True,
                  X[i][j] == instance[i][j])
              for i in range(9) for j in range(9) ]

s = Solver()
s.add(sudoku_c + instance_c)
if s.check() == sat:
    m = s.model()
    r = [ [ m.evaluate(X[i][j]) for j in range(9) ]
          for i in range(9) ]
    print_matrix(r)
else:
    print "failed to solve"

```

## Eight Queens

The eight queens puzzle is the problem of placing eight chess queens on an 8x8 chessboard so that no two queens attack each other. Thus, a solution requires that no two queens share the same row, column, or diagonal.



[load in editor](#)

```

# We know each queen must be in a different row.
# So, we represent each queen by a single integer: the column position
Q = [ Int('Q_%i' % (i + 1)) for i in range(8) ]

# Each queen is in a column {1, ... 8 }
val_c = [ And(1 <= Q[i], Q[i] <= 8) for i in range(8) ]

# At most one queen per column
col_c = [ Distinct(Q) ]

# Diagonal constraint
diag_c = [ If(i == j,
             True,
             And(Q[i] - Q[j] != i - j, Q[i] - Q[j] != j - i))
          for i in range(8) for j in range(i) ]

solve(val_c + col_c + diag_c)

```

# Application: Install Problem

The **install problem** consists of determining whether a new set of packages can be installed in a system. This application is based on the article [OPIUM: Optimal Package Install/Uninstall Manager](#). Many packages depend on other packages to provide some functionality. Each distribution contains a meta-data file that explicates the requirements of each package of the distribution. The meta-data contains details like the name, version, etc. More importantly, it contains **depends** and **conflicts** clauses that stipulate which other packages should be on the system. The depends clauses stipulate which other packages must be present. The conflicts clauses stipulate which other packages must not be present.

The install problem can be easily solved using Z3. The idea is to define a Boolean variable for each package. This variable is true if the package must be in the system. If package a depends on packages b, c and z, we write:

```
DependsOn(a, [b, c, z])
```

DependsOn is a simple Python function that creates Z3 constraints that capture the depends clause semantics.

```
def DependsOn(pack, deps):
    return And([ Implies(pack, dep) for dep in deps ])
```

Thus, Depends(a, [b, c, z]) generates the constraint

```
And(Implies(a, b), Implies(a, c), Implies(a, z))
```

That is, if users install package a, they must also install packages b, c and z.

If package d conflicts with package e, we write Conflict(d, e). Conflict is also a simple Python function.

```
def Conflict(p1, p2):
    return Or(Not(p1), Not(p2))
```

Conflict(d, e) generates the constraint Or(Not(d), Not(e)). With these two functions, we can easily encode the example in the [Opium article](#) (Section 2) in Z3Py as:

[load in editor](#)

```
def DependsOn(pack, deps):
    return And([ Implies(pack, dep) for dep in deps ])

def Conflict(p1, p2):
    return Or(Not(p1), Not(p2))

a, b, c, d, e, f, g, z = Booleans('a b c d e f g z')

solve(DependsOn(a, [b, c, z]),
      DependsOn(b, [d]),
      DependsOn(c, [Or(d, e), Or(f, g)]),
      Conflict(d, e),
      a, z)
```

Note that the example contains the constraint



```
DependsOn(c, [Or(d, e), Or(f, g)]),
```

The meaning is: to install c, we must install d or e, and f or g

Now, we refine the previous example. First, we modify `DependsOn` to allow us to write `DependsOn(b, d)` instead of `DependsOn(b, [d])`. We also write a function `install_check` that returns a list of packages that must be installed in the system. The function `Conflict` is also modified. It can now receive multiple arguments.

[load in editor](#)

```
def DependsOn(pack, deps):
    if is_expr(deps):
        return Implies(pack, deps)
    else:
        return And([ Implies(pack, dep) for dep in deps ])

def Conflict(*packs):
    return Or([ Not(pack) for pack in packs ])

a, b, c, d, e, f, g, z = Bools('a b c d e f g z')

def install_check(*problem):
    s = Solver()
    s.add(*problem)
    if s.check() == sat:
        m = s.model()
        r = []
        for x in m:
            if is_true(m[x]):
                # x is a Z3 declaration
                # x() returns the Z3 expression
                # x.name() returns a string
                r.append(x())
        print r
    else:
        print "invalid installation profile"

print "Check 1"
install_check(DependsOn(a, [b, c, z]),
              DependsOn(b, d),
              DependsOn(c, [Or(d, e), Or(f, g)]),
              Conflict(d, e),
              Conflict(d, g),
              a, z)

print "Check 2"
install_check(DependsOn(a, [b, c, z]),
              DependsOn(b, d),
              DependsOn(c, [Or(d, e), Or(f, g)]),
              Conflict(d, e),
              Conflict(d, g),
              a, z, g)
```

## Using Z3Py Locally

Z3Py is part of the Z3 distribution. It is located in the `python` subdirectory. To use it locally, you have to include the following command in your Python script.

```
from Z3 import *
```

The Z3 Python frontend directory must be in your PYTHONPATH environment variable. Z3Py will automatically search for the Z3 library (z3.dll (Windows), libz3.so (Linux), or libz3.dylib (OSX)). You may also initialize Z3Py manually using the command:

```
init("z3.dll")
```

## tutorials

- [advanced](#)
- [fixedpoints](#)
- [guide](#)
- [musmss](#)
- [strategies](#)

rise4fun © 2014 Microsoft Corporation - [terms of use](#) - [privacy & cookies](#) - [code of conduct](#)

