

# **BLACK BOX TESTING (II)**



**Random Testing**

# **Random testing (monkey testing)**

**Having difficulties to formulate equivalence classes (equivalence relation), random testing can be exercised**

**Random selection of inputs following some probability distribution function (uniform, normal, etc.)**

**Effectiveness of testing (number of test cases) depends upon the “size” of equivalence classes**

# Infinite monkey theorem



a monkey hitting keys at random on a typewriter keyboard for an infinite amount of time will almost surely type any given text, such as the complete works of William Shakespeare.

# **Random testing (monkey testing)**

**input domain  $E = [0,1]^n$**

**Equivalence class:**

**$E_1$ = hypercube: e - length of side**

**$E_2 = E - E_1$**

**Prob (x in  $E_1$ ) =  $e^n$**

# Random testing (monkey testing)

input domain  $E = [0,2]^n$

Equivalence class: hyperball of unit radius ( $r=1$ )

n	$r^n$	volume $V(\text{hyperball})$
2	4	$3.14 (\pi r^2)$
3	8	$4.18 (4/3\pi r^3)$
5	32	5.26
10	1.024	5.26
20		2.55
40		$3.60 \times 10^{-9}$
60		$3.09 \times 10^{-18}$

$$V = \frac{\pi^{n/2}}{\Gamma(1 + \frac{n}{2})} r^n$$

# Fuzz testing (fuzzing)

automated software testing:  
injecting invalid, random, unexpected inputs (data) to reveal  
software vulnerabilities

a spectrum of options: from random data to crafted inputs

## **Focus on anomalies:**

- memory leaks, failing built-in assertions, crashes
- exception handling
- buffer overflows
- injection flaws (SQL injections)
- denial of service (DOS)

# Fuzz testing: applications

2012, Google **ClusterFuzz**,  
a cloud-based fuzzing infrastructure for security-critical components of  
the Chromium web browser

2016, Microsoft **Project Springfield**,  
a cloud-based fuzz testing service for finding security critical faults in software.

2020, Microsoft **OneFuzz**,  
a self-hosted fuzzing-as-a-service platform automating the detection of software  
faults. Windows and Linux are supported.

# Operational Profiles

# Operational profiles

Some equivalence classes  $A_i$ 's used more frequently

Test software as if it were used by customers

**Operational profile (OP): list of disjoint operations and probabilities of occurrence**

Set S

Collection of subsets  $A_1, A_2, \dots, A_c$   
such that they satisfy the following conditions

• Mutually exclusive

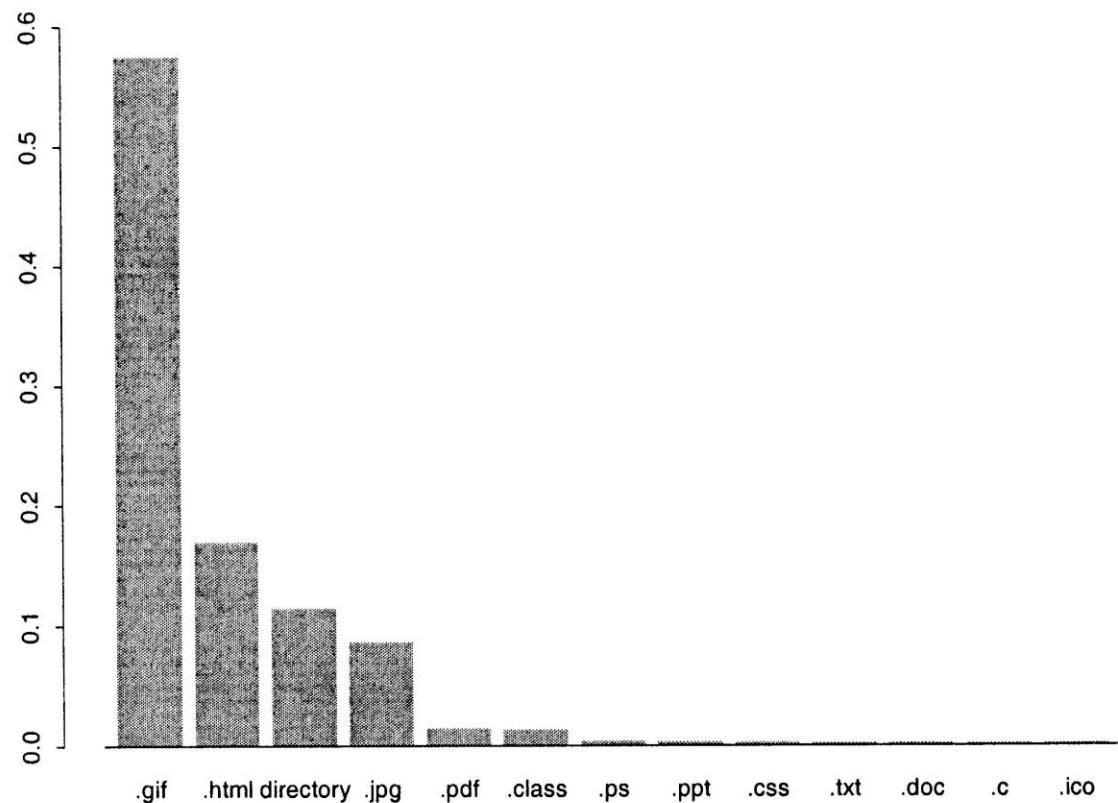
• Collectively exhaustive

# Operational profile

**Usage frequencies (hits) for different types of requested files for a given site**

File type	Hits	% of total
.gif	438536	57.47%
.html	128869	16.89%
directory	87067	11.41%
.jpg	65876	8.63%
.pdf	10784	1.41%
.class	10055	1.32%
.ps	2737	0.36%
.ppt	2510	0.33%
.css	2008	0.26%
.txt	1597	0.21%
.doc	1567	0.21%
.c	1254	0.16%
.ico	849	0.11%
Cumulative	753709	98.78%
Total	763021	100%

# Operational profile



# **Operational profiles**

**Progressive testing – start with testing operations with the higher probability of occurrence**

## **Benefits:**

- Productivity improvement and schedule gains
- Faster introduction of new products by implementing highly used features quickly to capture market share
- Better communication with customers and better customer relations
- High return on investment (lower cost)

# Benefits of operational profiles

For AT&T – PBX switching system project:

- Customer-reported problems and maintenance costs by factor of 10
- System testing time by factor of 2
- Product introduction time by 10%

# **Definition- operational profile**

**Profile – a set of disjoint (only one can occur at a time) alternatives with the probability that each will occur.**

**A occurs 60% of time; B occurs 40% time**

**Profile (A, 0.6) (B, 0.4)**

# Profile

OP considered as a prime candidate for testing *large scale software with many users and diverse usage environments*

Once OP has been constructed, it supports statistical testing by some sampling procedure to select test cases according to the highest probability values

# Profile

**Economic gain**

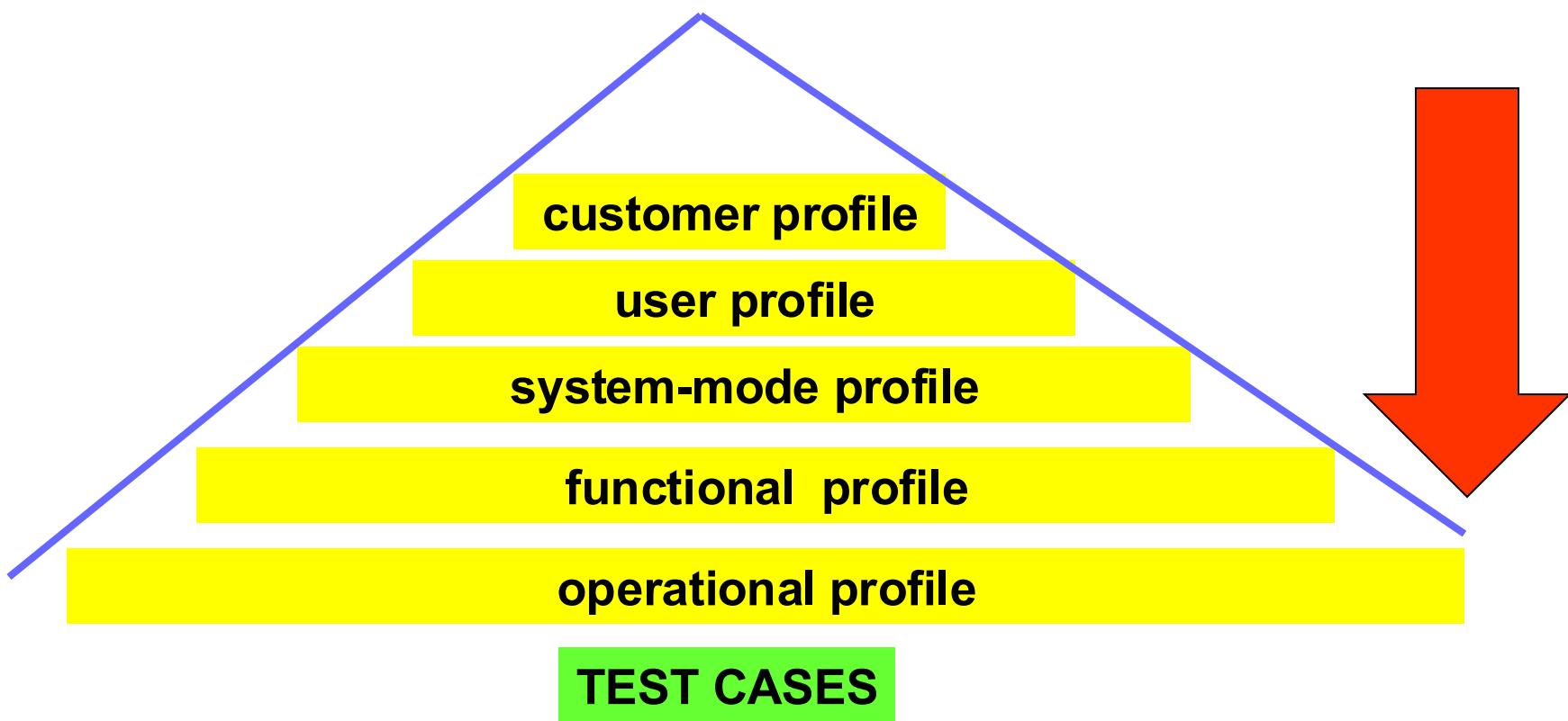
**Engineering judgment**

*Frequently used functionality*

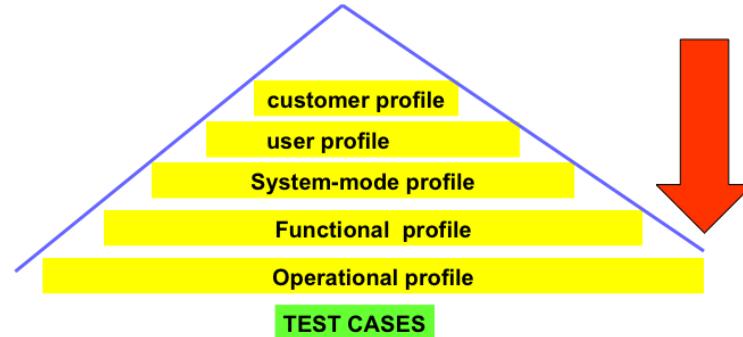
*Rarely used functionality whose failures could lead to disastrous consequences*

# Development of operational profiles: top-down approach (Musa)

Looking at use of system from a progressively narrowing perspective- from customer down to operation



# Profiles



**Customer profile**- person, group, institution that acquires the system

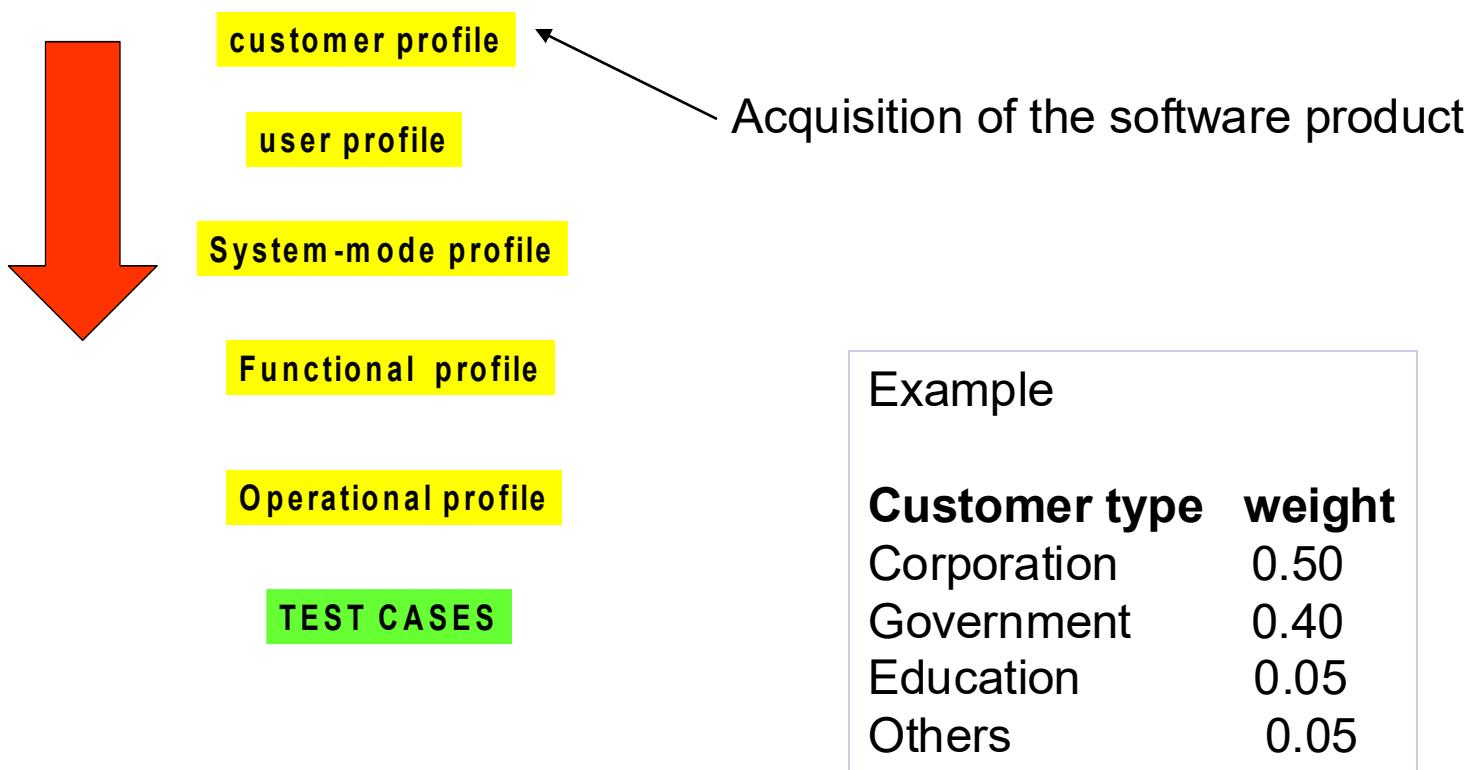
**User profile** – set of users who employ the system in the same way

**System mode-profile** - set of functions (operations) grouped for convenience in analyzing execution behavior. For instance, administrative mode, maintenance mode, overload mode, normal, initialization...

**Functional profile** – quantitative picture of the relative use of different functions (usually developed during requirement definition; a part of feasibility study)

**Operational profile**- consists of operations which represent a particular task with certain specific input variables

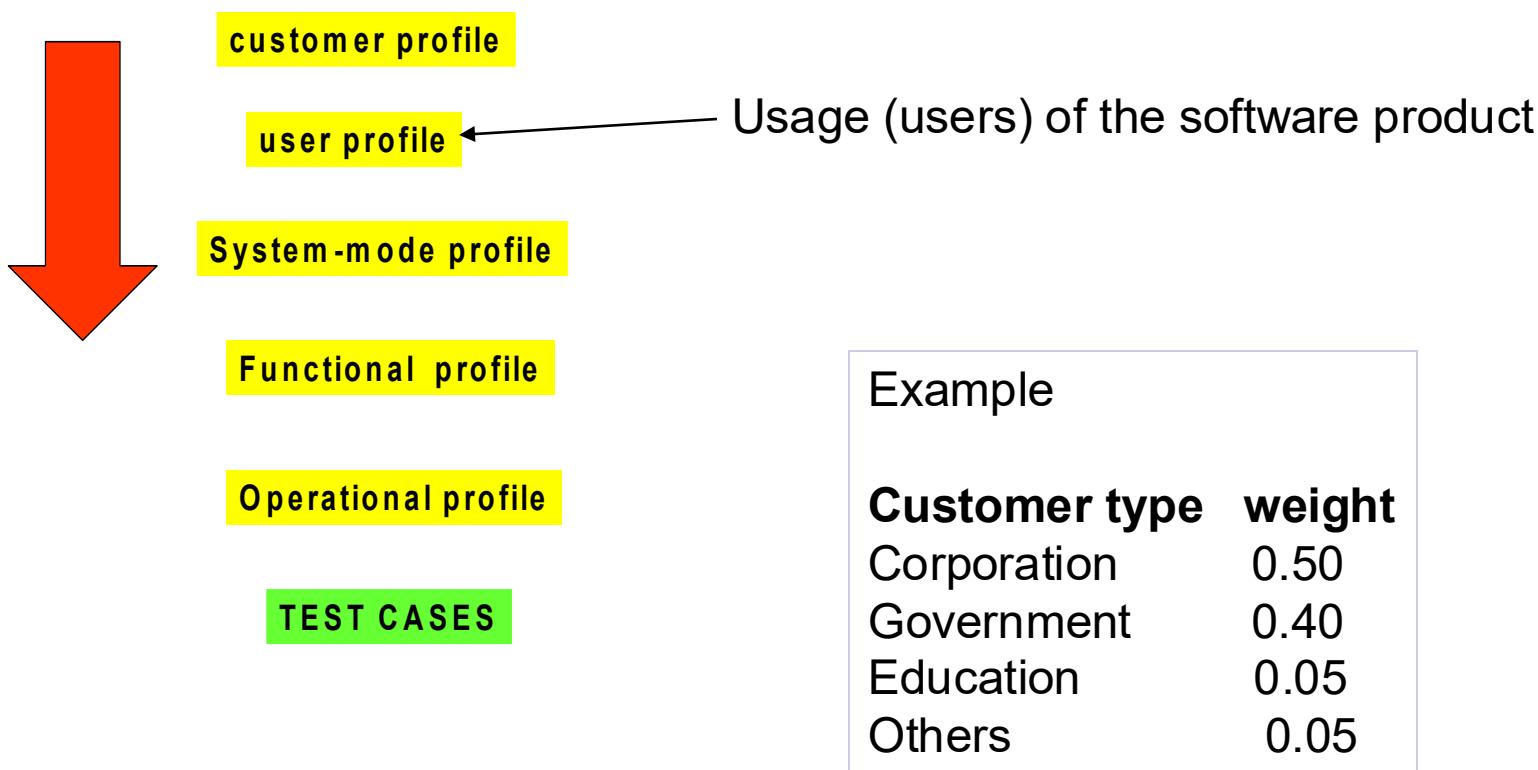
# Development of operational profiles



Example

<b>Customer type</b>	<b>weight</b>
Corporation	0.50
Government	0.40
Education	0.05
Others	0.05

# Development of operational profiles



# User profile

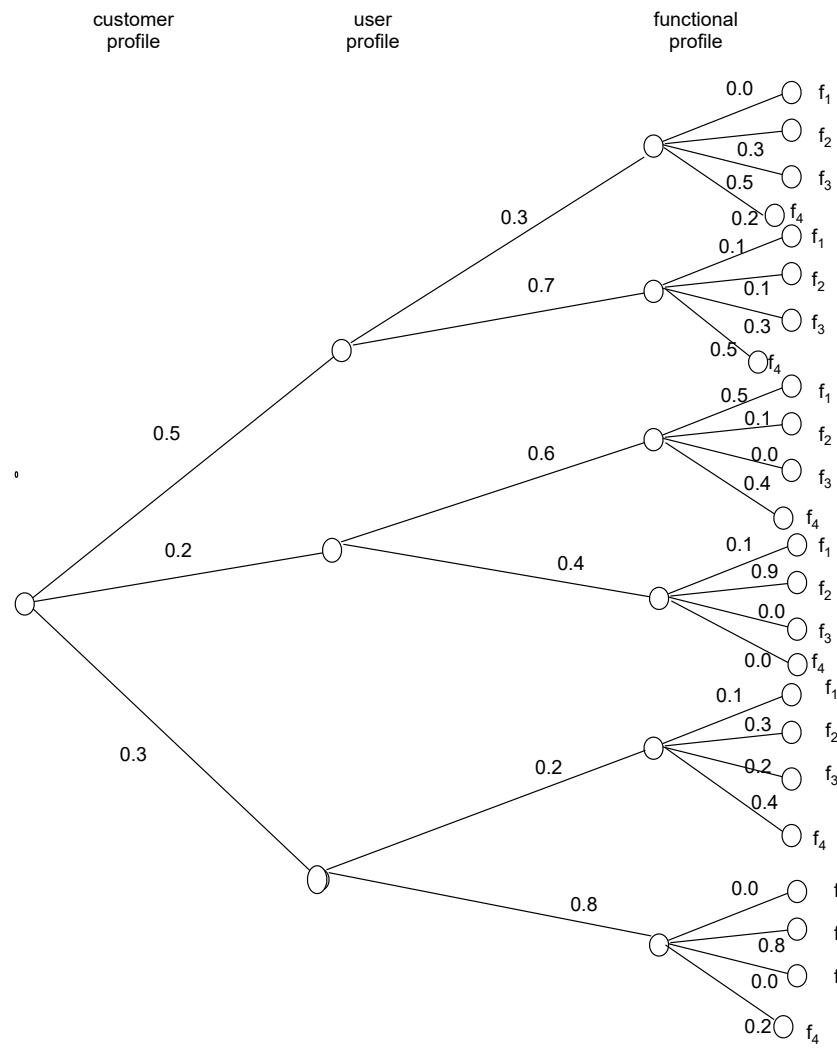
Example

**Customer type weight**

Corporation	0.50
Government	0.40
Education	0.05
Others	0.05

User Type	Customer type				<b>overall user profile</b>
	corp	gov	edu	others	
	0.50	0.40	0.05	0.05	
End user	0.80	0.90	0.90	0.70	<b>0.84</b>
Datab. Admin	0.02	0.02	0.02	0.02	<b>0.02</b>
Programmer	0.18	0.00	0.00	0.28	<b>0.104</b>
3 <sup>rd</sup> party	0.00	0.08	0.08	0.00	<b>0.036</b>

# User profile-graph representation



# **Construction of operational profiles**

**Measurements of usage  
(at customer installations; business sensitive data)**

**Survey of target customers**

**Usage estimation based on expert opinions**

# Faults and minimal number of tests

A given test is aimed at discovering a collection of faults

Determine a minimal number of tests “covering” all faults

fault	t1	t2	t3	t4
f1		1		
f2	1	1	1	
f3	1		1	
f4			1	1
f5		1		1

Fault-test coverage matrix  $D=[d_{ij}]$

# Faults and minimal number of tests

**Introduce binary variable:**

$c_i = 1$  if test  $i^{\text{th}}$   $t_i$  is included in a collection of tests,  
 $c_i = 0$ , otherwise

fault	t1	t2	t3	t4
f1		1		
f2	1	1	1	
f3	1		1	
f4			1	1
f5		1		1

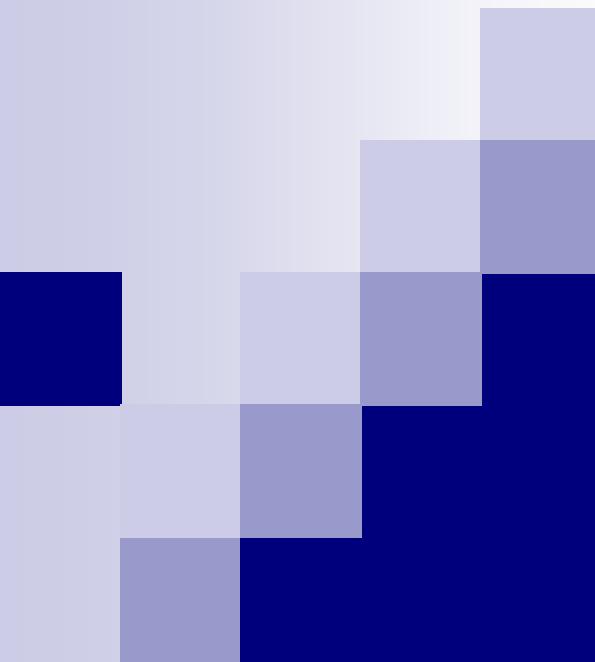
Select a minimal number of tests (collection of tests) so that all faults are covered

$$\text{Min } \{c_1 + c_2 + c_3 + c_4\}$$

subject to coverage all faults

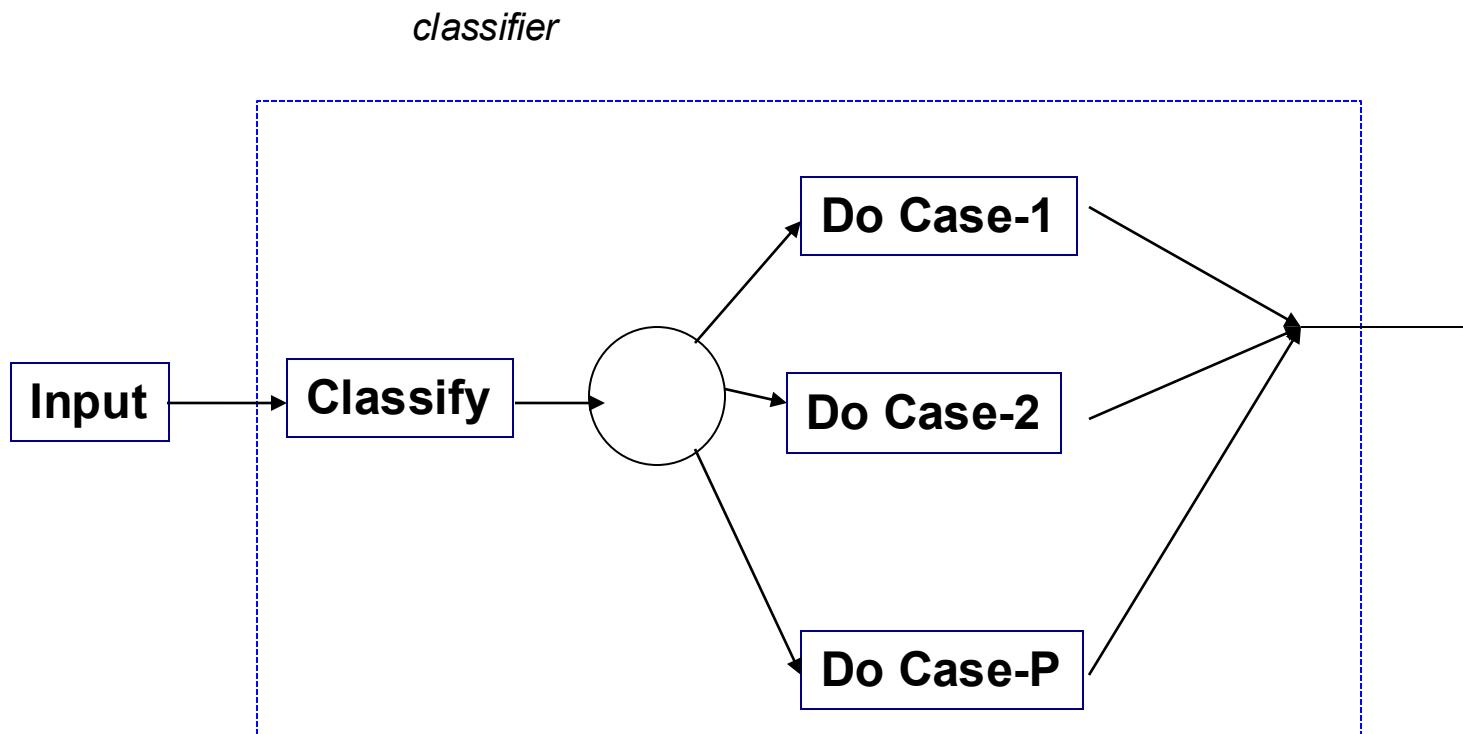
$$\sum_j d_{1j} c_j \geq 1 \quad \sum_j d_{2j} c_j \geq 1 \quad \sum_j d_{3j} c_j \geq 1$$

$$\sum_j d_{4j} c_j \geq 1 \quad \sum_j d_{5j} c_j \geq 1$$



# **Input Domain Testing**

# Input Domain Testing

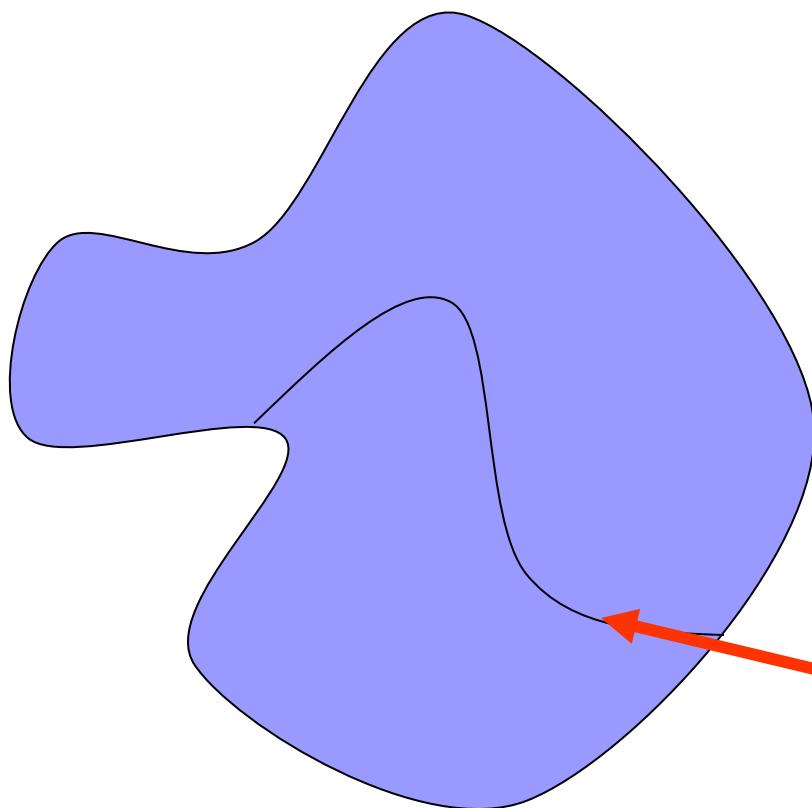


EXAMPLES – CATEGORIES OF COMPUTING

Parts of specifications given in terms of numerical inequalities

Heavy numeric processing with conditionals: payroll, taxes, financial computing

# Input domain testing: Basic notation (1)



**Input variables** as vectors of numbers

$$\mathbf{x} = [x_1 \ x_2 \ \dots \ x_n]^T$$

**Input domain**- all points representing all allowable inputs identified by the specifications

**Input sub-domain**- a subset of the input domain

$$f(x_1, x_2, \dots, x_n) \text{ rel } K$$

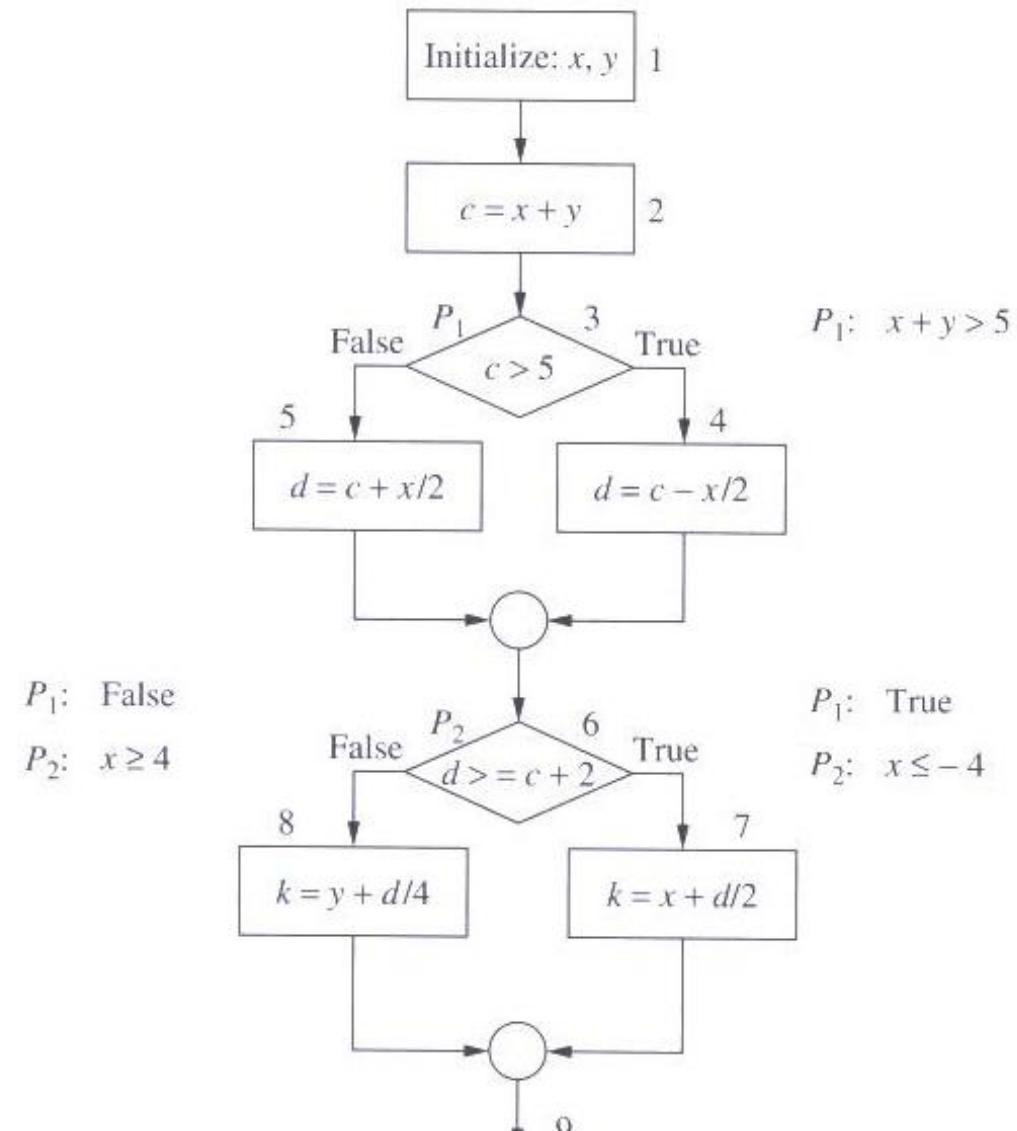
rel={ less than, greater than, equal,.....}

# Domain analysis: example (1)

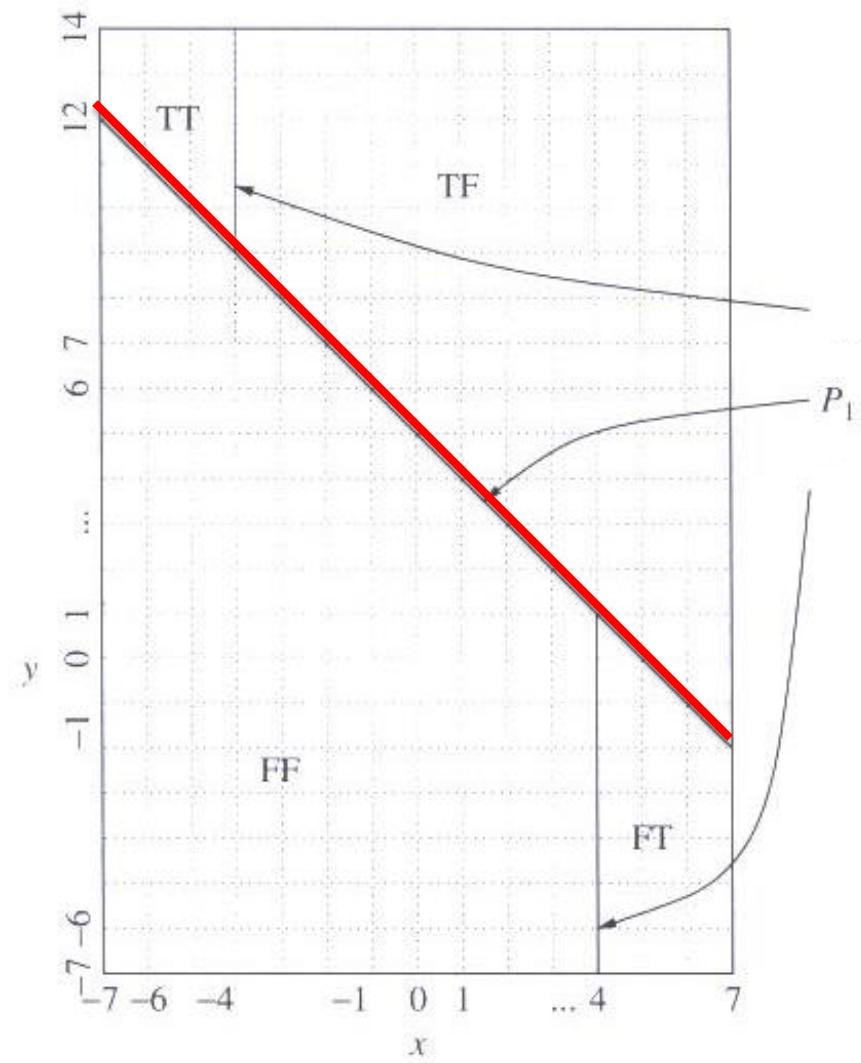
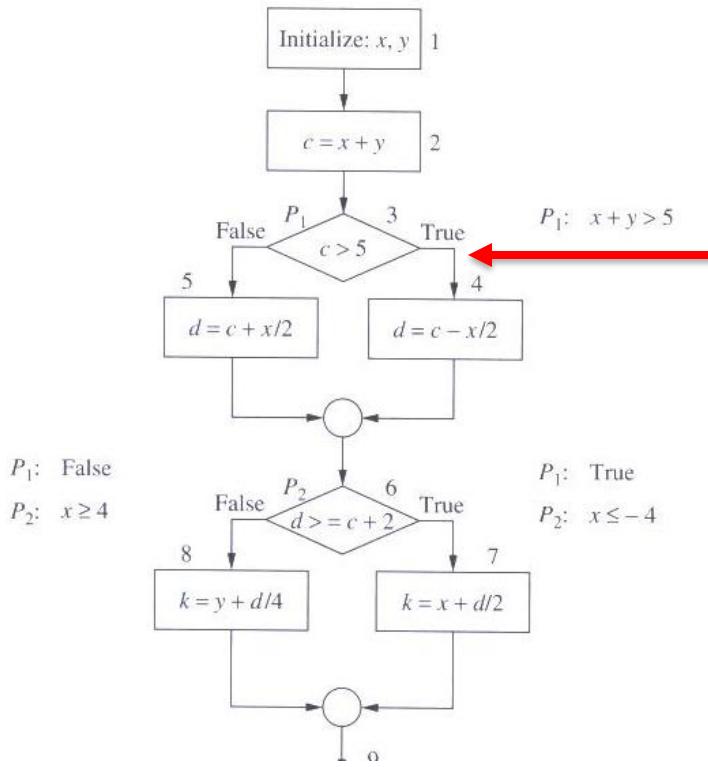
```
int codedomain(int x, int y){  
    int c, d, k  
    c = x + y;  
    if (c > 5) d = c - x/2;  
    else         d = c + x/2;  
    if (d >= c + 2) k = x + d/2;  
    else           k = y + d/4;  
    return(k);  
}
```

# Domain analysis: example (2)

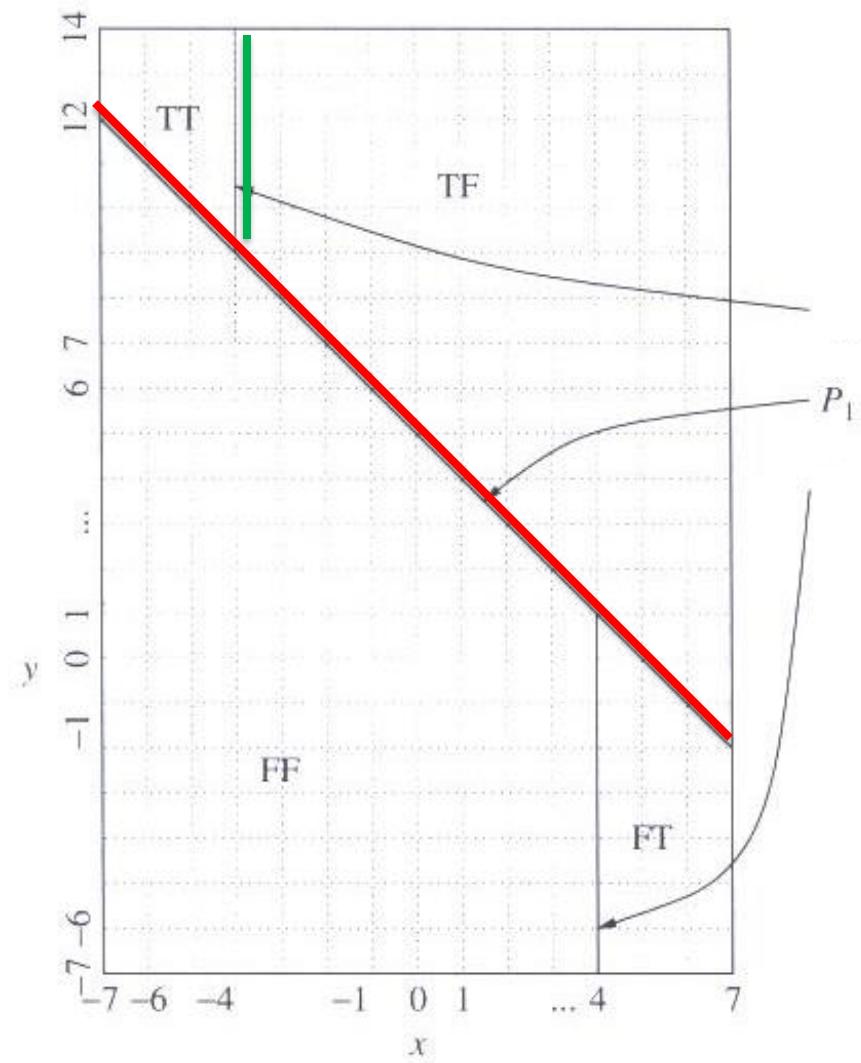
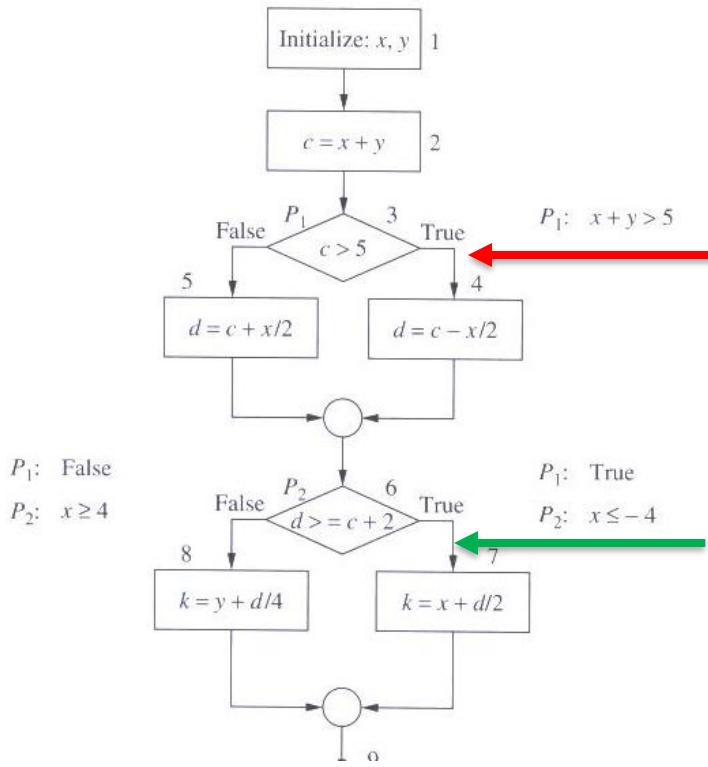
```
int codedomain(int x, int y){  
    int c, d, k;  
    c = x + y;  
    if (c > 5) d = c - x/2;  
    else d = c + x/2;  
    if (d >= c + 2) k = x + d/2;  
    else k = y + d/4;  
    return(k);  
}
```



# Domain analysis: example (3)

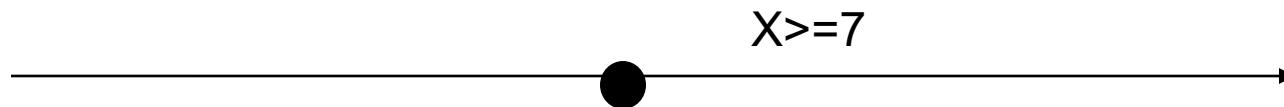


# Domain analysis: example (4)

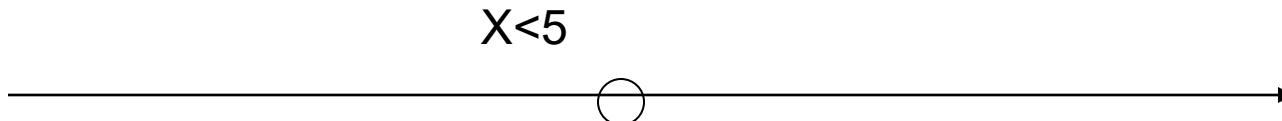


# Input domain testing: Basic notation (2a)

**Closed boundary** (with respect to a specific sub-domain) if all boundary points belong to this sub-domain



**Open boundary** (with respect to a specific sub-domain) none of the boundary points belongs to the sub-domain



# Input domain testing: Basic notation (2b)

**Open sub-domain** – a sub-domain with *all* open boundaries

**closed sub-domain** – a sub-domain with *all* closed boundaries

**Interior point** – a point belonging to a sub-domain but not on the boundary

**Exterior point** – a point not belonging to a sub-domain and not on its boundary

# Input domain testing: Basic notation (2c)



**side on which the domain is closed**

# Input domain testing: Basic notation (3)

**Domain partition** – partition of the input domain into a number of sub-domains  
(sub-domains mutually exclusive and exhaustive)

**Boundary** – where two sub-domains meet

$$f(x_1, x_2, \dots, x_n) = K \quad (\text{if inequalities used for sub-domains})$$

Linear and nonlinear boundaries  
(domains)

**Boundary point** – point on the boundary

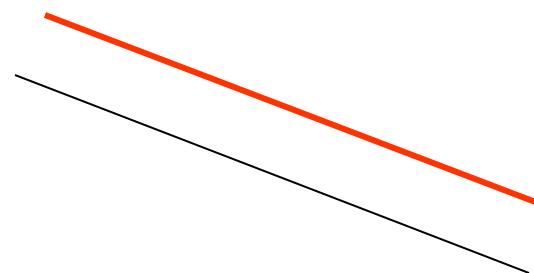
# Boundary problems

Specification – implementation gap

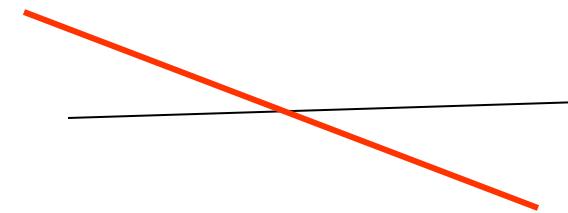
**Closure problem**  
( open – closed)



**Boundary shift**  
 $f(x_1, x_2, \dots, x_n) = K + \delta$



**Boundary tilt**  
 $f(x_1, x_2, \dots, x_n) = K$



# Boundary problems

**Missing boundary**



No boundary-  
All points receive the  
same treatment

**Extra boundary**



extra boundary-  
different treatment  
of points

# **Extreme Point Combination (EPC) Strategy**

**Domain testing strategy similar to capacity testing, stress testing or robustness testing (extreme input values, other limits are contested)**

**Heuristics: usage of extreme values (extreme points) combination**

# Extreme Point Combination (EPC) Strategy

For sub-domain, complete a simple domain analysis to identify the domain limits in each dimension (variable)

Choose for  $x_i$ : max  $x_i$ , min  $x_i$ , slightly under min  $x_i$ , slightly over max  $x_i$

Produce all possible combinations of inputs with each of its variables taking on one of the four values shown above. In n-dim space we end up with  $4^n$  points +1 -one point added inside the domain (to assure domain coverage strategy)

$n = 1 \quad 4+1 = 5$  points

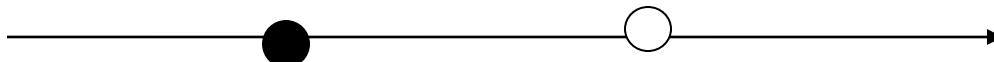
$n = 2 \quad 17$  points

# Extreme Point Combination (EPC) Strategy: Examples (1)

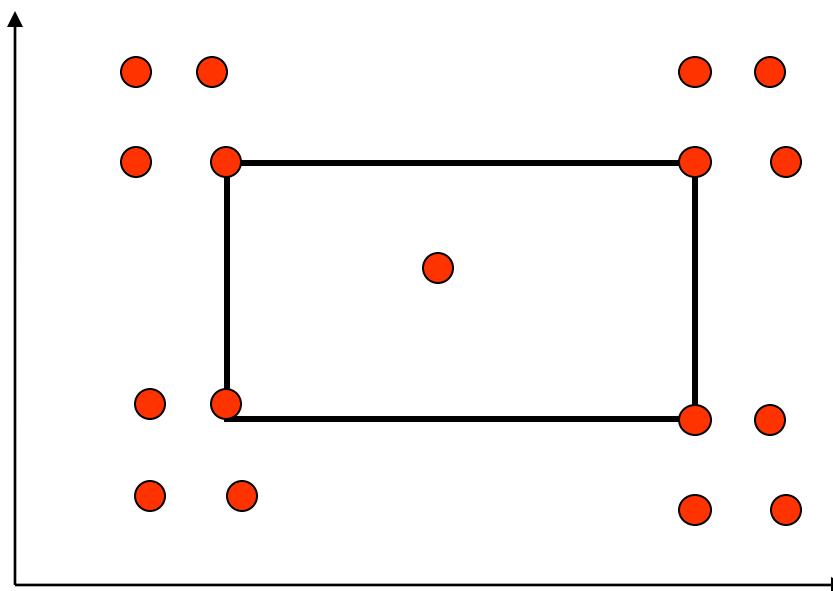
For sub-domain, complete a simple domain analysis to identify the domain limits in each dimension

Choose for  $x_i$ : max  $x_i$ , min  $x_i$ , slightly under min  $x_i$ , slightly over max  $x_i$

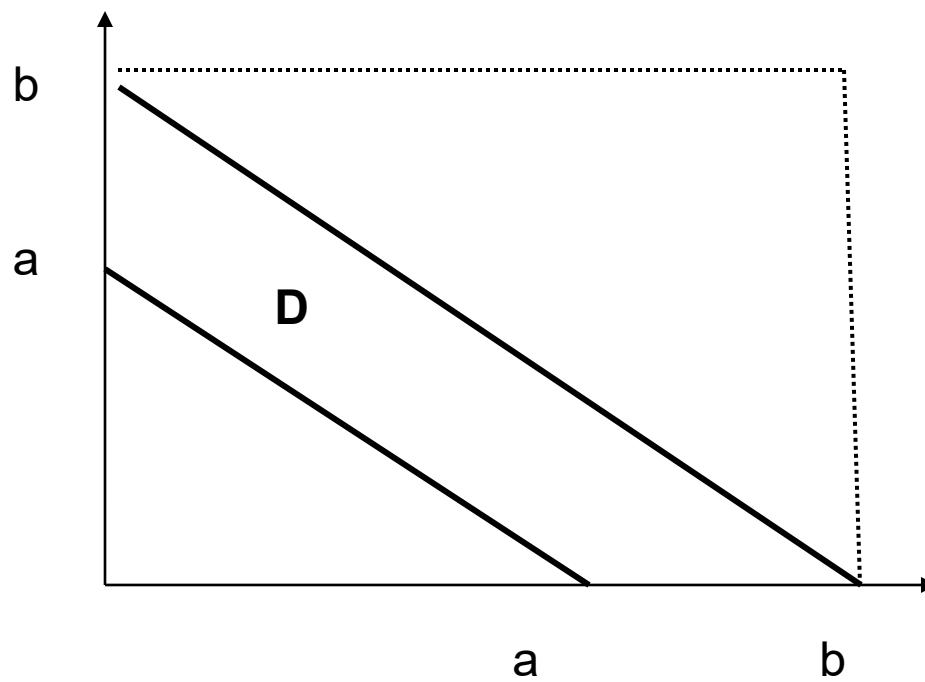
Produce all possible combinations of inputs with each of its variables taking on one of the four values shown above. In n-dim space we end up with  $4^n$  points +1 -one point inside the domain (domain coverage strategy)



# Extreme Point Combination (EPC) Strategy: Examples (2)

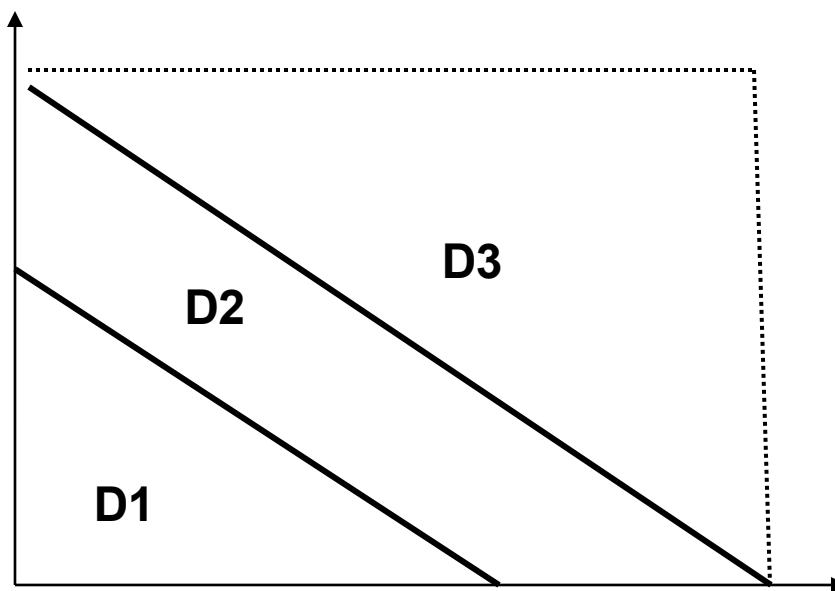


# Extreme Point Combination (EPC) Strategy: Examples (2a)



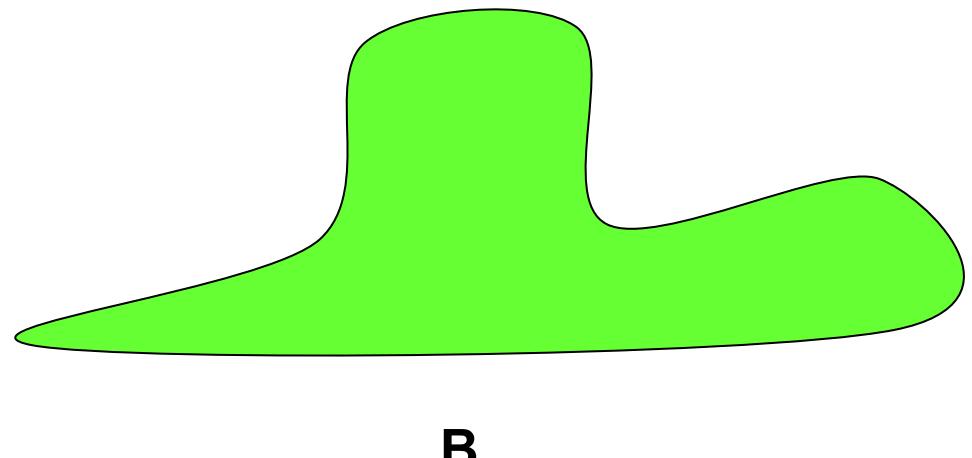
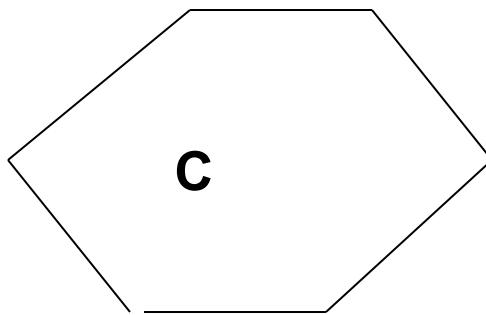
**Subdomain: D**

# Extreme Point Combination (EPC) Strategy: Examples (2b)



Subdomains: D1, D2, D3

# EPC in higher dimensional sub-domains



# Extreme Point Combination (EPC) for 1-dimensional sub-domain

Integers [0, 21)

EPC :

0, 21,

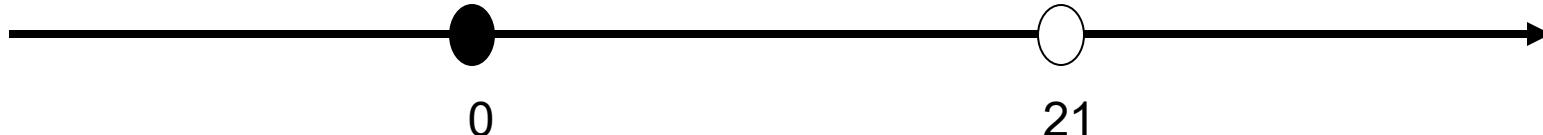
// min and max

-1, 22

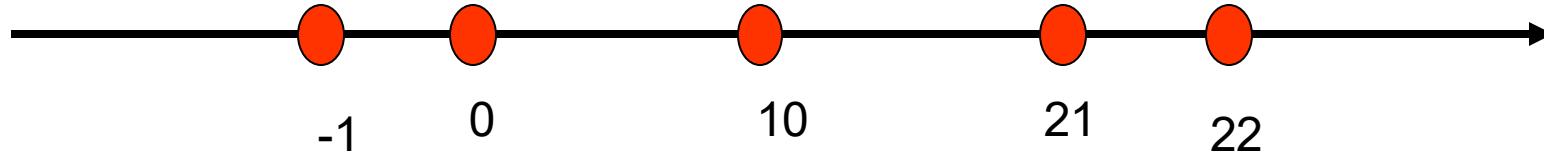
// below min and above max

10

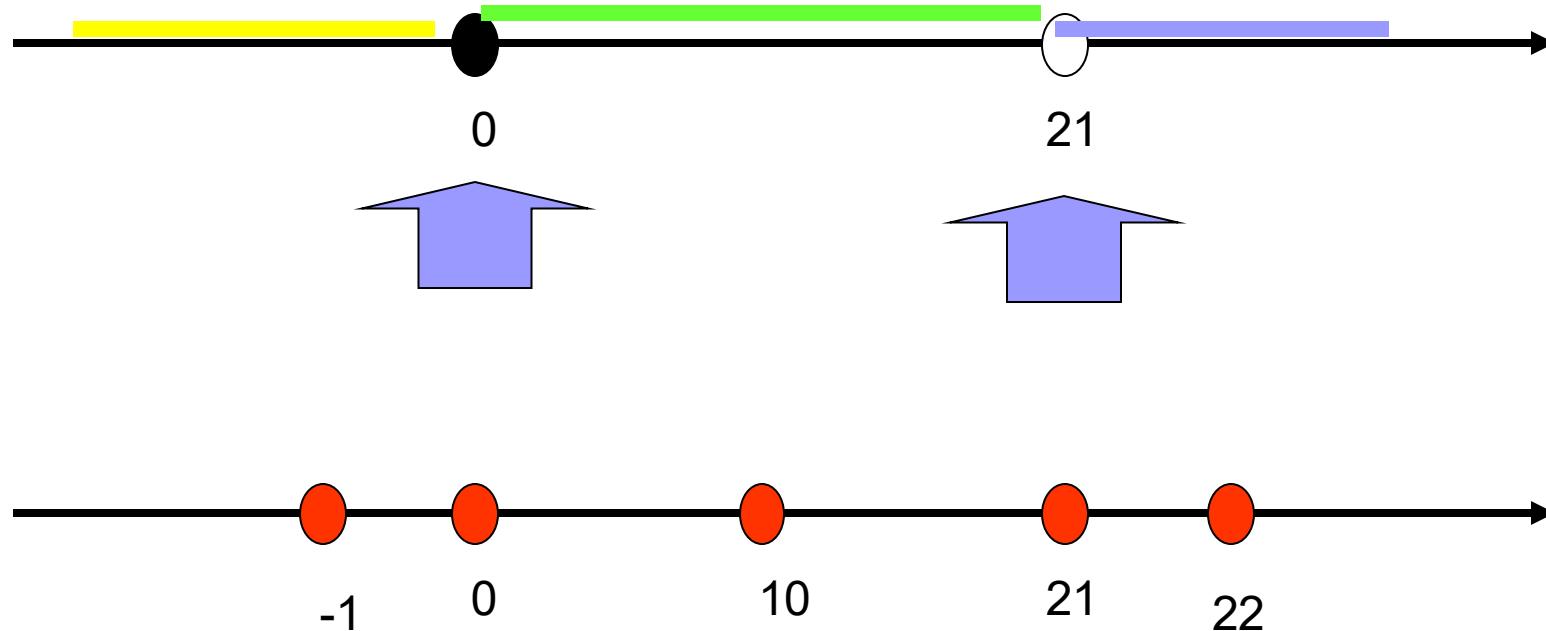
// interior point



# Extreme Point Combination (EPC) for 1-dimensional sub-domain

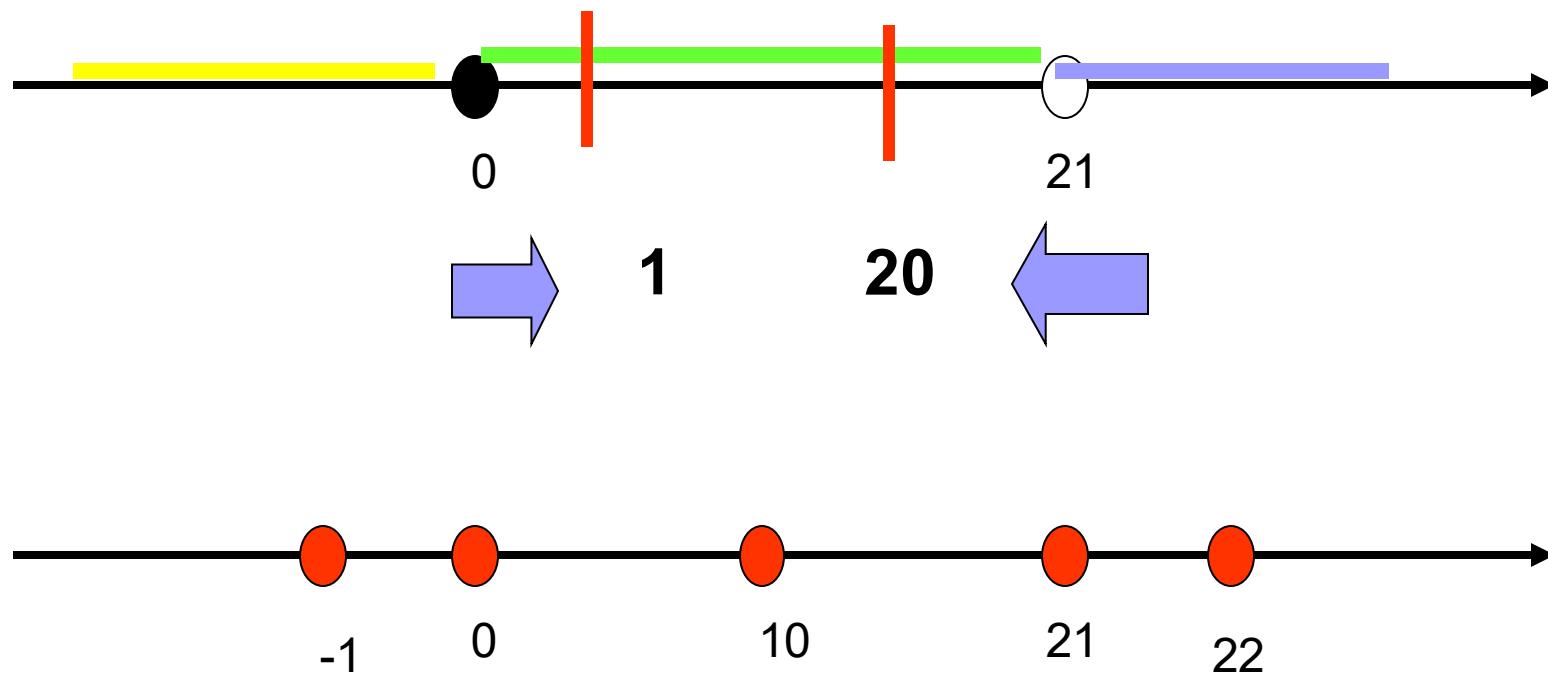


# Extreme Point Combination (EPC) for 1-dimensional sub-domain closure problem (open-closed)



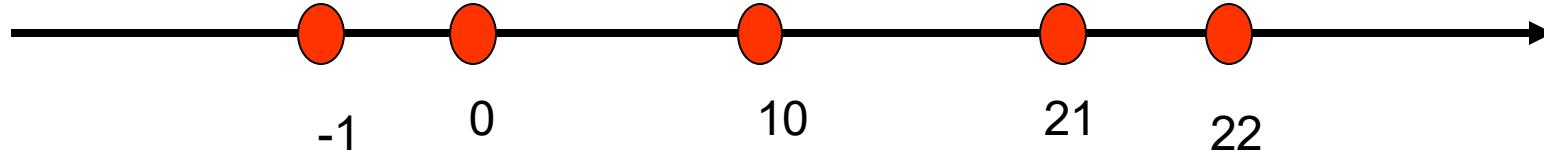
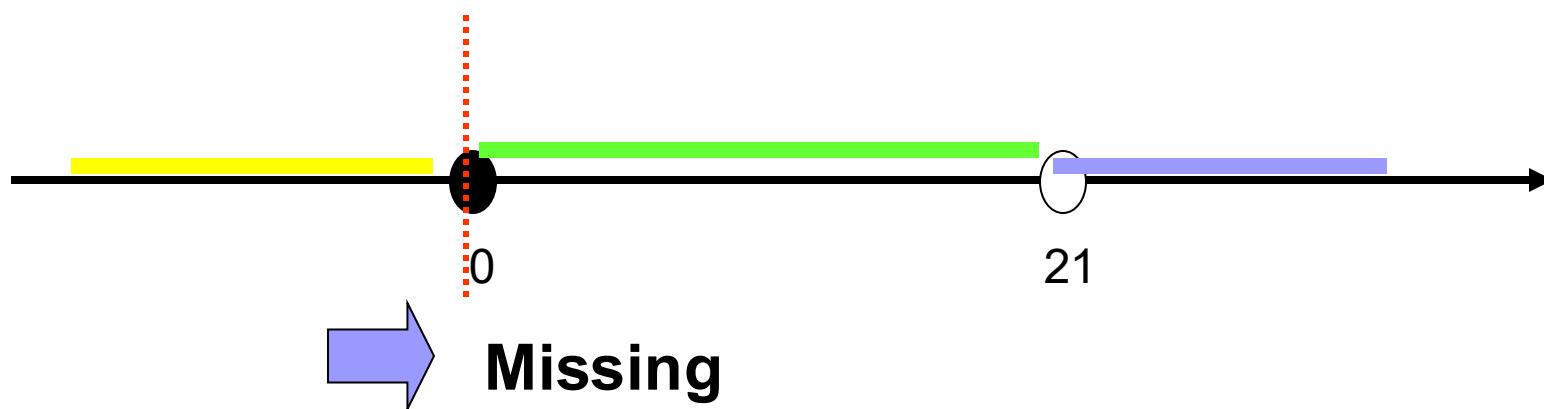
Closure problem is identified

# Extreme Point Combination (EPC) for 1-dimensional sub-domain boundary shift [1, 20]



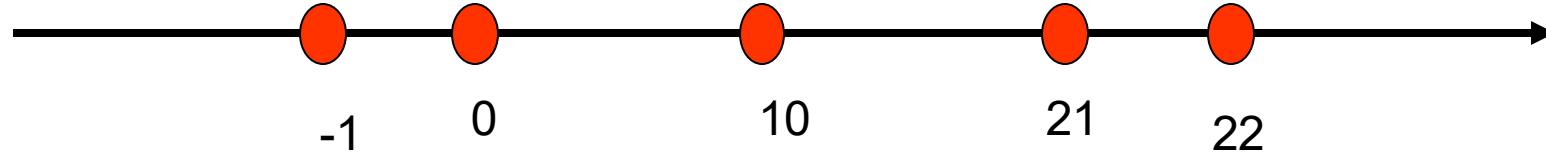
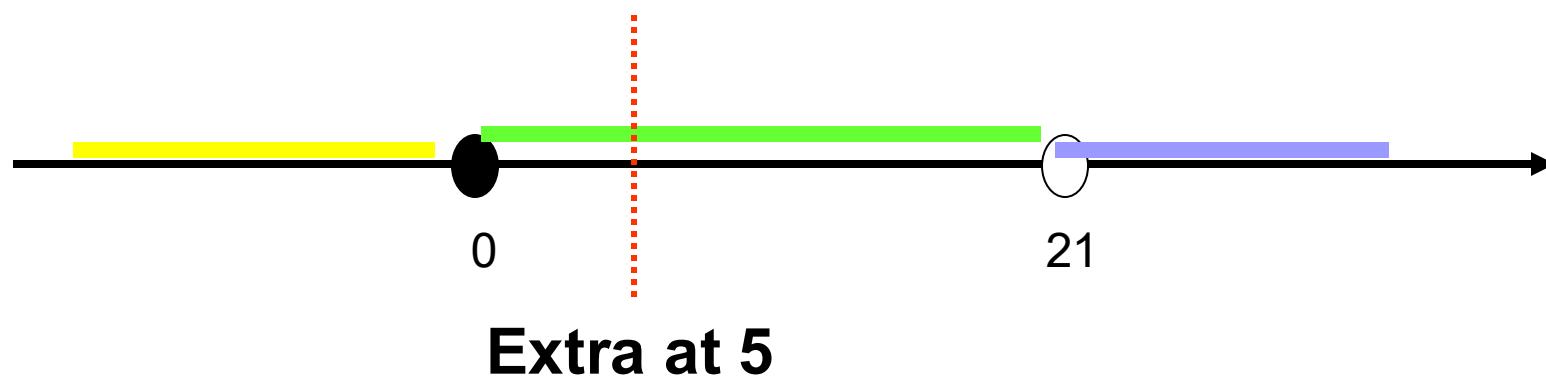
Boundary shift problem *could* be identified

# Extreme Point Combination (EPC) for 1-dimensional sub-domain missing boundary



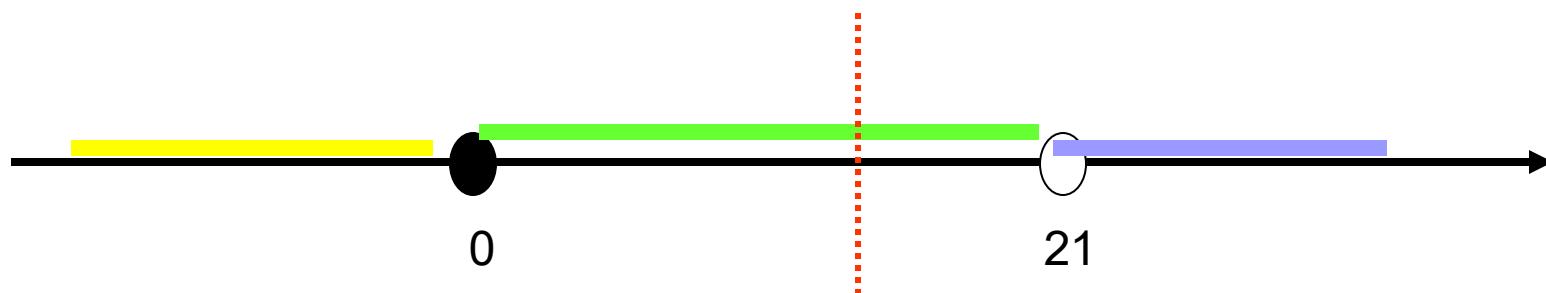
Missing boundary problem is identified

# Extreme Point Combination (EPC) for 1-dimensional sub-domain extra boundary

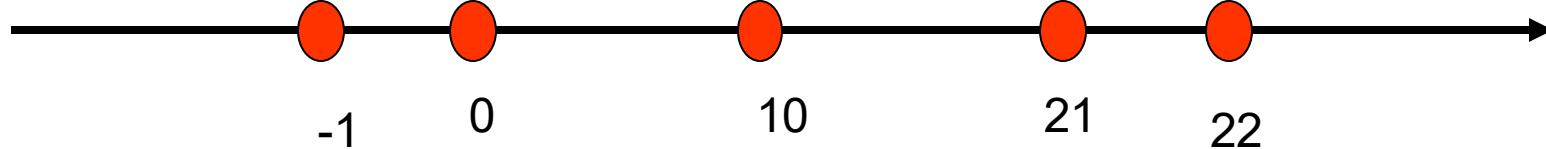


Extra boundary problem is identified

# Extreme Point Combination (EPC) for 1-dimensional sub-domain extra boundary



**Extra at 15**



Extra boundary problem is not identified

# Extreme Point Combination (EPC) for 1-dimensional sub-domain summary

<b>Closure</b>	YES
<b>Missing boundary</b>	YES

<b>Boundary shift</b>	maybe
<b>Extra boundary</b>	maybe

# Weak n x 1 strategy

“n” points located on the boundary -- **ON** points  
1 point that is **OFF**

**Linear** boundary  $f(x_1, x_2, \dots x_n) = K$

‘n’ independent points fully defines this boundary – locate **ON** points on the boundary

OFF point: if open boundary then all **ON** points receive exterior processing  
Choose **OFF** point so it receives interior processing; keep close to boundary

if closed boundary then all **ON** points receive interior processing  
Choose **OFF** point so it receives exterior processing; keep close to boundary

# Weak $n \times 1$ strategy

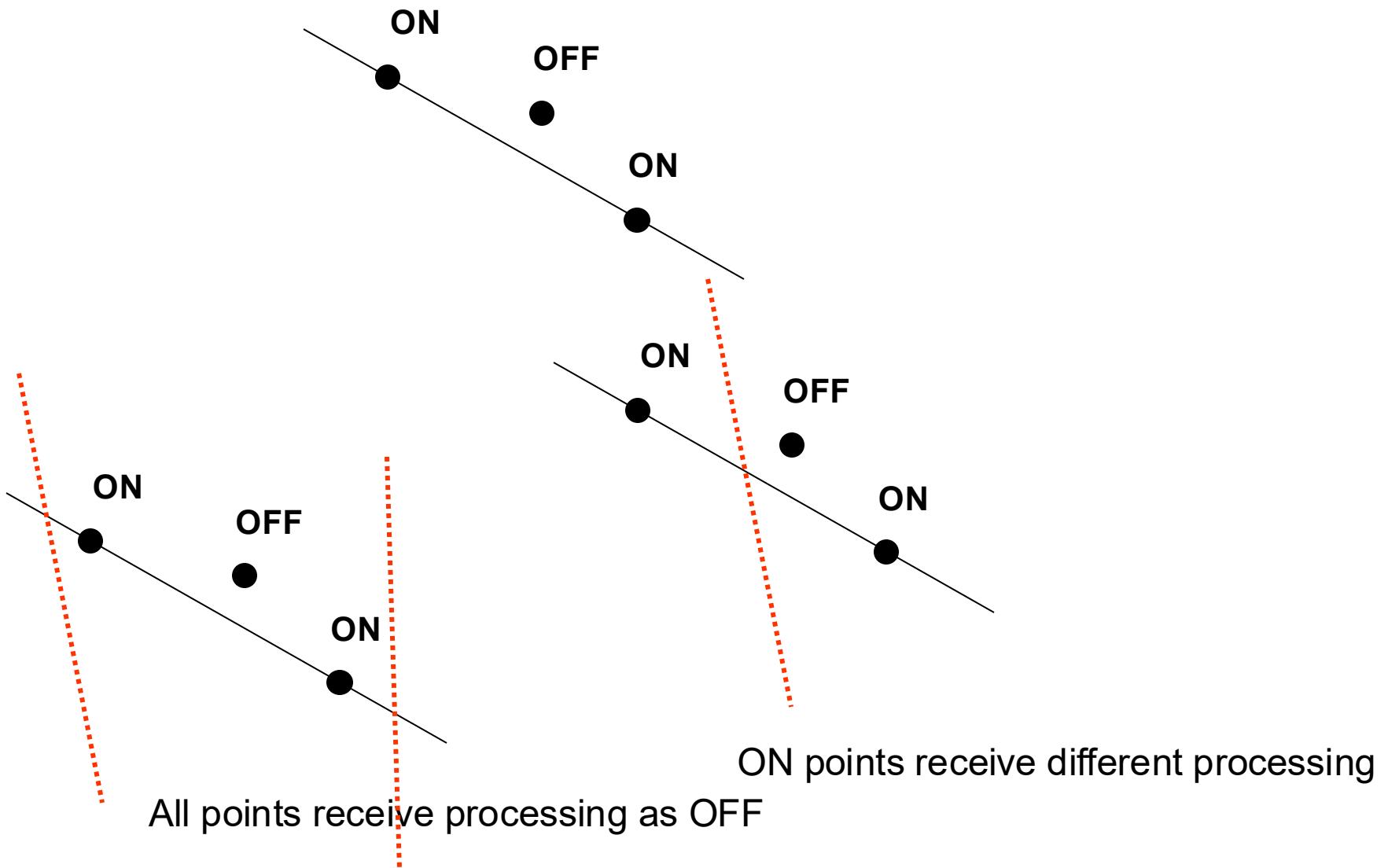
“n” points located on the boundary -- **ON** points  
1 point that is **OFF**

**ON** points on the boundary, say  $\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n$

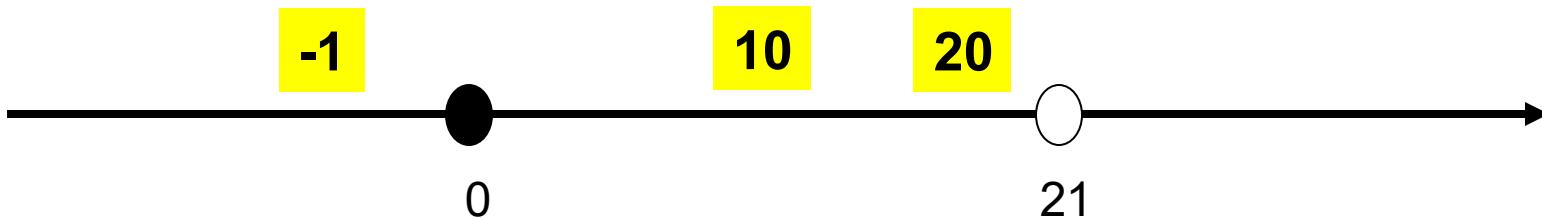
**OFF** point:

Midpoint between **ON** points,  $(\mathbf{x}_1 + \mathbf{x}_2 + \dots + \mathbf{x}_n)/n$ , move it small distance ( $\varepsilon$ ) off the boundary (outward or inward)

# Weak n x 1 strategy- boundary tilt



# Weak $n \times 1$ strategy- 1 dim example



**ON** points 0 and 21

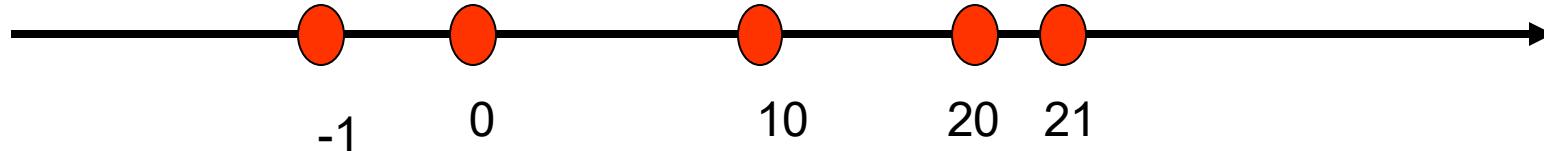
**OFF** points

0 closed boundary, receives interior processing, choose OFF as exterior, say -1

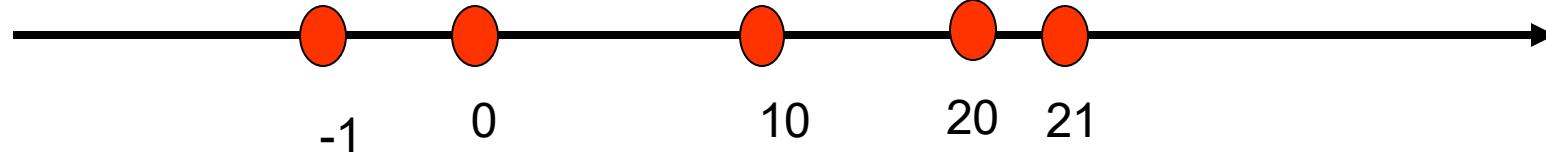
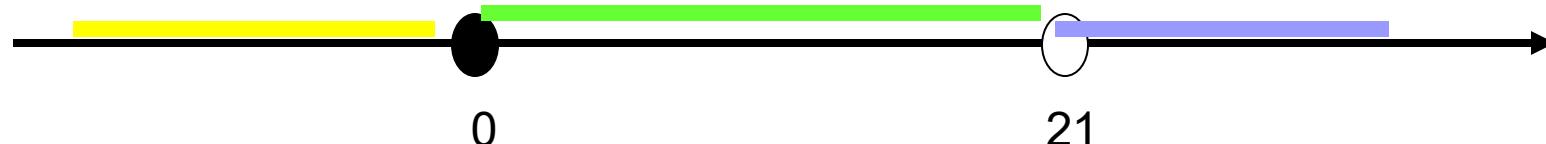
21 open boundary, receives exterior processing, choose OFF as interior, say 20

Also one point in the interior of subdomain, say 10

# Weak nx1 strategy for 1-dimensional sub-domain

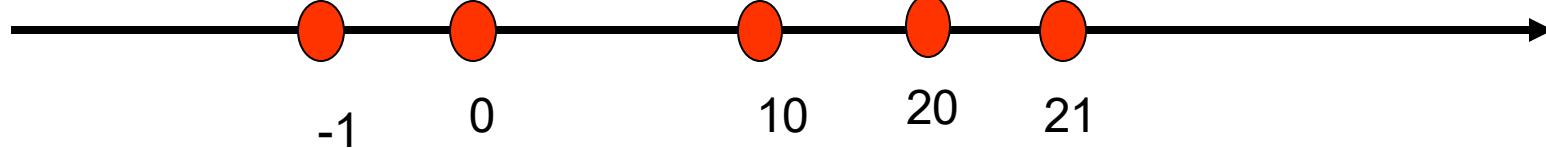
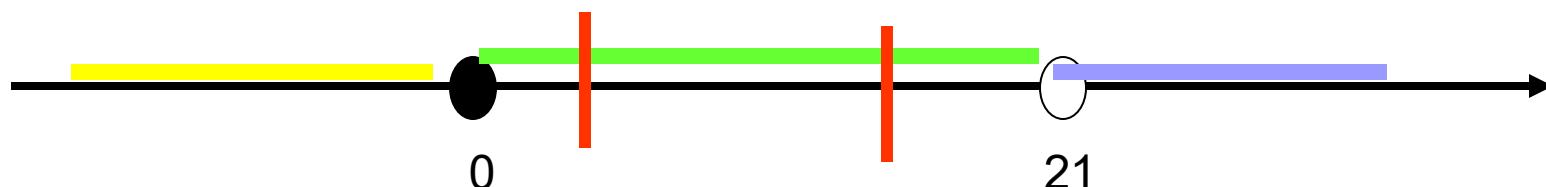


# Weak nx1 strategy for 1-dimensional sub-domain closure problem (open-closed)



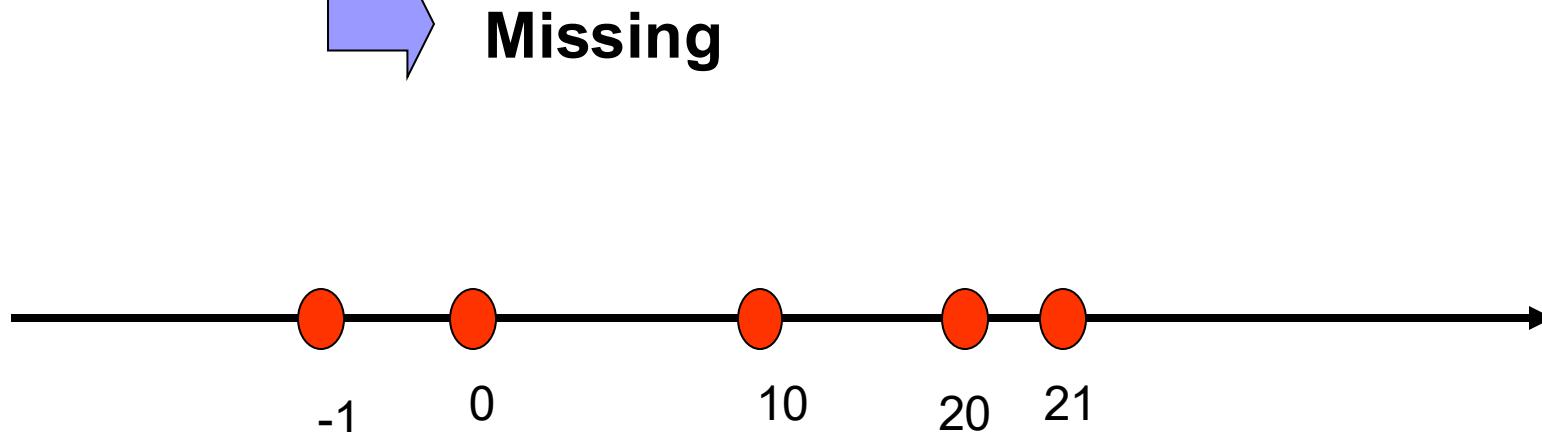
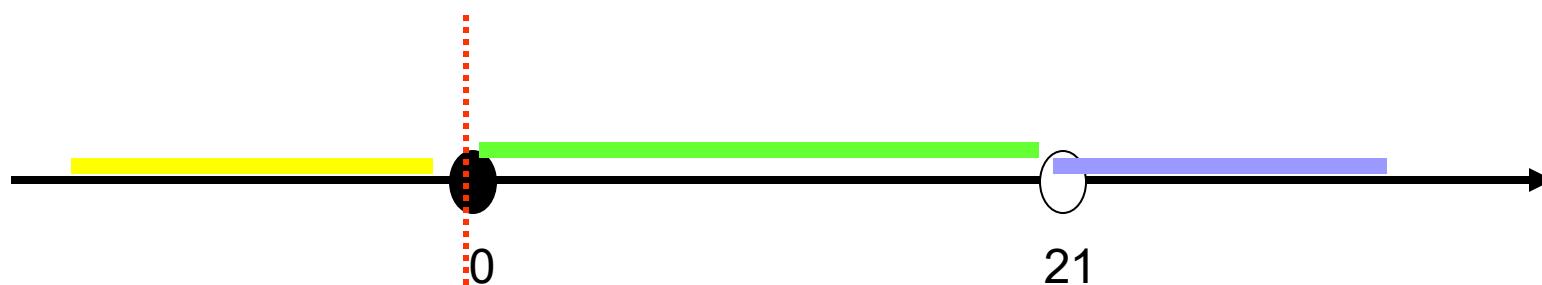
Closure problem is identified

# Weak nx1 strategy for 1-dimensional sub-domain boundary shift [1, 20]



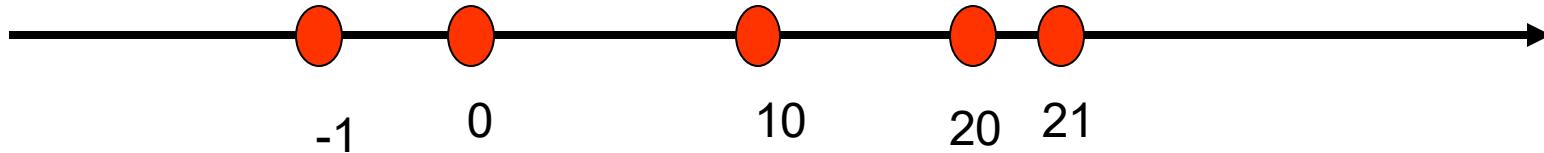
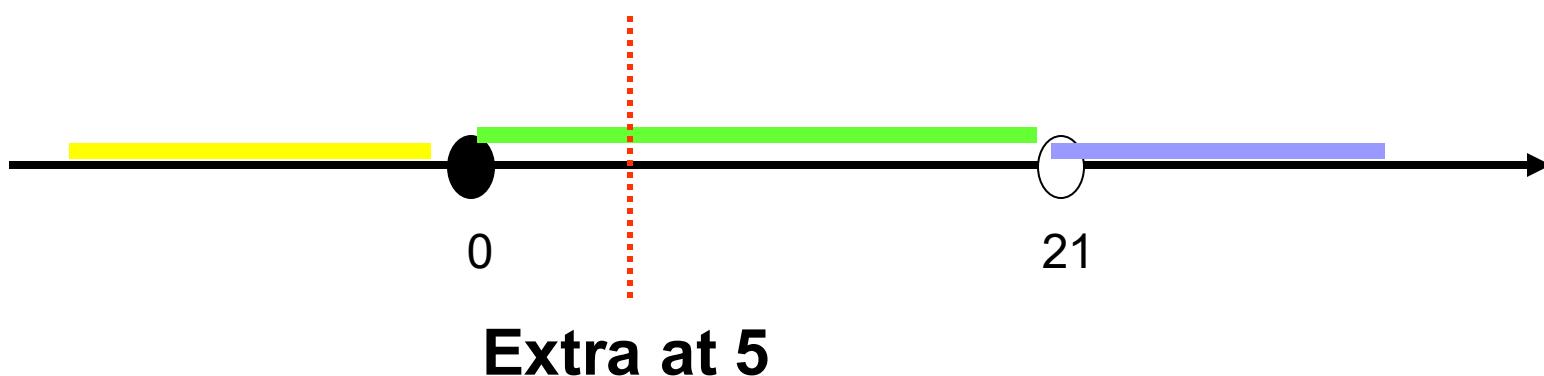
Boundary shift problem *is* identified

# Weak nx1 strategy for 1-dimensional sub-domain missing boundary



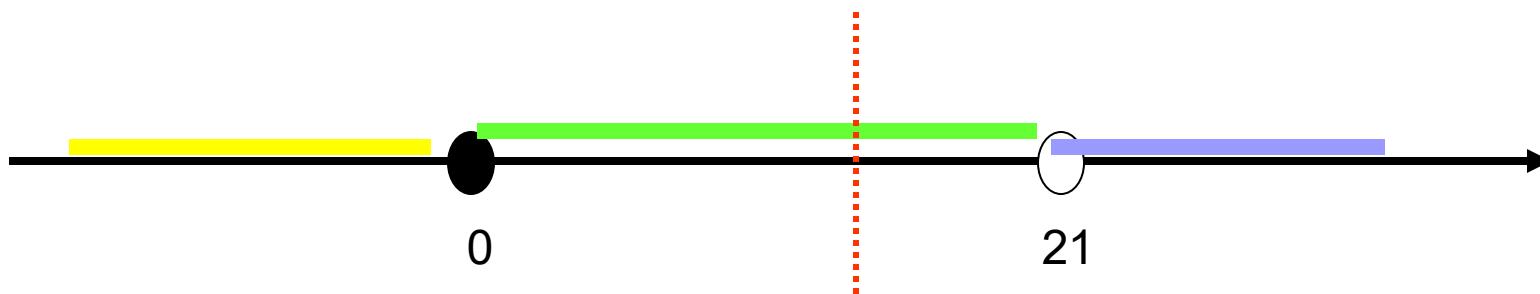
Missing boundary problem is identified

# Weak nx1 strategy for 1-dimensional sub-domain extra boundary

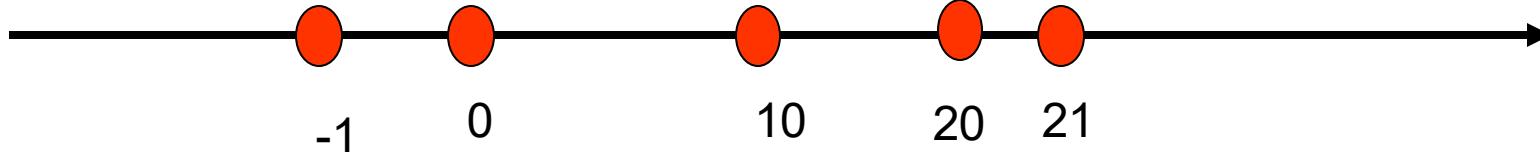


Extra boundary problem is identified

# Weak nx1 strategy for 1-dimensional sub-domain extra boundary



**Extra at 15**



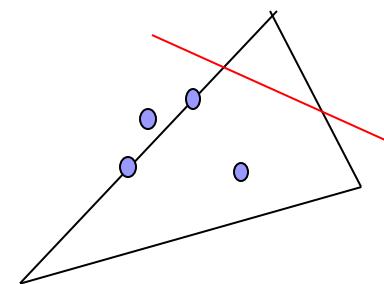
**Extra boundary problem is identified**

# Weak $n \times 1$ strategy

Closure problem

Missing boundary

Boundary tilt/shift

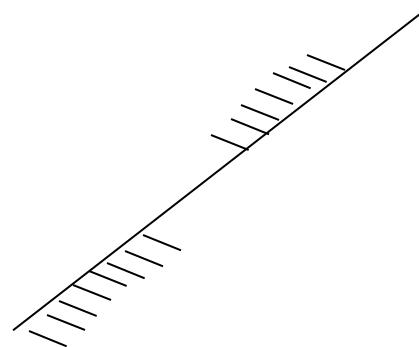


**Extra boundary** (in general- extra boundary near a vertex point being far away from any of the ON and OFF and the selected interior point)

# **strong n x 1 strategy**

**boundaries with inconsistencies**

**e.g., changing closure along the boundary**



# **Weak $n \times 1$ strategy and EPC**

**Consider sub-domain with “b” linear boundaries**

**Weak  $nx1$  strategy**

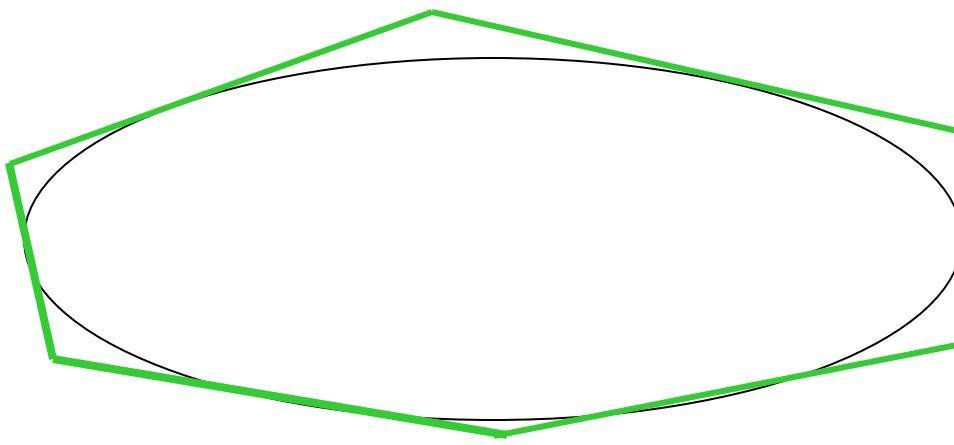
$$\text{No of points} = (n+1)b + 1$$

**EPC**

$$\text{No of points} = 4^n + 1$$

# Nonlinear boundaries

**Approximate boundary by a series of linear segments and formulate test cases for each segment (ON- OFF points)**



# Testing and specifications

## Inconsistencies in specifications

can be detected through

input domain testing

equivalence classes and boundary testing