

# The Pythagorean Theorem

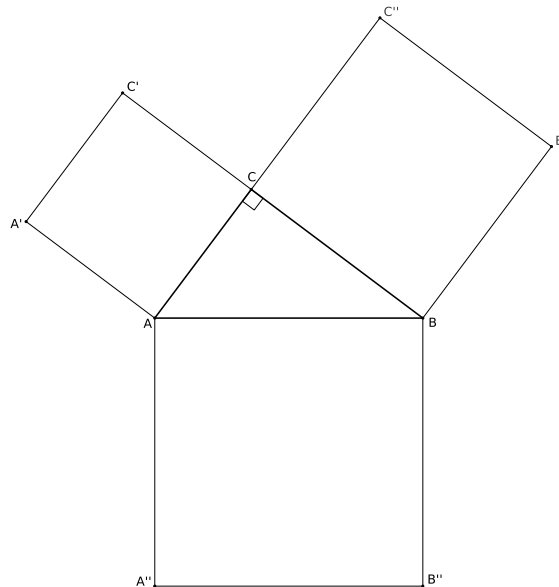
*In this activity we will prove the most famous theorem of all.*

**Question 1** Remind us, what is the most famous theorem of all and what exactly does it assert?

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## Euclid's proof

**Question 2** What would one need to prove about the following diagram to prove the Pythagorean Theorem?



Let's see if we can do this!

**Question 3** Draw a line perpendicular to  $\overline{AB}$  that passes through both  $C$  and  $\overline{A''B''}$ . Call the intersection between this line and  $\overline{AB}$ , point  $E$ ; call the intersection point between this line and  $\overline{A''B''}$ , point  $E'$ . Explain why  $\triangle ACA''$  has half the area of rectangle  $AEE'A''$ .

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**Question 4** Explain why  $\triangle ABA'$  has half the area of square  $ACC'A'$ .

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Learning outcomes:  
Author(s):

**Question 5** Explain why  $\triangle ACA''$  is congruent to  $\triangle ABA'$ .

**Question 6** Explain why area of square  $ACC'A'$  is equal to the area of rectangle  $AEE'A''$ .

**Question 7** Use similar ideas to complete a proof the Pythagorean Theorem.

### The converse

**Question 8** What is the converse to the Pythagorean Theorem? Is it true? How do you prove it?