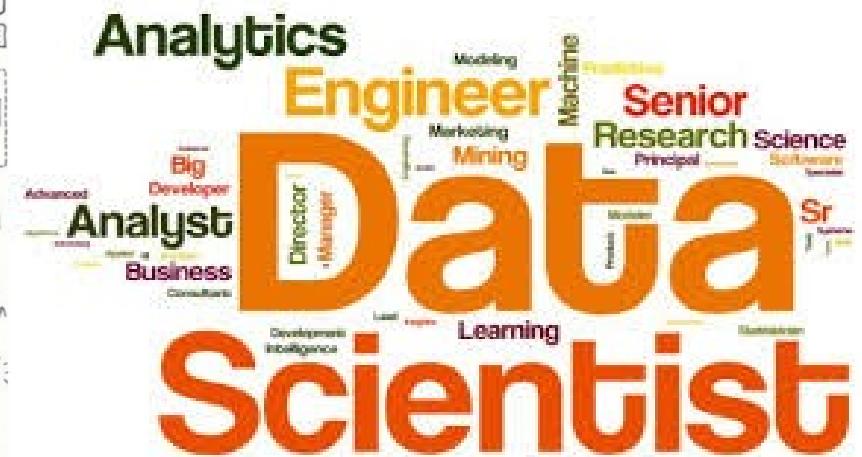
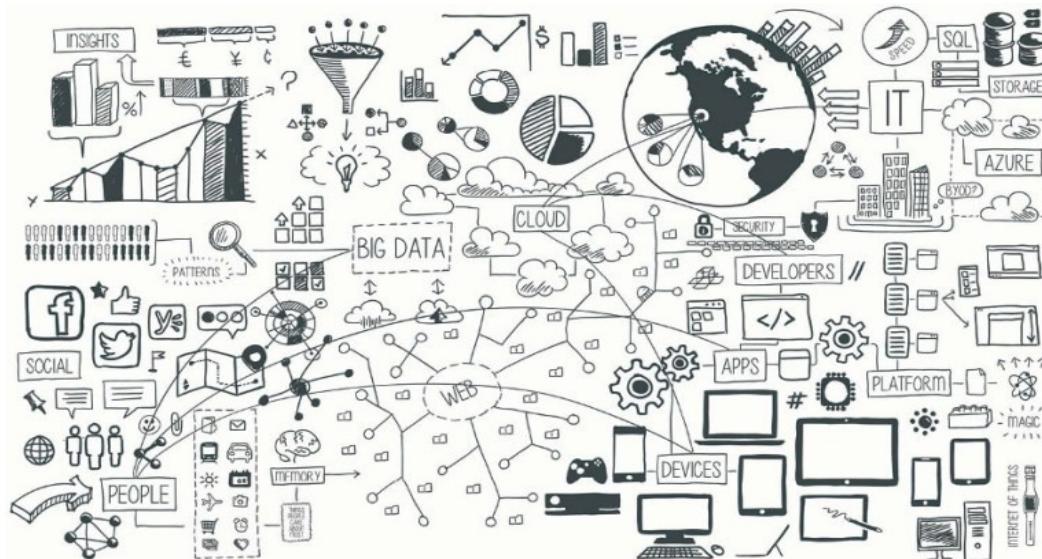


DataLab: Environment and Meteorology

Data Mining and Machine Learning in Climate. Statistical downscaling



Sixto Herrera García

Grupo de Meteorología
Univ. de Cantabria – CSIC
MACC / IFCA



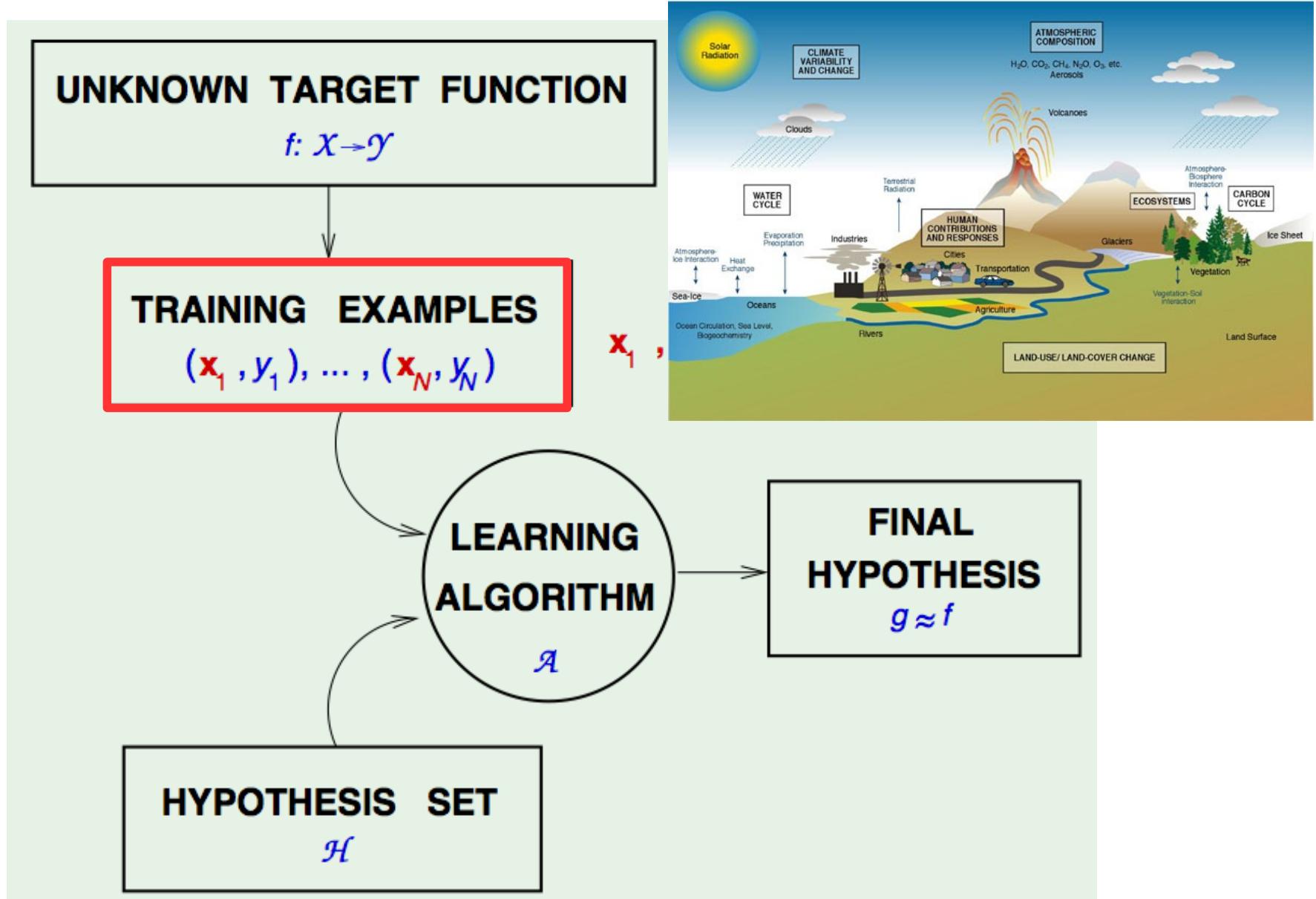
M1980 – Data Laboratory: Environment & Meteorology (16:00-18:00)

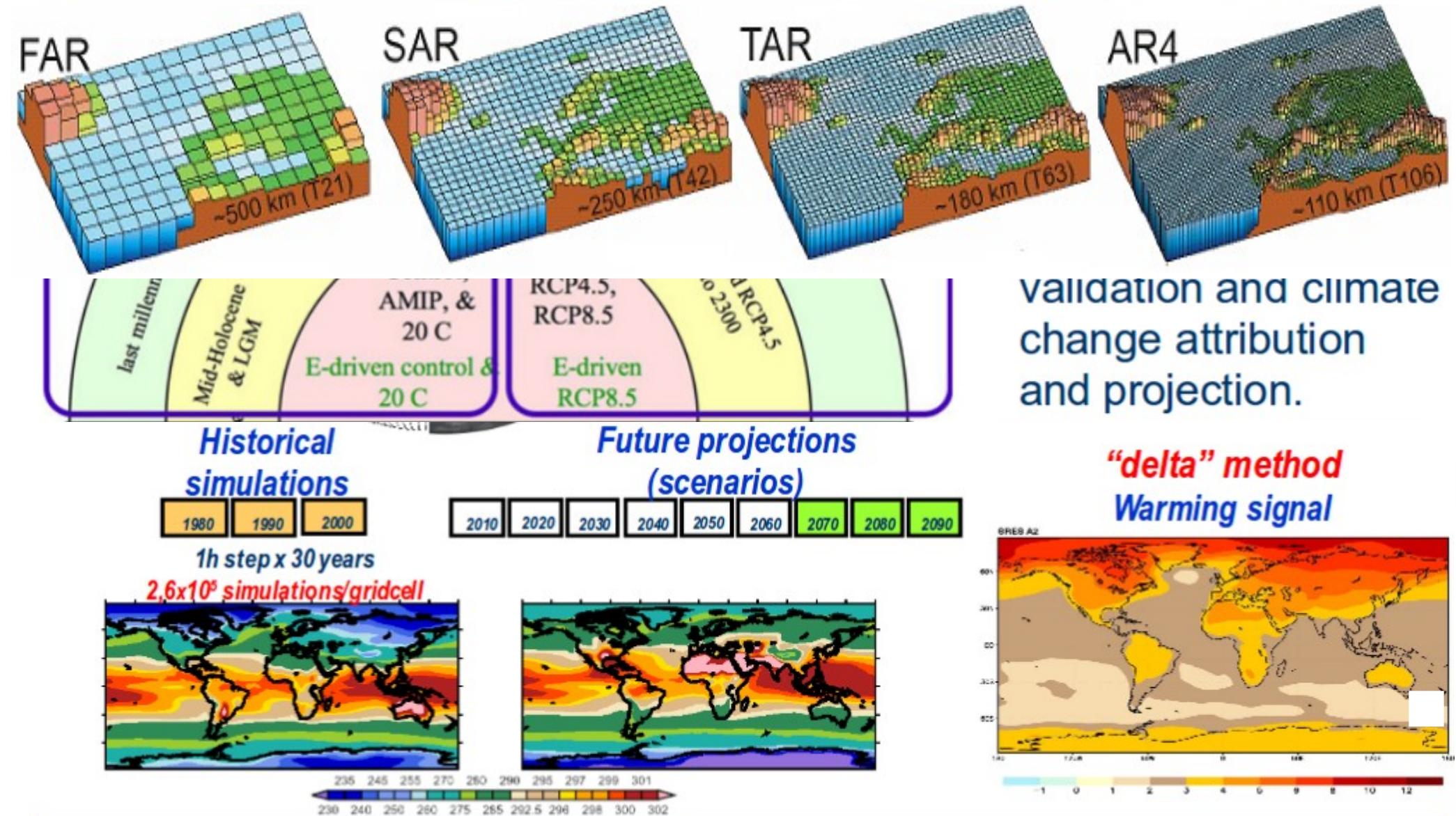
Virtual classroom: <https://meet.jit.si/M1980>

03/25	X	Introduction and Climate4R package	TL	JB
03/26	J	Climatic System & Models (DM & ML in Climate Science)	T	SH
03/27	V	Data Repositories: ESGF & MARS	TL	SH
03/30	L	Data Repositories: ESGF & MARS	TL	SH
03/31	M	Lab: Climate4R – Example 1	L	JB
04/01	X	Lab: Climate4R – Example 2	L	JB
04/02	J	Downscaling: Data Mining in Clime	T	SH
04/03	V	Lab: downscaleR	L	JB
04/06	L	Evaluation and Validation	T	SH
04/07	M	Lab: Evaluation and Validation	L	JB
04/08	X	Impacts	L	JB
04/13	L	Impacts	L	JB

SH - Sixto Herrera | **JB** - Joaquín Bedia

Atmosphere + Hydrosphere + Cryosphere + Lithosphere + Biosphere





Computational (and physical) constraints limit the resolution (~100-200 Km)

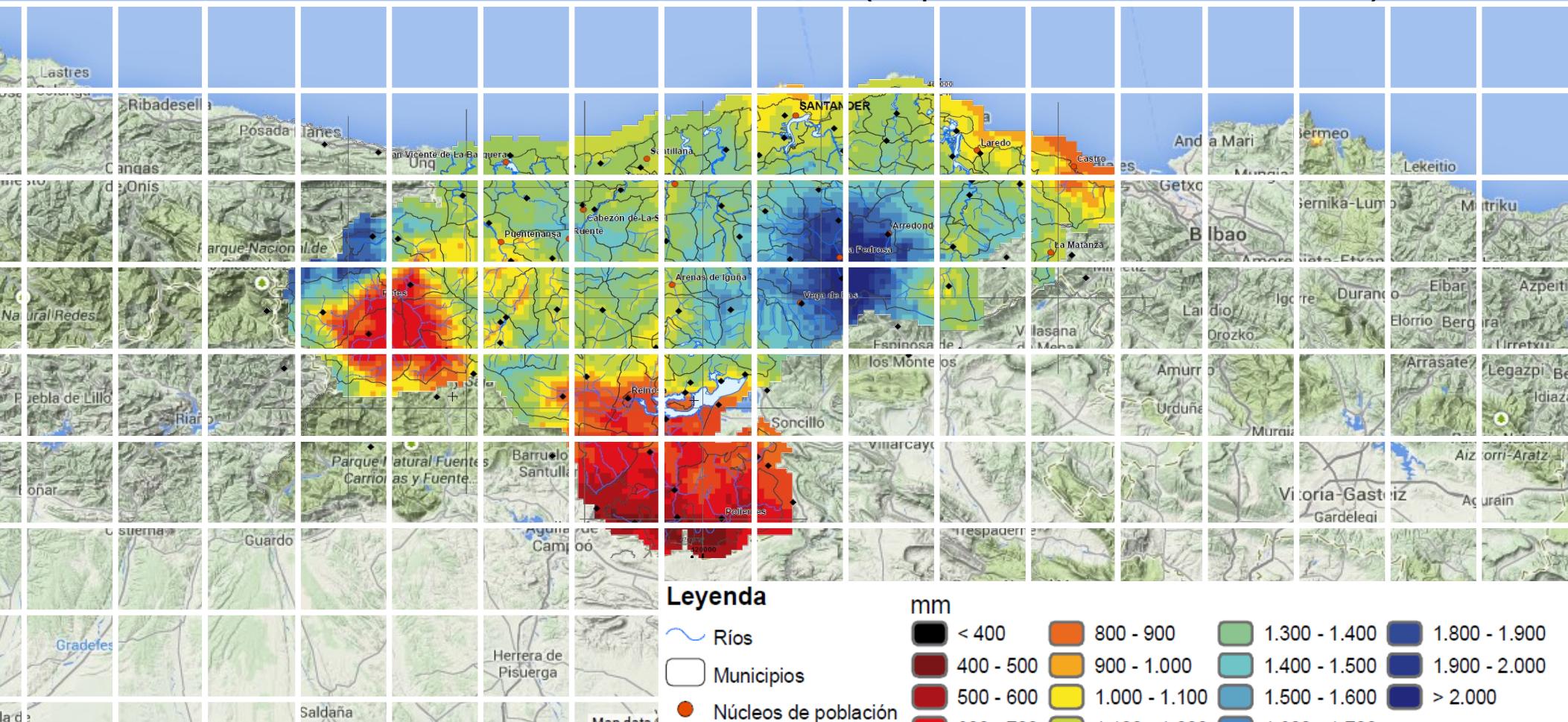
Weather Prediction (short-medium range)

Target → day

Days/weeks



15 km (~Operational Forecast ECMWF)



Elaborado por SIG Rural S.L. www.sigrural.com

Weather Prediction (short-medium range)

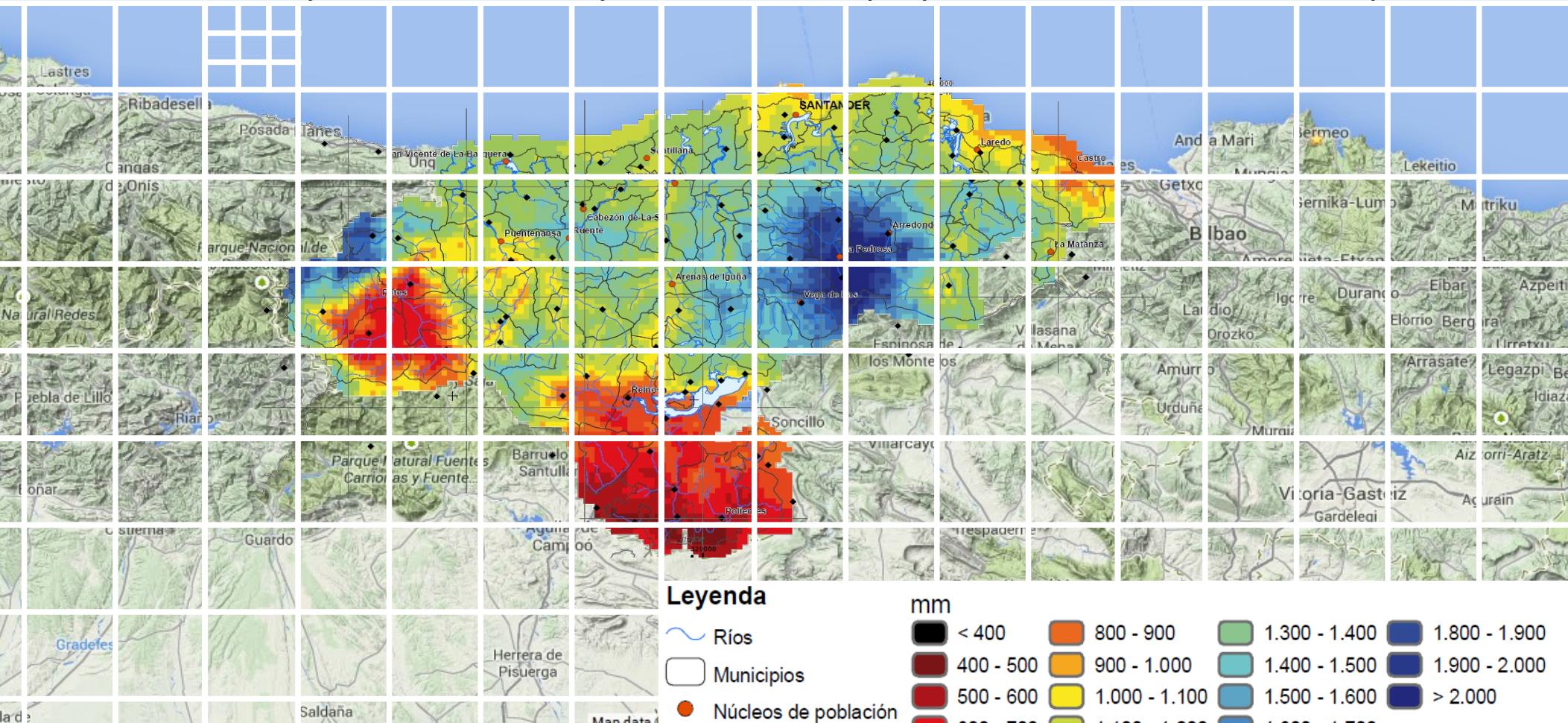
Target → day

Days/weeks



5 km (~AEMET HIRLAM)

15 km (~Operational Forecast ECMWF)



Elaborado por SIG Rural S.L. www.sigrural.com

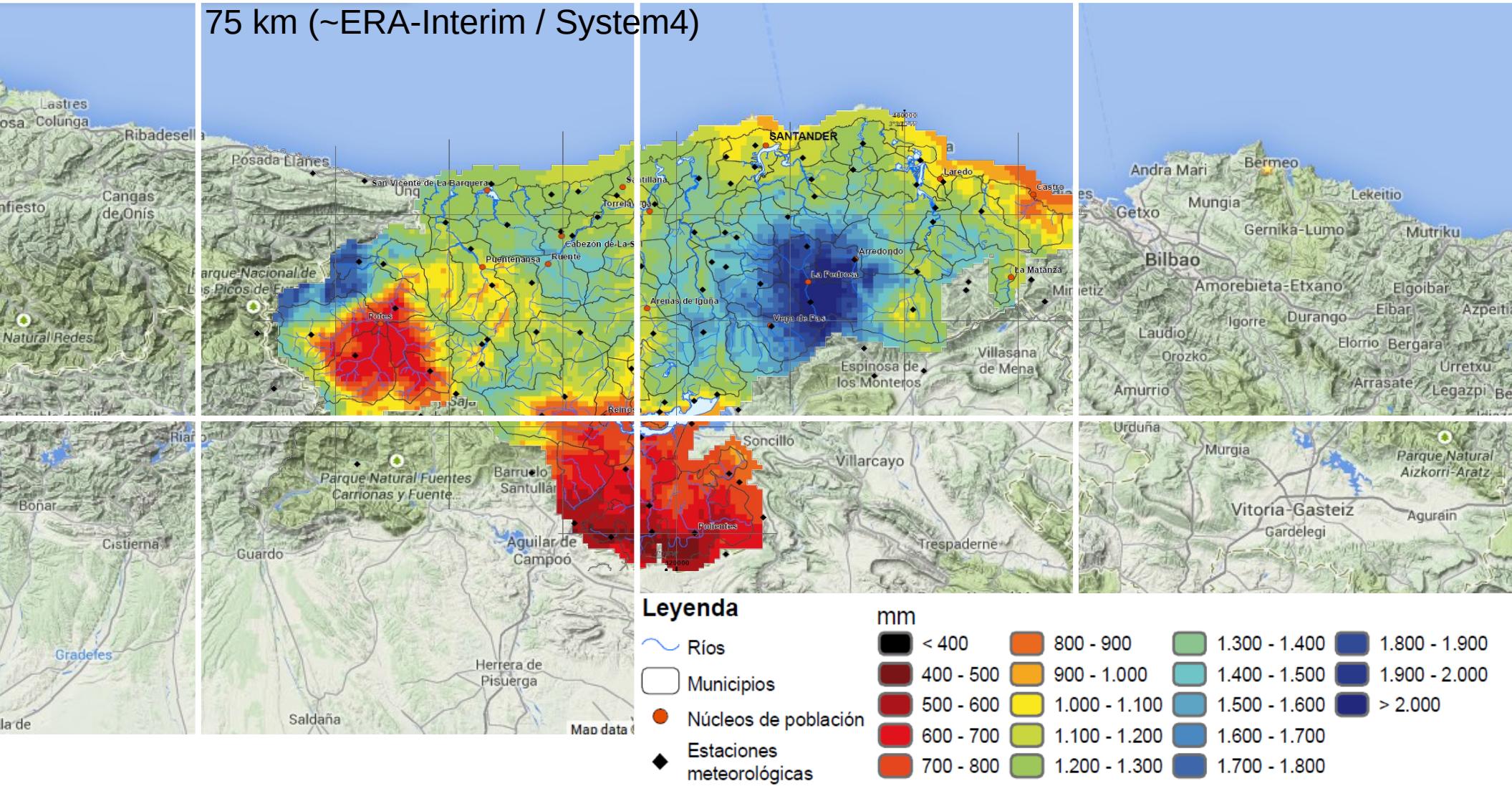
Seasonal Forecast (Prediction)

Month/Season

DEF MAM JJA SON

Target → season

75 km (~ERA-Interim / System4)

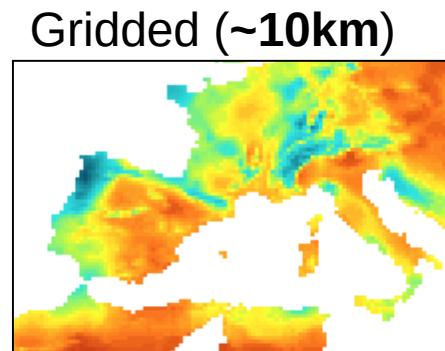
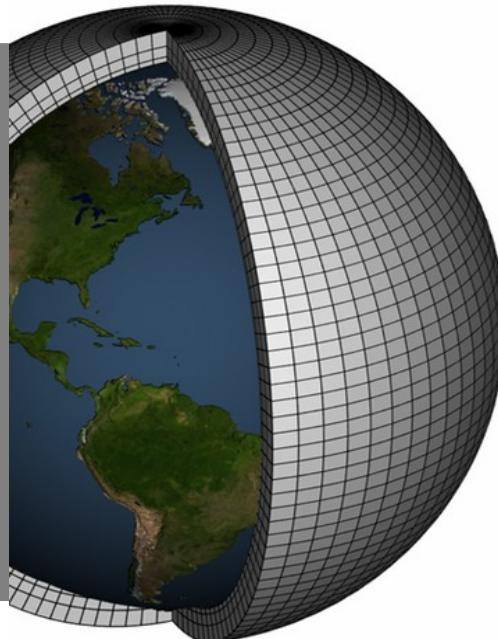


Elaborado por SIG Rural S.L. www.sigrural.com

“Real” World



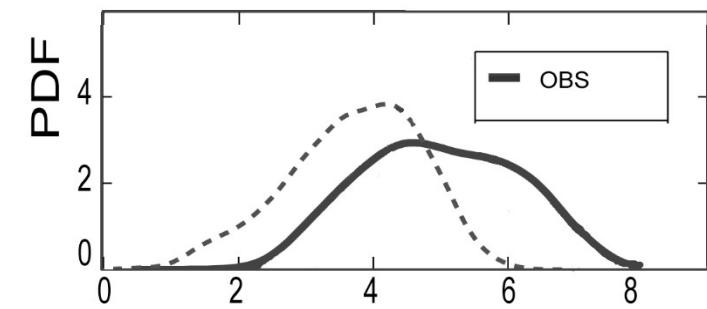
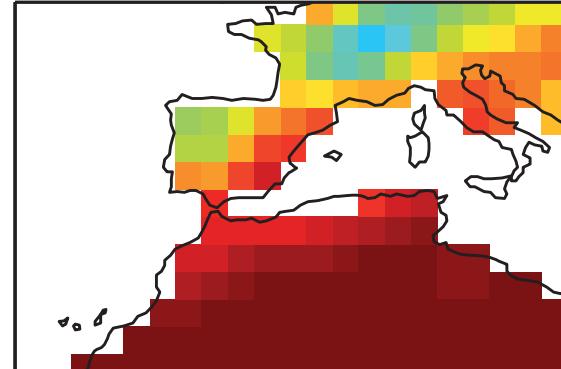
Model’s World



Gridded (~10km)



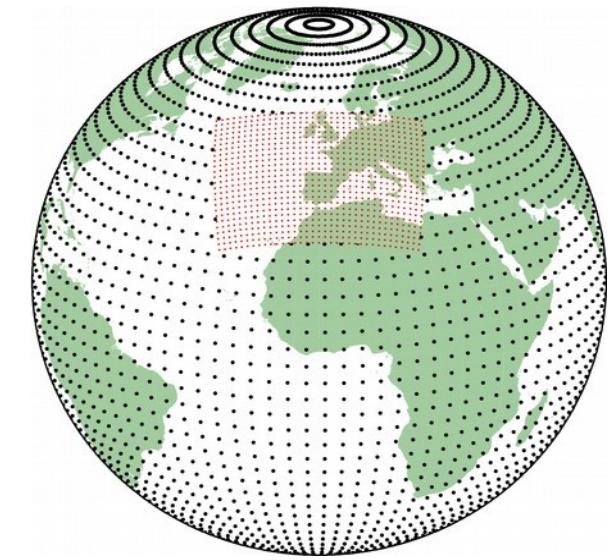
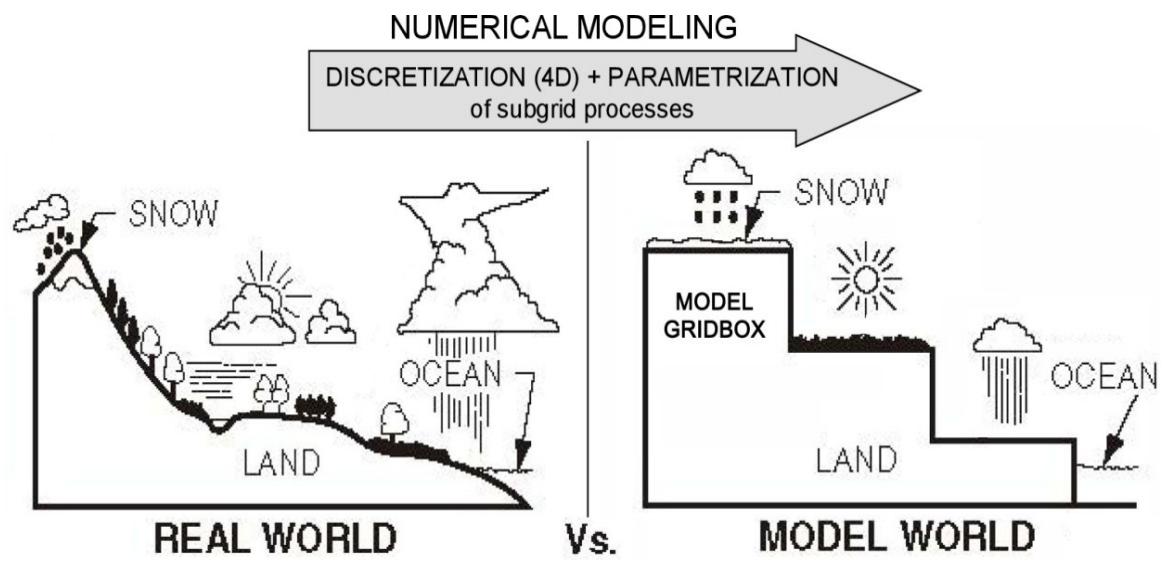
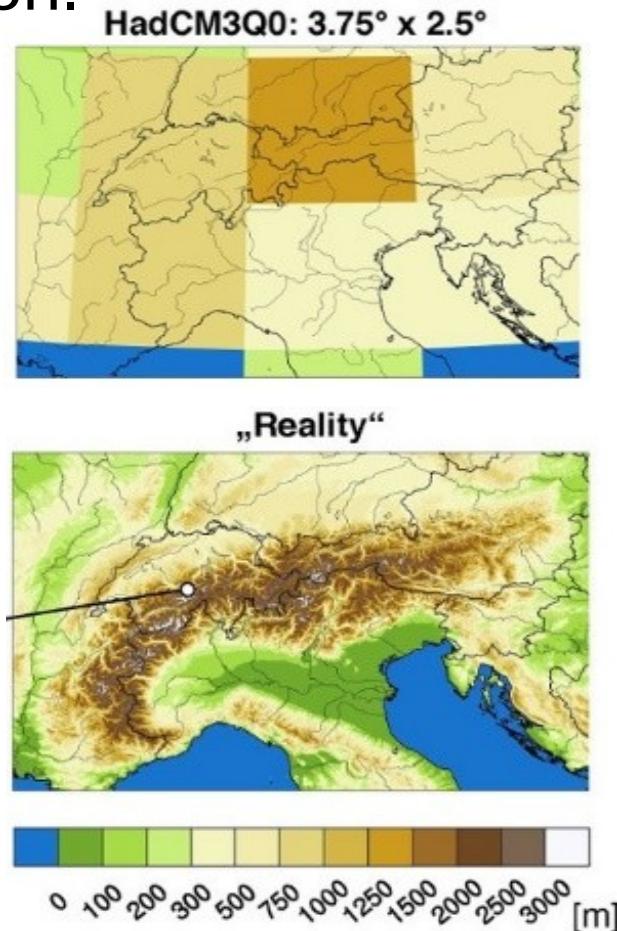
Locations



Climate Models have systematic biases w.r.t. observations:

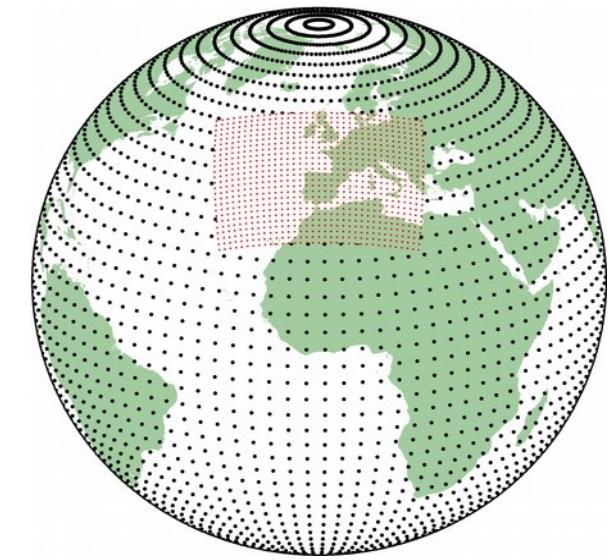
1. Systematic Bias
2. Different resolutions

Downscaling methods try to bridge the gap between the coarse resolution of the Global Climate Models (GCMs) and the local climate characteristics of a particular region.

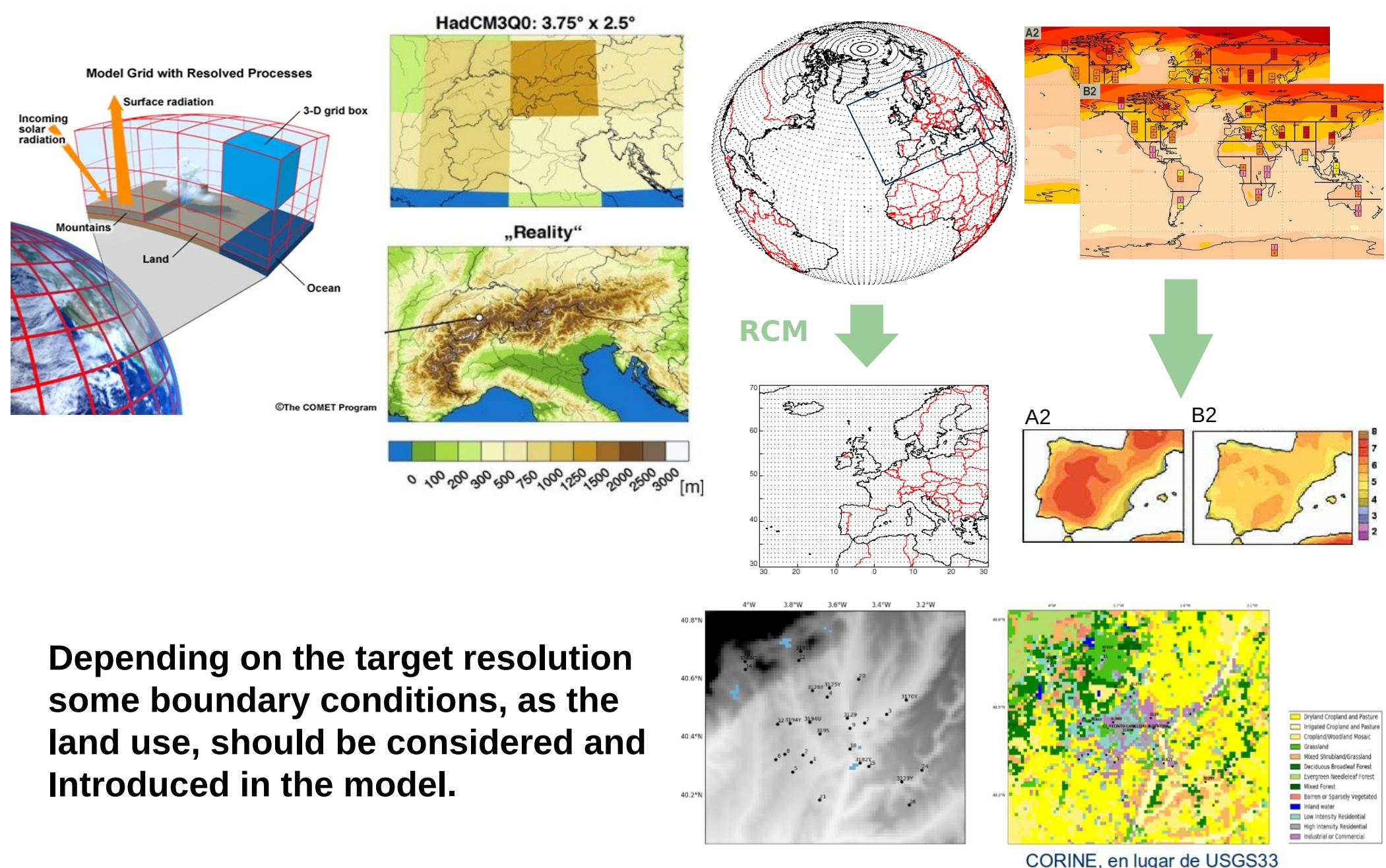


Downscaling methods try to bridge the gap between the coarse resolution of the Global Climate Models (GCMs) and the local climate characteristics of a particular region.

Dynamical Downscaling solves the climate equation system in a geographical domain covering the target region, letting to increase the final resolution of the simulation.



$$\begin{aligned}\frac{d\vec{v}}{dt} &= -\frac{1}{\rho} \vec{\nabla} p - \vec{\nabla} \phi + \vec{F} - 2\vec{\Omega} \times \vec{v} \\ \frac{\partial \rho}{\partial t} &= -\vec{\nabla} \cdot (\rho \vec{v}) \\ p &= \rho R T \\ Q &= C_p \frac{dT}{dt} - \frac{1}{\rho} \frac{dp}{dt} \\ \frac{\partial \rho q}{\partial t} &= -\vec{\nabla} \cdot (\rho q \vec{v}) + \rho(E - C)\end{aligned}$$





- 1) Incoming Solar Radiation
- 2) Scattering by Aerosols and Molecules
- 3) Absorption by the Atmosphere
- 4) Reflection/Absorption by Clouds
- 5) Emission of Longwave Radiation from Earth's Surface
- 6) Condensation
- 7) Turbulence
- 8) Reflection/Absorption at Earth's Surface
- 9) Snow
- 10) Soil Water/Snow Melt
- 11) Snow/Ice/Water Cover

- 12) Topography
- 13) Evaporation
- 14) Vegetation
- 15) Soil Properties
- 16) Rain (Cooling)
- 17) Surface Roughness
- 18) Sensible Heat Flux
- 19) Deep Convection (Warming)
- 20) Emission of Longwave Radiation from Clouds

©The COMET Program

A parameterization is a **statistical** representation of the **net effect** of processes occurring on **spatial scales smaller than the grid spacing** of a dynamical model (GCM, RCM, CRM, LES, ...) **over mean variables** at each grid cell.

Parameterizations are based on the **physics** of the processes, plus **simplifying (closure) assumptions** to relate unknown variables to prognostic (mean) model variables.

- Theory (e.g. known physical constants)
- Field campaigns
- Higher resolution models (CRM, LES)

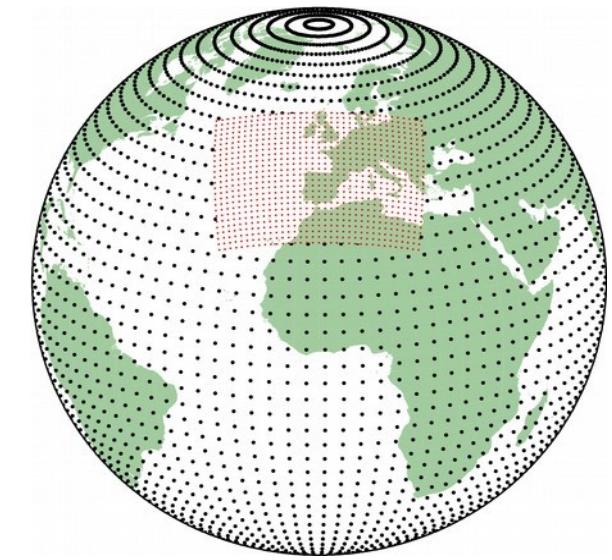
Parameters are obtained from:

Introduction

Downscaling

Downscaling methods try to bridge the gap between the coarse resolution of the Global Climate Models (GCMs) and the local climate characteristics of a particular region.

Dynamical Downscaling solves the climate equation system in a geographical domain covering the target region, letting to increase the final resolution of the simulation.



- 😊 Plenty of variables, including 3D
- 😊 Subdaily data available
- 😊 Variables are physically consistent
- 😐 Variables represent areal averages
- 😢 Computationally expensive
- 😢 Biases are commonplace
- 😢 Parameterizations: Stationary hypothesis

Generate a coordinated ensemble of high-resolution, historical/future regional climate projections for land-regions of the globe sampling; multiple GCM/RCP/RCM/ESDs methods. 1st phase based on CMIP5 historical-projection runs and/or ERA-int boundary data

Make data accessible & useable in common format/file structure

Foster coordination between downscaling efforts & encourage local participation, **in generating, analysing & communicating potential regional climate change and associated uncertainties & risks**

Initial emphasis on African climate & IAV: START/WCRP sponsored 3 analysis/IAV workshops for an Africa-CORDEX team in 2011-12

Similar activities now starting for South Asia, East Asia and South/Central America



Ejemplos:

- Dickinson et al. **1989**: 20 días (60km) x 3
 Giorgi et al. **1990**: 1 mes (60km) x 6
 Jones et al. **1995**: 10 años (50km) x 2
 Kidson & Thompson **1998**: 5 años (50km)
 Christensen et al. **1998**: 10 años (19km)
 Giorgi et al. **2004**: 30 años (50km) x 4
- PRUDENCE** several decades (50km)
ENSEMBLES centuries (25km)
EURO-CORDEX centuries (11km)

One Model/One Domain

- Common approach in the application of a RCM

Multi-Model/One Domain

- Approach of the Model Intercomparison Projects (MIPs)
 - EU: Regionalization, RACCS, MERCURE, PRUDENCE, ENSEMBLES
 - USA: PIRCS, NARCCAP
 - Etc: ARCMIP, SGMIP, ...

One Model/Several Domain

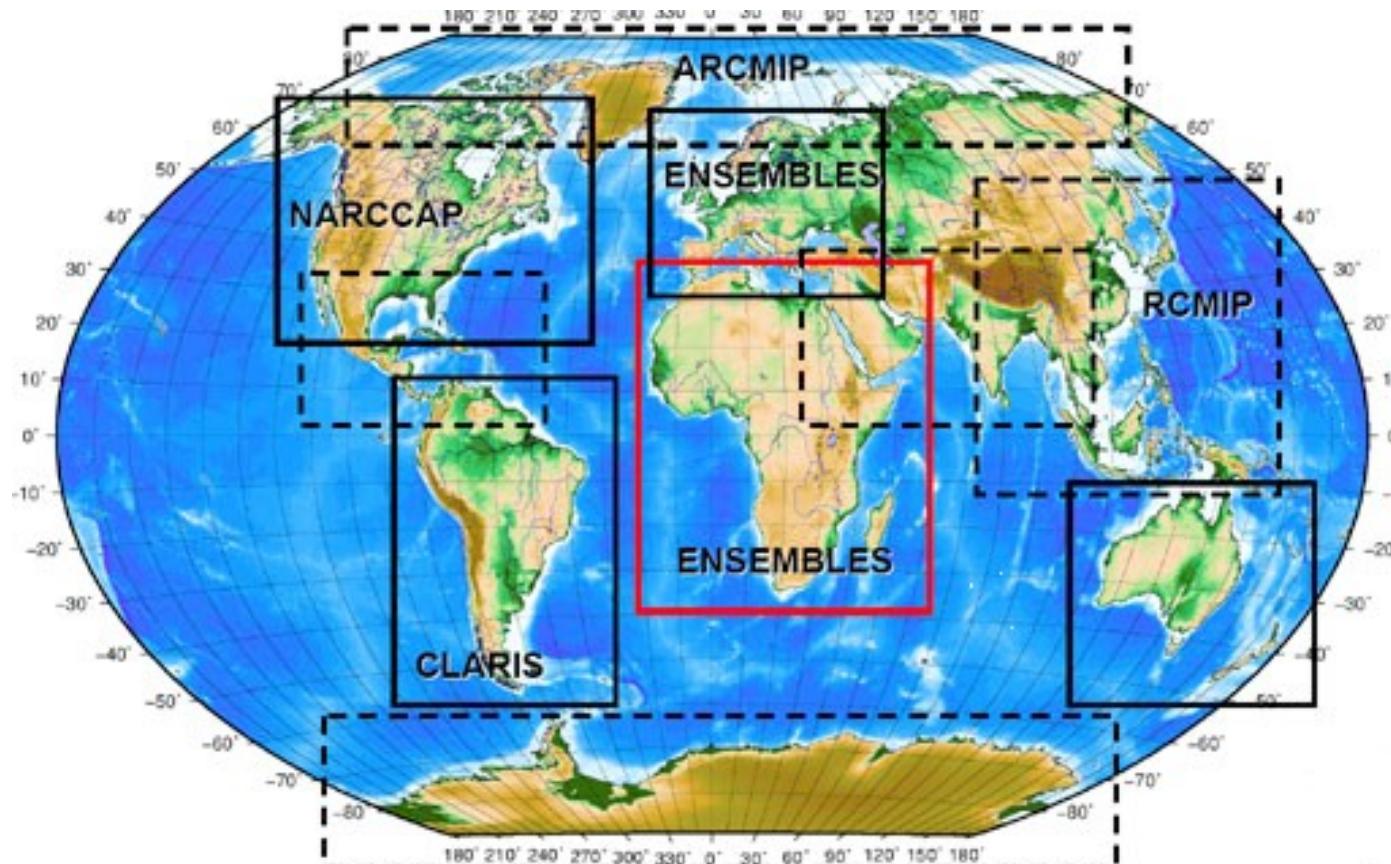
- Used to find problems of the model.

Multi-Model/Several Domain

- RCMs ran out of their "*natural*" domain
 - GEWEX **transferability** experiment
 - CORDEX (COordinated Regional Downscaling EXperiment)

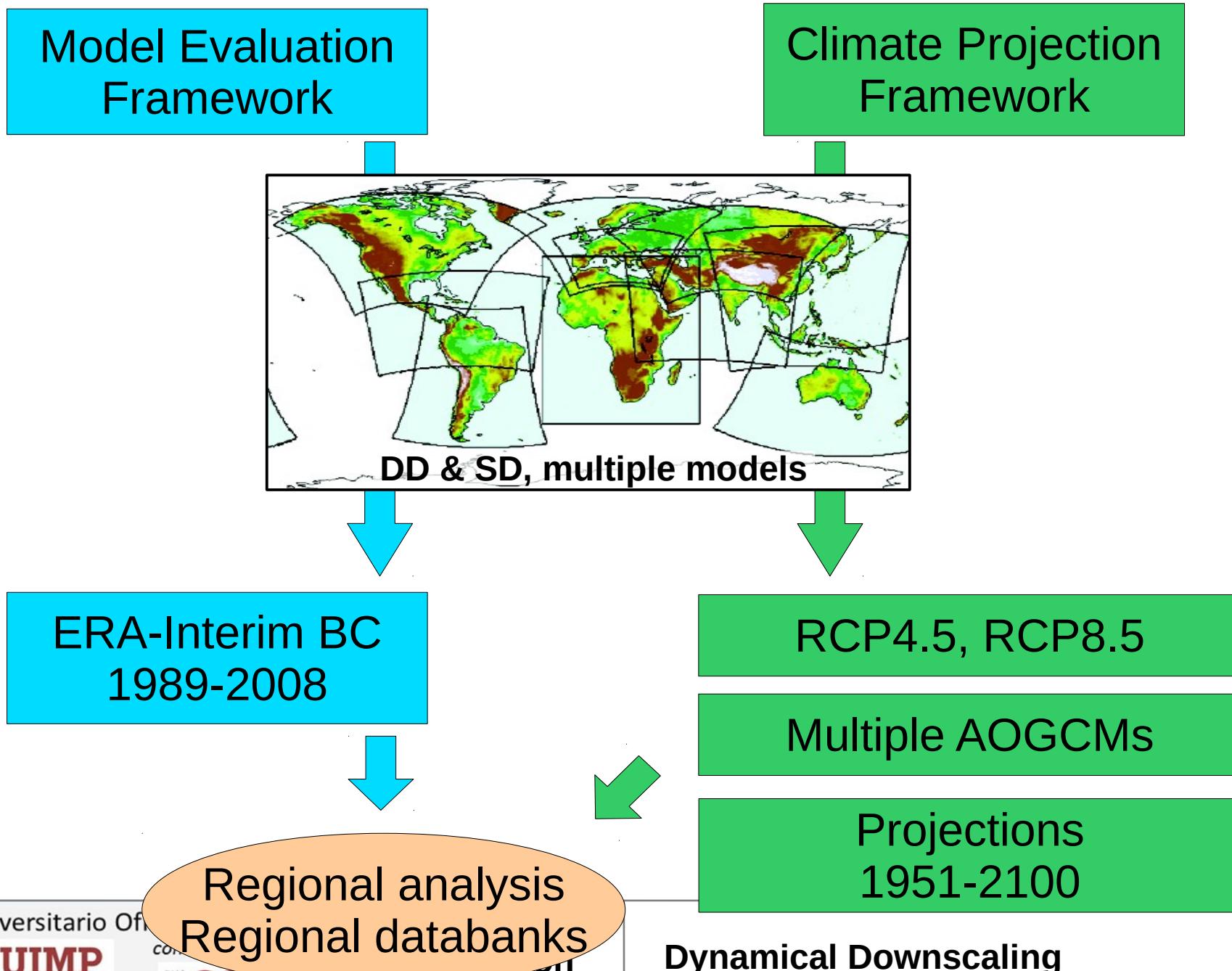
CORDEX Phase I experiment design

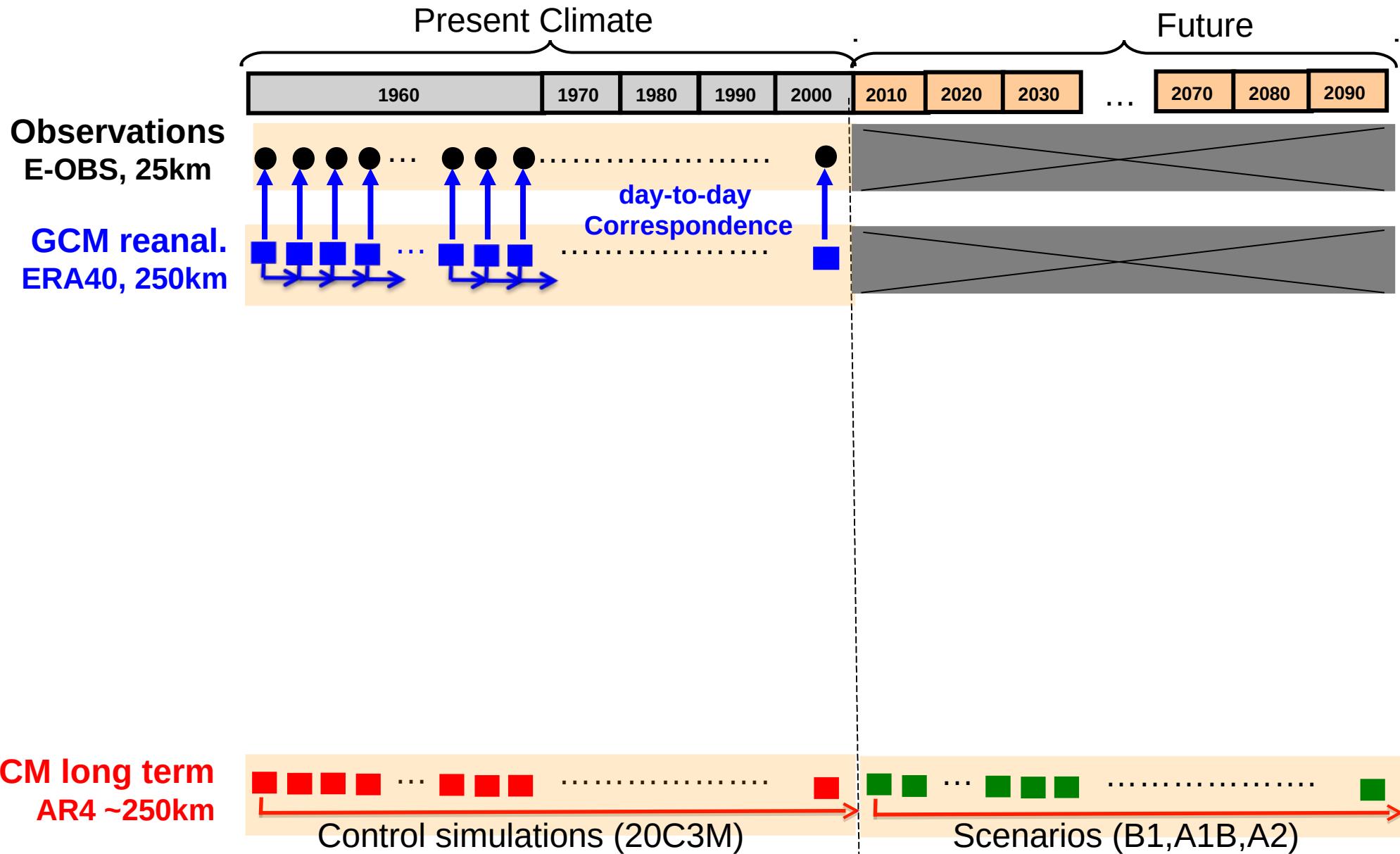
A WCRP-sponsored initiative for regional climate change projection with dynamical downscaling methods, aimed at providing regional climate change information (with initial focus in Africa) for the IPCC-AR5.

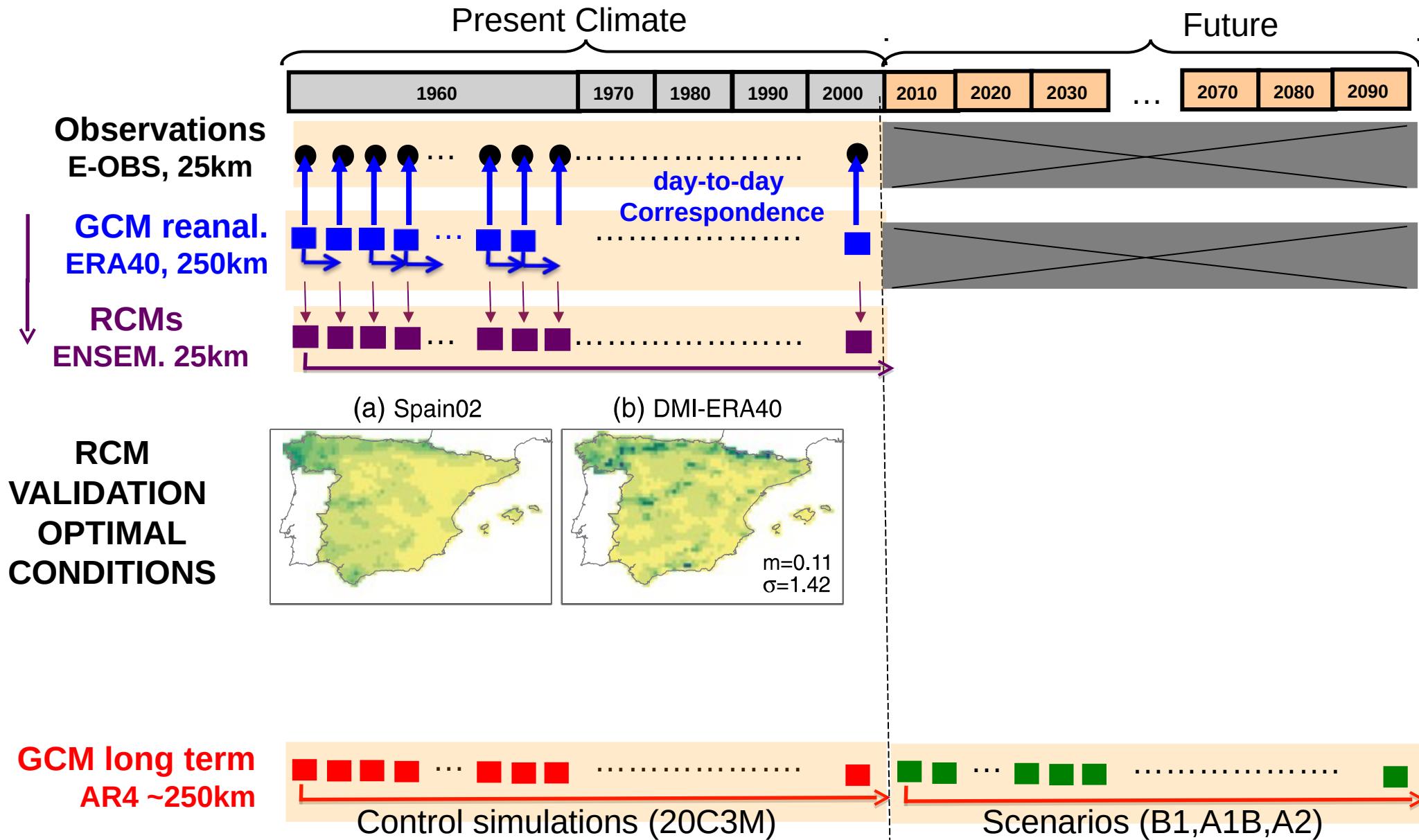


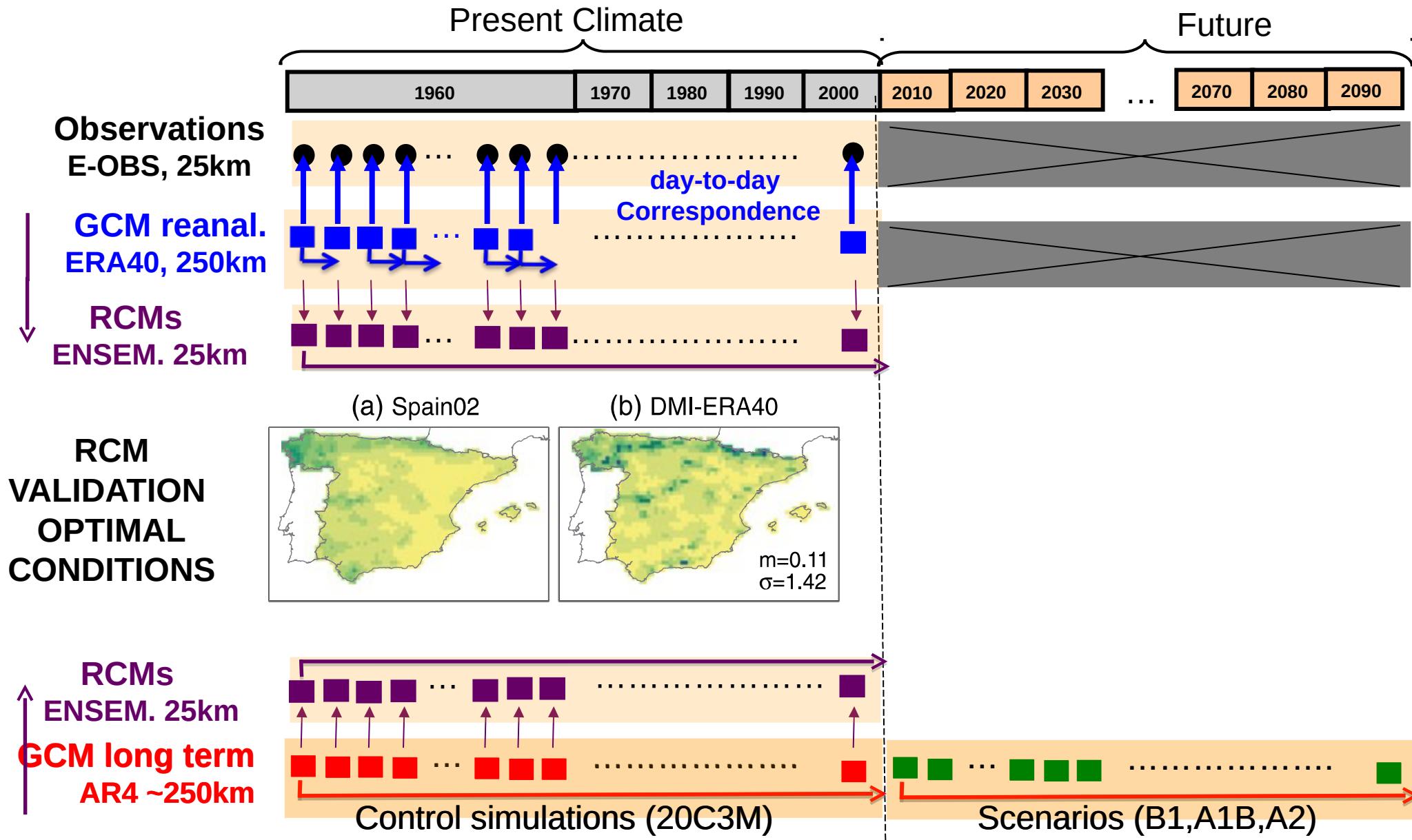
http://wcrp.ipsl.jussieu.fr/SF_RCD_CORDEX.html

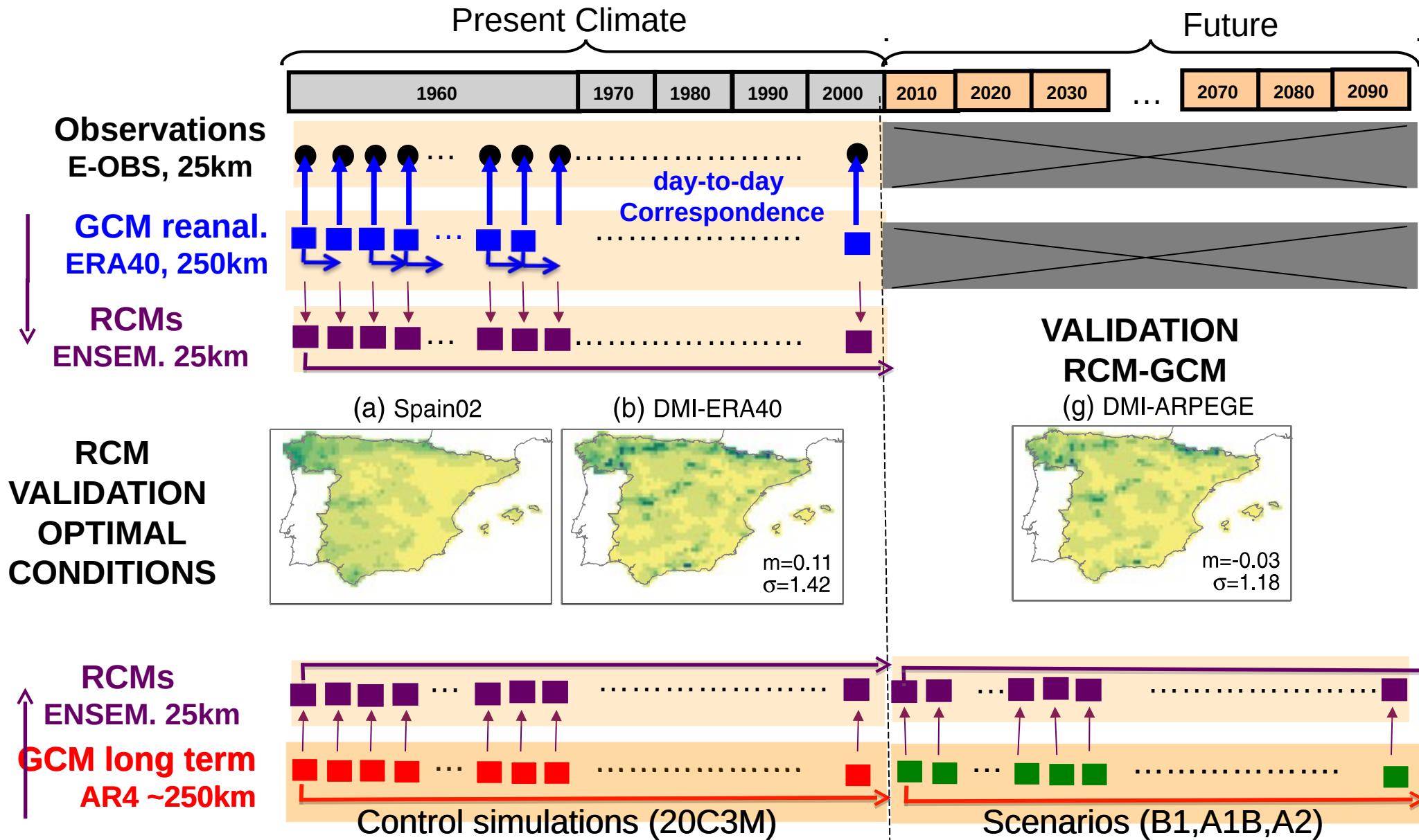
CORDEX Phase I experiment design

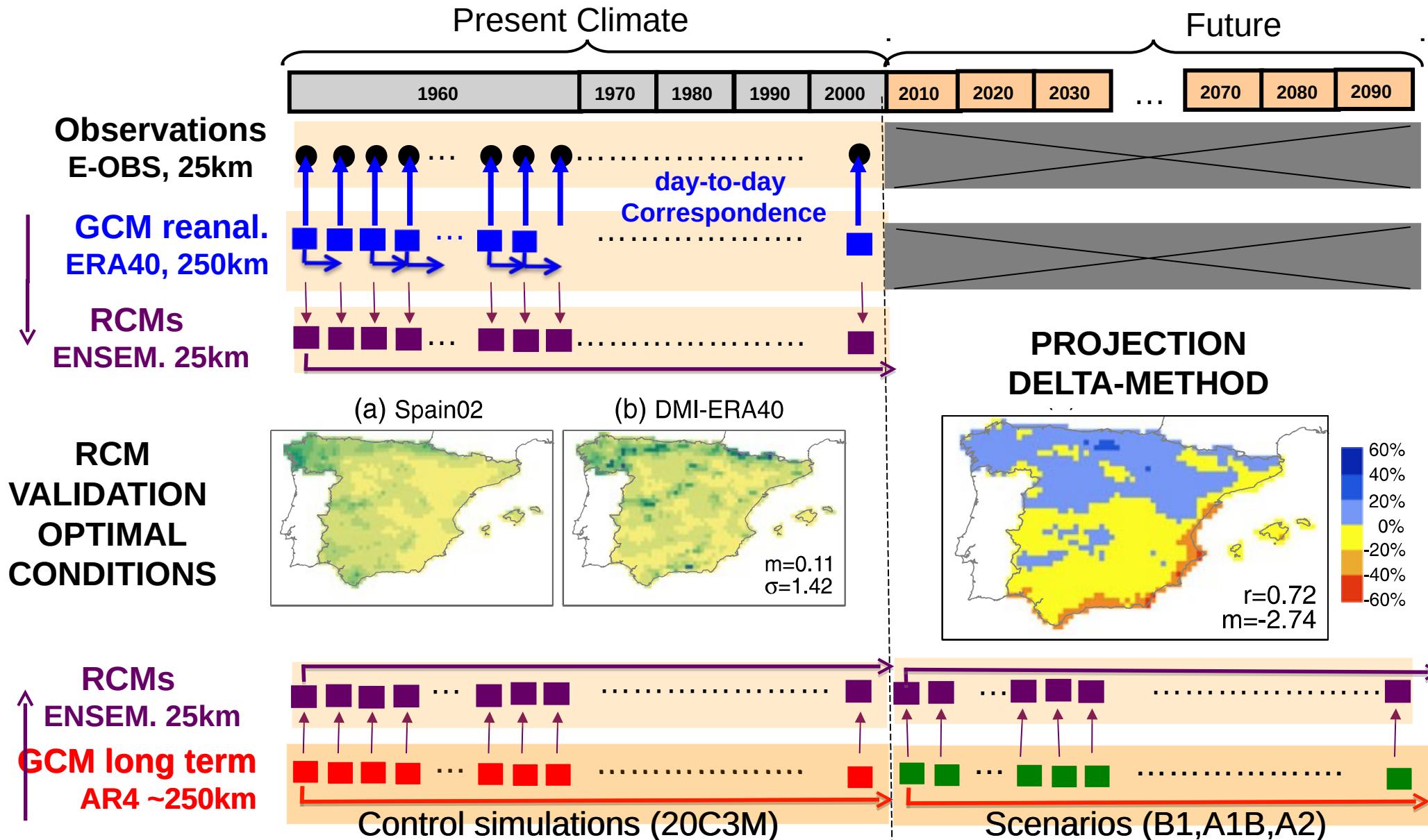








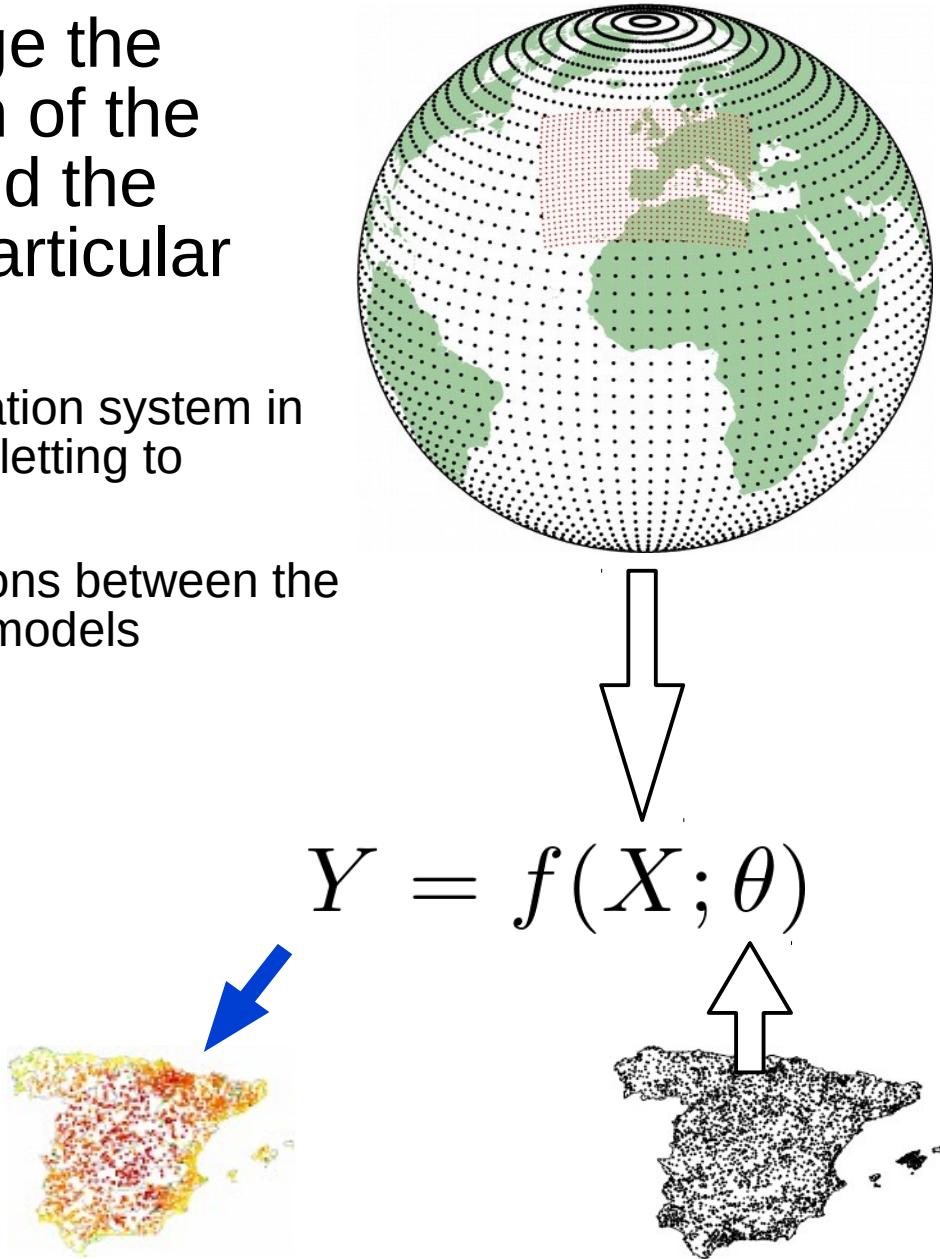


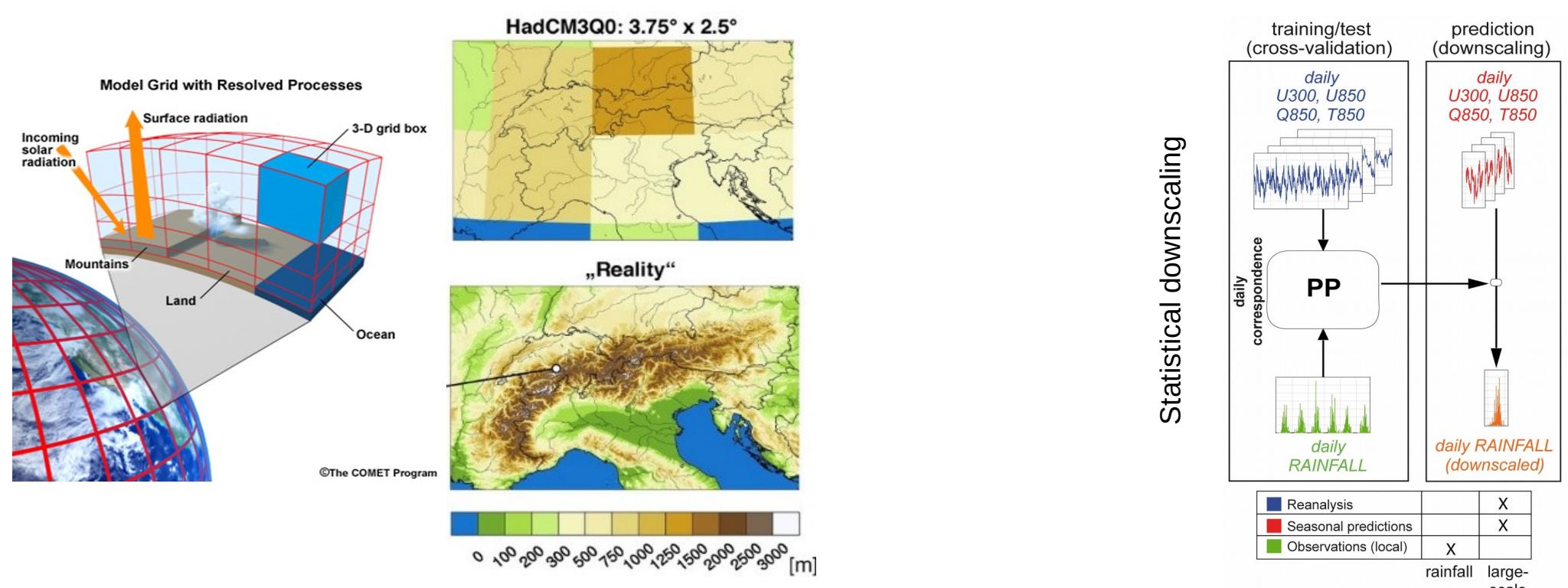


Downscaling methods try to bridge the gap between the coarse resolution of the Global Climate Models (GCMs) and the local climate characteristics of a particular region.

Dynamical Downscaling solves the climate equation system in a geographical domain covering the target region, letting to increase the final resolution of the simulation.

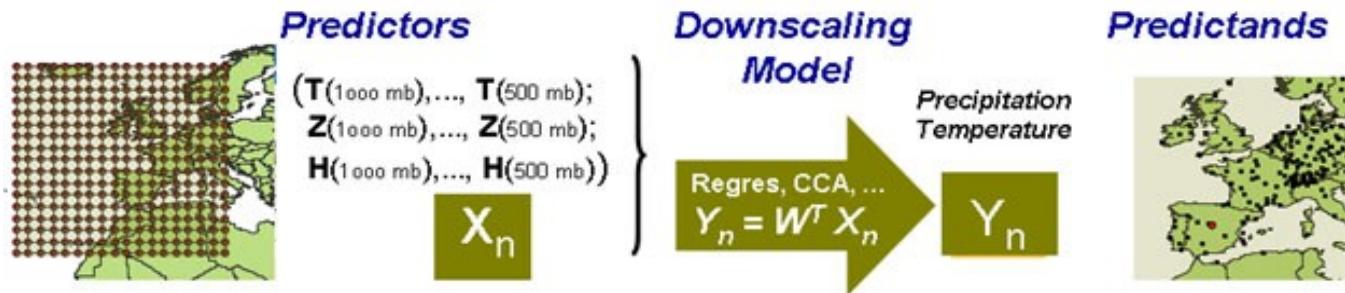
Statistical Downscaling looks for empirical relations between the local variables (**predictand**) and the given by the models (**predictors**).





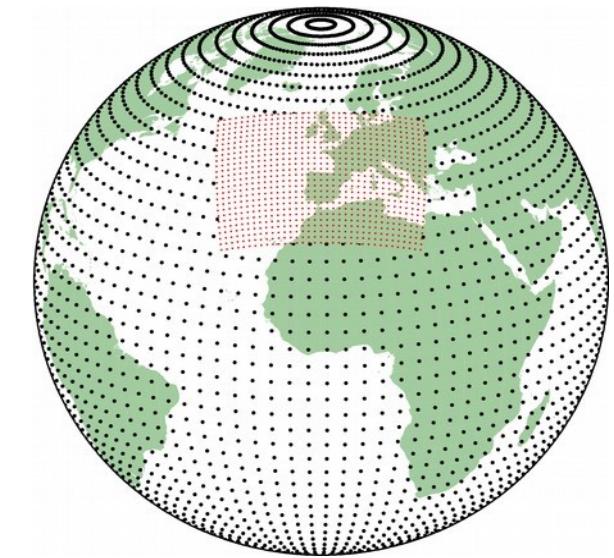
Statistical Downscaling

Statistical methods linking the local observed climate (**predictand Y**) with the global simulations given by the GCMs (**predictors X**), through some **function f** and/or **parameters θ** : $Y = f(X; \theta)$



Downscaling methods try to bridge the gap between the coarse resolution of the Global Climate Models (GCMs) and the local climate characteristics of a particular region.

Statistical Downscaling looks for empirical relations between the local variables (**predictand**) and the given by the models (**predictors**).



- :(Variables available as long as there are obs.
- :(Different variables probably do not keep physical or even spatial consistency
- :(Stationary hypothesis and extrapolation capabilities.
- : Variables keep the representativity of obs.
- : Computationally cheap
- : Biases are low
- : Non-meteorological variables (e.g. impact indices) could be directly produced.



Cordex ESD

Experiment protocol – Empirical statistical downscaling

- ESD Overview
- ESD Background
- ESD Experiment1 protocols
- ESD Reference Document
- Register for CORDEX ESD Experiment 1

<http://www.value-cost.eu/>

VALUE: COST Action ES1102 (2012-2015)

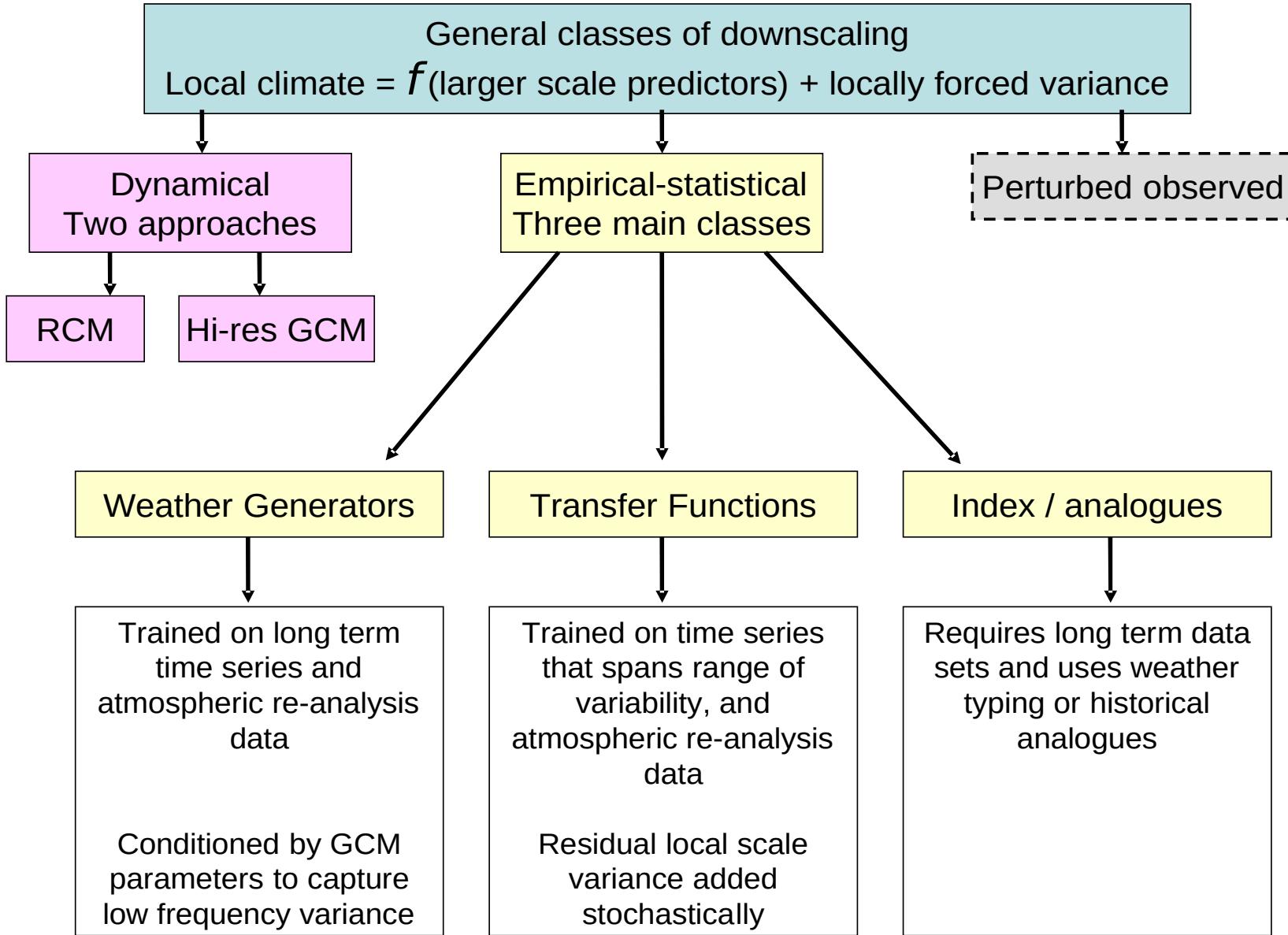
CONTRIBUTE TO THE VALIDATION



Login



Validating and Integrating Downscaling Methods for Climate Change Research

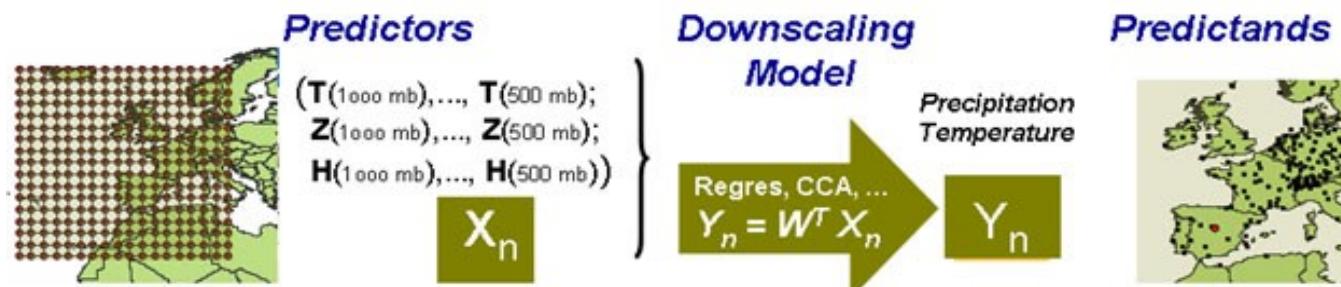


Source:
Bruce Hewitson
(CSAG)

Tech.		Generative		non-Generative	
Appro.		Deterministic	Stochastic	Deterministic	Stochastic
PP	Eventwise	Regression, Neural Nets.	GLMs	Analogs, weather types	Analog resampling
	Distribution	Regression on PDF parameters			
MOS	Eventwise	Regression, Neural Nets.	GLMs	Analogs	Analog resampling
	Distribution	Bias correction, parametric q-q map	Nonhomogeneous HMM	q-q map	

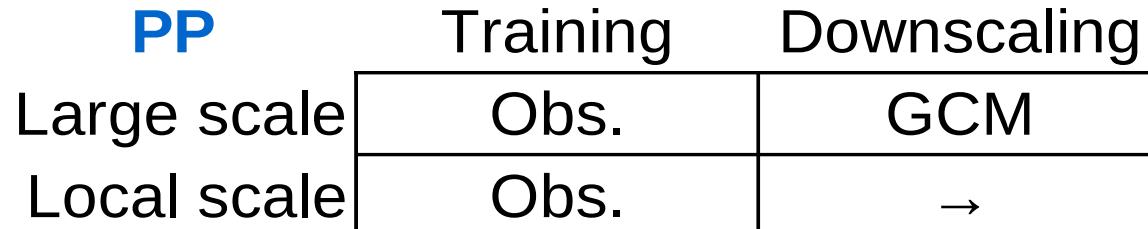
Statistical Downscaling

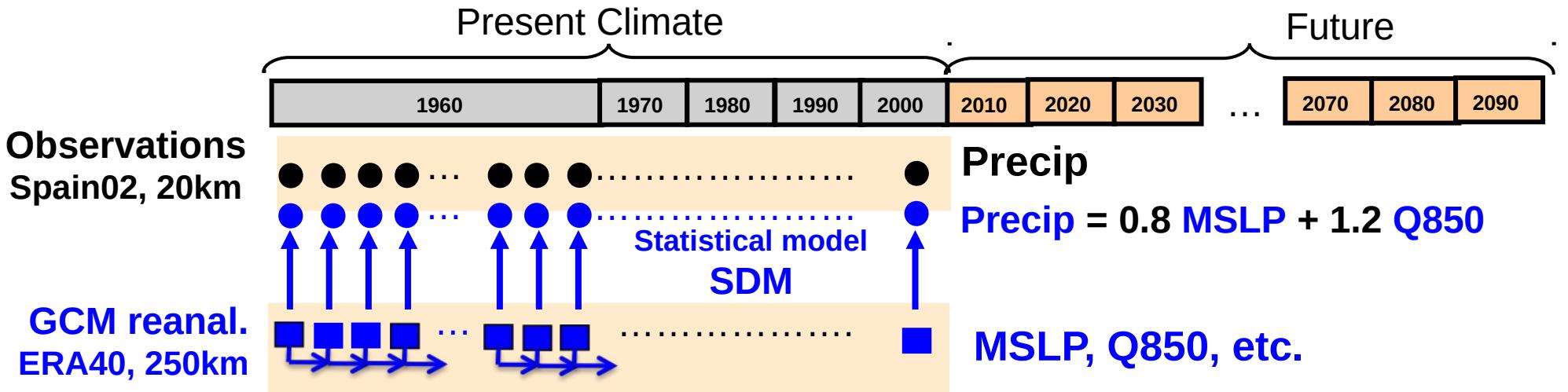
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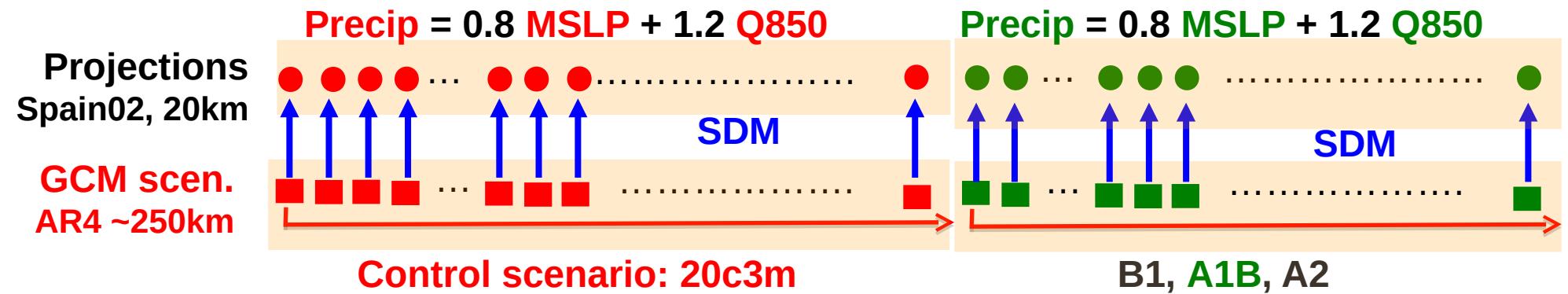
Tech.	Generative		non-Generative	
	Deterministic	Stochastic	Deterministic	Stochastic
Appro.				
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	Distribution	Regression on PDF parameters		
MOS	Eventwise	Regression, Neural Nets.	GLMs	Analogs
	Distribution	Bias correction, parametric q-q map	Nonhomogeneous HMM	q-q map

Perfect Prognosis (PP): Calibrated in the training phase using observational data for both the predictands and predictors (**reanalysis**). Since different GCMs are used in the training and downscaling phases, large-scale circulation variables well-resolved by the models are typically chosen as predictors in this approach. Variables directly influenced by model parameterizations and orography are not suitable predictors in this approach.





- Assumption 1: Reanalysis choice
- Assumption 2: Choosing consistent predictors: ■ ■
- Assumption 3: Stationarity/robustness: SDM ■ SDM ■



Present Climate



Journal of Hydrology 224 (1999) 187-201



A comparison of downscaled and raw GCM output: implications for climate change scenarios in the San Juan River basin, Colorado

R.L. Wilby^{a,*}, L.E. Hay^a, G.H. Leavesley^b

^aNational Center for Atmospheric Research, Boulder, CO 80307, USA
^bDivision of Geography, University of Derby, Meadow Lane, Derby DE2 3RG, UK
Water Resources Division, US Geological Survey, Denver Federal Center, Denver, CO 80225, USA
Received 2 December 1998; revised in revised form 23 April 1999; accepted 1 September 1999

Predictor variable	Abbreviation
<i>Surface variables</i>	
*Mean sea level pressure	mslp
Zonal velocity component	Us
Meridional velocity component	Vs
Strength of the resultant flow (hPa)	Fs
Vorticity (hPa)	Zs
Divergence (hPa)	Ds
2 m temperatures (°C)	T2m
Relative humidities (%)	RH
*Specific humidity (gm/kg)	SH
<i>Upper-atmosphere variables (500 hPa)</i>	
*500 hPa geopotential heights (m)	H
Zonal velocity component	Uu
Meridional velocity component	Vu
Strength of the resultant flow (hPa)	Fu
Vorticity (hPa)	Zu
Divergence (hPa)	Du

Introduction

PP: Typical predictors

Future



Available online at www.sciencedirect.com



Environment Modelling & Software 23 (2008) 813–831

Environmental
Modelling & Software

www.elsevier.com/locate/emosoft

Automated regression-based statistical downscaling tool

Masoud Hessami ^{a,*}, Philippe Gachon ^{b,c}, Taha B.M.J. Ouarda ^d, André St-Hilaire ^d

No.	Predictors	No.	Predictors
1	Mean sea level pressure	14	500 hPa divergence
2	Surface airflow strength	15	850 hPa airflow strength
3	Surface zonal velocity	16	850 hPa zonal velocity
4	Surface meridional velocity	17	850 hPa meridional velocity
5	Surface vorticity	18	850 hPa vorticity
6	Surface wind direction	19	850 hPa geopotential height
7	Surface divergence	20	850 hPa wind direction
8	500 hPa airflow strength	21	850 hPa divergence
9	500 hPa zonal velocity	22	Relative humidity at 500 hPa
10	500 hPa meridional velocity	23	Relative humidity at 850 hPa
11	500 hPa vorticity	24	Near surface relative humidity
12	500 hPa geopotential height	25	Surface specific humidity
13	500 hPa wind direction	26	Mean temperature at 2 m

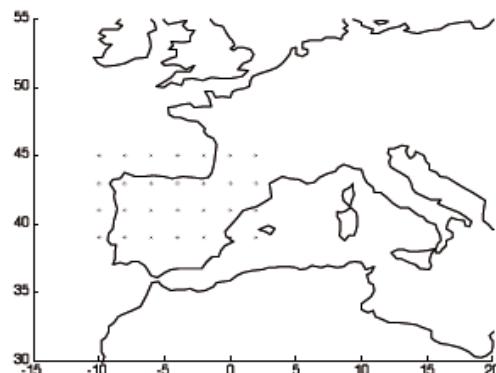


Figura 3. Área de estudio y rejilla utilizada para definir los predictores de los métodos de downscaling estadístico.

Variable	Nivel	Hora
Geopotencial	500	0 UTC
Geopotencial	1000	0 UTC
Temperatura	500	0 UTC
Temperatura	850	0 UTC
Humedad Relativa	850	0 UTC

140 parameters (5 variables, 28 gridboxes), n=16434

Redundancy (correlation):

Principal Components (*domain selection*)

Nearest grid-boxes

Both (e.g. 15 CPs + values in 1 gridbox)

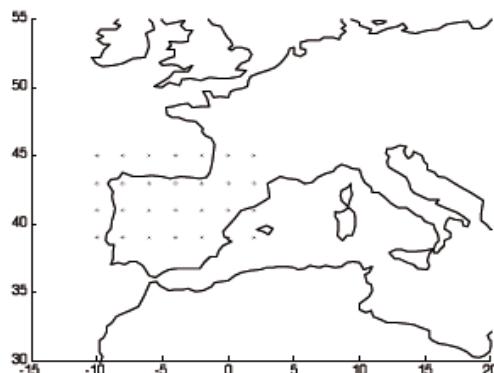


Figura 3. Área de estudio y rejilla utilizada para definir los predictores de los métodos de downscaling estadístico.

- :(sad face) PP approach strongly depends on the region and variable
- :(sad face) It is difficult to apply PP methods at continental scale
- :(sad face) Predictors' screening is a very time consuming task.

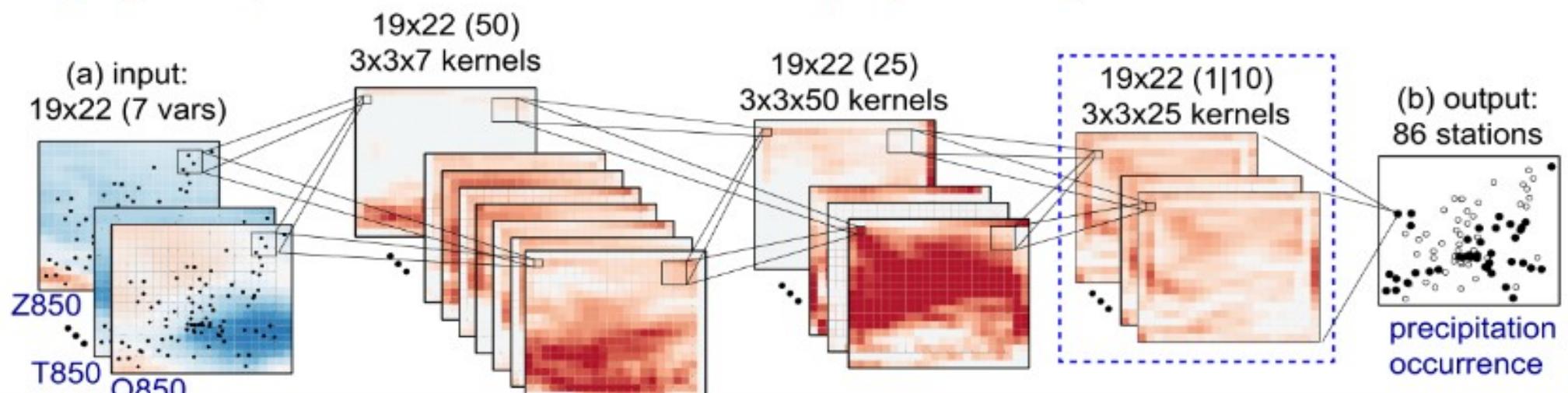
140 parameters (5 variables, 28 gridboxes), n=16434

Redundancy (correlation):

Principal Components (*domain selection*)
 Nearest grid-boxes
 Both (e.g. 15 CPs + values in 1 gridbox)

Convolution Neural Networks:

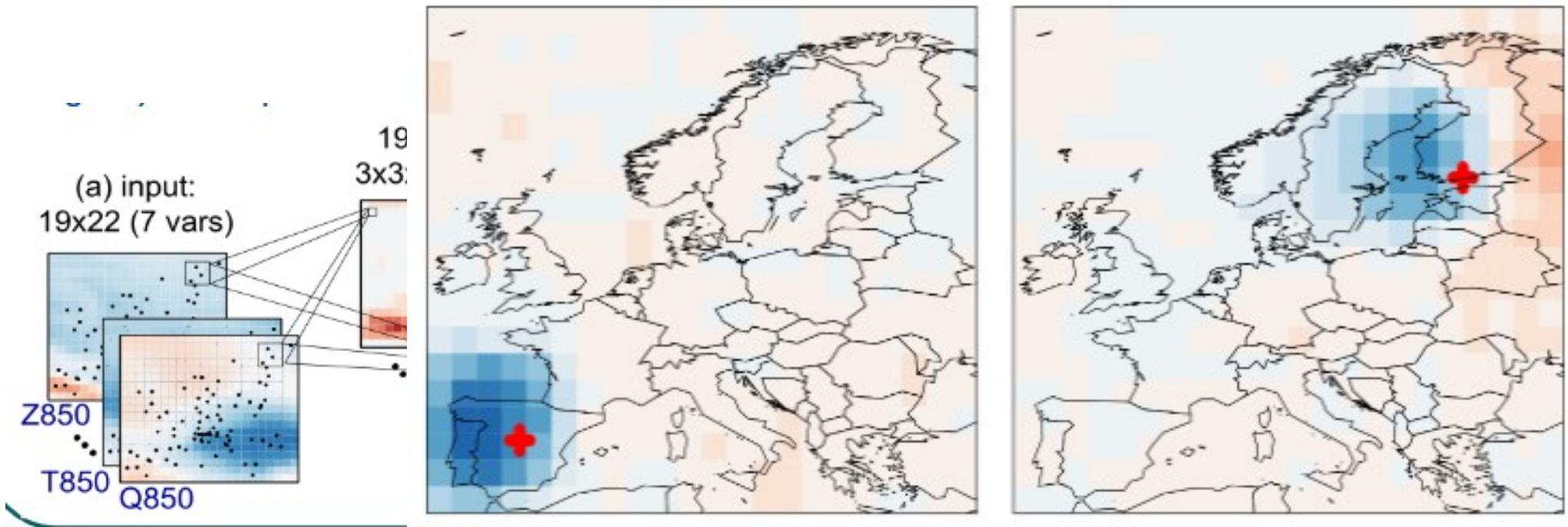
- Simplify the predictor's screening
- Can be applied to multi-variate problems (variables & location).
-



Baño-Medina y Gutiérrez (2018)

Convolution Neural Networks:

- Simplify the predictor's screening
- Can be applied to multi-variate problems (variables & location).
- Can be applied at continental scale

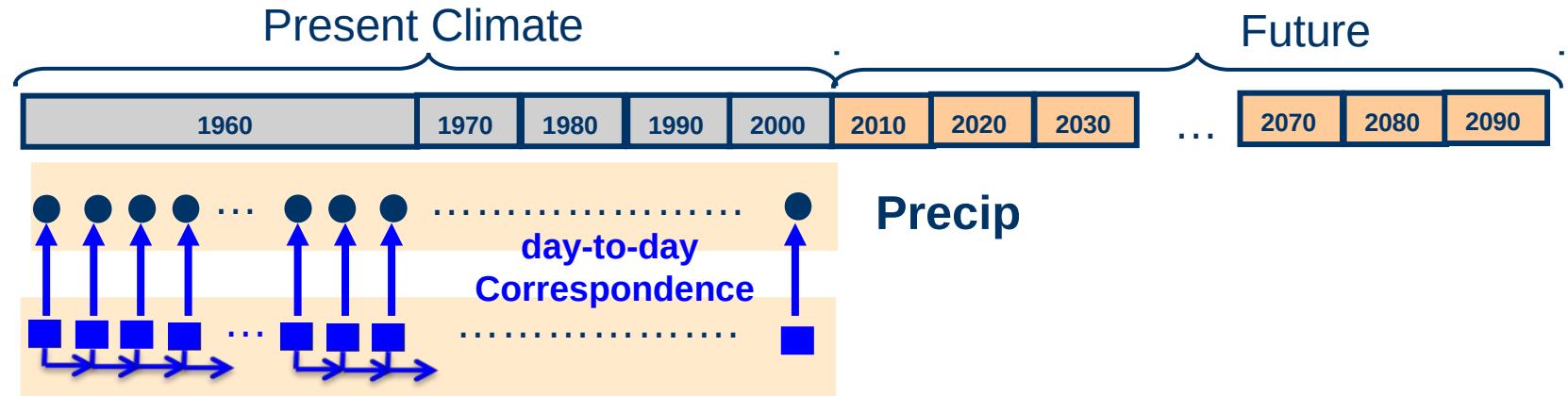


Baño-Medina y Gutiérrez (2018)

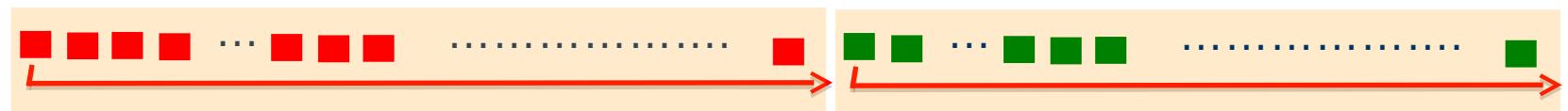
Tech.		Generative		non-Generative	
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Appro.	Eventwise	Regression, Neural Nets.	GLMs	Analogs, weather types	Analog resampling
	Distribution	Regression on PDF parameters			
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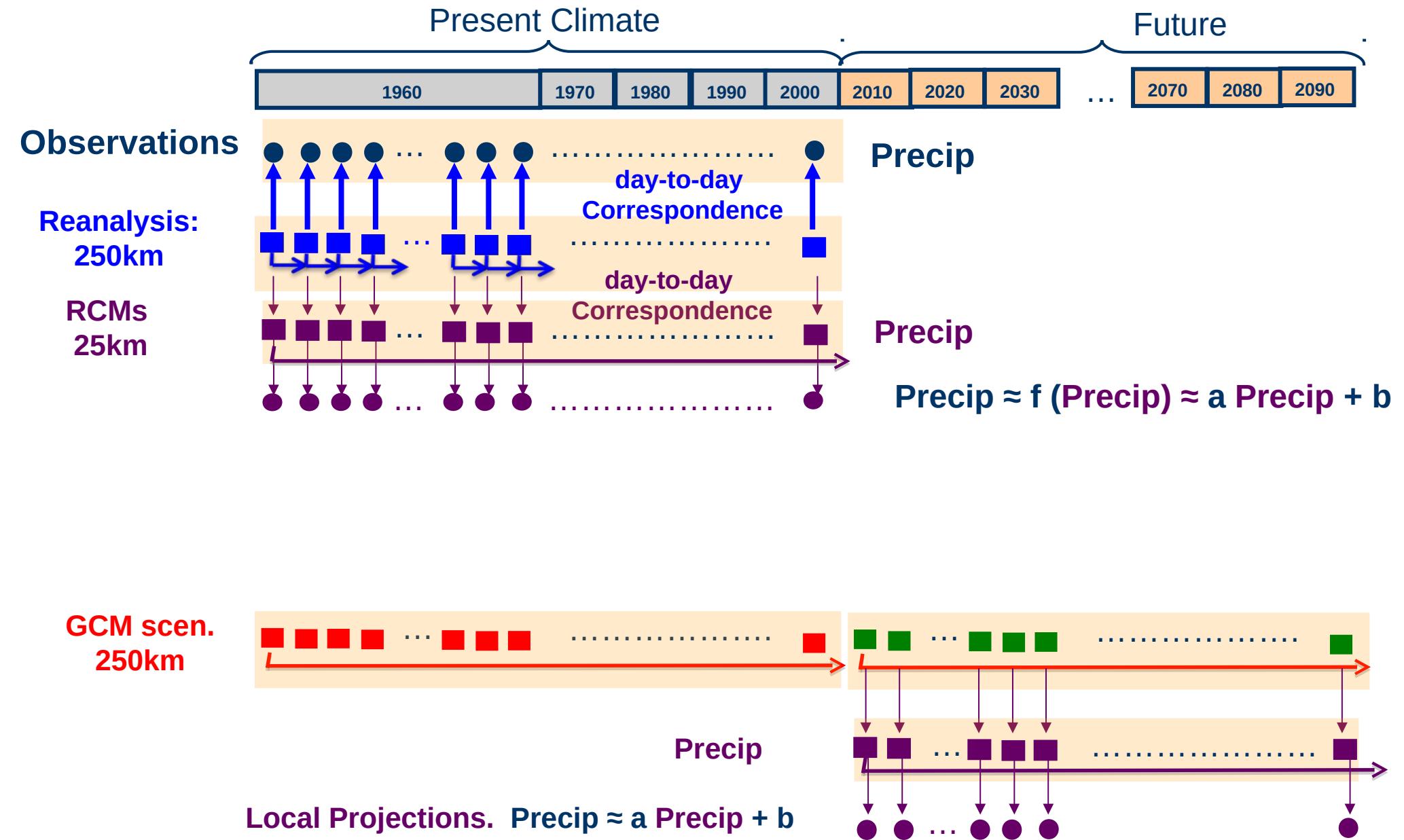
Model Output Statistics (MOS): Predictors are taken from the global (or regional) model for both training and downscaling phases. They require the model output to have day-to-day correspondence with observations. These methods can work with the variable of interest as predictor. For instance, local precipitation can be derived from the direct model precipitation forecasts.

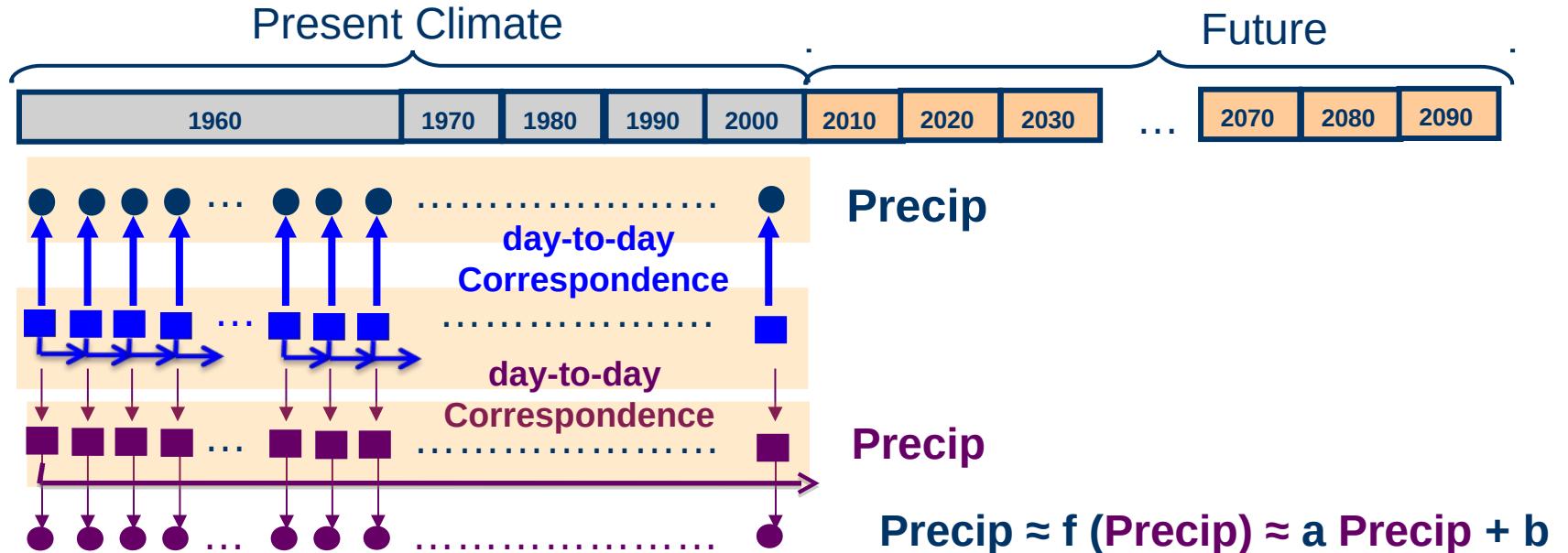
MOS	Training	Downscaling
Large scale	GCM	GCM
Local scale	Obs.	→



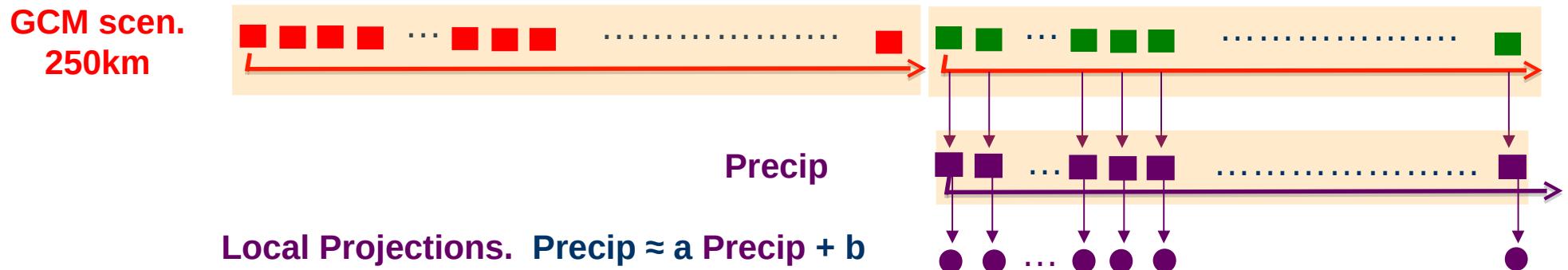
GCM scen.
250km







- Limitation 1: The Reanalysis-RCM coupling can be done with **nudging** (perfect correspondence) or in **climate mode** (only boundaries; partial correspondence). The latter is the typical situation in most databases.



- **Model Output Statistics (MOS):** The model is trained using observations and GCM outputs (which include biases/errors).

$$\text{precip}_{\text{obs}}[d] = f(\text{precip}_{\text{gcm}}[d])$$

*First introduced in weather forecast (Glahn and Lowry, 1972),
but problematic for climate projection.*

Adapted for climate projection under the name
“bias-correction” in a PDF-wise approach:

$$\text{PDF}(\text{precip}_{\text{obs}}) = F(\text{PDF}(\text{precip}_{\text{gcm}}))$$

- **Perfect Prognosis (PP):** The model is trained using observations and reanalysis (quasi-observations). Predictors are large-scale variables well represented by GCMs.

$$\text{precip}_{\text{obs}}[d] = f(\text{SLP}_{\text{rea}}[d], \text{Q850}_{\text{rea}}[d])$$

BIASES **RESOLUTION** **Model Output Statistics (MOS):** The model is trained using observations and GCM outputs (which include biases/errors).

$$\text{precip}_{\text{obs}}[d] = f(\text{precip}_{\text{gcm}}[d])$$

*First introduced in weather forecast (Glahn and Lowry, 1972),
but problematic for climate projection.*

RCMs

Adapted for climate projection under the name
“bias-correction” in a PDF-wise approach:

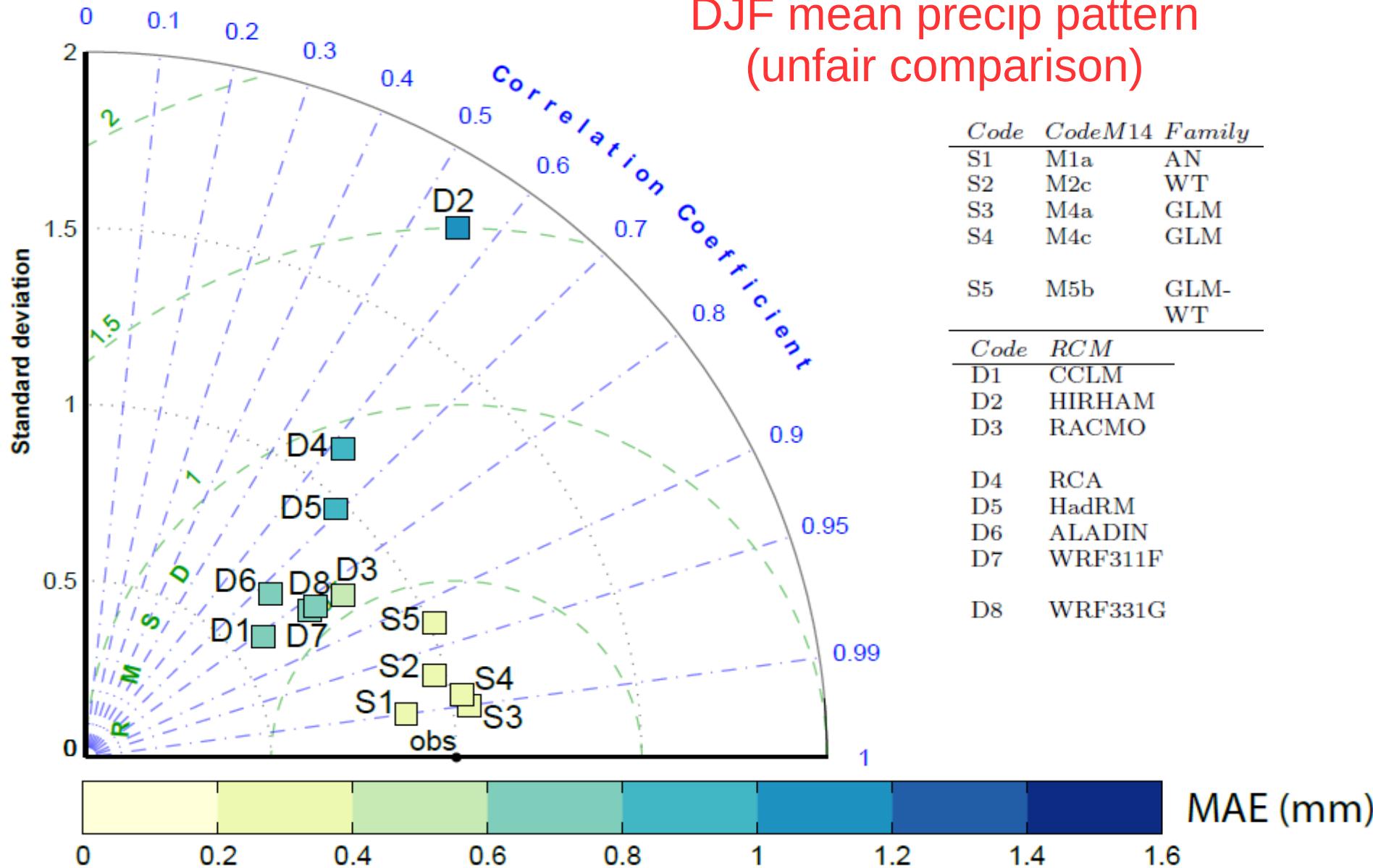
$$\text{PDF}(\text{precip}_{\text{obs}}) = F(\text{PDF}(\text{precip}_{\text{gcm}}))$$

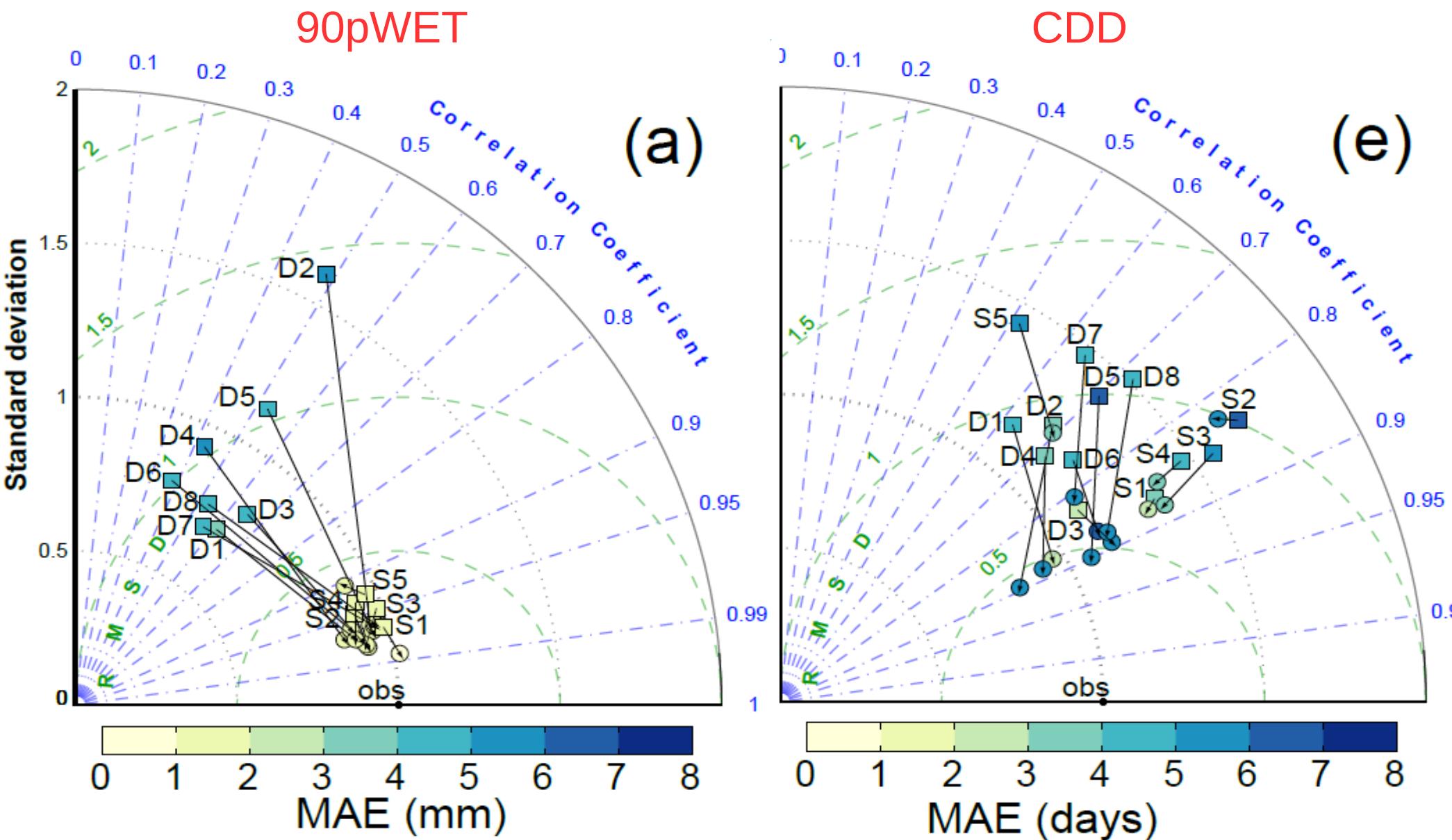
BIASES **RESOLUTION** **Perfect Prognosis (PP):** The model is trained using observations and reanalysis (quasi-observations). Predictors are large-scale variables well represented by GCMs.

GCMs

$$\text{precip}_{\text{obs}}[d] = f(\text{SLP}_{\text{rea}}[d], \text{Q850}_{\text{rea}}[d])$$

DJF mean precip pattern (unfair comparison)

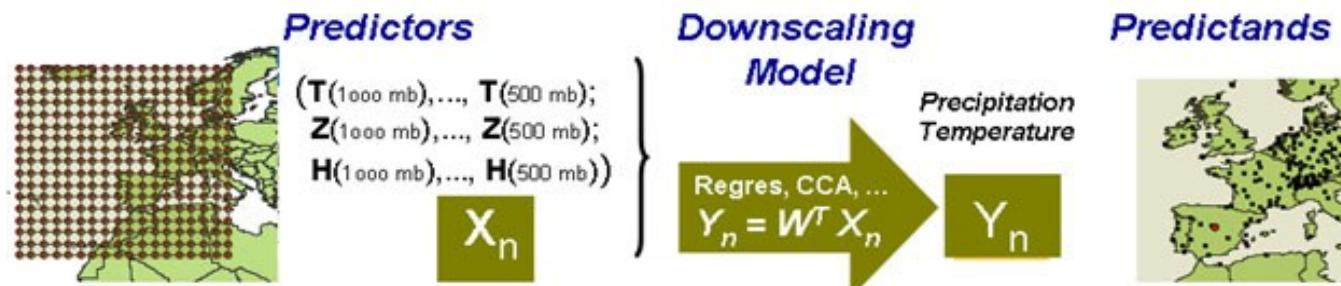




Tech.		Generative		non-Generative	
Appro.		Deterministic	Stochastic	Deterministic	Stochastic
PP	Eventwise	Regression, Neural Nets.	GLMs	Analogs, weather types	Analog resampling
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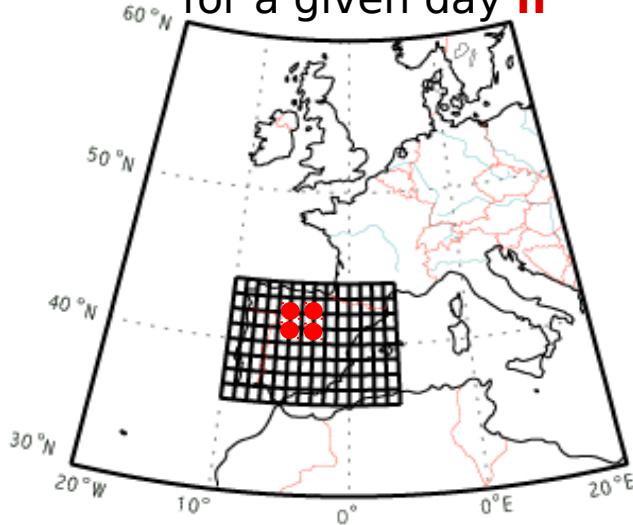
Statistical Downscaling

Statistical methods linking the local observed climate (**predictand Y**) with the global simulations given by the GCMs (**predictors X**), through some **function f** and/or **parameters θ** : $Y = f(X; \theta)$



Grids of atmospheric patterns

for a given day n



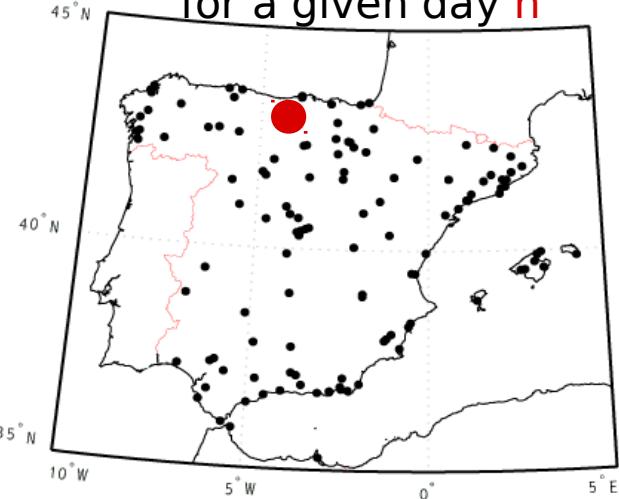
$$\left(\begin{array}{l} \mathbf{T}(1000 \text{ mb}), \dots, \mathbf{T}(500 \text{ mb}); \\ \mathbf{Z}(1000 \text{ mb}), \dots, \mathbf{Z}(500 \text{ mb}); \\ \dots; \\ \mathbf{H}(1000 \text{ mb}), \dots, \mathbf{H}(500 \text{ mb}) \end{array} \right) = \mathbf{X}_n \quad \right\}$$

Logistic regression
Probabilistic prediction

$$\hat{\mathbf{Y}}_n = F(a \mathbf{X}_n + b)$$

Predictands: *precip.*, etc.

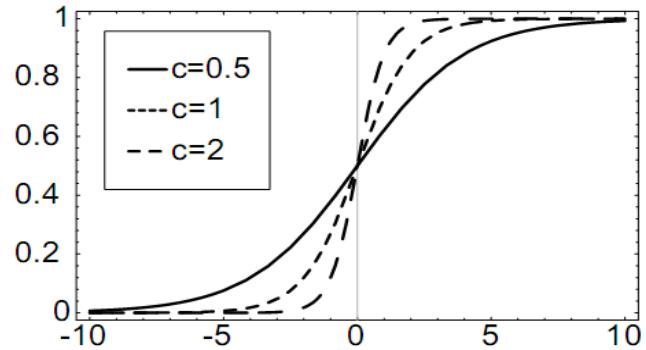
for a given day n

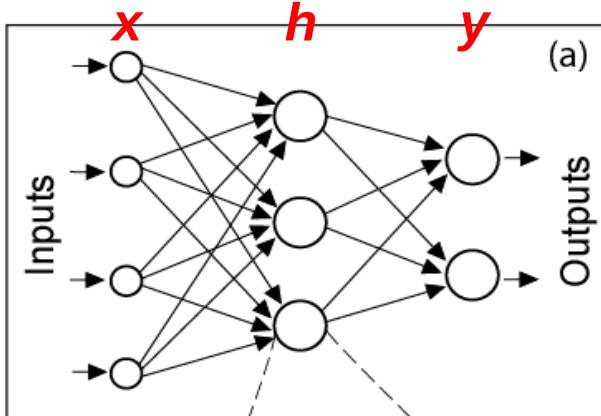


\mathbf{Y}_n

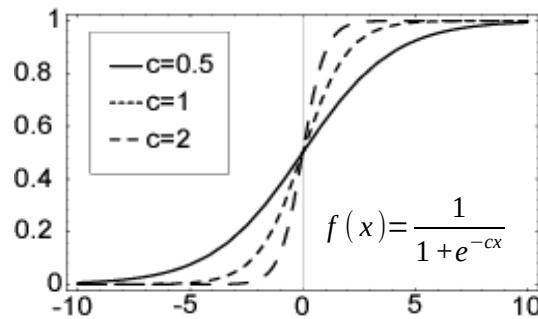
Linear regression:

$$\hat{\mathbf{Y}}_n = a \mathbf{X}_n + b$$





nonlinear function



$$y_j = f\left(\sum_i \beta_{ji} f\left(\sum_k \alpha_{ik} x_{kp}\right)\right)$$

↑ ↑ **h_i**
 Inputs $\{x_{1p}, \dots, x_{mp}\}$ Outputs $\{y_{1p}, \dots, y_{np}\}$

$$\begin{aligned} E(\alpha, \beta) &= \frac{1}{2} \sum_{j,p} (y_{jp} - f(\sum_i \beta_{ji} f(\sum_k \alpha_{ik} x_{kp})))^2 \\ &= \sum ||\mathbf{y}_p - f(\beta^T f(\alpha^T \mathbf{x}_p))|| \\ \Delta \beta_{ik} &= -\eta \frac{\partial E}{\partial \beta_{ik}}; \quad \Delta \alpha_{kj} = -\eta \frac{\partial E}{\partial \alpha_{kj}}, \end{aligned}$$

1. Init the neural weight with random values
2. Select the input and output data and train it
3. Compute the error associate with the output

$$\delta_{jp} = (y_{jp} - \hat{y}_{jp}) f'(\beta^T \hat{\mathbf{h}}_p)$$

4. Compute the error associate with the hidden neurons

$$\psi_{jp} = \sum_k \delta_{jp} \beta_{jk} f'(\alpha_k^T \mathbf{x}_p)$$

5. Comput

$$\Delta \beta_{jk} = \eta \hat{\mathbf{h}}_k \delta_{jp}, \quad \Delta \alpha_{ki} = -\eta \sum_j x_{ip} \delta_{jp} \psi_{jp},$$

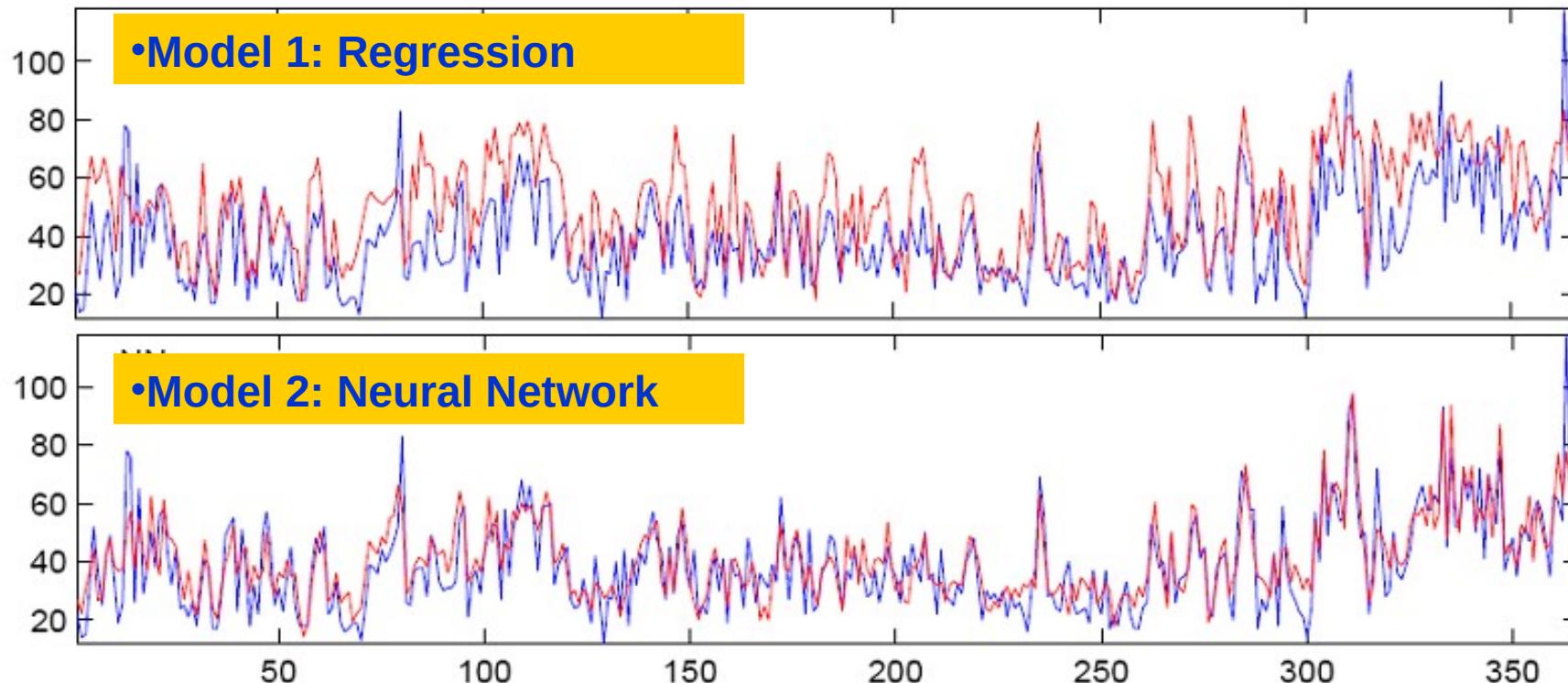
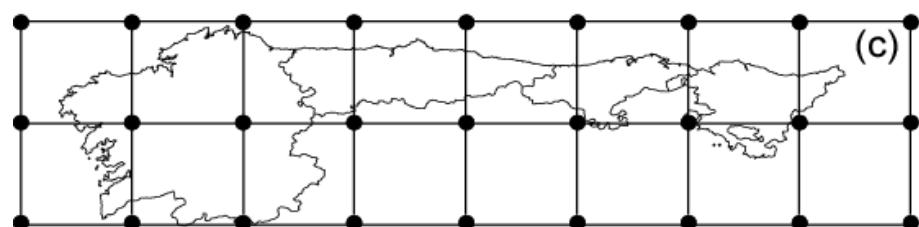
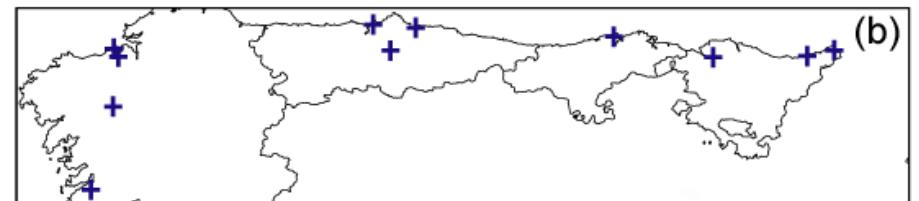
and update the neural weight according to these values

Wind Speed $\rightarrow [0, \infty)$

Observations from 1977- 2002.

ERA40 over 27 grid points for the same period

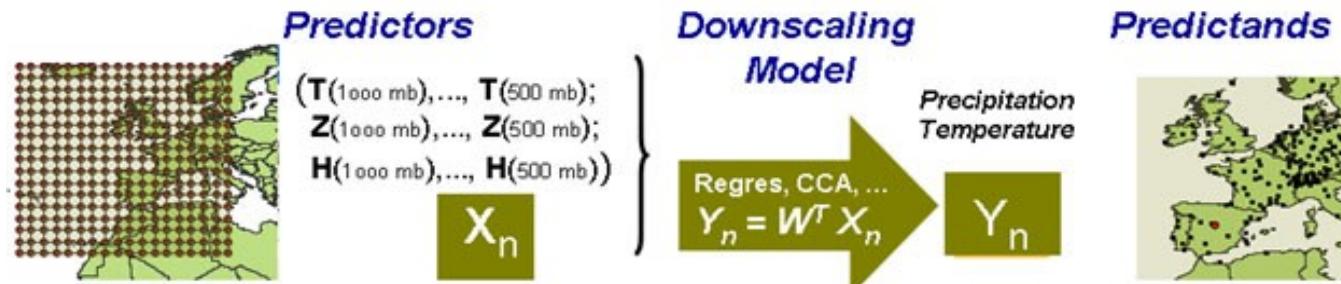
**60% for training and
40% for validation**



Tech.	Generative			non-Generative	
	Deterministic	Stochastic		Deterministic	Stochastic
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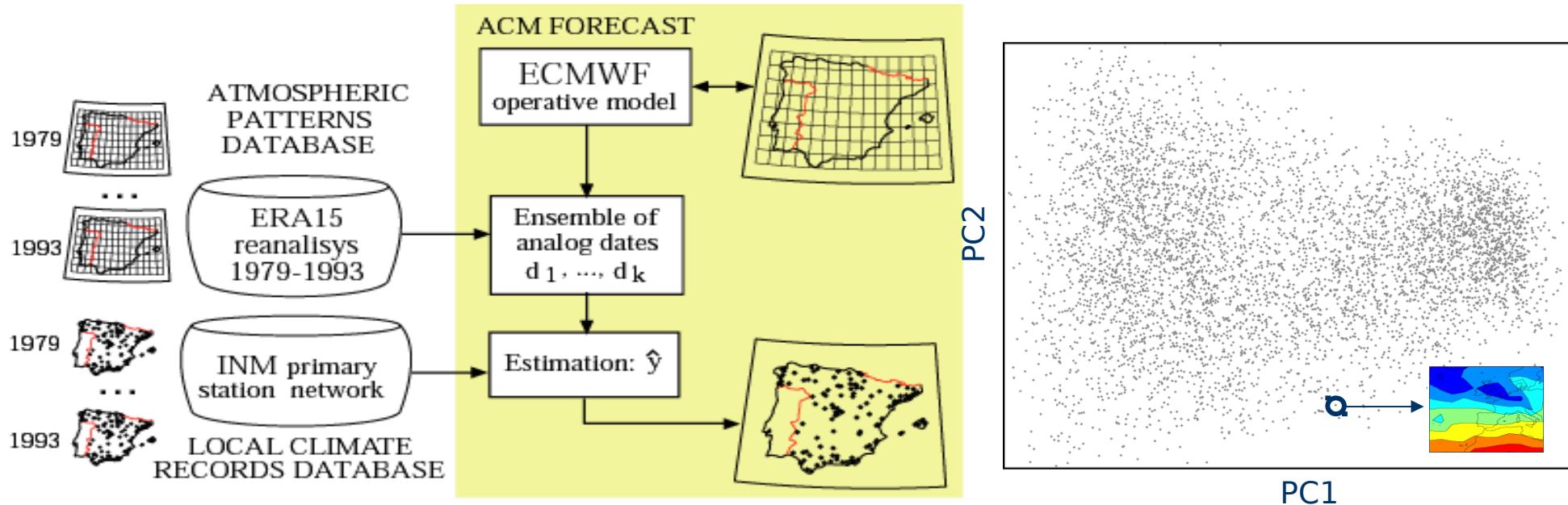
Statistical Downscaling

Statistical methods linking the local observed climate (**predictand Y**) with the global simulations given by the GCMs (**predictors X**), through some **function f** and/or **parameters θ** : $Y = f(X; \theta)$



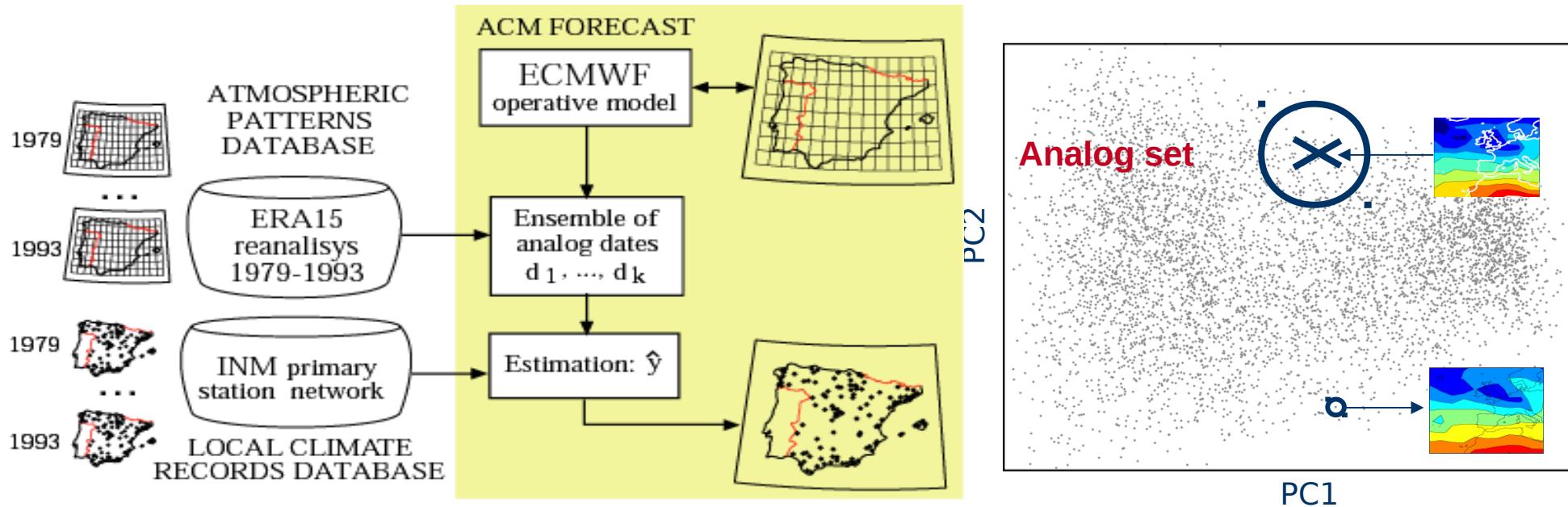
2. Analogs & Weather typing

The method of analogs (k-nearest neighbors) is one of the most popular techniques in statistical downscaling, introduced by E. Lorenz (1969).



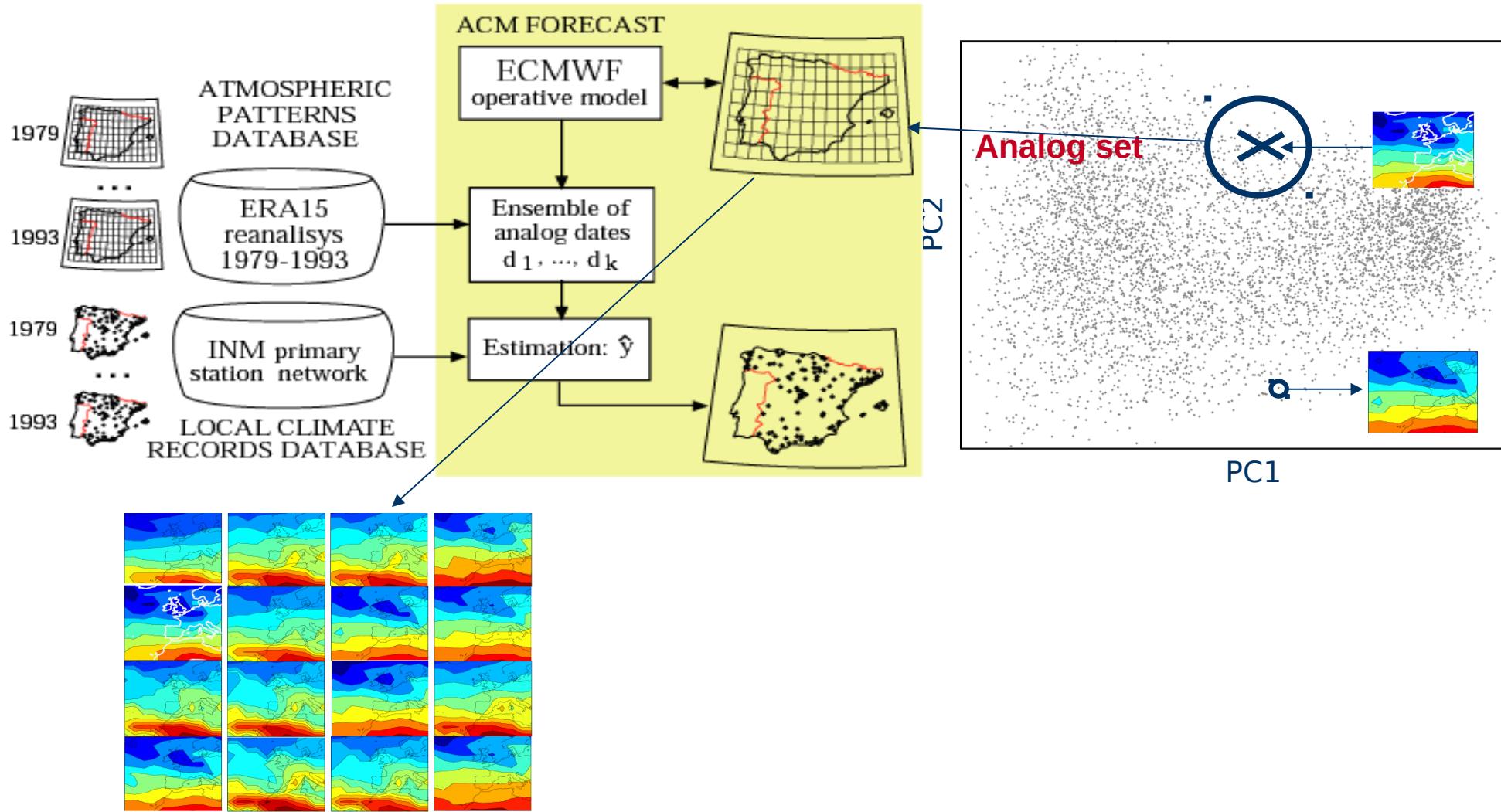
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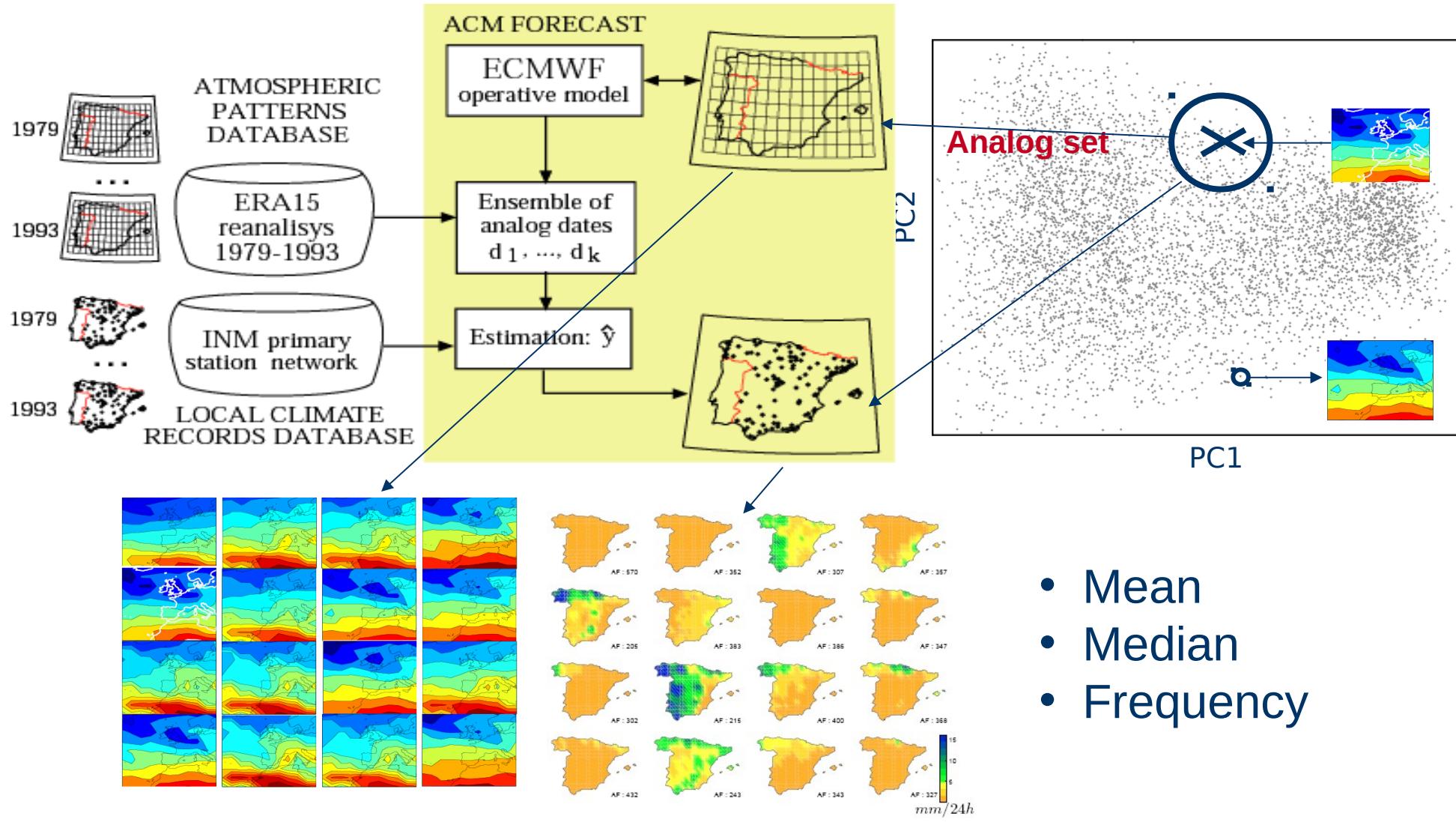
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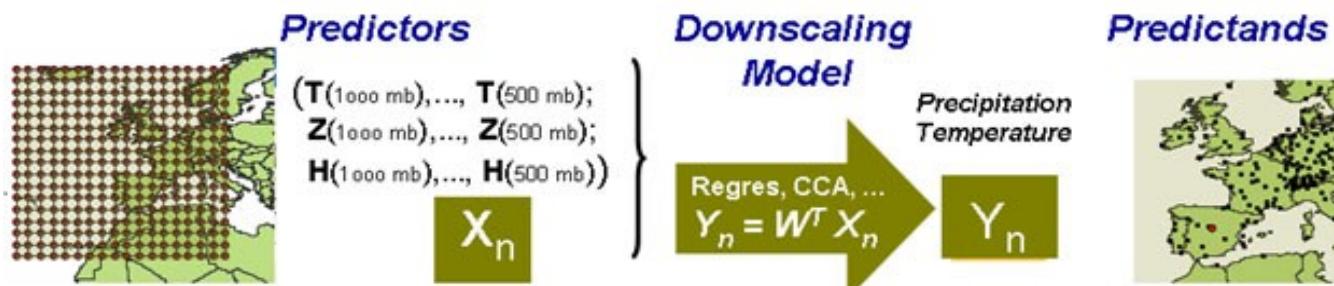
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There is **day-to-day** correspondence.

There is **not day-to-day** correspondence.

Statistical Downscaling

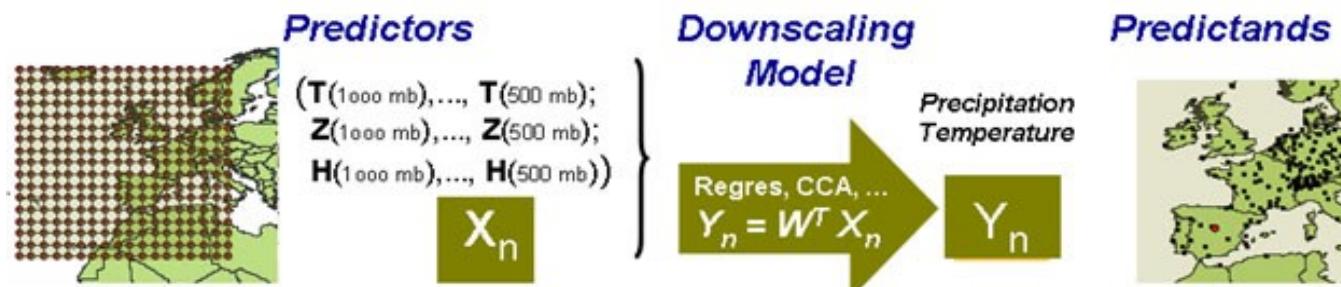
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Statistical Downscaling

Statistical methods linking the local observed climate (**predictand Y**) with the global simulations given by the GCMs (**predictors X**), through some **function f** and/or **parameters θ** : $Y = f(X; \theta)$



1. **Linear Transformation (ax+b):** unbiasing/ scaling (Déqué. 2007; global or local, Widmann et al. 2003; Schmidli et al. 2006), delta change (Hay et al. 2000). These methods were proposed to adjust the arithmetic mean and /or the standard deviation.
2. **Empirical CDF correction:** quantile-quantile mapping and variations (Themeßl et al., 2010; Mengual et al. 2011; Wilcke et al. 2013)
3. **CDF correction:** parametric adjust of the probability/cumulative distribution function (Vidal and Wade, 2008a, 2008b; Piani et al. 2010).
4. **Other approaches:** In the framework of the first Inter-Sectoral Impact Model Intercomparison Project, ISI-MIP, was developed a trend-preserving bias correction method (Hempel et al. 2013) designed to synthesise impact projections in the agriculture, water, biome, health, and infrastructure sectors at different levels of global warming.

Additive Correction

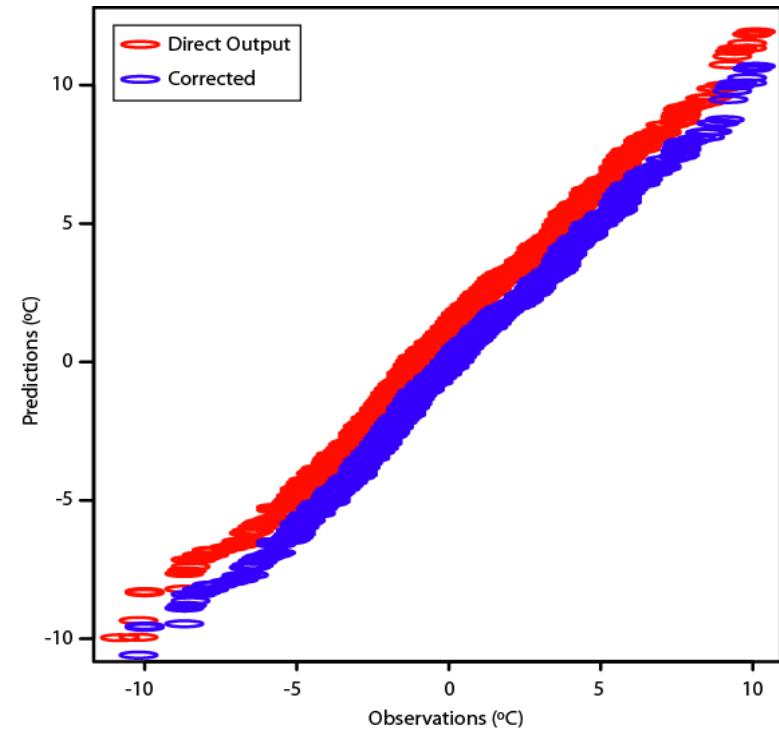
This method has the advantage of simplicity. Two straight-forward corrections consist of adding the climatological difference between future and control climate scenario simulations to an observed baseline (the so-called **delta method**) or removing the bias from future simulation by applying the climatological difference between the observed and control data (the **unbiasing method**; Déqué 2007).

1. The **delta approach** assumes that the variability in the test period remains unchanged.

$$Y_{sim(bc)} = Obs + \text{mean}(Y_{test} - Y_{prd})$$

1. The **unbiasing method** assumes that the GCM/RCM variability is perfect.

$$Y_{sim(bc)} = Y_{sim} + \text{mean}(Obs - Y_{prd})$$



Multiplicative Correction

This method is the equivalent to the linear correction but for precipitation-like variables. In this case both delta and scaling methods assume that the variability in the climate scenario changes in the same proportion than the mean.

1. Delta approach:

$$Y_{sim(bc)} = Obs * \text{mean}(Y_{sim})/\text{mean}(Y_{prd})$$

2. Scaling method:

$$Y_{sim(bc)} = Y_{sim} * \text{mean}(Obs)/\text{mean}(Y_{prd})$$

Bias correction: QQ Mapping

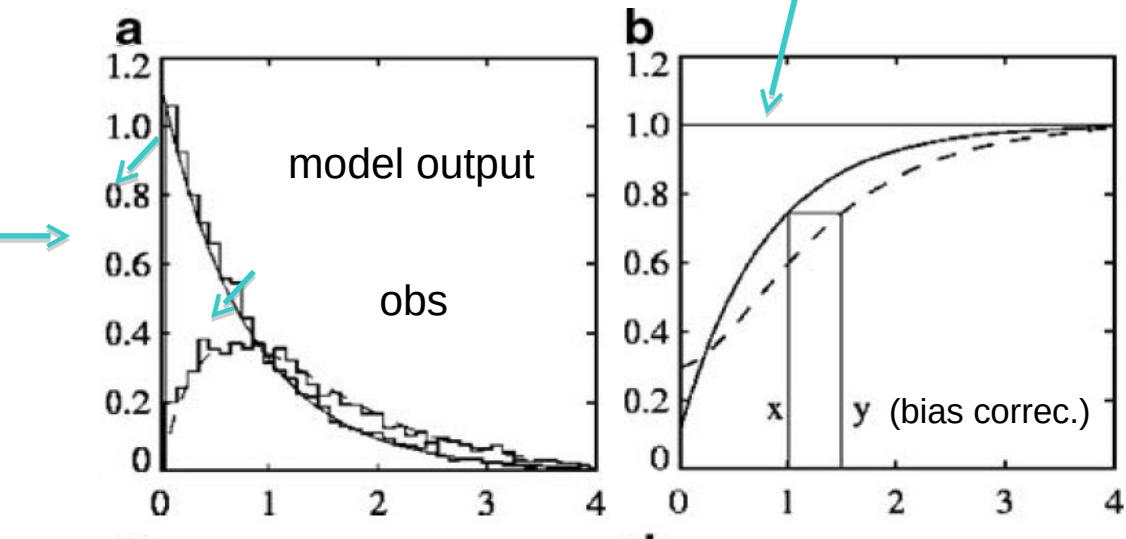
Fig. 1 Statistical correction applied to a synthetic dataset. **a** Synthetic pdf of simulated daily precipitation (solid line), synthetic pdf of observed daily precipitation (dashed line). **b** cdfs obtained by integrating the corresponding pdfs in **a**. **c** Transfer function obtained graphically from **b** by solving: $\text{cdf}_{\text{obs}}(y) = \text{cdf}_{\text{sim}}(x)$ (thick solid line). **d**

Source Piani et al. 2010

$$\text{pdf}(x) = \frac{e^{(-\frac{x}{\theta})} x^{(k-1)}}{\Gamma(k)\theta^k}$$

Requires a
“reference”
PDF !!!!

$$\text{cdf}(x) = \int_0^x \frac{e^{(-\frac{x}{\theta})} x'^{(k-1)}}{\Gamma(k)\theta^k} dx' + \text{cdf}(0)$$



More sensitive
to non-
stationarity
issues !!!!

Requires cross-validation
(e.g. Gutiérrez et al. 2013)

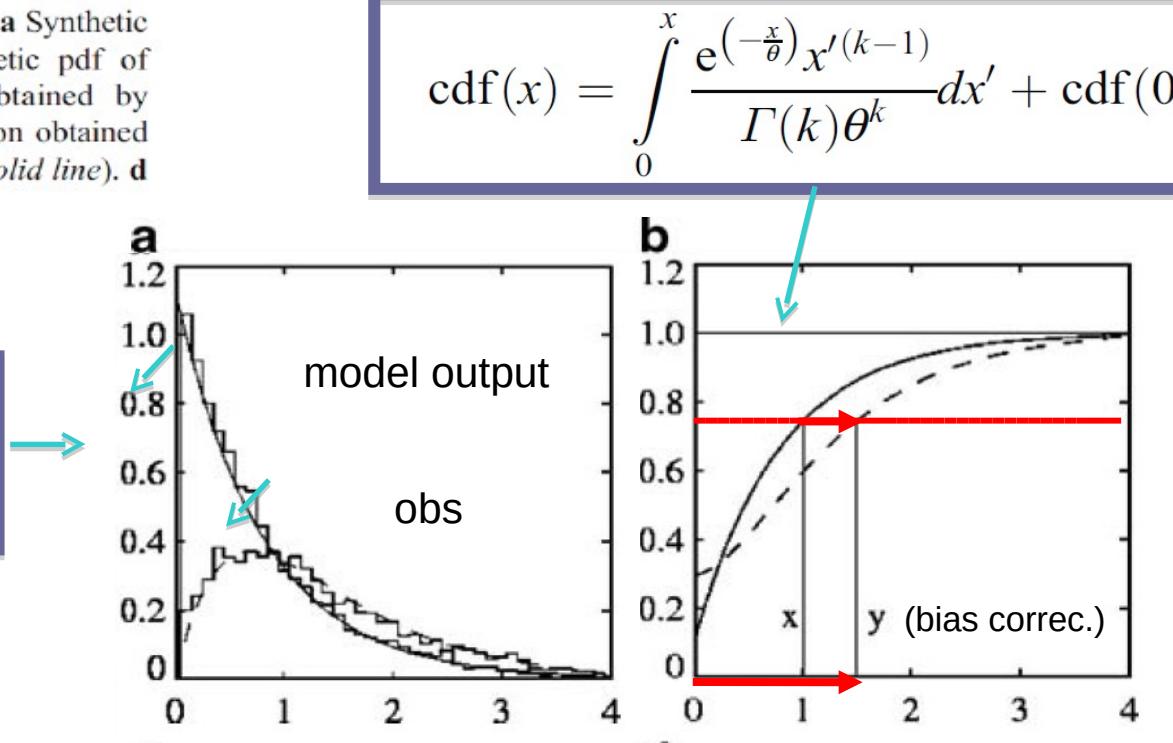
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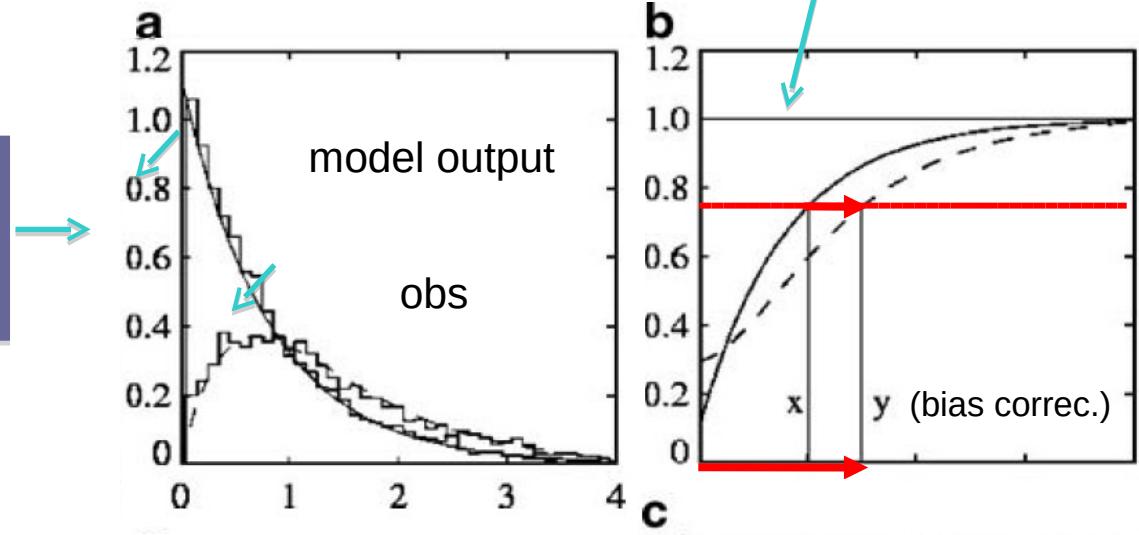
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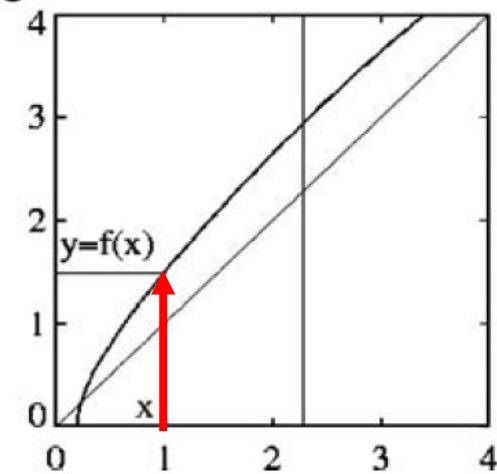
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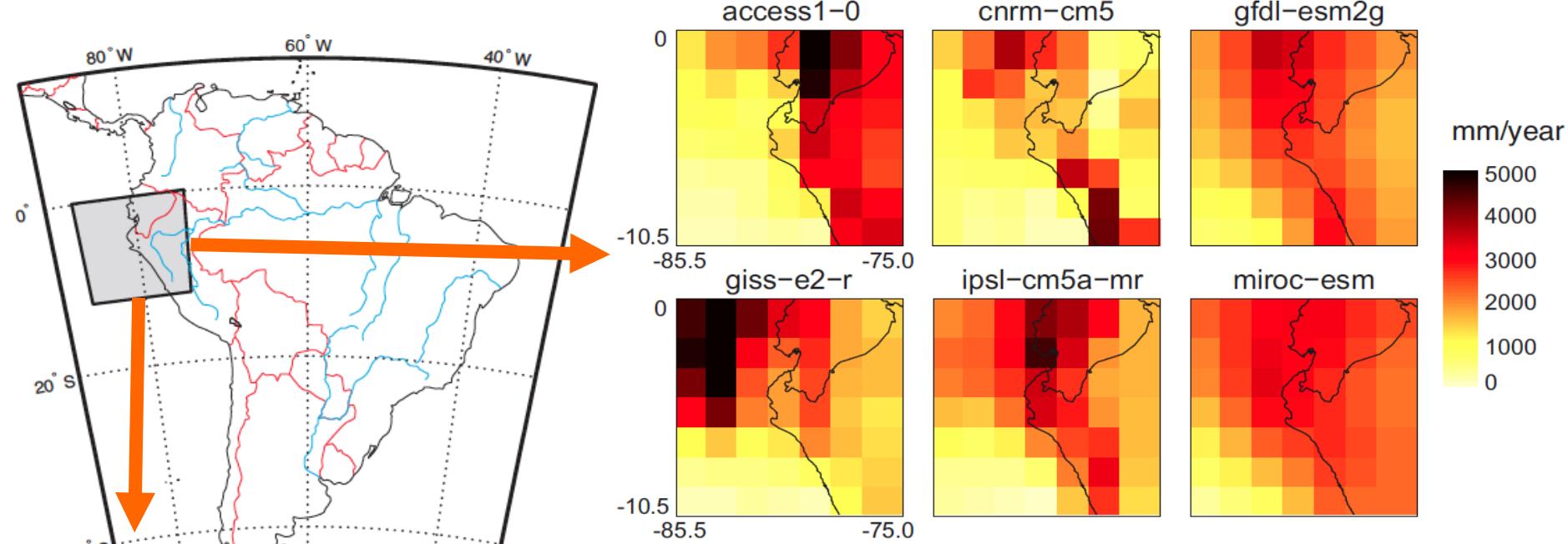
$$\text{pdf}(x) = \frac{e^{(-\frac{x}{\theta})} x^{(k-1)}}{\Gamma(k)\theta^k}$$



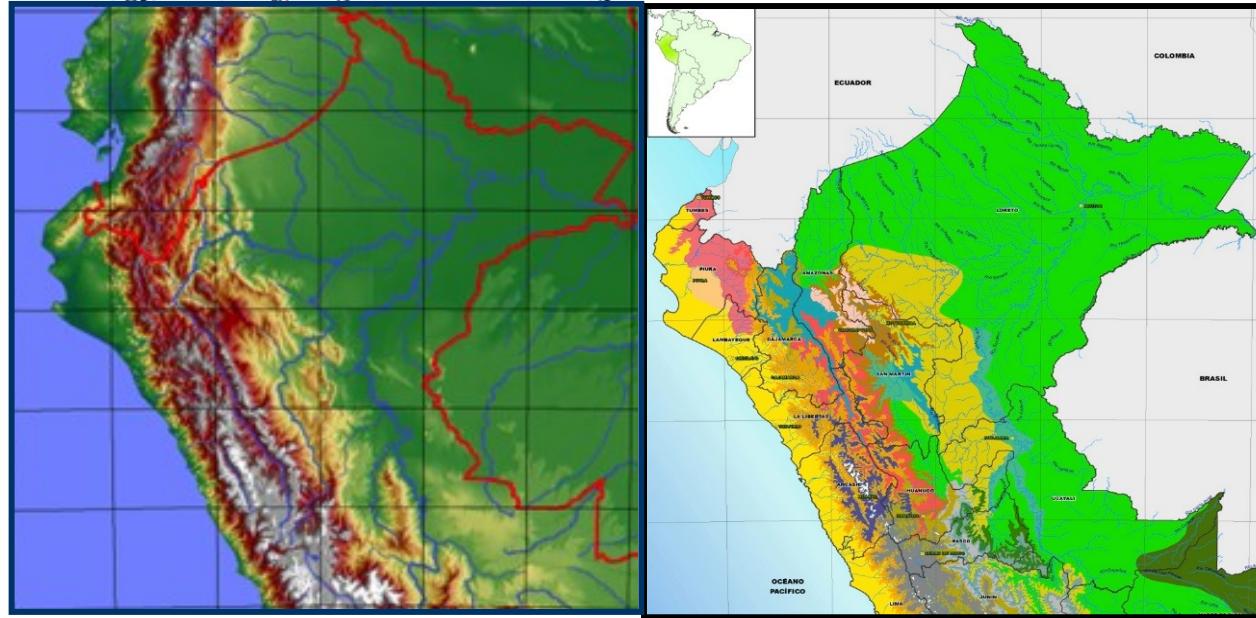
$$\text{cdf}_{\text{obs}}(f(x)) = \text{cdf}_{\text{sim}}(x)$$

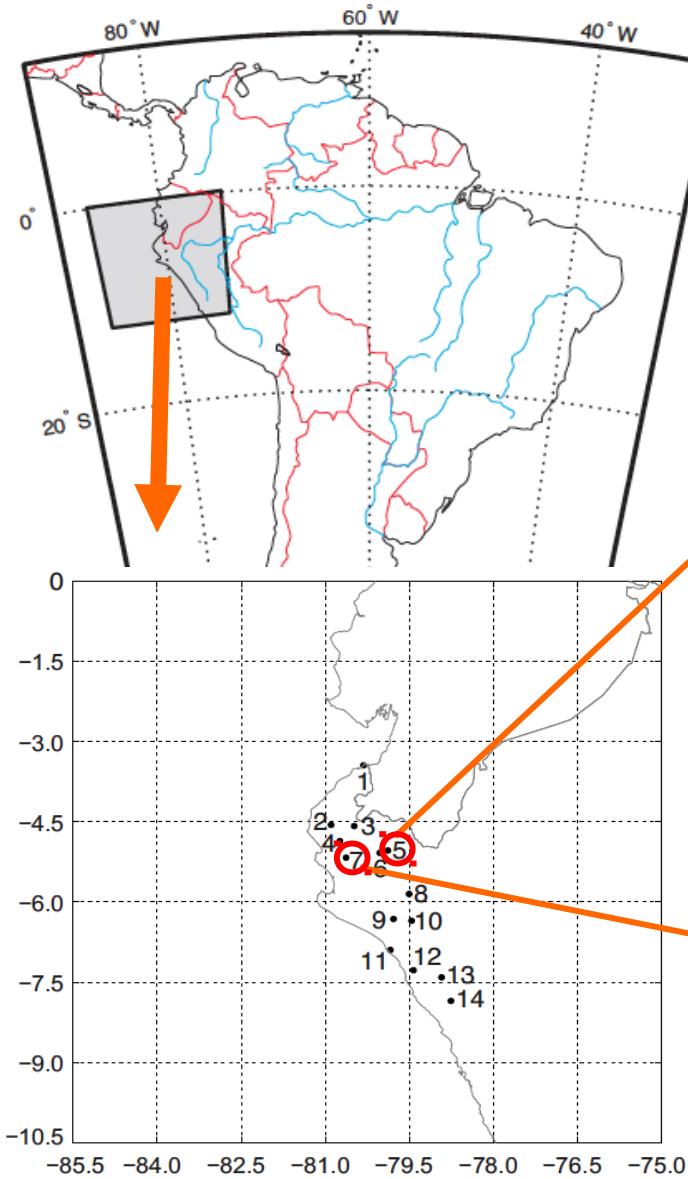
$$y = f(x) = \text{cdf}_{\text{obs}}^{-1}(\text{cdf}_{\text{prd}}(X))$$



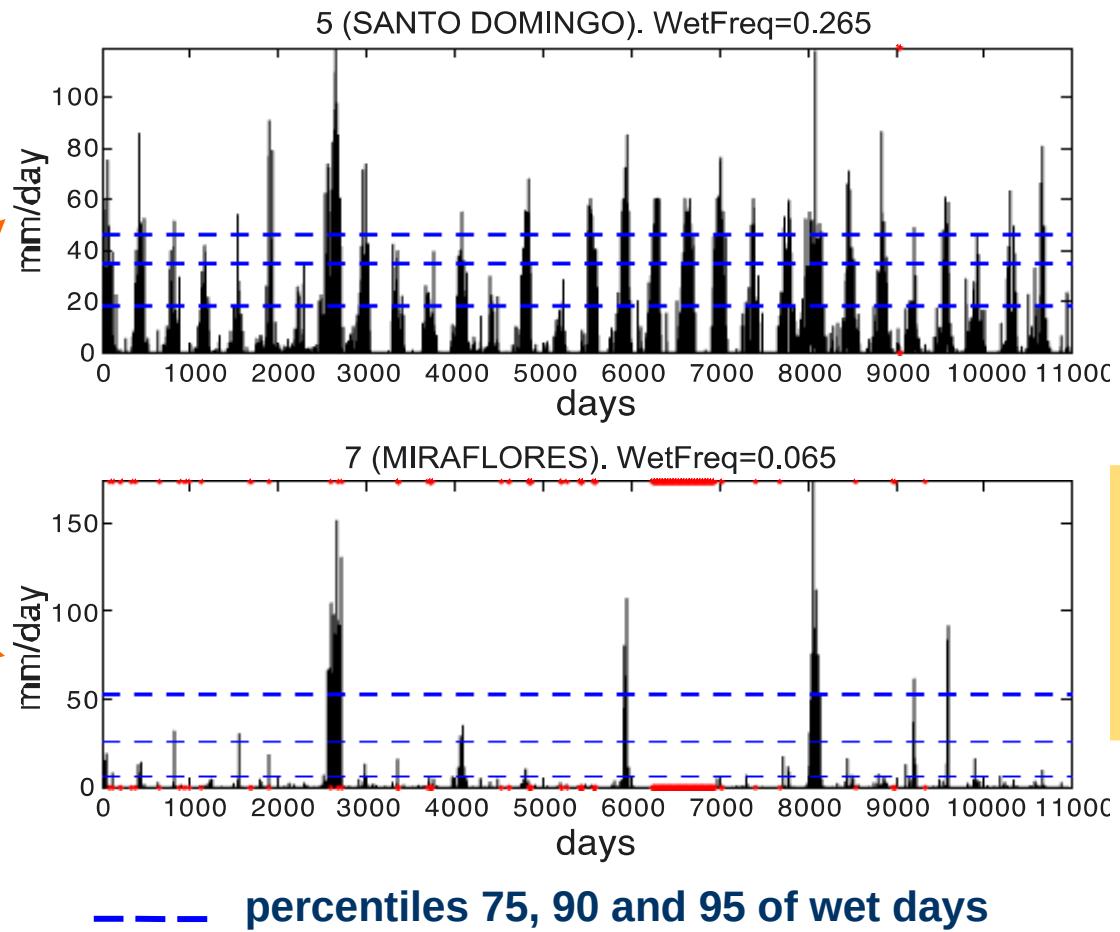


Mean yearly accumulated precipitation from six CMIP5 models over a 1.5° grid (*historical scenario 1976-2005*) →
Different *precip* patterns.
 ← elevation and climates



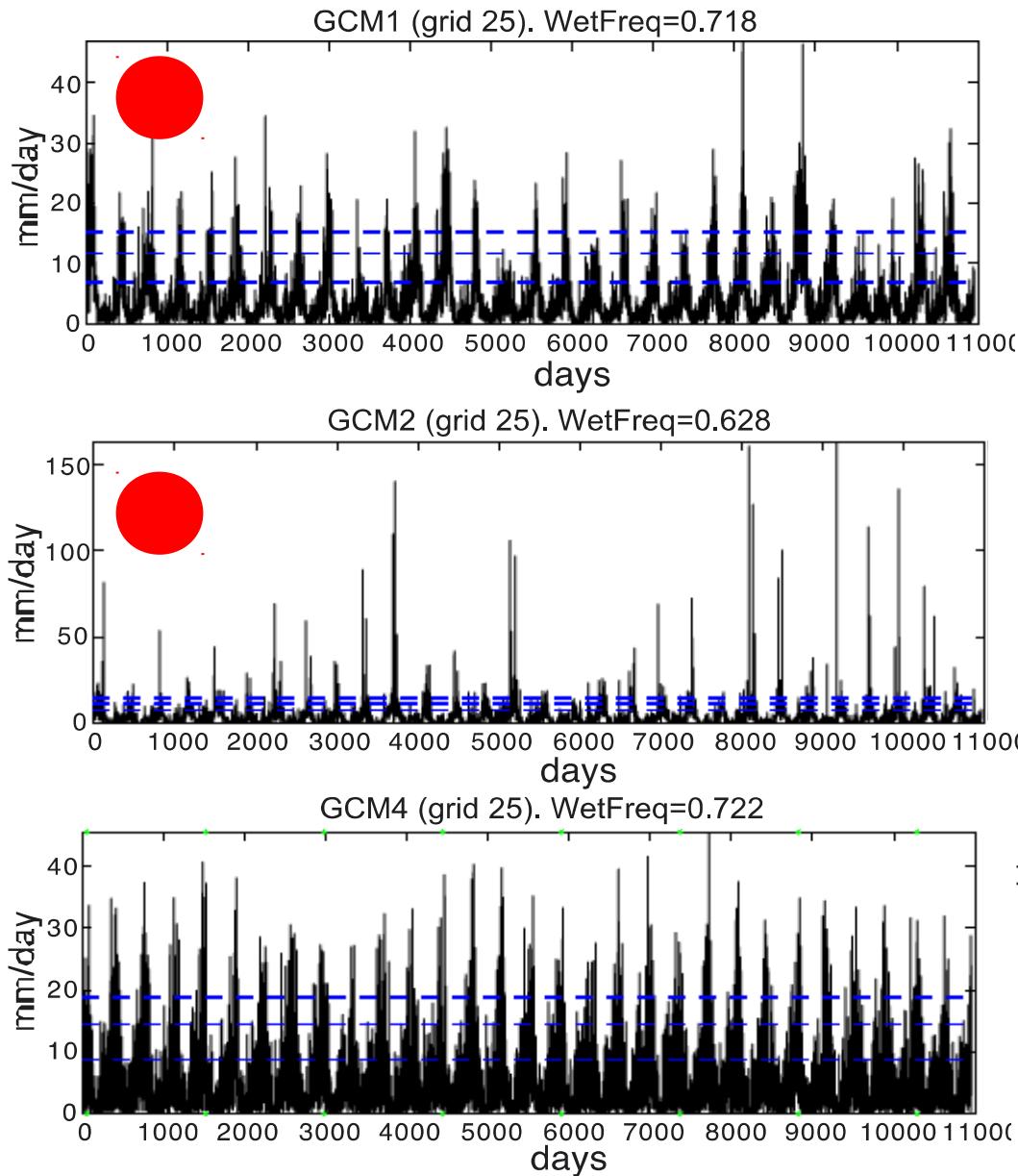


14 stations from SENAMHI with less than 10% of missing data in 1976-2005.
Two main different regimes (ENSO).



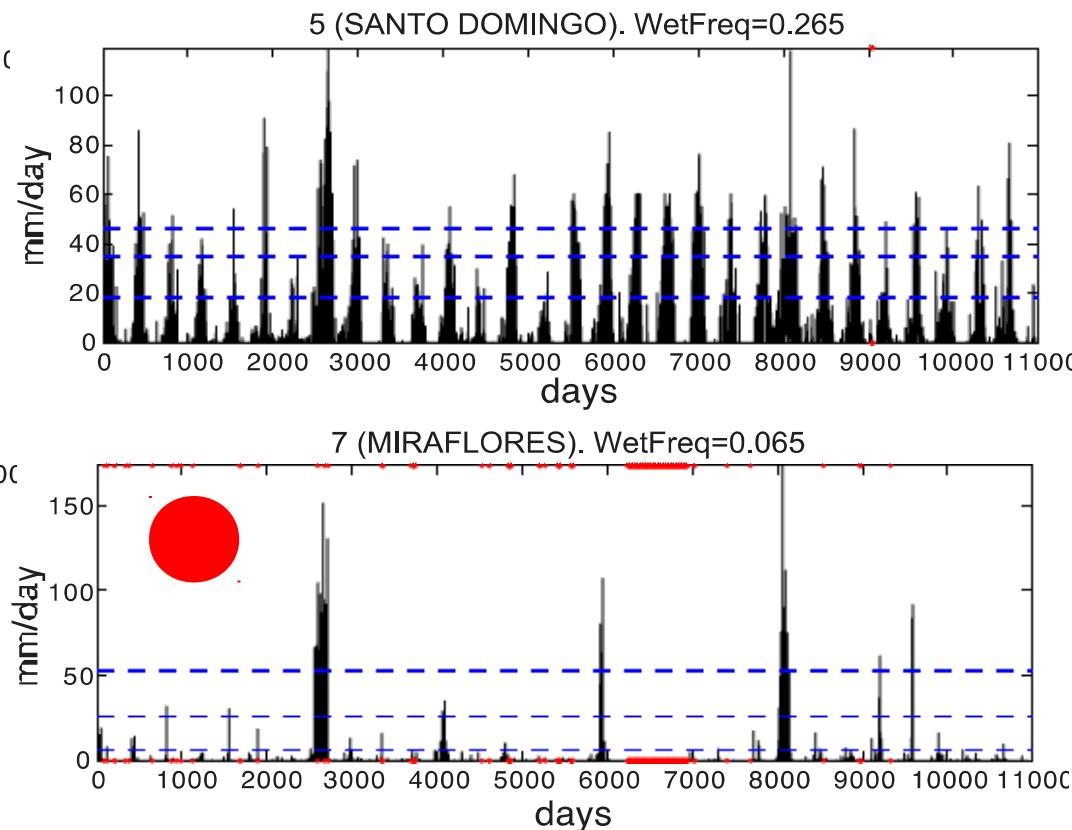
Values
over P90
only in
El Niño
years

Obs and Sim in the same gridbox



None of the six GCMs exhibits “values over P90 only in El Niño years”

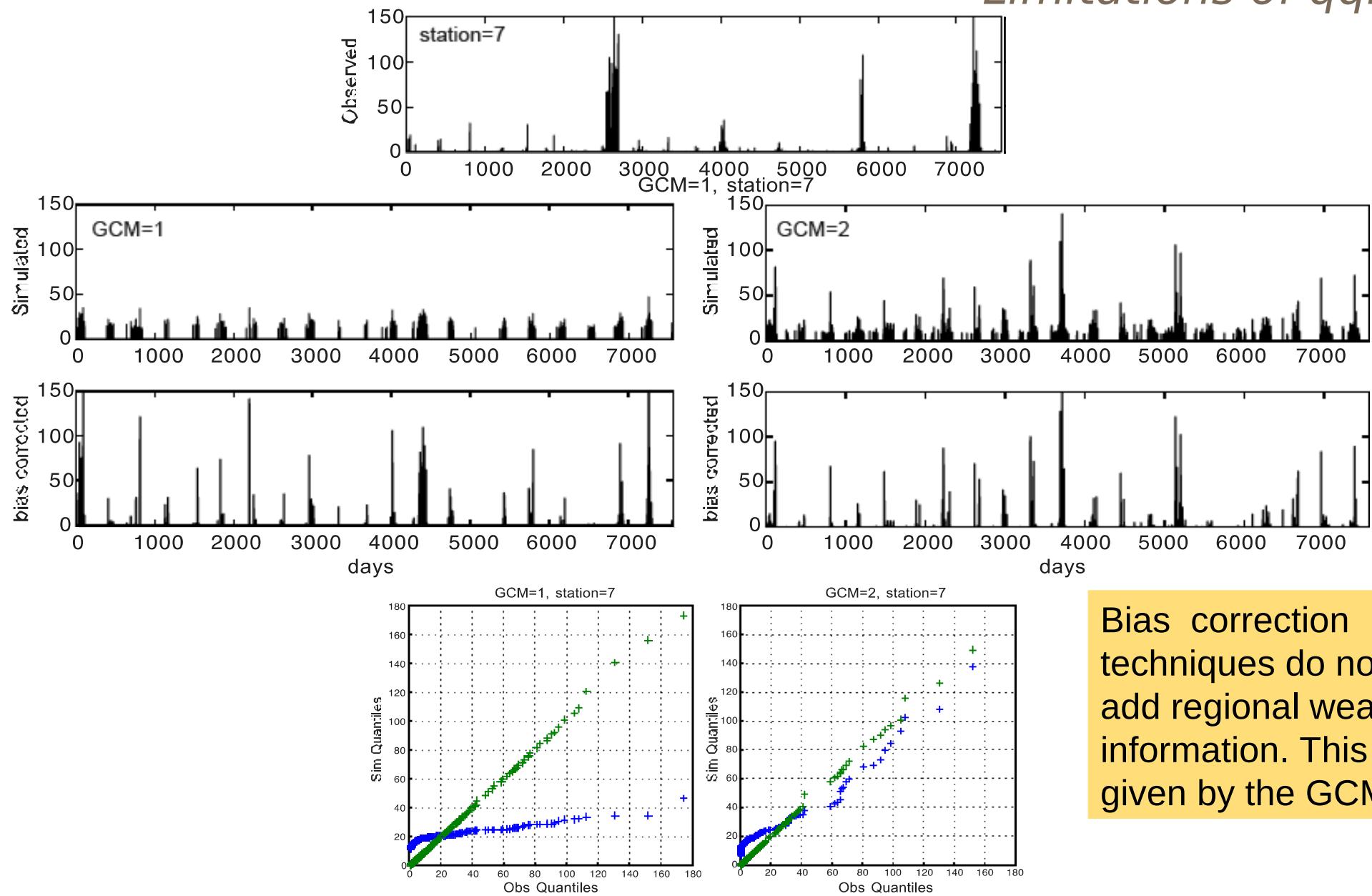
Thus, bias corrected data using *qqmap* will not exhibit El Niño regimes.



percentiles 75, 90 and 95 of wet days



Limitations of qqmap



precipitation, radiation, wind speed and surface pressure

snowfall, max. and min. temperature, wind components

Multiplicative²

ISI-MIP

Dependent Variables³

Temperature

Additive¹

Monthly Mean Correction

Daily Variability Correction

Freq. adjust and redistribute drizzle

Correction of precip. amount of wet days

Linear regression of the rank ordered daily anomalies.

variable name

average temperature¹

minimum temperature³

maximum temperature³

total precipitation²

snowfall³

shortwave radiation²

longwave radiation²

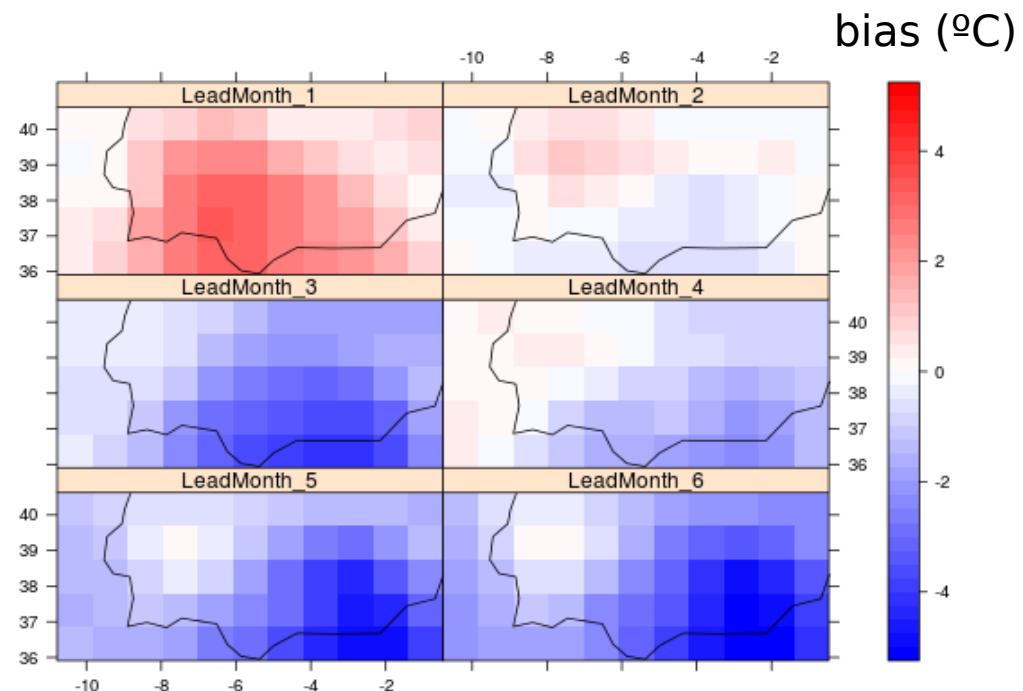
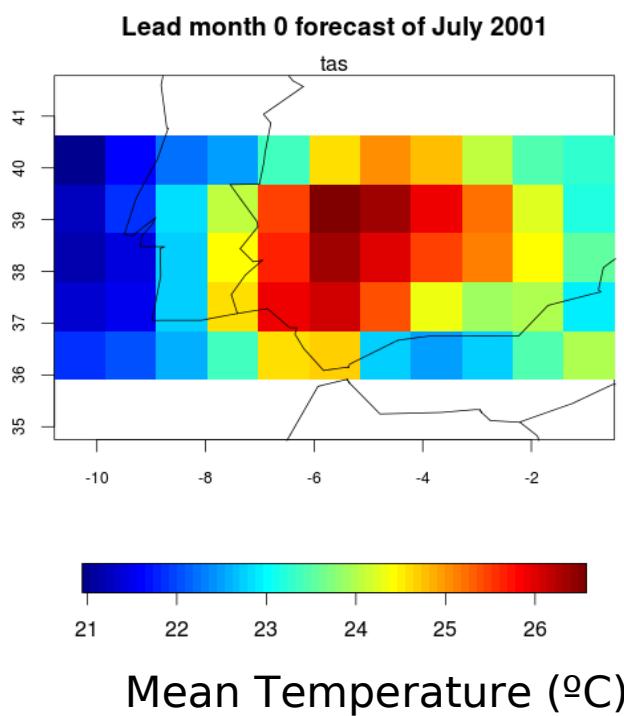
near-surface wind speed²

near-surface eastward wind³

near-surface northward wind³

surface pressure²

- 1. Calibration's quality** strongly depends and is limited by the **observations' quality**.
- 2. Stationary Hypothesis:** it is implicitly assumed that the bias doesn't change when applied to a non-observed period, introducing additional uncertainties (Raisanen and Raty, 2012; Maraun, 2012).



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