Math 352 Workshop 03

February 28, 2014	Due: March 3	Name:

Modeling with Linear Equations

In this worksheet, please pay special attention to the setup: formulation of the initial value problems involved. Feel free to use whatever electronic help you like: calculator, phone, tablet, laptop, Robocop, Skynet, etc. Include an appropriate amount of calculation work.}

They see me rollin'

A certain college graduate borrows \$8000 to buy a car. The lender charges interest at an annual rate of 10%. Assuming that interest is compounded continuously and that the borrower makes payments continuously at a constant annual rate k, determine the payment rate k that is required to pay off the loan in 3 years.

Life after debt

A home buyer can afford to spend no more than \$800/month on mortgage payments. Suppose that the interest rate is 9% and that the term of the mortgage is 20 y. Assume that interest is compounded continuously and that payments are also made continuously.

Determine the maximum amount that this buyer can afford to borrow.

Spring 2014 Math 352

Clean energy

A nuclear reactor sits at the bottom of a pool with volume 75000 kL. The water in the pool is not processed or filtered, so algae naturally grow in it (far enough from the reactor unit, anyway). Operators must keep this growth within reasonable and safe limits, or facility operations will be adversely affected.

(a) Suppose that, in the absence of other factors, algae reproduce in the pool at such a rate that their mass doubles every (100/9) ln(2) days. Formulate and solve an initial value problem that will give you the growth constant *r*. This growth constant depends only on the algae's reproductive characteristics and the conditions in the ambient environment (which, given the proximity of the reactor, are not uniformly friendly). Make the usual assumption: that the change in population is directly proportional to the current population.

(b) Reactor operators use a combination of filtering and poison techniques to remove algae at a constant rate (so that the same mass of algae is removed each day). Suppose that a new regulation is going into effect right now (at t=0) that requires zero algae measured 20 d from this moment. If the mass of algae that can be removed from the pool is $400\,\mathrm{g/hr}$, find the greatest mass of algae that can be present at t=0 such that the facility will still be in compliance when the regulation takes effect. You will need to formulate and solve an appropriate initial value problem using the growth constant you found above. Pay attention to the setup and resist the urge to jump right to the equation for the algae mass.