

## More on Runtime Environments

- How to **efficiently** implement procedure call and return in the presence of **higher-order functions** ?

*what are higher-order functions ?*

*how to extend stack frames to support higher-order functions ?*

*efficiency issues (execution time, space usage) ?*

- How to **efficiently** support memory allocation and de-allocation ?

*what are the data representations ?*

*what are the memory layout ?*

*explicit vs implicit memory de-allocation ?*  
(malloc-free vs. garbage collection)

## Procedure Parameters (in Pascal)

- Procedure parameters permit procedures to be invoked “out-of-scope”;

```

1  program main(input, output);
2
3  procedure b(function h(n : integer): integer);
4      var m : integer;
5      begin m := 6; writeln(h(2)) end;
6
7  procedure c;
8      var m : integer;
9      function f(n: integer): integer;
10         begin f := m + n end;
11         begin m := 0; b(f) end;
12 begin c end.
```

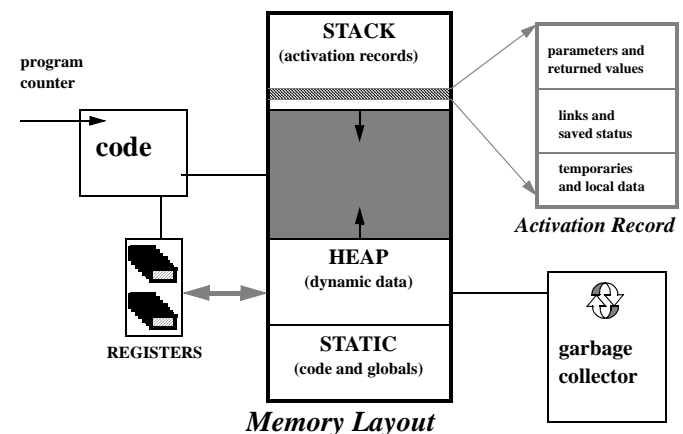
- Question:** how to get the correct environment when calling **h** inside **b** ?
- Solution:** *must pass static link along with f as if it had been called at the point it was passed (line 11).*

## Restrictions in C & Pascal

- C** does not allow nested procedures --- names in **C** are either local to some procedure or are global and visible in all procedures. Procedures in **C** can be passed as arguments or returned as results.
- Pascal** (or **Modula-2**, **Modula-3**, **Algol** ) allows procedure declarations to be nested, but procedure parameters are of restricted use, and procedures cannot be returned as result.
- Functional languages (e.g. **ML**, **Haskell**, **Scheme**, **Lisp**) support **higher-order functions** --- supporting both nested procedures and procedures passed as parameters or returned as results.

*supporting it is a big challenge to the compiler writers !*

## Traditional Stack Scheme



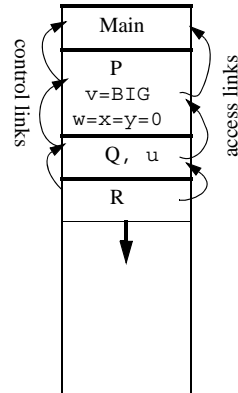
## Procedure Activations

### Nested Functions in ML

```

val BIG = big(N)
fun P(v,w,x,y) =
  let
    fun Q() =
      let val u = hd(v)
        fun R() =
          ... P(v,u,u,y) ...
        in ... R() ...
      end
    in ... Q() ...
  end
val result = P(BIG,0,0,0)

```



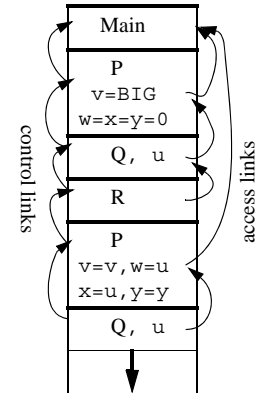
## Procedure Activations (cont'd)

### Nested Functions in ML

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fun P(v,w,x,y) =
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    fun Q() =
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      end
    in ... Q() ...
  end
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```



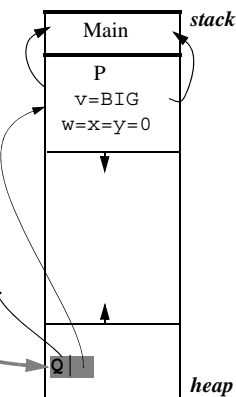
## Higher-Order Functions

### How to create a closure for Q?

```

fun P(v,w,x,y) =
  let
    fun Q() =
      let val u = hd(v)
        fun R() =
          ... (u,w+x+y+3) ...
        in ... R() ...
      end
    in Q
  end
val S = P(BIG,0,0,0)
val result = S()

```



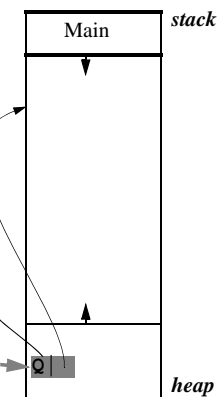
## Higher-Order Functions (cont'd)

### Q lost track of its environment

```

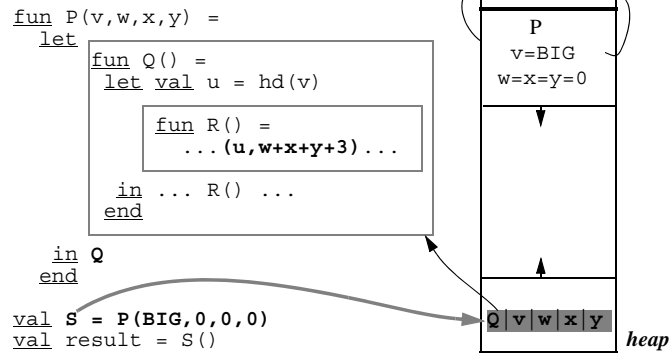
fun P(v,w,x,y) =
  let
    fun Q() =
      let val u = hd(v)
        fun R() =
          ... (u,w+x+y+3) ...
        in ... R() ...
      end
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  end
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```



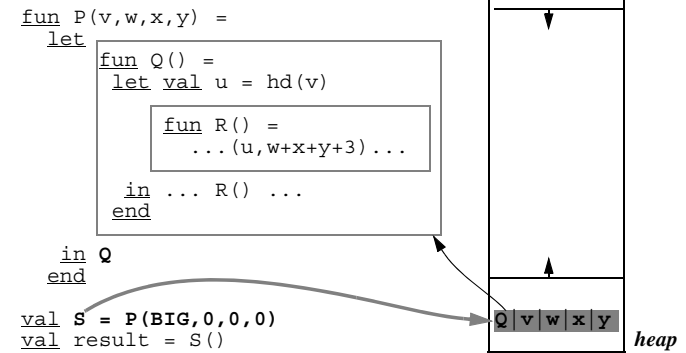
## Higher-Order Functions (cont'd)

**Q must copy the frame !**



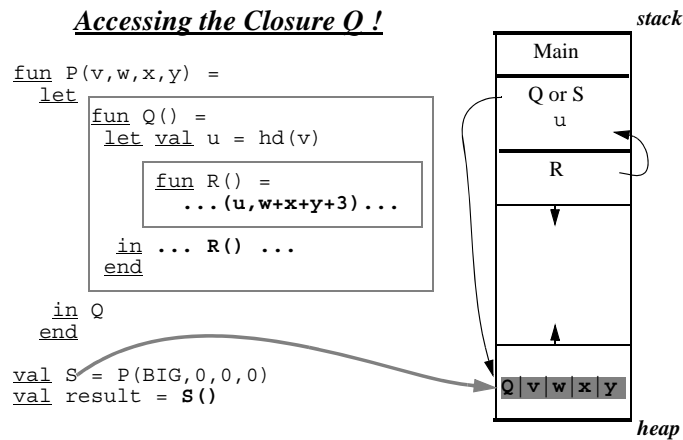
## Higher-Order Functions (cont'd)

**Q's environment is in the heap!**

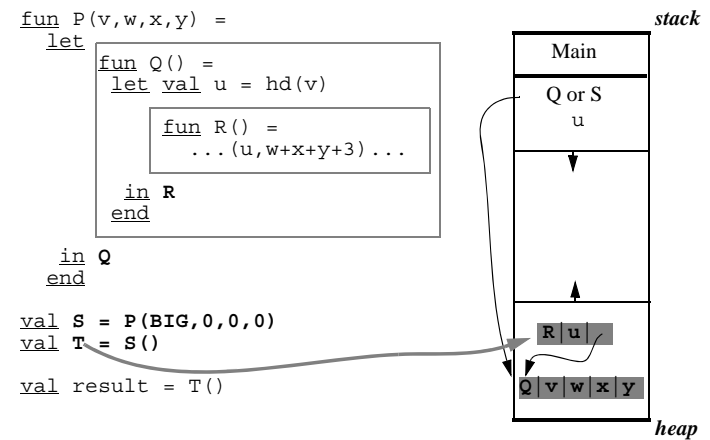


## Applying Higher-Order Functions

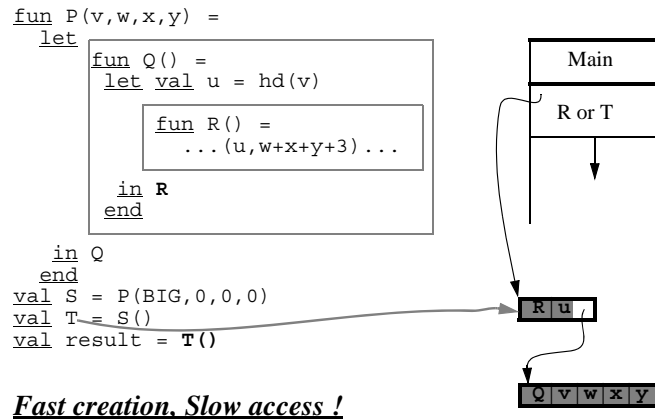
**Accessing the Closure Q !**



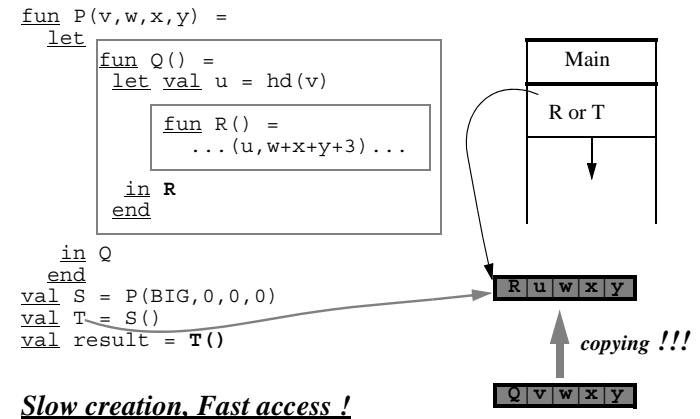
## Nested Higher-Order Functions



## Linked Closures



## Flat Closures



## Better Representations ?

- Closures cannot point to stack frame  
(different life time, so you must copy.)
- Linked closures --- fast creation, slow access  
Flat closures --- slow creation, fast access
- Stack frames with access links are similar to linked closures  
(accessing non-local variables is slow.)

***GOAL : We need good closure representations that have both fast access and fast creation !***

## Space Usage

### Space Leaks for Linked Closures

```

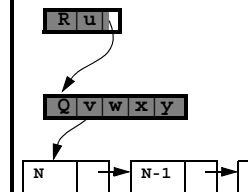
fun P(v,w,x,y) =
  let fun Q() =
        let val u = hd(v)
          fun R() = (u,w+x+y+3)
        in R
      end
    in Q
  end

fun loop (n,res) =
  if n<1 then res
  else (let val S = P(big(N),0,0,0)
        val T = S()
        in loop(n-1,T::res)
      end)

val result = loop(N,[])

```

**Linked Closures :**  
 $O(N^2)$



**Flat Closures :**  
 $O(N)$



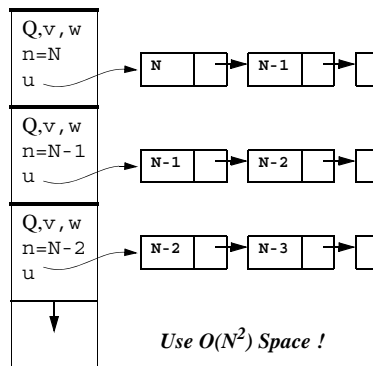
## Space Usage (cont'd)

### Space Leaks for Stack Allocations

```
fun P(x) = .....
```

```
  fun Q(n) = let
    val u = big(n)
    val v = P(u)
    val w = hd(u)
  in
    if n > 0
    then Q(n-1) + v(w)
    else ...
  end
```

```
  val result = Q(N)
```



"u" is dead after this call !

## Better Space Usage ?

- The **safe for space complexity** rule :

*Local variable must be assumed dead after its last use within its scope !*

- Stacks and linked closures are NOT safe for space
- Flat closures are safe for space
- SML/NJ : **unsafe version** = (2 to 80) x **safe version**

## Drawbacks of Stack Allocation

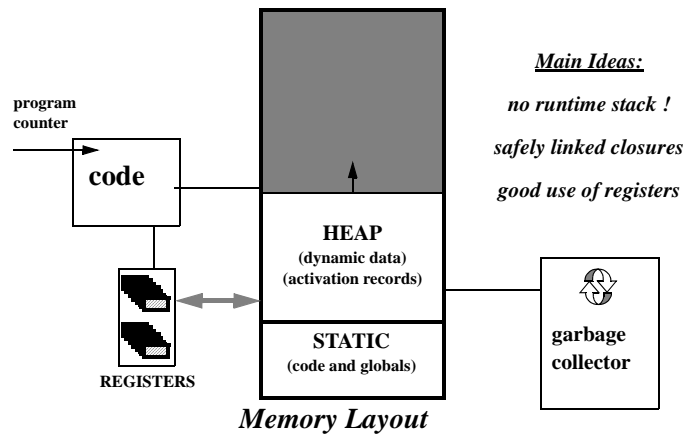
- inefficient space usage
- slow access to non-local variables
- expensive copying between stack and heap  
(activation records cannot be shared by closures)
- scanning roots is expensive in generational GC
- very slow first-class continuations (`call/cc`)
- correct implementation is complicated and messy

## Efficient Heap-based Compilation

*An efficient heap-based scheme has the following advantages:*

- very good space usage (safe for space complexity !)
- very fast closure creation and closure access
- closures can be shared with activation records
- fast `call/cc` and fast generational GC
- simple implementation

## Pure Heap-based Scheme



## Safely Linked Closures

### Safe for Space : use $O(N)$ space

```

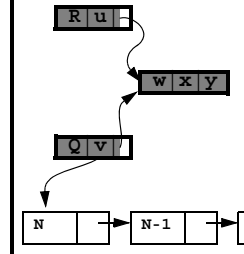
fun P(v,w,x,y) =
  let fun Q() =
        let val u = hd(v)
          fun R() = (u,w+x+y+3)
        in R
        end
    in Q
    end

fun loop (n,res) =
  if n<1 then res
  else (let val S = P(big(N),0,0,0)
        val T = S()
        in loop(n-1,T::res)
        end)

val result = loop(N, [])
  
```

### THE TRICK:

Variables  $w,x,y$  have same life time !



## Safely Linked Closures (cont'd)

### Shorter Access Path !

```

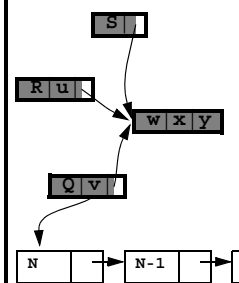
fun P(v,w,x,y) =
  let fun Q() =
        let val u = hd(v)
          fun R() =
              let fun S() = w+x+y+3
                in (S,u)
              end
        in R
        end
    in Q
    end

val T = P(big(N),0,0,0)
  
```

The number of links traversed is at most 1.

### THE TRICK:

Variables  $w,x,y$  have same life time !



## Good Use of Registers

- To avoid memory traffic, modern compilers often pass arguments, return results, and allocate local variables in machine registers.
- Typical parameter-passing convention on modern machines:
  - the first  $k$  arguments ( $k = 4$  or  $6$ ) of a function are passed in registers  $R_p, \dots, R_{p+k-1}$ , the rest are passed on the stack.
- Problem : extra memory traffic caused by passing args. in registers

```
function g(x : int, y : int, z :int) : int = x*y*z
```

```
function f(x : int, y : int, z : int) =
  let val a := g(z+3, y+3, x+4) in a*x+y+z end
```

Suppose function  $f$  and  $g$  pass their arguments in  $R_1, R_2, R_3$ ; then  $f$  must save  $R_1, R_2$ , and  $R_3$  to the memory before calling  $g$ .

## Good Use of Registers (cont'd)

*how to avoid extra memory traffic?*

- **Leaf procedures** (or functions) are procedures that do not call other procedures; e.g., the function `exchange`. The parameters of **leaf procedures** can be allocated in registers without causing any extra memory traffic.
- Use **global register allocation**, different functions use different set of registers to pass their arguments.
- Use register windows (as on SPARC) --- each function invocation can allocate a fresh set of registers.
- Allocate **closures** in registers or use **callee-save registers**
- When all fails --- save to the stack frame or to the heap.

## Closures in Registers ? No !

Module FOO: (in file "foo.sml")

```
fun pred(x) = ...v(w,x) ...
val result = BAR.filter(pred,...)
```

"pred" is an  
escaping function !

Its closure must be  
built on the heap !

Module BAR: (in file "bar.sml")

```
fun filter(p,l) =
  let fun h(s,z) =
        if (s=[]) then rev z
        else
          (let val a = car s
             val r = cdr s
             in if p a then h(r,a::z)
                else h(r,z)
            end)
        in h(l, [])
    end
```

**Escaping functions:**  
functions whose call  
sites are not all known  
at compile time !

## Closures in Registers ? Yes !

fun filter(p,l) = let

```
  fun h(s,z) =
    if (s=[]) then rev z
    else
      (let val a = car s
         val r = cdr s
         in if p a then h(r,a::z)
            else h(r,z)
        end)
  in h(l, [])
end
```

**Known functions:**

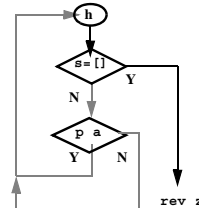
functions whose call sites  
are all known at compile  
time !

in h(l, [])  
end

"h" is a known function !

Its closure can be put in registers !  
{rev,p}

(e.g.,



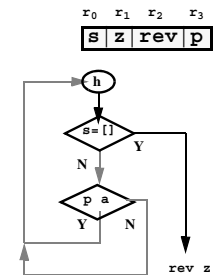
## "Lambda Lifting"

fun filter(p,l) = let

```
  fun h(s,z,rev,p) =
    if (s=[]) then rev z
    else
      (let val a = car s
         val r = cdr s
         in if p a then h(r,a::z,rev,p)
            else h(r,z,rev,p)
        end)
  in h(l, [], rev, p)
end
```

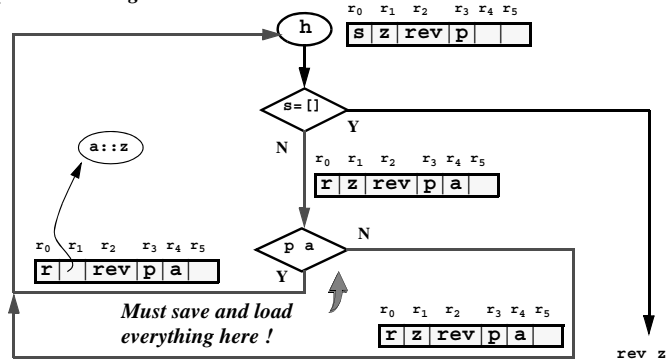
in h(l, [], rev, p)  
end

known functions can be rewritten into functions that  
are fully closed !  
(i.e. with no free variables !)



## “Spilled Activation Records”

We do not know how  
“p” treats the registers !



## Callee-save Registers

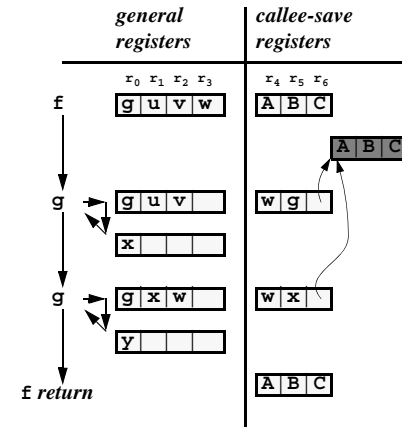
Convention :

Reserve  $k$  special registers !

Every function promises  
to always preserve these  
registers !

Example :  $k=3$  ( $x_4, x_5, x_6$ )

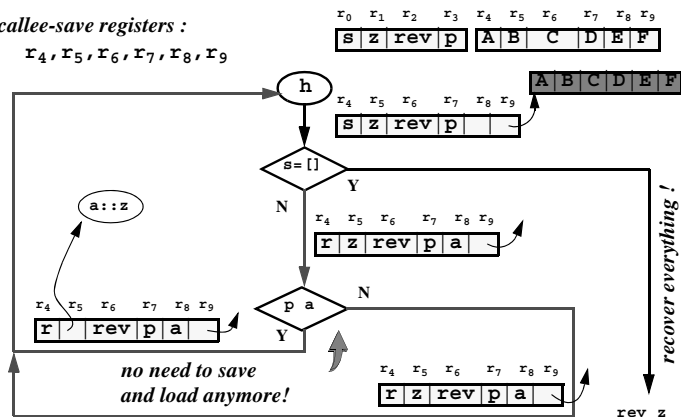
```
fun f(g,u,v,w) =
  let val x = g(u,v)
      val y = g(x,w)
  in x+y+w
  end
```



## Callee-save Registers (cont'd)

6 callee-save registers :

$x_4, x_5, x_6, x_7, x_8, x_9$



## Summary : A Uniform Solution

Take advantage of variable life time and compile-time  
control flow information !

“Spilled activation records” are also thought as closures !

- no runtime stack ----- everything is sharable
- all use *safely-linked closures* ----- to maximize sharing
- pass arguments and return results in registers
- allocating most closures in registers
- good use of callee-save registers