Spring 2012 MST.

WeBWorK assignment M151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs due 02/08/2012 at 06:00pm

## /1.1.1.pg

From Rogawski ET section 1.1, exercise 1.

Use a calculator to find a rational number r such that

$$|r - \pi^4| < 10^{-5}$$

 $r = _{-}$ 

Let a = -6 and b = 1. Select every inequality which is true.

Which inequalities are true?

- A. |a| < |b|
- B.  $\frac{a}{b} < 0$
- C. ab > 0
- D.  $\frac{1}{b} < \frac{1}{a}$  E. a < b

## 3. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs-

From Rogawski ET section 1.1, exercise 3.

Express the interval in terms of an inequality involving absolute value:

### 4. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs-

From Rogawski ET section 1.1, exercise 4.

Express the interval in terms of an inequality involving absolute value:

### 5. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs-

From Rogawski ET section 1.1, exercise 5.

Express the interval in terms of an inequality involving absolute value:

(0,4)

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

**Solution:** The correct solution is:

1. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs\_pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs\_ /1.1.10.pg

From Rogawski ET section 1.1, exercise 10.

Solve the inequality:

$$|x-2| < 7$$

Answer: \_\_\_

2. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphse: You may enter your answer in interval or inequality notation. If your solution includes a decimal value, please round to at least three decimal places. If the inequality has no solution, enter No solution .

# 7. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs-

From Rogawski ET section 1.1, exercise 11.

Solve the following inequality. Enter the answer in interval

|2x+1| < 7

Answer: \_

### 8. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs-/1.1.13.pg

From Rogawski ET section 1.1, exercise 13.

Express the set of numbers x satisfying the given condition as an interval:

SOLUTION: (Instructor solution preview: show the student solution after due date. )

**Solution:** The correct solution is:

(-11,11)

9. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs-

From Rogawski ET section 1.1, exercise 15.

Express the set of numbers x satisfying the given condition as an interval:

$$|x-9| < 10$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

**Solution:** 

The expression |x-9| < 10 is equivalent to -10 < x-9 <10. Therefore -1 < x < 19, which represents the interval (-1,19).

### 10. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_ands@raphs\_to the right of 4 or /1.1.17.pg

From Rogawski ET section 1.1, exercise 17.

Express the set of numbers x satisfying the given condition as an interval:

$$|7x - 4| \le 5$$

SOLUTION: (Instructor solution preview: show the student solution after due date. )

#### Solution:

The expression  $|7x-4| \le 5$  is equivalent to  $-5 \le 7x-4 \le 5$ .

Therefore  $-1 \le 7x \le 9$  and then  $-\frac{1}{7} \le x \le \frac{9}{7}$ , (or  $-0.142857142857143 \le x \le 1.28571428571429$ )

which represent the interval  $\left[-\frac{1}{7}, \frac{9}{7}\right]$ 

### 11. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_ $6\overline{7}$ aphs- $r1 = 27.\overline{27} - 0.\overline{27} = 99r1.$ /1.1.23.pg

From Rogawski ET section 1.1, exercise 23.

Match the inequalities 1. - 6. with the corresponding statements A - F:

- $-1. |a-\frac{1}{10}| < 4$
- a 2.  $|a 4| < \frac{1}{10}$ a 3. |a 3| < 10
- $_{--}4. \ a > 10$
- \_\_\_5. |a| > 4
- \_\_\_6. 1 < *a* < 4
  - A. a lies to the right of 10
  - B. The distance from a to 2.5 is at most 1.5
  - C. a lies either to the left of -4 or to the right of 4
  - D. a lies between -7 and 13
  - E. a is less than 4 units from 1/10
  - F. The distance from a to 4 is less than 1/10

Note that you only have four attempts on this question.

SOLUTION: (Instructor solution preview: show the student solution after due date.)

### **Solution:**

On the number line, numbers greater than 10 appear to the

hence a > 10 is equivalent to the numbers to the right of 10.

|a-4| measures the distance from a to 4; hence  $|a-4| < \frac{1}{10}$ 

by those numbers less than  $\frac{1}{10}$  from 4

 $|a - \frac{1}{10}|$  measures the distance from a to  $\frac{1}{10}$ ; hence  $|a - \frac{1}{10}| <$ 

by those numbers that are less than 4 units from  $\frac{1}{10}$ 

The inequality |a| > 4 is equivalent to a > 4 or a < -4; that

to the left of -4.

The interval described by the inequality |a-3| < 10 has a center at 3 and a radius of 10; that is

the interval of those numbers between -7 and 13.

The interval described by the inequality 1 < x < 4 has a center at 2.5 and a radius of 1.5

### 12. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graph /1.1.31.pg

From Rogawski ET section 1.1, exercise 31.

Express the repeating decimal  $r1 = 0.\overline{27}$  as a fraction. **Hint:** 100r1 - r1 is an integer.

Then express the repeating decimal  $r^2 = 0.4\overline{6}$  as a fraction.

SOLUTION: (Instructor solution preview: show the student solution after due date. )

### **Solution:**

Let  $r1 = 0.\overline{27}$ . We observe that  $100r1 = 27.\overline{27}$ . Therefore

Then 
$$r1 = \frac{27}{99} = \frac{3}{11}$$
.

Now let  $r2 = 0.4\overline{6}$ . Then  $100r2 = 46.\overline{6}$ . Therefore 100r2 - 10r2 = 90r2 = 42and  $r2 = \frac{42}{90} = \frac{7}{15}$ 

# 13. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graph

Find domain and range of the function:

$$f(x) = -13x$$

Domain: \_\_\_ Range:

**Note:** Write the answer in interval notation. If the answer includes more than one interval write the intervals separated by the "union" symbol, U. If needed enter  $-\infty$  as - infinity and  $\infty$ as infinity.

## 14. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graph

Find domain and range of the function

$$g(t) = t^4$$

Domain: \_\_ Range:

Note: Write the answer in interval notation. If the answer includes more than one interval write the intervals separated by the "union" symbol, U. If needed enter  $-\infty$  as - infinity and  $\infty$ as infinity.

## /1.1.43.pg

Find domain and range of the function

$$f(x) = \sqrt{100 - 5x}$$

Domain: \_\_\_

Range:

Note: Write the answer in interval notation. If the answer includes more than one interval write the intervals separated by the "union" symbol, U. If needed enter  $-\infty$  as - infinity and  $\infty$ as infinity.

### 16. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_G /1.1.49.pg

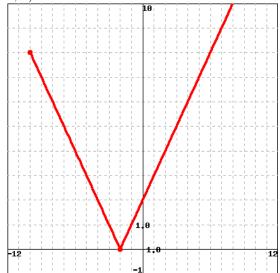
From Rogawski ET section 1.1, exercise 49.

Find the interval on which the function f(x) = |x+2| is increasing:

SOLUTION: (Instructor solution preview: show the student solution after due date. )

### **Solution:**

A graph of the function y = |x+2| is shown below. From the graph we see that the function is increasing on the interval  $(-2,\infty)$ .



### 17. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs-/1.1.51.pg

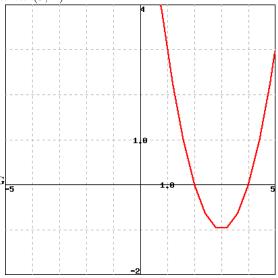
From Rogawski ET section 1.1, exercise 51.

Find the interval on which the function  $f(x) = (x-3)^2 - 1$  is increasing:

SOLUTION: (Instructor solution preview: show the student solution after due date. )

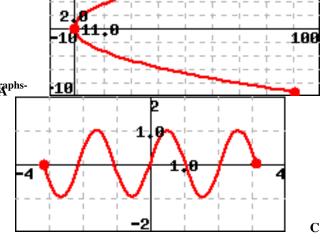
### **Solution:**

A graph of the function  $y = (x-3)^2 - 1$  is shown below. 15. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphshe graph we see that the function is increasing on the interval  $(3, \infty)$ 

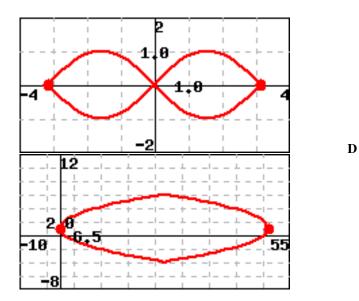


### $\textbf{18.} \hspace{0.1cm} \textbf{(1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graphs and Graphs and Graphs and Graphs and Graphs are also as a second control of the problems and Graphs are also as a second control of the problems and Graphs are also as a second control of the problems and Graphs are also as a second control of the problems and Graphs are also as a second control of the problems and Graphs are also as a second control of the problems and Graphs are also as a second control of the problems and Graphs are also as a second control of the problems. The problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems. The problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems. The problems are also as a second control of the problems are also as a second control of the problems. The problems are also as a second control of the problems are also as a second control of the problems. The problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems. The problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems. The problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems. The problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems are also as a second control of the problems. The problems are also as a second control of the problems are also as a second control of the prob$ /1.1.59.pg

From Rogawski ET section 1.1, exercise 59



В



Which one of the graphs is a function?

A.

B.

C.

D.

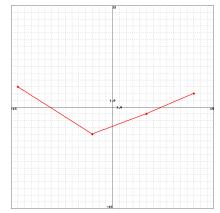
SOLUTION: (Instructor solution preview: show the student solution after due date. )

### **Solution:**

(B) is the graph of a function. (C), (A), and (D) all fail the vertical line test.

From Rogawski ET section 1.1, exercise 61.

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What are the domain and range of f(x) shown in the graph above?

Domain: \_ Range: \_ **Evaluate:** f(-3) =

20. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_Graph /1.1.67.pg

From Rogawski ET section 1.1, exercise 67.

Suppose that f(x) has a domain of [6, 17] and a range of [8, 15]. What are the domain and range of:

(a) f(x) + 4 Domain \_\_\_\_ Range \_\_ (b) f(x+4) **Domain** \_\_\_\_ **Range** \_

(c) f(4x) **Domain** \_\_\_\_ Range \_\_\_\_

(d) 4f(x) **Domain** \_\_\_\_ **Range** \_\_

SOLUTION: (Instructor solution preview: show the student solution after due date. )

### **Solution:**

- (a) f(x) + 4 is obtained by shifting f(x) upwards by 4 units. Therefore the domain remains [6,17] while the range becomes
- (b) f(x+4) is obtained by shifting f(x) by 4 units left along the x axis. Therefore the domain becomes [2, 13] while the range remains [8, 15]
- (c) f(4x) is obtained by compressing f(x) by a factor of 4. Therefore the domain becomes  $\left[\frac{6}{4}, \frac{17}{4}\right]$  while the range remains [8, 15].

19. (1 pt) Problems/setM151\_01\_01\_Real\_Numbers\_Functions\_Equations\_and\_G(a) is obtained by stretching f(x) vertically by a factor of 4. Therefore the domain remains [6,17] while the range becomes [32, 60].

WeBWorK assignment M151\_01\_02\_Linear\_and\_Quadratic\_Functions due 02/08/2012 at 06:00pm MST.

Spring 2012

## $\begin{tabular}{ll} \bf 1. & (1~pt)~Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.1.pg \end{tabular}$

From Rogawski ET section 1.2, exercise 1.

Find the slope, the *y*-intercept, and the *x*-intercept of the line y = 35 - 7x.

slope: \_\_\_\_\_ y-intercept: \_\_\_\_\_ x-intercept: \_\_\_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** Because the equation of the line is given in slope-intercept form, the slope is the coefficient of x and the y-intercept is the constant term: that is, m = -7 and the y-intercept is 35. To determine the x-intercept, substitute y = 0 and then solve for x: 0 = 35 - 7x or x = 5.

## 2. (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.3.pg

From Rogawski ET section 1.2, exercise 3.

Find the slope, the *y*-intercept, and the *x*-intercept of the line 7x + 3y = -2.

slope: \_\_\_\_\_ y-intercept: \_\_\_\_\_ x-intercept: \_\_\_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** To determine the slope and *y*-intercept, we first solve the equation for *y* to obtain the slope-intercept form. This yields  $y = -\frac{7}{3}x - \frac{2}{3}$ . From here, we see that the slope is  $m = -\frac{7}{3}$  and the *y*-intercept is  $-\frac{2}{3}$ . To determine the *x*-intercept, substitute y = 0 and solve for *x*: 7x = -2 or  $x = -\frac{2}{7}$ .

## 3. (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1,2.5.pg

From Rogawski ET section 1.2, exercise 5.

Find the slope of the line y = 6x - 3.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** m = 6

## **4.** (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.7.pg

From Rogawski ET section 1.2, exercise 7.

Find the slope of the line 10y - 6x = -10.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** First solve the equation for y to obtain the slope-intercept form. This yields  $y = \frac{3}{5}x - 1$ . The slope of the line is therefore  $m = \frac{3}{5}$ .

## 5. (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.9.pg

From Rogawski ET section 1.2, exercise 9.

The equation of the line that has slope 2 and y-intercept -8 can be written in the form y = mx + b where

 $m = \underline{\hspace{1cm}}$   $b = \underline{\hspace{1cm}}$ 

## $\textbf{6.} \quad (1 \ \, pt) \ \, Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.11.pg \\$

From Rogawski ET section 1.2, exercise 11.

The equation of the line that has slope 3 and passes through the point (3, -4) can be written in the form y = mx + b where

 $m = \underline{\hspace{1cm}}$  $b = \underline{\hspace{1cm}}$ 

## $\begin{tabular}{ll} \bf 7. & (1~pt)~Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.13.pg \end{tabular}$

From Rogawski ET section 1.2, exercise 13.

The equation of the line that is horizontal and passes through the point (4, -9) can be written in the form y = mx + b where

 $m = \underline{\hspace{1cm}}$  $b = \underline{\hspace{1cm}}$ 

## $\textbf{8.} \quad \textbf{(1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.15.pg}$

From Rogawski ET section 1.2, exercise 15.

The equation of the line that passes through the point (9,9) and is parallel to the line 2x + 3y = 2 can be written in the form y = mx + b where

 $m = \underline{\hspace{1cm}}$  $b = \underline{\hspace{1cm}}$ 

## **9.** (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.17.pg

From Rogawski ET section 1.2, exercise 17.

The equation of the line that passes through the point (6,9) and is perpendicular to the line 4x + 2y = 2 can be written in the form y = mx + b where

 $m = \underline{\hspace{1cm}}$   $b = \underline{\hspace{1cm}}$ 

## ${\bf 10.}\ (1\ pt)\ Problems/set M151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.23.pg$

From Rogawski ET section 1.2, exercise 23.

The equation of the line that has x-intercept 1 and y-intercept 2 can be written in the form y = mx + b where

m =\_\_\_\_\_\_b =\_\_\_\_\_

### 11. (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.24.pg

From Rogawski ET section 1.2, exercise 24.

A line of slope m = 5 passes through the point (1,8). Find y such that (7, y) lies on the line.

### 12. (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.25.pg

From Rogawski ET section 1.2, exercise 25.

Determine whether there exists a constant c such that the line x + cy = -8

Has slope -8 \_\_\_

Passes through (-9, -7)

Is horizontal \_\_\_

Is vertical

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

Solution: Rewriting the equation of the line in slopeintercept form gives  $y = -\frac{x}{c} + \frac{1}{c}$ . To have slope -8 requires

 $-\frac{1}{c} = -8$  or  $c = \frac{1}{8}$ . Substituting x = -9 and y = -7 into the equation of the line gives -9 - 7c = -8 or  $c = -\frac{1}{7}$ .

From (a), we know the slope of the line is  $-\frac{1}{a}$ . There is no value for c that will make this slope equal to 0.

With c = 0, the equation becomes x = -8. This is the equation of a vertical line.

## 13. (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-

From Rogawski ET section 1.2, exercise 27.

Materials expand when heated. Consider a metal rod of length  $L_0$  at temperature  $T_0$ . If the temperature is changed by an amount  $\Delta T$ , then the rod's length changes by  $\Delta L = \alpha L_0 \Delta T$ , where  $\alpha$  is the thermal expansion coefficient. For steel,  $\alpha =$  $1.24 \times 10^{-5} \, {}^{\circ}\text{C}^{-1}$ .

(a) A steel rod has length  $L_0 = 60$  cm at  $T_0 = 20$ °C. What is the length at  $T = 80^{\circ}\text{C}$ ?

\_ cm

(b) Find its length at  $T = 70^{\circ}$ C if its length at  $T_0 = 40^{\circ}$ C is  $L_0 = 55 \text{ in.}$ 

\_ in

(c) Express L as a function of T if  $L_0 = 55$  in. at  $T_0 = 40$ °C. Note: Type 'a' for 'α' and note that WeBWorK is case-sensitive.

### 14. (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.29.pg

From Rogawski ET section 1.2, exercise 29.

Find x such that (-10, -3), (0, -10), and (x, -8) lie on a line.

x =

SOLUTION: (Instructor solution preview: show the student solution after due date. )

**Solution:** The slope of the line determined by the points (-10, -3) and (0, -10) is

$$\frac{-10 - (-3)}{0 - (-10)} = -\frac{7}{10}.$$

To lie on the same line, the slope between (0, -10) and (b, -8)must also be  $-\frac{7}{10}$ . Thus, we require

$$\frac{-8 - (-10)}{b - 0} = \frac{2}{b} = -\frac{7}{10},$$

or  $b = -\frac{20}{7}$ .

### 15. (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.31.pg

From Rogawski ET section 1.2, exercise 31.

The electrical current I flowing through a wire is measured when different voltages V are applied. Based on the following data, does I appear to be a linear function of V?

<i>V</i> (V)	0.5	2	3.5	5
I(A)	0.088	0.353	0.618	0.883

- A. Yes
- B. No

Note that you only have one attempt on this question.

SOLUTION: (Instructor solution preview: show the student solution after due date.)

**Solution:** Examine the slope between consecutive data points. The first pair of data points yields a slope of

$$\frac{0.353 - 0.088}{2 - 0.5} \approx 0.1767,$$

while the second pair of data points yields a slope of

$$\frac{0.618 - 0.353}{3.5 - 2} \approx 0.1767,$$

and the last pair of data points yields a slope of

$$\frac{0.883 - 0.618}{5 - 3.5} \approx 0.1767.$$

Because the three slopes are equal, I appears to be a linear function of V.

### 16. (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.33.pg

From Rogawski ET section 1.2, exercise 33.

Find the roots of the quadratic polynomials. If the polynomial has more than one root, enter your answers separated by a comma.

a) 
$$6 - (6x^2 + 9x)$$

Answer: \_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

**Solution:** 

$$x = \frac{9 \pm \sqrt{81 - 4(-6)(6)}}{2(-6)} = \frac{9 \pm \sqrt{225}}{-12} = -2 \text{ or } \frac{1}{2}$$

$$x = \frac{-1 \pm \sqrt{1 - 4(5)(-9)}}{2(5)} = \frac{-1 \pm \sqrt{181}}{10} = 1.24536 \text{ or } -1.44536$$

## $17. \ (1\ pt)\ Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.35.pg$

From Rogawski ET section 1.2, exercise 35. Complete the square and find the minimum or maximum value of the quadratic function  $y = x^2 - 14x + 49$ .

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:**  $y = (x - 7)^2$ ; therefore, the minimum value of the quadratic polynomial is 0, and this occurs at x = 7.

## $18. \ (1\ pt)\ Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.37.pg$

From Rogawski ET section 1.2, exercise 37. Complete the square and find the minimum or maximum value of the quadratic function  $y = x^2 - 18x + 84$ .

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

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**Solution:**  $y = x^2 - 18x + 81 - 81 + 84 = (x - 9)^2 + 3$ ; therefore, the minimum value of the quadratic polynomial is 3, and this occurs at x = 9.

## $\textbf{19.} \ \, \textbf{(1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.39.pg}$

From Rogawski ET section 1.2, exercise 39. Complete the square and find the minimum or maximum value of the quadratic function  $y = 1 - (9x^2 + 5x)$ .

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:**  $y = 1 - \left(9x^2 + 5x\right) = -9\left(x^2 + \frac{5}{9}x + \frac{25}{324}\right) + 1 + \frac{25}{36} = -9\left(x + \frac{5}{18}\right)^2 + \frac{61}{36}$ ; therefore, the maximum value of the quadratic polynomial is  $\frac{61}{36}$ , and this occurs at  $x = -\frac{5}{18}$ .

## **20.** (1 pt) Problems/setM151\_01\_02\_Linear\_and\_Quadratic\_Functions-/1.2.41.pg

From Rogawski ET section 1.2, exercise 41. Complete the square and find the minimum or maximum value of the quadratic function  $y = 5x^2 - 7x$ .

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:**  $y = 5x^2 - 7x = 5\left(x^2 - \frac{7}{5}x + \frac{49}{100}\right) - \frac{49}{20} = 5\left(x - \frac{7}{10}\right)^2 - \frac{49}{20}$ ; therefore, the minimum value of the quadratic polynomial is  $-\frac{49}{20}$ , and this occurs at  $x = \frac{7}{10}$ .

### 1. (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.1.pg From Rogawski ET section 1.3, exercise 1.

Determine the domain of the function.

$$f(x) = x^{0.75}$$

- A.  $x \ge 0$
- B. x≠0
- C. all Real numbers
- D.  $x \le 0$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** Since we're working on the real-number plane, x must be positive (negatives lead to imaginary numbers).

## **2.** (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.5.pg From Rogawski ET section 1.3, exercise 5.

Determine the domain of the function.

$$f(x) = \frac{1}{x+1}$$

- A.  $x \neq -1$
- B.  $x \le -1$
- C.  $x \ge -1$
- D. all Real numbers

Note that you only have two attempts on this question.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** The domain of a rational function  $\frac{P(x)}{Q(x)}$  is the set of numbers x such that  $Q(x) \neq 0$ .

## 3. (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.13.pg

From Rogawski ET section 1.3, exercise 13.

Identify the following function as polynomial, rational, algebraic, or transcendental.

$$f(x) = 9x^3 + 8x^2 - 9x - 3$$

- A. algebraic
- B. polynomial
- C. transcendental
- D. rational

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** A polynomial is a sum of multiples of power functions ( $g(x) = x^m$ ) with whole number exponents.

This is a polynomial, since  $x^3$ ,  $x^2$ ,  $x^1$ , and  $x^0$  are all power functions with whole number exponents, and the given expression is a sum of multiples of those power functions.

### 4. (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.15.pg

From Rogawski ET section 1.3, exercise 15.

Identify the following function as polynomial, rational, algebraic, or transcendental.

$$f(x) = \sqrt{10x^3 + 9x^2 - 6x - 2}$$

- A. algebraic
- B. transcendental
- C. polynomial
- D. rational

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** An algebraic function is produced by taking sums, products, and quotients of roots of polynomials and rational functions.

This is an algebraic function, since  $10x^3 + 9x^2 - 6x - 2$  is a polynomial and the given function is the root of  $10x^3 + 9x^2 - 6x - 2$ .

### 5. (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.19.pg

From Rogawski ET section 1.3, exercise 19.

Identify the following function as polynomial, rational, algebraic, or transcendental.

$$f(x) = \frac{2x^3}{9 - 10x^2}$$

- A. rational
- B. algebraic
- C. polynomial
- D. transcendental

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

Solution: Rational.

### 6. (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.21.pg

From Rogawski ET section 1.3, exercise 21.

Identify the following function as polynomial, rational, algebraic, or transcendental.

$$f(x) = \sin(3x^2 + 1)$$

- A. rational
- B. transcendental
- C. polynomial
- D. algebraic

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

Solution: Transcendental.

### 7. (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.23.pg

From Rogawski ET section 1.3, exercise 23.

Identify the following function as polynomial, rational, algebraic, or transcendental.

1

$$f(x) = 1x^2 - 6x + 6x^{-1}$$

- A. algebraic
- B. rational
- C. transcendental
- D. polynomial

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

Solution: Rational.

**8.** (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.25.pg From Rogawski ET section 1.3, exercise 25.

Is  $f(x) = 3^{x^2}$  a transcendental function?

- A. yes
- B. no

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

Solution: Yes.

**9.** (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.27.pg From Rogawski ET section 1.3, exercise 27.

Calculate the composite functions  $f \circ g$  and  $g \circ f$ , and determine their domains.

$$f(x) = \sqrt{2x}, g(x) = x + 3$$
  
 $f(g(x)) =$ \_\_\_\_\_\_ Domain: \_\_\_\_\_\_

**Note:** Write the domain in interval notation. If the domain includes more than one interval write the intervals separated by the "union" symbol, U. If needed enter  $-\infty$  as - *infinity* and  $\infty$  as *infinity*.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

Solution:

$$f(g(x)) = 2^{x^3}; D: \Re$$
$$g(f(x)) = 2^{3x}; D: \Re$$

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10. (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.29.pg From Rogawski ET section 1.3, exercise 29.

Calculate the composite functions  $f \circ g$  and  $g \circ f$ , and determine their domains.

$$f(x) = 5^{x}, g(x) = x^{2}$$

$$f(g(x)) =$$
Domain: \_\_\_\_\_\_
Domain: \_\_\_\_\_\_

**Note:** Write the domain in interval notation. If the domain includes more than one interval write the intervals separated by the "union" symbol, U. If needed enter  $-\infty$  as - *infinity* and  $\infty$  as *infinity*.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** 

$$f(g(x)) = 5^{x^2}; D: \Re$$
$$g(f(x)) = 5^{2x}; D: \Re$$

**11.** (1 pt) Problems/setM151\_01\_03\_Function\_Classes/1.3.31.pg From Rogawski ET section 1.3, exercise 31.

Calculate the composite functions  $f \circ g$  and  $g \circ f$ , and determine their domains.

$$f(x) = \cos(x), g(x) = 2x^3 + 8x^2 - 6$$
  
 $f(g(x)) =$ \_\_\_\_\_\_\_ Domain: \_\_\_\_\_\_  
 $g(f(x)) =$ \_\_\_\_\_\_\_ Domain: \_\_\_\_\_\_

**Note:** Write the domain in interval notation. If the domain includes more than one interval write the intervals separated by the "union" symbol, U. If needed enter  $-\infty$  as - *infinity* and  $\infty$  as *infinity*.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** 

$$f(g(x)) = (\cos(2 * x^3 + 8 * x^2 - 6)); D : \Re$$
  
$$g(f(x)) = (2 * [\cos(x)]^3 + 8 * [\cos(x)]^2 - 6); D : \Re$$

## $\begin{array}{lll} \textbf{1.} & (1 \hspace{1mm} pt) \hspace{1mm} Problems/set M151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.1.pg \end{array}$

From Rogawski ET section 2.2, exercise 1.

Fill in the table and guess the value of the limit:

$$\lim_{x \to 2} f(x)$$
, where  $f(x) = \frac{x^3 - 8}{x^2 - 4}$ 

x	f(x)
2.002	
2.001	
2.0005	
2.0001	
1.9999	
1.9995	
1.999	
1.998	

$$\lim_{x \to 2} \frac{x^3 - 8}{x^2 - 4} = \underline{\hspace{1cm}}$$

## $\begin{array}{lll} \textbf{2.} & (1 \hspace{1mm} pt) \hspace{1mm} Problems/set M151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.2.pg \end{array}$

From Rogawski ET section 2.2, exercise 2.

Fill in the table and guess the value of the limit:

$$\lim_{x\to 0} f(x)$$
, where  $f(x) = \frac{\cos(x)-1}{4x}$ 

х	f(x)
0.002	
0.001	
0.0005	
0.0001	
-0.0001	
-0.0005	
-0.001	
-0.002	

$$\lim_{x \to 0} \frac{\cos(x) - 1}{4x} = \underline{\qquad}$$

# $\begin{tabular}{ll} \bf 3. & (1 \ pt) \ Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.3.pg \end{tabular}$

From Rogawski ET section 2.2, exercise 3.

Fill in the table and guess the value of the limit:

$$\lim_{x \to 8} f(x), \text{ where } f(x) = \frac{x^2 - 12x + 32}{x^2 - 17x + 72}$$

X	f(x)
8.002	
8.001	
8.0001	
7.9999	
7.999	
7.998	

$$\lim_{x \to 8} \frac{x^2 - 12x + 32}{x^2 - 17x + 72} = \underline{\hspace{1cm}}$$

## 4. (1 pt) Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.5.pg

From Rogawski ET section 2.2, exercise 5.

Fill in the table and guess the value of the limit:

$$\lim_{x\to 0} f(x)$$
, where  $f(x) = \frac{e^x - x - 1}{3x^2}$ 

	х	0.5	0.1	0.05	0.01	0.001
ſ	f(x)					

х	-0.001	-0.01	-0.05	-0.1	-0.5
f(x)					

$$\lim_{x \to 0} \frac{e^x - x - 1}{3x^2} = \underline{\hspace{1cm}}$$

## $\begin{array}{lll} \textbf{5.} & \textbf{(1 pt)} & Problems/set M151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.7.pg \end{array}$

From Rogawski ET section 2.2, exercise 7.

Determine  $\lim_{x\to 7} f(x)$  for the function f(x) shown in the figure

18 18 18 18 18 18

The limit as  $x \rightarrow 7$  is \_\_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

### **Solution:**

The graph suggests that  $f(x) \rightarrow 8$  as  $x \rightarrow 7$ 

#### 6. $(1\ pt)\ Problems/set M151\_02\_02\_Numerical\_Graphical\_Limits-$ /2.2.9.pg

From Rogawski ET section 2.2, exercise 9,10.

(a) Evaluate the limit:

$$\lim_{x \to 13} x =$$
\_\_\_\_

 $x \rightarrow 13$  (b) Evaluate the limit:

$$\lim_{x\to 4.1}\sqrt{5} = \underline{\hspace{1cm}}$$

### (1 pt) Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.13.pg

From Rogawski ET section 2.2, exercise 13.

Verify that  $\lim 3x + 2 = 17$  using the limit definition. See Example 1.

**Solution:** Let f(x) = 3x + 2. To show that  $\lim_{x \to 2} 3x + 2 = 17$ ,

we must show that \_\_\_\_\_ becomes  $\boxed{?}$  when x is sufficiently close (but not equal to) \_\_\_\_.

We have

$$|f(x) - 17| = |$$
 \_\_\_\_ | -17| = | \_\_\_ | = \_\_ | \_\_\_ |. Since  $|f(x) - 17| =$ is a multiple of \_\_\_,

we can make | ? | by taking x sufficiently close to | ... **OED** 

#### 8. (1 pt) Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.21.pg

From Rogawski ET section 2.2, exercise 21.

Estimate the limit numerically or state that the limit doesn't

$$\lim_{x \to 5} \frac{\sqrt{x} - 5}{x - 25} = \underline{\hspace{1cm}}$$

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does not

SOLUTION: (Instructor solution preview: show the student solution after due date. )

#### **Solution:**

X	f(x)	х	f(x)
5.002	0.138188061487005	4.998	0.138205143526948
5.001	0.138192330960632	4.999	0.138200871980372
5.0005	0.138194465956463	4.9995	0.138198736466304
5.0001	0.138196174077482	4.9999	0.138197028179449

The limit as  $x \rightarrow 1$  is 0.13820.

### 9. (1 pt) Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-

From Rogawski ET section 2.2, exercise 23.

Estimate the limit numerically or state that the limit doesn't

$$\lim_{x \to 5} \frac{x^2 - 3x - 10}{x^2 - 4x - 5} = \underline{\hspace{1cm}}$$

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does not

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

#### **Solution:**

X	f(x)	X	f(x)
5.002	1.16661112962346	4.998	1.16672224074692
5.001	1.16663889351775	4.999	1.16669444907485
5.0005	1.16665277893509	4.9995	1.16668055671306
5.0001	1.16666388893518	4.9999	1.16666944449074

The limit as  $x \to 5$  is  $\frac{7}{6}$ 

#### 10. (1 pt) Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.25.pg

From Rogawski ET section 2.2, exercise 25.

Estimate the limit numerically or state that the limit doesn't

$$\lim_{x \to 0} \frac{\sin(5x)}{x} = \underline{\qquad}$$

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does

SOLUTION: (Instructor solution preview: show the student solution after due date. )

#### **Solution:**

х	-0.01	-0.005	0.005	Ī
f(x)	4.99791692706783	4.99947918294247	4.99947918294247	Ī

The limit as  $x \to 0$  is 5

#### 11. (1 pt) Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.27.pg

From Rogawski ET section 2.2, exercise 27.

Estimate the limit numerically or state that the limit doesn't

$$\lim_{x\to 0} \frac{\sin 8x}{x^2} = \underline{\hspace{1cm}}$$

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does

SOLUTION: (Instructor solution preview: show the student solution after due date. )

#### **Solution:**

x	-0.001	-0.0001	0.0001	
f(x)	-7999.91466693973	-79999.991466667	79999.991466667	7

The limit doesn't exist. As  $x \to 0-$ ,  $f(x) \to -\infty$ ; similarly, as  $x \to 0+, f(x) \to \infty$ .

## 12. (1 pt) Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.29.pg

From Rogawski ET section 2.2, exercise 29.

Estimate the limit numerically or state that the limit doesn't exist.

$$\lim_{h\to 0}\cos\left(\frac{9}{h}\right) = \underline{\qquad}$$

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does not exist.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

$\boldsymbol{x}$		plusmn;0.1		plusmn;0.	01
	plusmn;0.001		plusmn;0.0001		
f(x)	-0.448074	0.0662467	-0.788179	0.94062	i

The limit doesn't exist since  $\cos\left(\frac{9}{h}\right)$  oscillates infinitely often as  $h \to 0$ .

## $\begin{tabular}{ll} \bf 13. & (1\ pt)\ Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.31.pg \end{tabular}$

From Rogawski ET section 2.2, exercise 31.

Estimate the limit numerically or state that the limit doesn't

$$\lim_{h \to 0} \frac{4^h - 1}{h} = \underline{\qquad}$$

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does not exist.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

h	-0.05	-0.001	0.001	
f(h)	1.33934016926385	1.38533389897111	1.3872557113	5

The limit as  $x \to 0$  is approximately 1.38629436111989. (The exact answer is  $\ln 4$ ).

## $\begin{tabular}{ll} \bf 14. & (1\ pt)\ Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.33.pg \end{tabular}$

From Rogawski ET section 2.2, exercise 33.

Estimate the limit numerically or state that the limit doesn't exist.

$$\lim_{x \to 1+} \frac{\sec^{-1}(x)}{\sqrt{x^2 - 1}} = \underline{\hspace{1cm}}$$

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does not exist

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

#### **Solution:**

х	1.01	1.001	1.0005	1.0001
f(x)	0.99338	0.999334	0.999667	0.999933

The limit as  $x \to 1 + is \frac{\sqrt{2}\sqrt{2}}{2} \approx 1$ .

## $\begin{tabular}{ll} \bf 15. & (1\ pt)\ Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.35.pg \end{tabular}$

From Rogawski ET section 2.2, exercise 35.

Estimate the limit numerically or state that the limit doesn't exist.

$$\lim_{x \to 0} \frac{\tan^{-1}(9x)}{\sin^{-1}(x) - x} = \underline{\hspace{1cm}}$$

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does not exist.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### Solution:

10

_				
X	-0.001	-0.0001	0.0001	
f(x)	53998517.7912643	5399998270.84354	5399998270.84354	

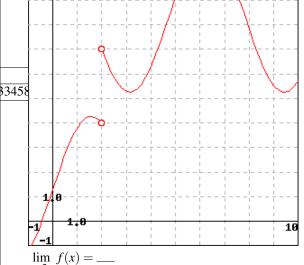
As  $x \to 0$ ,  $f(x) \to \infty$ , so the limit doesn't exist.

## **16.** (1 pt) Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.37.pg

From Rogawski ET section 2.2, exercise 37.

Determine  $\lim_{x\to 2+} f(x)$ ,  $\lim_{x\to 2-} f(x)$ , and  $\lim_{x\to 2} f(x)$  for the function shown in figure.

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does not exist.



$$\lim_{x\to 2-} f(x) = \underline{\qquad}$$

$$\lim_{x \to 2+} f(x) = \underline{\qquad}$$

$$\lim_{x\to 2} f(x) = \underline{\hspace{1cm}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

The left hand limit is  $\lim_{x \to a} f(x) = 4$ , whereas the right-hand limit is  $\lim_{x\to 2+} f(x) = 7$ . Accordingly the two-sided limit doesn't exist.

#### **17.** $(1\ pt)\ Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-$ /2.2.38.pg

From Rogawski ET section 2.2, exercise 38.

Let *F* be the function whose graph is shown below.

Evaluate each of the following expressions.

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does not exist.

1. 
$$\lim_{x \to \infty} F(x) =$$

$$2. \quad \lim_{x \to \infty} F(x) = \underline{\qquad}$$

3. 
$$\lim_{x \to -1} F(x) =$$
\_\_\_

4. 
$$F(-1) =$$
\_\_\_\_

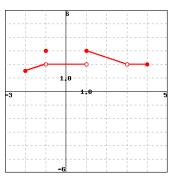
5. 
$$\lim F(x) =$$

$$6. \quad \lim_{x \to 1} F(x) = \underline{\qquad}$$

7. 
$$\lim_{x \to 1^+} F(x) = \underline{\hspace{1cm}}$$

8. 
$$\lim_{x \to 1} F(x) = \underline{\hspace{1cm}}$$

9. 
$$F(3) =$$
\_\_\_



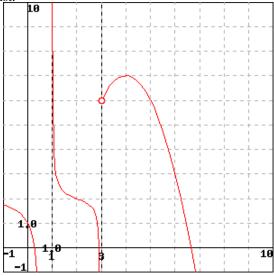
The graph of y = F(x).

18. (1 pt) Problems/setM151\_02\_02\_Numerical\_Graphical\_Limits-/2.2.45.pg

From Rogawski ET section 2.2, exercise 45.

Determine the one or two-sided limits of f(x) at c = 1 and c = 3 for the function shown in figure.

Enter inf for  $\infty$ , -inf for  $-\infty$ , and DNE if the limit does not



$$\lim_{x \to 1^{-}} f(x) = \underline{\hspace{1cm}}$$

$$\lim_{x \to 1+} f(x) = \underline{\qquad}$$

$$\lim_{x \to 1} f(x) = \underline{\qquad}$$
$$\lim_{x \to 3^{-}} f(x) = \underline{\qquad}$$

$$\lim_{x \to 3-} f(x) = \underline{\qquad}$$

$$\lim_{x \to 3+} f(x) = \underline{\qquad}$$

$$\lim_{x \to 3} f(x) = \underline{\qquad}$$

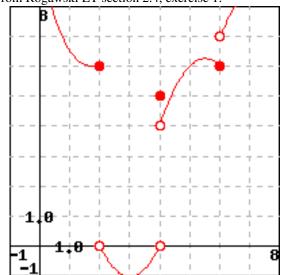
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## **1.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.pq5.pg From Rogawski ET section 2.4, exercise PQ5.

Select True or False, depending on whether the statement is true or false.

- ? 1. If f(x) and g(x) are continuous at x = a, then f(x)/g(x) is continuous at x = a.
- ? 2. If the left- and right-hand limits of f(x) as  $x \to a$  exist, then f has a removable discontinuity at x = a.
- ? 3. f(x) is continuous at x = a if the left- and right-hand limits of f(x) as  $x \to a$  exist and are equal.

**2.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.1.pg From Rogawski ET section 2.4, exercise 1.



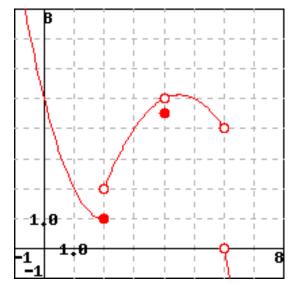
State whether the function shown in the figure is left-continuous, right-continuous, or neither at the following points:

? 1. at 
$$x = 6$$

? 2. at 
$$x = 4$$

$$\frac{1}{?}$$
 3. at  $x = 2$ 

**3.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.3.pg From Rogawski ET section 2.4, exercise 3.



(a) At which point c does f(x) have a removable discontinuity?

c = \_\_\_

(b) What value should be assigned to f(c) to make f continuous at x = c?

Assign f(c) =

# **4.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.17.pg From Rogawski ET section 2.4, exercise 17.

Determine the point(s) at which the function  $f(x) = \frac{1}{x}$  is discontinuous and state the type of discontinuity: removable, jump, infinite, or none of these.

x = *Hint: If more than one point, separate each with a comma.* 

? 1. Choose the type

## **5.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.19.pg From Rogawski ET section 2.4, exercise 19.

Determine the point(s) at which the function  $f(x) = \frac{x+3}{|x+4|}$  is discontinuous and state the type of discontinuity: removable, jump, infinite, or none of these.

x = *Hint: If more than one point, separate each with a comma.* 

? 1. Choose the type

# **6.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.23.pg From Rogawski ET section 2.4, exercise 23.

Determine the point(s) at which the function  $f(x) = \frac{1}{x^2 - 64}$  is discontinuous and state the type of discontinuity: removable, jump, infinite, or none of these.

x = *Hint: If more than one point, separate each with a comma.* 

? 1. Choose the type

**7.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.25.pg From Rogawski ET section 2.4, exercise 25.

Enter T or F depending on whether the statement is true or false. (You must enter T or F – True and False will not work.)

\_\_\_1. The function  $f(x) = 3 \cdot x^{\frac{3}{2}} - 9 \cdot x^3$  is right continuous at x = 0.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

The function  $f(x) = 3 \cdot x^{\frac{3}{2}} - 9 \cdot x^3$  is continuous for x > 0. At x = 0 it is right-continuous. (It is not defined for x < 0).

**8.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.27.pg From Rogawski ET section 2.4, exercise 23.

Determine the point(s) at which the function  $f(x) = \frac{1-2x}{x^2-10x+9}$  is discontinuous and state the type of discontinuity: removable, jump, infinite, or none of these.

x = *Hint: If more than one point, separate each with a comma.* 

? 1. Choose the type

**9.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.29.pg From Rogawski ET section 2.4, exercise 29.

Determine the point(s) at which the function  $f(x) = \frac{x^2 - 16x + 60}{10}$ 

is discontinuous and state the type of discontinuity: removable, jump, infinite, or none of these.

x = *Hint: If more than one point, separate each with a comma.* 

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? 1. Choose the type

**10.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.67.pg From Rogawski ET section 2.4, exercise 67.

Evaluate the limit  $\lim_{x \to 0} \tan(24 \cdot x)$ .

$$\lim_{x \to \frac{\pi}{8}} \tan(24 \cdot x) = \underline{\qquad}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

$$\lim_{x \to \frac{\pi}{8}} \tan(24 \cdot x) = \tan(24 \cdot \frac{\pi}{8}) = 0$$

**11.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.73.pg From Rogawski ET section 2.4, exercise 73.

Evaluate the limit  $\lim_{x \to 0} 10^{x^2 - 4 \cdot x}$ .

$$\lim_{x \to 2} 10^{x^2 - 4 \cdot x} = \underline{\hspace{1cm}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

$$\lim_{x\to 2} 10^{x^2-4\cdot x} = 10^{2^2-4\cdot 2} = 0.0001.$$

**12.** (1 pt) Problems/setM151\_02\_04\_Limits\_and\_Continuity/2.4.77.pg From Rogawski ET section 2.4, exercise 77.

Evaluate the limit  $\lim_{x \to 4} \sin^{-1}(\frac{x}{4})$ .

$$\lim_{x \to 4} \sin^{-1}\left(\frac{x}{4}\right) = \underline{\qquad}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

$$\lim_{x \to 4} \sin^{-1}(\frac{x}{4}) = \sin^{-1}(\frac{4}{4}) = \frac{\pi}{2}.$$

Spring 2012

### 1. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.PQ3.pg From Rogawski ET section 3.1, exercise PQ3.

For which value of *x* is  $\frac{f(x)-f(3)}{x-3} = \frac{f(7)-f(3)}{4}$ ?

## 2. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.1.pg

From Rogawski ET section 3.1, exercise 1.

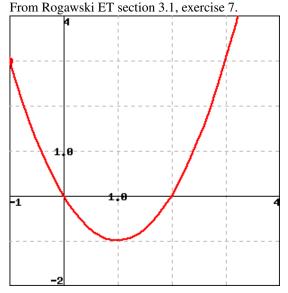
Let f(x) be the function  $3x^2 - 9x + 2$ . Then the quotient  $\frac{f(4+h)-f(4)}{h}$  can be simplified to ah+b for:

b =\_\_\_

Compute f'(4) by taking the limit as  $h \to 0$ .

f'(4) =\_\_\_

## 3. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.7.pg



Calculate the slope of the secant line through the points on the graph where x = 1 and x = 3.

slope =

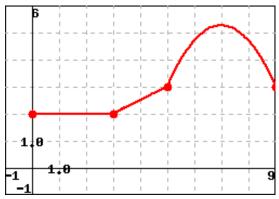
SOLUTION: (Instructor solution preview: show the student solution after due date.)

The slope of the secant line is  $\frac{f(3)-f(1)}{3-1} = \frac{3-(-1)}{2} = 2$ 

### 4. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.11.pg

From Rogawski ET section 3.1, exercise 11.

Let f(x) be the function whose graph is shown below.



Determine f'(a) for a = 1, 2, 4, 7.

f'(1) =\_\_\_ f'(2) =\_\_\_\_\_

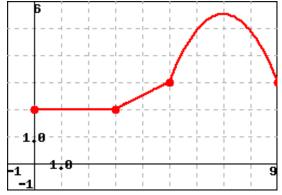
f'(4) = 1f'(7) = 1

SOLUTION: (Instructor solution preview: show the student solution after due date. )

**Solution:** Remember that the value of the derivative of f at x = a can be interpreted as the slope of the line tangent to the graph of y = f(x) at x = a. From the figure, we see that the graph of y = f(x) is a horizontal line (that is, a line with zero slope) on the interval  $0 \le x \le 3$ . Accordingly, f'(1) = f'(2) = 0. On the interval  $3 \le x \le 5$ , the graph of y = f(x) is a line of slope 0.5; thus, f'(4) = 0.5. Finally, the line tangent to the graph of y = f(x) at x = 7 is horizontal, so f'(7) = 0.

### 5. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.13.pg From Rogawski ET section 3.1, exercise 13.

Let f(x) be the function whose graph is shown below.



Which is larger?

- A. f'(7.5)
- B. f'(8.5)

**Note:** Don't just guess. You are allowed only one attempt to answer for credit.

SOLUTION: (Instructor solution preview: show the student solution after due date. )

**Solution:** The line tangent to the graph of y = f(x) at x = 7.5has a larger slope than the line tangent to the graph of y = f(x)at x = 8.5. Therefore, f'(7.5) is larger than f'(8.5).

### 6. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.15.pg

From Rogawski ET section 3.1, exercise 15.

Use the definition of the derivative to find the derivative of: f(x) = 12x - 5.

$$f'(x) =$$
\_\_\_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

### **Solution:**

$$\lim_{h \to 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \to 0} \frac{12x + 12h - 5 - 12x + 5}{h} = \lim_{h \to 0} \frac{12h}{h} = \lim_{h \to 0} 12 = 12$$

### 7. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.17.pg

From Rogawski ET section 3.1, exercise 17.

Use the definition of the derivative to find the derivative of: f(t) = -9 - 6t.

$$f'(t) = \underline{\hspace{1cm}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

### **Solution:**

Solution:
$$\lim_{h \to 0} \frac{f(t+h) - f(t)}{h} = \lim_{h \to 0} \frac{(-9 - 6t - 6h) - (-9 - 6t)}{h} = \lim_{h \to 0} \frac{-6h}{h} = \lim_{h \to 0} \frac{-6h}{h}$$

### 8. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.19.pg

From Rogawski ET section 3.5, exercise 19.

Let  $f(x) = \frac{1}{x}$ . Compute the difference quotient for f(x) at a = -2 with h = 0.2

The difference quotient =  $_{-}$ 

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

The difference quotient is  $\frac{f(x+h)-f(x)}{h} = \frac{\frac{1}{-2+0.2}-\frac{1}{-2}}{0.2} =$ -0.277778.

### 9. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.23.pg

From Rogawski ET section 3.1, exercise 23.

Let 
$$f(x) = 9x^2 + 4x + 8$$
.

Then using the limit definition of the derivative,

 $\lim_{h \to \infty} \frac{f(6+h)-f(6)}{h}$  can be simplified to rh+s for:

Taking the limit as  $h \to 0$ , compute the derivative at x = 6. f'(6) =\_\_\_\_\_

Find an equation of the tangent line at x = 6.

### 10. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.25.pg

From Rogawski ET section 3.1, exercise 25.

Let 
$$f(x) = x^3$$
.

Then using the limit definition of the derivative,

 $\lim_{h \to \infty} \frac{f(10+h) - \widetilde{f}(10)}{h}$  can be simplified to  $rh^2 + sh + t$  for:

s =\_\_\_

Taking the limit as  $h \to 0$ , compute the derivative at x = 10.

Find an equation of the tangent line at x = 10.

### 11. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.29.pg

From Rogawski ET section 3.1, exercise 29.

Let 
$$f(x) = \frac{1}{9x}$$
.

Compute the derivative at x = 2 using the limit definition.

$$f'(2) =$$
\_\_\_\_\_

Find an equation of the tangent line at x = 2.

 $y = _{-}$ 

### 12. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.31.pg

From Rogawski ET section 3.1, exercise 31.

Let 
$$f(x) = x - 9$$
.

Compute the derivative at x = -9 using the limit definition.

$$f'(-9) =$$
\_\_\_\_\_

Find an equation of the tangent line at x = -9.

### 13. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.33.pg

From Rogawski ET section 3.1, exercise 33.

Let 
$$f(x) = \frac{1}{x+8}$$
.

Compute the derivative at x = -7 using the limit definition.

$$f'(-7) =$$
\_\_\_\_

Find an equation of the tangent line at x = -7.

### 14. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.39.pg

From Rogawski ET section 3.1, exercise 39.

Let 
$$f(x) = \frac{1}{\sqrt{4x}}$$
.

Compute the derivative at x = 36 using the limit definition.

$$f'(36) =$$
\_\_\_\_

Find an equation of the tangent line at x = 36.

### 15. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.48.pg

From Rogawski ET section 3.1, exercise 48.

Below is an "oracle" function. An oracle function is a function presented interactively. When you type in a t value, and press the -f-> button the value f(t) appears in the right hand window. There are three lines, so you can calculate three different values of the function at one time.

Use the oracle function to calculate a few values near 0.89. Use these values to calculate a few difference quotients of f(x). Then estimate f'(0.89) by taking an average of difference quotients at h and -h.

$$f'(0.89) =$$
\_\_\_\_\_

The java Script calculator was displayed here

Remember this technique for finding velocities. Later we will use the same method to find the derivative of functions such as f(t).

### 16. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.53.pg

From Rogawski ET section 3.1, exercise 53.

The limit below represents a derivative f'(a). Find f(x) and a.

$$\lim_{h \to 0} \frac{(3+h)^4 - 81}{h}$$

$$f(x) = \underline{\hspace{1cm}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

Solution: The difference quotient

$$\frac{(3+h)^4-81}{h}$$

has the form

$$\frac{f(a+h)-f(a)}{h}$$

where  $f(x) = x^4$  and a = 3.

## 17. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.55.pg

From Rogawski ET section 3.1, exercise 55.

The limit below represents a derivative f'(a). Find f(x) and a.

$$\lim_{h\to 0}\frac{\cos(\pi+h)+1}{h}$$

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$$f(x) = \underline{\hspace{1cm}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** The difference quotient

$$\frac{\cos(\pi+h)+1}{h}$$

has the form

$$\frac{f(a+h)-f(a)}{h}$$

where  $f(x) = \cos(x)$  and  $a = \pi$ .

### 18. (1 pt) Problems/setM151\_03\_01\_Derivative\_Def/3.1.57.pg

From Rogawski ET section 3.1, exercise 57.

The limit below represents a derivative f'(a). Find f(x) and a.

$$\lim_{h\to 0}\frac{5^{2+h}-25}{h}$$

$$f(x) = \underline{\hspace{1cm}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** The difference quotient

$$\frac{5^{2+h}-25}{h}$$

has the form

$$\frac{f(a+h)-f(a)}{h}$$

where  $f(x) = 5^x$  and a = 2.

## 1. (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.PQ1.pg From Rogawski ET section 3.2, exercise PQ1.

What is the slope of the tangent line through the point (2, f(2)) if f is a function such that  $f'(x) = x^2$ ?

Answer: \_\_\_

## **2.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.PQ2.pg From Rogawski ET section 3.2, exercise PQ2.

Suppose f'(-3) = 2 and g'(-3) = 6.

- (a) Then (f-g)'(-3) =
- (b) Then (8f + 10g)'(-3) =\_\_\_\_
- (c) Can we evaluate (fg)'(-3) using the information given and the rules presented in this section?
  - A. No
  - B. Yes

## **3.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.PQ3.pg From Rogawski ET section 3.2, exercise PQ3.

To which of the following does the Power Rule apply?

- $\bullet \ \ A. \ f(x) = e^x$
- B.  $f(x) = x^{\pi}$
- C.  $f(x) = \sqrt[9]{x}$
- D.  $f(x) = x^{(2)}$
- E.  $f(x) = 2^e$
- F.  $f(x) = \pi^x$

## **4.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.1.pg From Rogawski ET section 3.2, exercise 1.

Let f(x) = 15x - 11.

Compute f'(x) using the limit definition.

f'(x) =\_\_\_\_\_

## **5.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.3.pg From Rogawski ET section 3.2, exercise 3.

Let 
$$f(x) = 11 - 2x^3$$
.

Compute f'(x) using the limit definition.

f'(x) =\_\_\_\_\_

## **6.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.5.pg From Rogawski ET section 3.2, exercise 5.

Let 
$$f(x) = \frac{1}{x}$$
.

Compute f'(x) using the limit definition.

f'(x) =\_\_\_\_\_

## 7. (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.7.pg From Rogawski ET section 3.2, exercise 7.

Let 
$$f(x) = 7\sqrt{x}$$
.

Compute f'(x) using the limit definition.

$$f'(x) =$$
\_\_\_\_\_

**8.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.9.pg From Rogawski ET section 3.2, exercise 9.

Use the Power Rule to compute the derivative.

$$\frac{d}{dx}x^{5}|_{x=-1} = \underline{\hspace{1cm}}$$

## **9.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.11.pg From Rogawski ET section 3.2, exercise 11.

Use the Power Rule to compute the derivative.

$$\frac{d}{dt}t^{2/3}|_{t=3} =$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

**Solution:** 

$$\frac{d}{dt}t^{2/3} = \frac{2}{3}t^{-1/3}$$
, so  $\frac{d}{dt}t^{2/3}|_{t=3} = \frac{2}{3}(3)^{-1/3} = \frac{2}{3\sqrt[3]{3}}$ .

## **10.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.13.pg From Rogawski ET section 3.2, exercise 13.

Use the power rule to compute the derivative.

$$\frac{d}{dx}x^{0.5} =$$
\_\_\_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** 

$$\frac{d}{dx}x^{0.5} = 0.5(x^{0.5-1}) = 0.5x^{-0.5}.$$

## **11.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.15.pg From Rogawski ET section 3.2, exercise 15.

Use the Power Rule to compute the derivative.

$$\frac{d}{dt}t^{\sqrt{3}} = \underline{\hspace{1cm}}$$

## **12.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.17.pg From Rogawski ET section 3.2, exercise 17.

Let 
$$f(x) = x^3$$
.

Compute the derivative at x = 1.

$$f'(1) =$$
\_\_\_\_

Find an equation of the tangent line at x = 1.

## **13.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.19.pg From Rogawski ET section 3.2, exercise 19.

Let 
$$f(x) = 3\sqrt{x} + 9x$$
.

Compute the derivative at x = 25.

$$f'(25) =$$
\_\_\_\_\_

Find an equation of the tangent line at x = 25.

**14.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.23.pg From Rogawski ET section 3.2, exercise 23.

Calculate the derivative of the function:  $f(x) = 3x^3 + 4x^2 + 5x - 5$ 

$$f'(x) =$$
\_\_\_\_\_

15. (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.25.pg
From Rogawski ET section 3.2, exercise 25.

Calculate the derivative of the function:  $f(x) = 3x^3 + (-4)x^{-1}$ 

$$f'(x) =$$
\_\_\_\_

**16.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.27.pg From Rogawski ET section 3.2, exercise 27.

Calculate the derivative of the function:  $g(z) = 2z^{-3} + 2z^2 - 4z + 6$ 

$$g'(z) =$$
\_\_\_\_\_

17. (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.29.pg From Rogawski ET section 3.2, exercise 29.

Calculate the derivative of the function:  $f(s) = \sqrt[6]{s} + \sqrt[8]{s}$  $f'(s) = \underline{\hspace{1cm}}$ 

**18.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.31.pg From Rogawski ET section 3.2, exercise 31.

Calculate the derivative of the function:  $f(x) = (x-3)^3$  *Hint*: Expand.

$$f'(x) = \underline{\hspace{1cm}}$$

**19.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.33.pg From Rogawski ET section 3.2, exercise 33.

Calculate the derivative of the function: P(z) = (3z+7)(8z-3)

$$P'(z) = \underline{\hspace{1cm}}$$

**20.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.35.pg From Rogawski ET section 3.2, exercise 35.

Calculate the derivative of the function:  $g(x) = e^{-5}$ 

$$g'(x) =$$
\_\_\_\_\_

**21.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.39.pg From Rogawski ET section 3.2, exercise 39.

Let 
$$f(x) = \frac{8}{5}$$
.

Calculate the indicated derivative.

$$f'(4) =$$
\_\_\_\_\_

**22.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.41.pg From Rogawski ET section 3.2, exercise 41.

Let 
$$T = 3C^{\frac{8}{3}}$$
.

Calculate the indicated derivative.

$$\frac{dT}{dC}|_{C=5} =$$

**23.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.55.pg From Rogawski ET section 3.2, exercise 55.

Find all values of x where the tangent lines to  $y = x^3$  and  $y = x^4$  are parallel.

$$x =$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** Let  $f(x) = x^3$  and let  $g(x) = x^4$ . The two graphs have parallel tangent lines at all x where f'(x) = g'(x).

$$f'(x) = g'(x)$$

$$3x^2 = 4x^3$$

$$3x^2 - 4x^3 = 0$$

$$x^2(3-4x)=0$$

hence, x = 0 or  $x = \frac{3}{4}$ .

**24.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.57.pg From Rogawski ET section 3.2, exercise 57.

Determine coefficients a and b such that  $p(x) = x^2 + ax + b$  satisfies p(1) = -9 and p'(1) = -2.

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** Let  $p(x) = x^2 + ax + b$  satisfy p(1) = -9 and p'(1) = -2. Since p'(x) = 2x + a, this implies -9 = p(1) = 1 + a + b and -2 = p'(1) = 2 + a; i.e., a = -4 and b = -6.

**25.** (1 pt) Problems/setM151\_03\_02\_Derivative\_as\_Function/3.2.77.pg From Rogawski ET section 3.2, exercise 77.

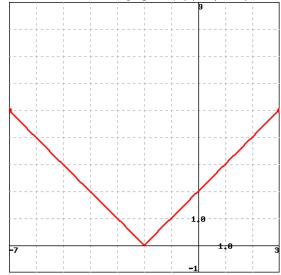
Find the points c (if any) such that f'(c) does not exist.

$$f(x) = |x+2|$$

c =\_\_\_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** Here is the graph of f(x) = |x+2|.



Its derivative does not exist at x = -2. At that value of x there is a sharp point.

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### 1. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.1.pg

From Rogawski ET section 3.7, exercise 1.

Given the following functions:  $f(u) = u^{5/2}$  and  $g(x) = x^6 + 1$ . Find:

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

#### **Solution:**

f(g(x))	f'(u)	f'(g(x))	g'(x)	$(f \circ g)'$
$(x^6+1)^{\frac{5}{2}}$	$\frac{5}{2}u^{\frac{3}{2}}$	$\frac{5}{2}(x^6+1)^{\frac{3}{2}}$	$6x^{5}$	$15x^5(x^6+1)^{\frac{3}{2}}$

### 2. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.3.pg

From Rogawski ET section 3.7, exercise 3.

Given the following functions:  $f(u) = \tan(u)$  and  $g(x) = x^3$ . Find:

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

f(g(x))	f'(u)	f'(g(x))	g'(x)	$(f \circ g)'$
$tan(x^3)$	sec <sup>2</sup> u	$sec^2(x^3)$	$3x^2$	$3x^2sec^2(x^3)$

### 3. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.5.pg

From Rogawski ET section 3.7, exercise 5.

Let 
$$y = (x + 2\cos(x))^2$$
.

Find g(x) and f(x) so that  $y = (f \circ g)(x)$ , and compute the derivative using the Chain Rule.

$$f(x) = \underline{\qquad}$$

$$g(x) = \underline{\qquad}$$

$$(f \circ g)'(x) = \underline{\qquad}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

#### **Solution:**

Let 
$$f(x) = x^2$$
,  $g(x) = x + 2\cos(x)$ , and  $(f \circ g)(x) = (x + 2\cos(x))^2$ . Then

$$\frac{dy}{dx} = f'(g(x))g'(x) = 2(x + 2\cos(x))^{1}(1 - 2\sin(x)).$$

### 4. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.7.pg

From Rogawski ET section 3.7, exercise 7.

Calculate  $\frac{d}{dx}\cos(u)$  for the following choices of u(x):  $u(x) = 2 - x^2$ ,  $\frac{d}{dx}\cos(u(x)) = \underline{\hspace{1cm}}$ 

$$u(x) \equiv 2 - x$$
,  $\frac{1}{dx}\cos(u(x)) \equiv$ 

$$u(x) = x^{-5}, \frac{d}{dx}\cos(u(x)) =$$
\_\_\_\_\_

$$u(x) = \tan(x), \frac{d}{dx}\cos(u(x)) =$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### Solution:

(a)  $cos(u(x)) = cos(2-x^2)$ .  $\frac{d}{dx}cos(u(x)) = -sin(u(x)) \cdot u'(x) = -sin(2-x^2)(-2x) = 2xsin(2-x^2)$ .

(b)  $cos(u(x)) = cos(x^{-5})$ .  $\frac{d}{dx}cos(u(x)) = -sin(u(x)) \cdot u'(x) = -sin(x^{-5})(-5x^{-6}) = 5x^{-6}sin(x^{-5})$ .

(c) 
$$cos(u(x)) = cos(tanx)$$
.  

$$\frac{d}{dx}cos(u(x)) = -sin(u(x)) \cdot u'(x) = -sin(tanx)(sec^2x).$$

### 5. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.9.pg

From Rogawski ET section 3.7, exercise 9.

Use the General Power Rule to find the derivative.

$$y = \left(x^5 + 5\right)^6$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** Recall the General Power Rule:

In this case, 
$$g(x) = n(g(x))^{n-1}g'(x)$$
  
In this case,  $g(x) = x^5 + 5$  and therefore  $g'(x) = 5x^4$ . Thus,  $y' = 6(x^5 + 5)^5 \cdot 5x^4$ .

### 6. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.11.pg

From Rogawski ET section 3.7, exercise 11.

Use the General Power Rule to find the derivative.

$$y = \sqrt{14x - 4}$$

### 7. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.13.pg

From Rogawski ET section 3.7, exercise 13.

Use the Generalized e-to-the-x Rule to find the derivative.

$$y = e^{12 - x^2}$$

y' =\_\_\_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** Recall the General Power Rule:

$$\frac{d}{dx}e^{g(x)} = g'(x)e^{g(x)}$$

In this case,  $g(x) = 12 - x^2$  and therefore g'(x) = -2x. Thus,  $y' = -2xe^{12-x^2}$ .

### 8. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.15.pg

From Rogawski ET section 3.7, exercise 15.

Let 
$$f(u) = \csc(u)$$
 and  $g(x) = 91x - 43$ .

Find the derivative of  $f \circ g$ .

$$(f \circ g)'(x) = \underline{\hspace{1cm}}$$

### 9. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.17.pg

From Rogawski ET section 3.7, exercise 17.

Let 
$$f(u) = e^u$$
 and  $g(x) = x + x^{-4}$ .

Find the derivative of  $f \circ g$ .

$$(f \circ g)'(x) = \underline{\hspace{1cm}}$$

### 10. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.19.pg

From Rogawski ET section 3.7, exercise 19.

Let 
$$f(u) = \csc(u)$$
 and  $g(x) = 2x^2 + 3x + 11$ .

Find the derivatives of f(g(x)) and g(f(x)).

$$\frac{\frac{d}{dx}f(g(x)) = \underline{\qquad}}{\frac{d}{dx}g(f(x)) = \underline{\qquad}}$$

### 11. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.21.pg

From Rogawski ET section 3.7, exercise 21.

Use the Chain Rule to find the derivative.

$$y = \sin(x^6)$$

### 12. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.25.pg

From Rogawski ET section 3.7, exercise 25.

Use the Chain Rule to find the derivative.

$$y = (1t^2 + 5t + 4)^{-7/2}$$

$$y' = \underline{\hspace{1cm}}$$

### 13. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.29.pg

From Rogawski ET section 3.7, exercise 29.

Use the Chain Rule to find the derivative.

$$y = \sec^8\left(e^{6x}\right)$$

### 14. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.33.pg

From Rogawski ET section 3.7, exercise 33.

Use the Chain Rule to find the derivative.

$$v = e^{\frac{9}{x}}$$

## 15. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.35.pg

From Rogawski ET section 3.7, exercise 35.

Find the derivative of using the appropriate rule or combination of rules.

$$y = \tan(8x + 2)$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** For this, we use the Chain Rule with f(x) = tanx and g(x) = 8x + 2.

$$f'(x) = sec^2x$$

$$g'(x) = 8$$
 and thus

$$y' = f'(g(x)) * g'(x) = 8sec^2(8x+2).$$

### 16. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.37.pg

From Rogawski ET section 3.7, exercise 37.

Find the derivative using the appropriate rule or combination of rules.

$$y = 3x \tan(8 + 4x)$$

$$v' =$$
\_\_\_\_\_

### 17. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.39.pg

From Rogawski ET section 3.7, exercise 39.

Find the derivative using the appropriate rule or combination of rules.

$$y = (4x + 25)^{\frac{1}{2}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** For this, we use the Chain Rule with  $f(x) = x^{\frac{1}{2}}$  and g(x) = 4x + 25.

$$f'(x) = \frac{1}{2}x^{-\frac{1}{2}}$$
  
 $g'(x) = 4$  and thus

$$g'(x) = 4$$
 and thus  
 $y' = f'(g(x)) * g'(x) = 2(4x + 25)^{-0.5}$ .

### 18. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.43.pg

From Rogawski ET section 3.7, exercise 43.

Find the derivative using the appropriate rule or combination of rules.

$$y = \sqrt{\sin(9x)\cos(4x)}$$

## **19.** (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.49.pg From Rogawski ET section 3.7, exercise 49.

Find the derivative using the appropriate rule or combination of rules.

$$y = \sqrt{\cos(x) + \tan(x^9)}$$

### 20. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.51.pg

From Rogawski ET section 3.7, exercise 51.

Find the derivative using the appropriate rule or combination of rules.

$$y = \sec^6(x) + \sec\left(x^6\right)$$

### 21. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.53.pg

From Rogawski ET section 3.7, exercise 53.

Find the derivative of using the appropriate rule or combination of rules.

$$y = \sqrt{\frac{z+4}{z-7}}$$

### 22. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.57.pg

From Rogawski ET section 3.7, exercise 57.

Find the derivative using the appropriate rule or combination of rules.

$$y = \cot^7\left(x^5\right)$$

$$y' =$$
\_\_\_\_\_\_

### 23. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.59.pg

From Rogawski ET section 3.7, exercise 59.

Find the derivative of using the appropriate rule or combination of rules.

$$y = (1 + (x^3 + 6)^6)^5$$

### 24. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.63.pg

From Rogawski ET section 3.7, exercise 63.

Find the derivative of using the appropriate rule or combination of rules.

$$y = \left(4e^{9x} + 9e^{-4x}\right)^5$$

### 25. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.65.pg

From Rogawski ET section 3.7, exercise 65.

Find the derivative using the appropriate rule or combination of rules.

$$y = \cos(te^{-7t})$$

$$v' =$$

### **26.** (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.67.pg

From Rogawski ET section 3.7, exercise 67.

Find the derivative using the appropriate rule or combination of rules.

$$y = e^{\left(x^2 + 7x + 1\right)^2}$$

$$y' =$$
\_\_\_\_\_\_

## 27. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.71.pg

From Rogawski ET section 3.7, exercise 71.

Find the derivative of using the appropriate rule or combination of rules.

$$y = \sqrt{kx + d}$$

### 28. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.73.pg

From Rogawski ET section 3.7, exercise 73.

Compute 
$$\frac{df}{dx}$$

if 
$$\frac{df}{du} = -7$$
 and  $\frac{du}{dx} = 6$ .  
 $\frac{df}{dx} = \underline{\hspace{1cm}}$ 

## 29. (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.77.pg

From Rogawski ET section 3.7, exercise 77.

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Compute the derivative of  $h(\sin(x))$  at  $x = \pi/6$ , assuming h'(0.5) = 12.

Answer: \_\_\_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

$$\frac{d}{dx}h(sinx) = h'(sinx) \cdot (sinx)' = h'(sinx)cosx$$
So,
$$\frac{d}{dx}h(sinx)|_{x=\frac{\pi}{6}} = h'(sin\frac{\pi}{6})cos\frac{\pi}{6} = h'(0.5)\frac{\sqrt{3}}{2} = 6\sqrt{3}.$$

**30.** (1 pt) Problems/setM151\_03\_07\_Chain\_Rule/3.7.89.pg From Rogawski ET section 3.7, exercise 89.

Compute the second derivative of sin(g(x)) at x = 3, assuming that  $g(3) = \pi/4$ , g'(3) = 4, and g''(3) = 9.

Answer: \_\_\_\_\_

### 1. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.3.pg From Rogawski ET section 3.8, exercise 3.

Differentiate the expression  $x^2y^4$  with respect to x. (Use D for  $\frac{dy}{dx}$ ).

The result is \_

SOLUTION: (Instructor solution preview: show the student solution after due date.)

**Solution:** Assuming that y depends on x, then  $\frac{d}{dx}(x^2y^4) = x^2 \cdot 4y^{4-1}D + y^4 \cdot 2x^{2-1} = 4x^2y^3D + 2x^1y^4$ .

### 2. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.5.pg From Rogawski ET section 3.8, exercise 5.

Differentiate the expression  $(x^2 + y^2)^5$  with respect to x. (Use D for  $\frac{dy}{dx}$ ).

The result is

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** Assuming that y depends on x, then by the chain rule  $\frac{d}{dx}((x^2+y^2)^5) = 5(x^2+y^2)^4(2x+2yD)$ .

### 3. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.7.pg From Rogawski ET section 3.8, exercise 7.

Differentiate the expression  $z + z^7$  with respect to x. (Use D for  $\frac{dz}{dx}$ ).

The result is

SOLUTION: (Instructor solution preview: show the student solution after due date. )

**Solution:** Assuming that z depends on x, then by the chain rule  $\frac{d}{dx}(z+z^7) = D + D \cdot 7z^6$ .

### 4. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.9.pg From Rogawski ET section 3.8, exercise 9.

Calculate the derivative of y with respect to x.

$$3y^5 + 9x^4 = 7$$

$$\frac{dy}{dx} = \underline{\qquad}$$

### 5. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.11.pg From Rogawski ET section 3.8, exercise 11.

Calculate the derivative of y with respect to x.

$$x^2y + 2xy^2 = x + y$$

$$\frac{dy}{dx} =$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

### **Solution:**

Let 
$$x^2y + 2xy^2 = x + y$$
. Then  $2x^{2-1}y + x^2\frac{dy}{dx} + 2^2xy^{2-1}\frac{dy}{dx} + 2y^2 = 1 + \frac{dy}{dx}$ 

$$\frac{dy}{dx} = \frac{2yx + 2y^2 - 1}{1 - x^2 - 4xy}$$

### 6. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.13.pg From Rogawski ET section 3.8, exercise 13.

Calculate the derivative of y with respect to x.

$$x^2y + y^3 - 10x = 60$$

$$\frac{dy}{dx} = \underline{\hspace{1cm}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

### **Solution:**

We apply the product rule and the chain rule together:

we apply the product rule and the 
$$2x^{2-1}y + x^2 \frac{dy}{dx} + 3y^{3-1} \frac{dy}{dx} - 10 = 0$$

$$(3y^2 + x^2) \frac{dy}{dx} = 10 - 2xy$$

$$\frac{dy}{dx} = \frac{10 - 2xy}{3y^2 + x^2}$$

### 7. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.17.pg From Rogawski ET section 3.8, exercise 17.

Calculate the derivative of y with respect to x.

$$y^{\frac{-3}{2}} + x^{\frac{3}{2}} = 1$$

$$\frac{dy}{dx} =$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

#### **Solution:**

Let 
$$y^{\frac{-3}{2}} + x^{\frac{3}{2}} = 1$$
. Then  $\frac{-3}{2}y^{\frac{-3-2}{2}} + \frac{3}{2}x^{\frac{3-2}{2}} = 0$ , whence  $\frac{dy}{dx} = x^{\frac{1}{2}}y^{\frac{5}{2}}$ 

### 8. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.21.pg From Rogawski ET section 3.8, exercise 21.

Calculate the derivative of y with respect to x.

$$1y + \frac{x}{y^1} = 1$$
$$\frac{dy}{dx} = \underline{\hspace{1cm}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

### **Solution:**

Let 
$$1y + \frac{x}{y^1} = 1$$
. Then

$$1\frac{dy}{dx} + \frac{1}{y^1} - \frac{1x}{y^2}\frac{dy}{dx} = 0,$$
 whence

$$\frac{1}{y^1} = \left(\frac{1x}{y^2} + 1\right) \frac{dy}{dx} \text{ whence}$$

$$\frac{1}{y^1} = \left[1\left(\frac{x+y^2}{y^2}\right)\right] \frac{dy}{dx}$$
and finally
$$\frac{dy}{dx} = \frac{y}{1(x+y^2)}.$$

9. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.23.pg From Rogawski ET section 3.8, exercise 23.

Calculate the derivative of y with respect to x.

$$\sin(x+y) = 4x + \cos(y)$$

$$\frac{dy}{dx} = \underline{\hspace{1cm}}$$

10. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.25.pg From Rogawski ET section 3.8, exercise 25.

Calculate the derivative of y with respect to x.

$$xe^y = 3xy + 4y^4$$

$$\frac{dy}{dx} = \underline{\hspace{1cm}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

To solve for  $\frac{dy}{dx}$ , we must think of y as a function of x and differentiate both sides of the equation, using the chain rule where appropriate:

$$e^y + xe^y \frac{dy}{dx} = 3y + 3x \frac{dy}{dx} + 16y^3 \frac{dy}{dx}$$

Now, lets simplify and move the terms with a  $\frac{dy}{dx}$  to the right, and keep the terms without a  $\frac{dy}{dx}$  to the left:

$$e^{y} - 3y = (3x + 16y^{3} - xe^{y})\frac{dy}{dx}$$

Finally, we can solve for  $\frac{dy}{dx}$ :  $\frac{dy}{dx} = \frac{e^y - 3y}{3x + 16y^3 - xe^y}$ 

$$\frac{dy}{dx} = \frac{e^y - 3y}{3x + 16y^3 - xe^y}$$

11. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.27.pg From Rogawski ET section 3.8, exercise 27.

Find 
$$\frac{dy}{dx}$$
 at the point  $(2, -3)$ .

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$$(x+3)^2 - 4(3y+2)^2 = -171$$
$$\frac{dy}{dx}|_{(2,-3)} = \underline{\qquad}$$

12. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.29.pg From Rogawski ET section 3.8, exercise 29.

Find an equation of the tangent line at the point (2,4).

$$xy - 7y = -20$$

13. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.31.pg From Rogawski ET section 3.8, exercise 31.

Find an equation of the tangent line at the point (1,1).

$$6x^{\frac{2}{3}} + 2v^{\frac{2}{3}} = 8$$

14. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.41.pg From Rogawski ET section 3.8, exercise 41.

Differentiate the equation  $x^5 + 5xy^3 = 13$  with respect to the variable t and express  $\frac{dy}{dt}$  in terms of  $\frac{dx}{dt}$ . (Use D for  $\frac{dx}{dt}$ ).

$$\frac{dy}{dt} = \underline{\qquad}$$

 $\frac{dy}{dt} = \frac{}{}$  **SOLUTION:** (Instructor solution preview: show the student solution after due date. )

**Solution:** Let  $x^5 + 5xy^3 = 13$ . Then  $5x^{5-1}\frac{dx}{dt} + 5 \cdot 3xy^{3-1}\frac{dy}{dt} + 5y^3\frac{dx}{dt} = 0$ , whence  $\frac{dy}{dt} = \frac{-D \cdot 5x^4 - 5Dy^3}{5x \cdot 3y^2}$ 

15. (1 pt) Problems/setM151\_03\_08\_Implicit\_Differentiation/3.8.43.pg From Rogawski ET section 3.8, exercise 43.

Differentiate the equation  $y^7 + 2xy + x^4 = 0$  with respect to the variable t and express  $\frac{dy}{dt}$  in terms of  $\frac{dx}{dt}$ . (Use D for  $\frac{dx}{dt}$ ).

$$\frac{dy}{dt} =$$

SOLUTION: (Instructor solution preview: show the student solution after due date. )

**Solution:** Let  $y^7 + 2xy + x^4 = 0$ . Then  $7y^{7-1}\frac{dy}{dt} + 2 \cdot x\frac{dy}{dt} + 2 \cdot y\frac{dx}{dt} + 4y^{4-1}\frac{dx}{dt} = 0$ , whence  $\frac{dy}{dt} = \frac{-D(4x^3 + 2y)}{2x + 7y^6}$ 

### 1. (1 pt) Problems/setM151\_03\_11\_Related\_Rates/3.11.1.pg

From Rogawski ET section 3.11, exercise 1.

Consider a rectangular bathtub whose base is 83ft<sup>2</sup>.

How fast is the water level rising if water is filling the tub at a rate of 0.1ft<sup>3</sup>/min?

Answer: \_

### 2. (2 pts) Problems/setM151\_03\_11\_Related\_Rates/3.11.3.pg From Rogawski ET section 3.11, exercise 3.

The radius of a circular oil slick expands at a rate of 8 m/min.

(a) How fast is the area of the oil slick increasing when the radius is 25 m?

 $\frac{dA}{dA} =$ 

(b) If the radius is 0 at time t = 0, how fast is the area increasing after 2 min?

$$\frac{dA}{dt} = \underline{\hspace{1cm}}$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

**Solution:** Let r be the radius of the oil slick and A its area. Then  $A = \pi r^2$  and  $\frac{dA}{dt} = 2\pi r \frac{dr}{dt}$ . Substituting r = 25 and  $\frac{dr}{dt} = 8$ , we find  $\frac{dA}{dt} = 2\pi (25) (8) \approx 1256.63706143592 \text{ m}^2/\text{min.}$ Since  $\frac{dr}{dt} = 8$  and r(0) = 0, it follows that  $r(t) = 8 \cdot t$ . Thus,  $r(2) = 8 \cdot 2$  and  $\frac{dA}{dt} = 2\pi (8 \cdot 2)(8) \approx 804.247719318987 \text{m}^2/\text{min.}$ 

## 3. (2 pts) Problems/setM151\_03\_11\_Related\_Rates/3.11.5.pg

From Rogawski ET section 3.11, exercise 5.

Assume that the radius r of a sphere is expanding at a rate of

The volume of a sphere is  $V = \frac{4}{3}\pi r^3$  and its surface area is  $SA = 4\pi r^2$ .

(a) Determine the rate at which the volume is changing with respect to time when r = 14in.

 $\frac{dV}{dt} =$  \_\_\_\_\_\_ (b) Determine the rate at which the surface area is changing . . . when the radius is r = 14in.

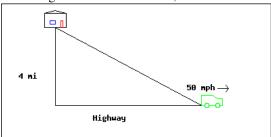
 $\frac{dSA}{dt} = \underline{\phantom{C}}$  **SOLUTION:** (Instructor solution preview: show the student solution after due date. )

**Solution:** As the radius is expanding at 14 inches per minute, we know that  $\frac{dr}{dt} = 14$  in./min. Taking the derivative with respect to t of the equation  $V = \frac{4}{3}\pi r^3$  yields

$$\frac{dV}{dt} = \frac{4}{3}\pi \left(3r^2 \frac{dr}{dt}\right) = 4\pi r^2 \frac{dr}{dt}.$$

Substituting 
$$r = 14$$
 and  $\frac{dr}{dt} = 13$  yields  $\frac{dV}{dt} = 4\pi 14^2(13) = \text{in./min.}$ 

From Rogawski ET section 3.11, exercise 9.



A road perpendicular to a highway leads to a farmhouse located 4 mi away. An automobile travels past the farmhouse at a speed of 50mph.

How fast is the distance between the automobile and the farmhouse increasing when the automobile is 7 mi past the intersection of the highway and the road?

Answer:

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

#### **Solution:**

Let *l* denote the distance between the automobile and the farmhouse, let d denote the distance between the farmhouse and the intersection of the highway and the road, and let s denote the distance past the intersection of the highway and the road. Then  $l^2 = d^2 + s^2$ . Taking the derivative of both sides of this equation yields  $2l\frac{dl}{dt} = 2s\frac{ds}{dt}$ , so:

$$\frac{dl}{dt} = \frac{s}{l} \frac{ds}{dt}$$

Equation yields 
$$2t \frac{dt}{dt} = 2s \frac{ds}{dt}$$
, so.

When the auto is 7 miles past the intersection, we have

$$\frac{dl}{dt} = 50 \frac{7}{\sqrt{4^2 + 7^2}} \approx 43.4122 \text{ mph}$$

### 5. (1 pt) Problems/setM151\_03\_11\_Related\_Rates/3.11.15.pg

From Rogawski ET section 3.11, exercise 15.

At a given moment, a plane passes directly above a radar station at an altitude of 5 miles.

(a) If the plane's speed is 400 mph, how fast is the distance between the plane and the station changing half an hour later?

(b) How fast is the distance between the plane and the station changing when the plane passes directly above the station?

SOLUTION: (Instructor solution preview: show the student solution after due date.)

**Solution:** Let x be the distance of the plane from the station along the ground and h the distance through the air.

By the Pythagorean Theorem, we have  $h^2 = x^2 + 5^2 = x^2 +$ 

Thus  $2h\frac{dh}{dt} = 2x\frac{dx}{dt}$ , and  $\frac{dh}{dt} = \frac{x}{h}\frac{dx}{dt}$ . After an half hour,  $x = \frac{1}{2} \times 400 = 200$  miles. With x = 200,  $h = \sqrt{200^2 + 25}$ , and  $\frac{dx}{dt} = \frac{200}{\sqrt{200^2 + 25}} \times 400 \approx 399.875058563249$  mph.

When the plane is directly above the station, x = 0, so the distance between the plane and the station is not changing, for at this instant we have  $\frac{dh}{dt} = \frac{0}{5} \times 400 = 0$  mph.

### 6. (1 pt) Problems/setM151\_03\_11\_Related\_Rates/3.11.17.pg From Rogawski ET section 3.11, exercise 17.

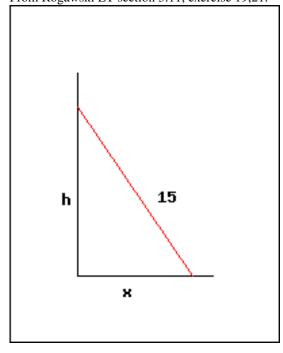
A hot air balloon rising vertically is tracked by an observer located 4 mi from the lift-off point. At a certain moment, the angle between the observer's line-of-sight and the horizontal is  $\frac{\pi}{6}$ , and it is changing at a rate of 0.1 rad/min. How fast is the balloon rising at this moment?

Answer: \_

SOLUTION: (Instructor solution preview: show the student solution after due date.)

**Solution:** Let y be the height of the balloon (in miles) and  $\boldsymbol{\theta}$  the angle between the line-of-sight and the horizontal. Via 

### 7. (2 pts) Problems/setM151\_03\_11\_Related\_Rates/3.11.21.pg From Rogawski ET section 3.11, exercise 19,21.



Consider a ladder that is 15 ft tall sliding down a wall. The variable h is the height of the ladder's top at time t, and x is the distance from the wall to the ladder's bottom.

(a) Assume the bottom slides away from the wall at a rate of 3ft/s. Find the velocity of the top of the ladder at time t=3 if the bottom is 3 ft from the wall at time t = 0.

Answer: \_\_\_

(b) Suppose that h(0) = 13 and the top slides down the wall at a rate of 2ft/s. Calculate x and dx/dt at t = 3 s.

$$x = \underline{\qquad \qquad }$$

$$\frac{dx}{dt} = \underline{\qquad \qquad }$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

Let x denote the distance from the base of the ladder to the wall, and h denote the height of the top of the ladder from the floor. The ladder is 15 ft long, so  $h^2 + x^2 = 15^2$ . At any time t, x = 3 + 3t. Therefore, at time t = 3, the base is 3 + 3(3) = 12from the wall. To find the rate at which the top of the ladder is moving, we solve for  $\frac{dh}{dt}$  in the equation  $2h\frac{dh}{dt} + 2x\frac{dx}{dt} = 0$  and

thus we obtain 
$$\frac{dh}{dt} = \frac{-12*3}{\sqrt{15^2 - 12^2}} \approx -4 \text{ ft/s}.$$

### 8. (1 pt) Problems/setM151\_03\_11\_Related\_Rates/3.11.25.pg

From Rogawski ET section 3.11, exercise 25.

Suppose that both the radius r and height h of a circular cone change at a rate of 9 cm/s. How fast is the volume of the cone changing when r = 7 and h = 19?

The volume is changing at a rate of \_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

### **Solution:**

Let r be the radius, h be the height, and V be the volume of a right circular cone. Then  $V = \frac{1}{3}\pi r^2 h$ , whence

$$\frac{dV}{dt} = \frac{1}{3}\pi \left(r^2 \frac{dh}{dt} + 2hr \frac{dr}{dt}\right).$$
When  $r = 7$ ,  $h = 19$ , and  $\frac{dr}{dt} = \frac{dh}{dt} = 9$ , we find: 
$$\frac{dV}{dt} = \frac{\pi}{3} \left(7^2 \cdot 9 + 2 \cdot 19 \cdot 7 \cdot 9\right) \approx 2968.81 \text{ cm}^3/\text{s}.$$

### 9. (1 pt) Problems/setM151\_03\_11\_Related\_Rates/3.11.27.pg From Rogawski ET section 3.11, exercise 27.

A searchlight rotates at a rate of 2 revolutions per minute.

The beam hits a wall located 15 miles away and produces a dot of light that moves horizontally along the wall. How fast is this dot moving when the angle  $\theta$  between the beam and the line through the searchlight perpendicular to the wall is  $\frac{\pi}{4}$ ? Note that  $d\theta/dt = 2(2\pi) = 4\pi$ .

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

#### **Solution:**

Let y be the distance between the dot of light and the point of intersection of the wall and the line through the searchlight perpendicular to the wall. Let  $\theta$  be the angle between the beam of light and the line. Using trigonometry, we have  $\tan \theta = \frac{y}{15}$ . Therefore,  $\sec^2 \theta \cdot \frac{d\theta}{dt} = \frac{1}{15} \frac{dy}{dt}$ , and  $\frac{dy}{dt} = 15 \frac{d\theta}{dt} \sec^2 \theta$ . With  $\theta = \frac{\pi}{4}$  and  $\frac{d\theta}{dt} = 4\pi$ , we find  $\frac{dy}{dt} = 15 (4\pi) \frac{1}{\cos^2 (\pi/4)} = 120\pi \approx 376.991118430775 \text{ mi/min.}$ 

Converting to miles per hour gives  $\frac{dy}{dt} \approx 22619.4671058465 \text{ mph. } 80 \text{ cm}^3/\text{min.}$   $\frac{dP}{dt} = \frac{dP}{dt}$ 

## **10.** (1 pt) Problems/setM151\_03\_11\_Related\_Rates/3.11.31.pg From Rogawski ET section 3.11, exercise 31.

A jogger runs around a circular track of radius 70 ft. Let (x,y) be her coordinates, where the origin is the center of the track. When the jogger's coordinates are (42,56), her *x*-coordinate is changing at a rate of 17 ft/s. Find dy/dt.

$$dy/dt =$$

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** We have  $x^2 + y^2 = 70^2$ . Thus  $2x \frac{dx}{dt} + 2y \frac{dy}{dt} = 0$ , and  $\frac{dy}{dt} = -\frac{x}{y} \frac{dx}{dt}$ . With x = 42, y = 56, and  $\frac{dx}{dt} = 17$ ,  $\frac{dy}{dt} = -\frac{42}{56}(17) = -12.75 \text{ ft/s}$ .

## **11.** (1 pt) Problems/setM151\_03\_11\_Related\_Rates/3.11.33.pg From Rogawski ET section 3.11, exercise 33.

The pressure P (in kilopascals) and volume V (in cubic centimeters) of an expanding gas are related by the formula  $PV^b = C$ , where b and C are constants (this holds in adiabatic expansion, without heat gain or loss).

Find 
$$\frac{dP}{dt}$$
 if  $b = 1.7$ ,  $P = 9$  kPa,  $V = 90$  cm<sup>3</sup>, and  $\frac{dV}{dt} = 80$  cm<sup>3</sup>/min.

 $\frac{dP}{dt} = \frac{dP}{dt}$  **SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

Let 
$$PV^b = C$$
. Then
$$PbV^{b-1}\frac{dV}{dt} + V^b\frac{dP}{dt} = 0,$$
whence
$$\frac{dP}{dt} = -\frac{Pb}{V}\frac{dV}{dt}.$$
Substituting  $b = 1.7, P = 9, V = 90$ , and  $\frac{dV}{dt} = 80$ ,
$$\frac{dP}{dt} = -\frac{(9)(1.7)}{90}(80) \approx -13.6 \text{ kPa/min}.$$

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1. (2 pts) Problems/setM151_04_01_Lin_Approx_Apps/4.1.PQ1.p	g
From Rogawski ET section 4.1, exercise PQ1.	

(a) Estimate 
$$g(9.1) - g(9)$$
 if  $g'(9) = 2$ .

$$f(4.6) \approx$$
 \_\_\_\_\_\_

### 2. (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.PQ3.pg From Rogawski ET section 4.1, exercise PQ2.

The velocity of a train at a given instant is 140 ft/s. How far does the train travel during the next half-second (use the Linear Approximation)?

Answer: \_\_

### 3. (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.1.pg From Rogawski ET section 4.1, exercise 1.

Consider f(x) = x.

Use the Linear Approximation to estimate  $\Delta f = f(1.02)$ f(1).

$$\Delta f \approx$$
\_\_\_\_\_

### 4. (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.5.pg

From Rogawski ET section 4.1, exercise 5.

Consider  $f(x) = e^{3x}$ .

Use the Linear Approximation to estimate  $\Delta f = f(3.04)$ f(3).

$$\Delta f \approx$$
\_\_\_\_\_

### 5. (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.7.pg From Rogawski ET section 4.1, exercise 7.

Consider  $f(x) = 9\ln(x)$ .

Use the Linear Approximation to estimate  $\Delta f = f((e^6) +$  $0.4) - f(e^6)$ .

$$\Delta f \approx$$
 \_\_\_\_\_

## 6. (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.9.pg

From Rogawski ET section 4.1, exercise 9.

Estimate  $\Delta f$  using the Linear Approximation and use a calculator to compute both the error and the percentage error.

$$f(x) = \sqrt{3+x},$$
  $a = 3,$   $\Delta x = 1$   
 $\Delta f \approx \underline{\hspace{1cm}}$ 

The error in the Linear Approximation is \_\_\_\_

The percentage error is \_

**SOLUTION:** (Instructor solution preview: show the student solution after due date. )

### **Solution:**

Let 
$$f(x) = \sqrt{3+x}$$
,  $a = 3$ ,  $\Delta x = 1$ . Then  $f'(x) = \frac{1}{2}(3+x)^{-1/2}$   
 $f'(a) = f'(3) = \frac{1}{2}(3+3)^{-1/2} = \text{and}$ 

$$\Delta f \approx f'(a)\Delta x = (1) = 0.204124145231932$$

The actual change is:  $\Delta f = f(a + \Delta x) - f(a) = f(4)$  $f(3) \approx$ 

The error in the Linear Approximation is therefore: |-0.204124145231932| =

In percentage terms, the error is:  $| \times 100\% = \%$ .

### 7. (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.11.pg From Rogawski ET section 4.1, exercise 11.

Estimate  $\Delta f$  using the Linear Approximation and use a calculator to compute both the error and the percentage error.

$$f(x) = \sin x$$
,  $a = 0$ ,  $\Delta x = 0.08$   
 $\Delta f \approx \underline{\qquad}$ 

The error in the Linear Approximation is \_\_

The percentage error is \_

SOLUTION: (Instructor solution preview: show the student solution after due date. )

**Solution:** The linear approximation to  $\Delta f$  at x = 0 is  $f'(0)\Delta x = \cos(0)\Delta x = \Delta x = 0.08$ .

The error is  $|\sin(0.08) - 0.08| = |0.0799146939691727 -$ 0.08 = 8.53060308273063e - 05. The percentage error is  $\frac{\sin(0.08) - L(0.08)}{\sin(0.08) - L(0.08)} \mid \times 100\% = 0.106746364892811\%.$ 

### 8. (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.13.pg From Rogawski ET section 4.1, exercise 13.

Estimate  $\Delta f$  using the Linear Approximation and use a calculator to compute both the error and the percentage error.

$$f(x) = \cos x,$$
  $a = \frac{\pi}{4},$   $\Delta x = 0.03$   
 $\Delta f \approx \underline{\hspace{1cm}}$ 

The error in the Linear Approximation is \_\_\_\_ The percentage error is \_

SOLUTION: (Instructor solution preview: show the student solution after due date.)

Let 
$$f(x) = \cos(x)$$
,  $a = \frac{\pi}{4}$ ,  $\Delta x = 0.03$ . Then  $f'(x) = -\sin(x)$ ,  $f'(a) = f'(\frac{\pi}{4}) = -\sin(\frac{\pi}{4}) = -0.707107$ 

$$\Delta f \approx f'(a)\Delta x = -0.707107 \cdot 0.03 = -0.0212132$$

The actual change is:  $\Delta f = f(a + \Delta x) - f(a) = f(\frac{\pi}{4} + 0.03)$  $f(\frac{\pi}{4}) = -0.0215282$ 

The error in the Linear Approximation is therefore:

|-0.0215282+0.0212132|=0.000314992 In percentage terms, the error is:  $|\frac{0.000314992}{-0.0215282}|\times100\%=1.46316\%$ 

**9.** (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.15.pg From Rogawski ET section 4.1, exercise 15.

Estimate  $\Delta f$  using the Linear Approximation and use a calculator to compute both the error and the percentage error.

$$f(x) = x^{1/3}e^{x-1},$$
  $a = 1,$   $\Delta x = 0.3$   
 $\Delta f \approx \underline{\hspace{1cm}}$ 

The error in the Linear Approximation is \_\_\_\_\_

The percentage error is \_\_\_\_\_

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** The linear approximation to  $\Delta f$  at x=1 is  $f'(1)\Delta x$ . The derivative is  $f'(x)=\frac{1}{3}x^{-2/3}e^{x-1}+x^{1/3}e^{x-1}$ , so  $f'(1)=\frac{1}{3}1^{-2/3}e^{1-1}+1^{1/3}e^{1-1}=1/3+1=4/3$ . Thus, the linear approximation to  $\Delta f=\frac{4}{3}\Delta x=0.4$ .

The error is  $|\Delta f - 0.4| = |f(1+0.3) - f(1) - 0.4| = 0.0732263.$ 

The percentage error is  $\mid \frac{error}{actualvalue} \mid \times 100\% = \mid \frac{error}{f(1+\Delta x)} \mid \times 100\% = \mid \frac{0.0732263}{1.47323} \mid \times 100\% = 15.4738\%.$ 

**10.** (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.19.pg From Rogawski ET section 4.1, exercise 19.

Estimate the quantity using Linear Approximation and find the error using a calculator.

$$\frac{1}{\sqrt{119}} - \frac{1}{11}$$
The Linear Approximation is:  $\Delta f \approx$  \_\_\_\_\_\_

The error in Linear Approximation is \_\_\_\_\_

**11.** (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.31.pg From Rogawski ET section 4.1, exercise 31.

The side s of a square carpet is measured at 9 ft. Estimate the maximum error in the area A of the carpet if s is accurate to within 7/8 in.

$$\Delta A \approx$$
\_\_\_\_\_  $ft^2$ 

**12.** (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.35.pg From Rogawski ET section 4.1, exercise 35.

The *stopping distance* for an automobile (after applying the brakes) is approximately  $F(s) = 1.2s + 0.059s^2$  ft, where s is the speed in mph. Use the Linear Approximation to estimate the stopping distance per additional mph when s = 25 and when s = 70

When 
$$s = 25$$
 mph,  $\Delta F \approx$  \_\_\_\_\_  
When  $s = 70$  mph,  $\Delta F \approx$  \_\_\_\_

**13.** (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.41.pg From Rogawski ET section 4.1, exercise 41.

Find the linearization L(x) of  $y = 10\sin(2x)\cos(x)$  at a = 0. L(x) =

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** The linearization L(x) of y at a = 0 is given by the formula L(x) = y(0) + y'(0)(x - 0) = 0 + 20x = 20x.

**14.** (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.43.pg From Rogawski ET section 4.1, exercise 43.

Find the linearization of 
$$y = (2+x)^{-1/2}$$
 at  $a = 0$ .  
 $L(x) =$ 

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

Let 
$$f(x)=(2+x)^{-1/2}$$
. Then  $f'(x)=-\frac{1}{2}(2+x)^{-3/2}$   $f'(a)=f'(0)=-\frac{1}{2}(0+2)^{-3/2}=-0.176777$  The linearization at  $a=0$  is:  $L(x)=f'(a)(x-a)+f(a)==-0.176777(x-0)+0.707107==-0.176777x-0.707107$ 

**15.** (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.45.pg From Rogawski ET section 4.1, exercise 45.

Find the linearization 
$$L(x)$$
 of  $y = (5 + 4x^2)^{-1/2}$  at  $a = 0$ .

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

**Solution:** The linearization L(x) of yat a = 0 is given by the formula  $L(x) = y(0) + y'(0)(x - 0) = 5^{-1/2} + (0)(x) = 5^{-1/2}$ .

**16.** (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.47.pg From Rogawski ET section 4.1, exercise 47.

Find the linearization of  $y = \sin^{-1} x$  at  $a = \frac{1}{2}$ .

Find the linearization of 
$$y = \sin^{-1} x$$
 at  $a = \frac{1}{2}$ .  
 $L(x) = \underline{\qquad}$ 

**SOLUTION:** (Instructor solution preview: show the student solution after due date.)

### **Solution:**

Let 
$$f(x) = \sin^{-1} x = \arcsin x$$
 Then  $f'(x) = \frac{1}{\sqrt{1 - x^2}}$   
 $f'(a) = f'(\frac{1}{2}) = \frac{1}{\sqrt{1 - \frac{1}{2}^2}} = 1.1547$ 

The linearization at a = 0.5 is: L(x) = f'(a)(x-a) + f(a) = 1.1547(x-0.5) + 0.523599 = 1.1547x + (-0.0537515)

**Solution:** The linearization L(x) of y at a=1 is given by the formula  $L(x)=y(1)+y'(1)(x-1)=0+(e^{9x})(x-1)=e^9x-e^9$ .

18. (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.53.pg
From Rogawski ET section 4.1, exercise 53.
Approximate using linearization and use a calculator to compute the percentage error.

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$\sqrt{65} \approx $	
The percentage error is	

**19.** (1 pt) Problems/setM151\_04\_01\_Lin\_Approx\_Apps/4.1.57.pg
From Rogawski ET section 4.1, exercise 57.
Approximate using linearization and use a calculator to compute the percentage error.

$$(125.995)^{1/3}$$
  
 $(125.995)^{1/3} \approx$  \_\_\_\_\_\_  
The percentage error is \_\_\_\_\_\_