$$FI \xrightarrow{\ Fcata_\phi\ } FA$$

$$\downarrow in \qquad\qquad \downarrow \phi$$

$$I \xrightarrow{\ cata_\phi\ } A$$

$$\phi \circ Fcata_\phi = cata_\phi \circ in$$