

September 5, 2014

Due: End of class today

Name: _____

1 Coordinates revisited

We'll do these once or twice a week. They are usually collected a day later. This one will be collected at the end of class.

1.1 Warm-up

The first major topic in this course is the geometry of 3-dimensional Euclidean space \mathbf{R}^3 . Many people struggle with visualizing in this space or find it difficult to translate coordinate information into geometric information. This workshop will encourage you to rethink coordinates in the familiar Euclidean plane in preparation for the later discussion.

- As you work through the questions, check your answers with either Chelsea or Dr. Rosoff before going on.
- Raise a hand if you are really stuck.
- Talk a lot! Class goes better the more you talk to each other.
- Get up and work in a group at the board! There's plenty of room, and it is easier to see what others are up to.

1.2 Coordinates

Draw a coordinate plane, and plot the line $y = 2$.

1. What do all the points on the line $y = 2$ have in common? Answer as *clearly* and *succinctly* as you can. (Try to avoid referring to points' coordinates. The idea here is to remember how coordinates are defined in the first place.)
2. Give the best definition you can for the idea of "distance between a point and a line".
3. What do all the points on the line $x = -3$ have in common? What's the difference between $x = -3$ and $x = 3$?

4. How do you plot points? Where's the point $(2, 3)$? What does this point have to do with the lines you have been drawing?
5. Now draw yourself a 3-space, like on the board. What are the points $z = -1$? What shape do they make? Try to draw this shape.
6. Draw $y = -2$ in your 3-space. What's the difference between $y = -2$ and $y = 2$? Now Try to draw $x = 4$ in your 3-space. Where does $(4, 2, -1)$ live?
7. Given two points (x_0, y_0, z_0) and (x_1, y_1, z_1) , write down a formula for the square of the distance between them. Use the definitions of the coordinates you've figured out. If you are having trouble, try the exercise in just 2 dimensions first.