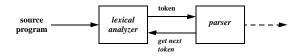
Lexical Analysis

• Read source program and produce a list of tokens ("linear" analysis)



- The lexical structure is specified using regular expressions
- · Other secondary tasks:
 - (1) get rid of white spaces (e.g., \t, \n, \sp) and comments
 - (2) line numbering

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 1 of 40

CS421 COMPILERS AND INTERPRETERS

The Lexical Structure

Output after the Lexical Analysis ---- token + associated value

LET 51	FUNCTION 56	<pre>ID(do_nothing1) 65</pre>
LPAREN 76	ID (a) 77	COLON 78
ID (int) 80	COMMA 83	ID (b) 85
COLON 86	ID(string) 88	RPAREN 94
EQ 95	<pre>ID(do_nothing2)</pre>	99
LPAREN 110	ID (a) 111	PLUS 112
INT (1) 113	RPAREN 114	FUNCTION 117
<pre>ID(do_nothing2)</pre>	126	LPAREN 137
ID (d) 138	COLON 139	ID (int) 141
RPAREN 144	EQ 146	
<pre>ID(do_nothing1)</pre>	150	LPAREN 161
ID (d) 162	COMMA 163	STRING (str) 165
RPAREN 170	IN 173	
<pre>ID(do_nothing1)</pre>	177	LPAREN 188
INT (0) 189	COMMA 190	STRING(str2) 192
RPAREN 198	END 200	EOF 203

CS421 COMPILERS AND INTERPRETERS

Example: Source Code

A Sample Toy Program:

What do we really care here?

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis: Page 2 of 40

Tokens

CS421 COMPILERS AND INTERPRETERS

• Tokens are the <u>atomic unit</u> of a language, and are usually <u>specific strings</u> or <u>instances</u> of <u>classes</u> of strings.

Tokens	Sample Values	Informal Description
LET	let	keyword LET
END	end	keyword END
PLUS	+	
LPAREN	(
COLON	:	
STRING	"str"	
RPAREN)	
INT	49, 48	integer constants
ID	do_nothing1, a, int, string	letter followed by letters, digits, and under scores
EQ	=	
EOF		end of file

Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis : Page 3 of 40 Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis : Page 4 of 40

Lexical Analysis, How?

• First, write down the <u>lexical specification</u> (how each token is defined?)

using **regular expression** to specify the lexical structure:

```
identifier = letter (letter | digit | underscore)* letter = a | \dots | z | A | \dots | Z digit = 0 | 1 | \dots | 9
```

 Second, based on the above lexical specification, build the lexical analyzer (to recognize tokens) by hand,

Regular Expression Spec ==> NFA ==> DFA ==> Transition Table ==> Lexical Analyzer

• Or just by using lex --- the lexical analyzer generator

Regular Expression Spec (in lex format) ==> feed to lex ==> Lexical Analyzer

Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis: Page 5 of 40

CS421 COMPILERS AND INTERPRETERS

Regular Expressions and Regular Languages

- Given an alphabet Σ , the **regular expressions** over Σ and their corresponding **regular languages** are
 - a) \emptyset denotes \emptyset ; ε , the empty string, denotes the language $\{\varepsilon\}$.
 - b) for each a in Σ , a denotes { a } --- a language with one string.
 - c) if R denotes L_R and S denotes L_S then R / S denotes the language $L_R \cup L_S$, i.e, $\{ x \mid x \in L_R \text{ or } x \in L_S \}$.
 - d) if R denotes L_R and S denotes L_S then RS denotes the language L_RL_S , that is, $\{xy \mid x \in L_R \text{ and } y \in L_S \}$.
 - e) if R denotes L_R then R^* denotes the language L_R^* where L^* is the union of all L^i (i=0,..., ∞) and L^i is just $\{x_1x_2...x_j \mid x_1 \in L, ..., x_i \in L\}$.
 - f) if R denotes L_R then (R) denotes the same language L_R

CS421 COMPILERS AND INTERPRETERS

Regular Expressions

 regular expressions are concise, linguistic characterization of regular languages (regular sets)

- each regular expression define a regular language --- a <u>set of strings</u> over some alphabet, such as ASCII characters; each member of this set is called a sentence, or a word
- · we use regular expressions to define each category of tokens

For example, the above identifier specifies a set of strings that are a sequence of letters, digits, and underscores, starting with a letter.

Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis: Page 6 of 40

Example

CS421 COMPILERS AND INTERPRETERS

Regular Expression	Explanation	
a*	0 or more a's	
a ⁺	1 or more a's	
(a b)*	all strings of a's and b's (including ε)	
(aa ab ba bb)*	all strings of a's and b's of even length	
[a-zA-Z]	shorthand for "a b z A Z"	
[0-9]	shorthand for "0 1 2 9"	
0([0-9])*0	numbers that start and end with 0	
(ab aab b)*(a aa e)	?	
?	all strings that contain foo as substring	

• the following is **not** a regular expression:

 a^nb^n (n > 0)

Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis : Page 7 of 40

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 8 of 40

Lexical Specification

Using regular expressions to specify tokens

```
keyword = begin | end | if | then | else
identifier = letter (letter | digit | underscore)*
integer = digit+
relop = < | <= | = | <> | > | >=
letter = a | b | ... | z | A | B | ... | Z
digit = 0 | 1 | 2 | ... | 9
```

- Ambiguity: is "begin" a keyword or an identifier?
- Next step: to construct a token recognizer for languages given by regular expressions --- by using finite automata!

given a string x, the token recognizer says "yes" if x is a sentence of the specified language and says "no" otherwise

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 9 of 40

CS421 COMPILERS AND INTERPRETERS

Transition Diagrams (cont'd)

The token recognizer (for identifiers) based on transition diagrams:

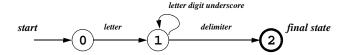
Next: 1. finite automata are generalized transition diagrams! 2. how to build finite automata from regular expressions?

Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis: Page 11 of 40

CS421 COMPILERS AND INTERPRETERS

Transition Diagrams

- Flowchart with states and edges; each edge is labelled with characters; certain subset of states are marked as "final states"
- Transition from state to state proceeds along edges according to the next input character



- Every string that ends up at a final state is accepted
- If get "stuck", there is no transition for a given character, it is an error
- Transition diagrams can be easily translated to programs using case statements (in C).

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 10 of 40

CS421 COMPILERS AND INTERPRETERS

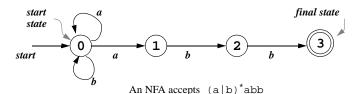
Finite Automata

- Finite Automata are similar to transition diagrams; they have states and labelled edges; there are one unique start state and one or more than one final states
- Nondeterministic Finite Automata (NFA):
 - a) ε can label edges (these edges are called ε -transitions)
 - b) some character can label 2 or more edges out of the same state
- Deterministic Finite Automata (DFA):
 - a) no edges are labelled with ϵ
 - b) each charcter can label at most **one** edge out of the same state
- NFA and DFA accepts string x if there exists a path from the start state to a
 final state labeled with characters in x

NFA: multiple paths **DFA:** one unique path

Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis: Page 12 of 40

Example: NFA

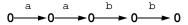


There are many possible moves --- to accept a string, we only need one sequence of moves that lead to a final state.

input string: aabb

One successful sequence: $0 \longrightarrow 0 \longrightarrow 1 \longrightarrow 2 \longrightarrow 0$

Another unsuccessful sequence:



Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis: Page 13 o

CS421 COMPILERS AND INTERPRETERS

Transition Table

• Finite Automata can also be represented using transition tables

For NFA, each entry is a set of states:

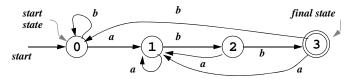
STATE	а	b
0	{0,1}	{0}
1	-	{2}
2	-	{3}
3	-	-

For DFA, each entry is a unique state:

STATE	а	b
0	1	0
1	1	2
2	1	3
3	1	0

CS421 COMPILERS AND INTERPRETERS

Example: DFA

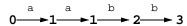


A DFA accepts (a|b)*abb

There is only one possible sequence of moves --- either lead to a final state and accept or the input string is rejected

input string: aabb

The sucessful sequence:



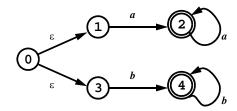
Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 14 of 40

CS421 COMPILERS AND INTERPRETERS

NFA with ϵ -transitions

1. NFA can have ϵ -transitions --- edges labelled with ϵ



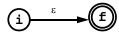
accepts the regular language denoted by (aa*|bb*)

Regular Expressions -> NFA

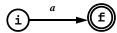
- How to construct NFA (with ε -transitions) from a regular expression?
- Algorithm: apply the following construction rules, use unique names for all the states. (inportant invariant: always one final state!)

1. Basic Construction

• •



• $a \in \Sigma$



Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 17 of 40

age 17 of 40

RE -> NFA (cont'd) 2. "Inductive" Construction • $R_1 \mid R_2$ • N_1 : NFA for R_1 N_2 : NFA for R_2 • N_1 or N_2 : NFA for N_2 the new and unique final state for N_1 and N_2 • $R_1 R_2$ merge: final state of N_1 and initial state of N_2 initial state • N_1 or N_2 final state final state

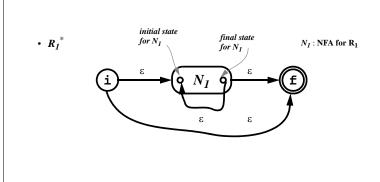
Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 18 of 40

CS421 COMPILERS AND INTERPRETERS

RE -> **NFA** (cont'd)

2. "Inductive" Construction (cont'd)

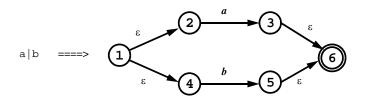


CS421 COMPILERS AND INTERPRETERS

Example: RE -> NFA Converting the regular expression: $(a|b)^*abb$

a (in a|b) ==> a

 $(in \ a | b) = 5$



CS421 COMPILERS AND INTERPRETERS

Example: RE -> NFA (cont'd)

Converting the regular expression: (a|b)*abb

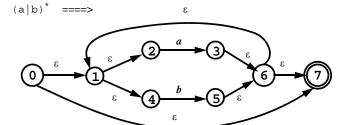
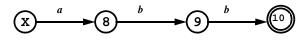


abb ====> (several steps are omitted)



Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 21 of 40

CS421 COMPILERS AND INTERPRETERS

$NFA \rightarrow DFA$

- NFA are non-deterministic; need DFA in order to write a deterministic prorgam!
- There exists an algorithm ("subset construction") to convert any NFA to a DFA that accepts the same language
- States in DFA are sets of states from NFA; DFA simulates "in parallel" all possible moves of NFA on given input.
- Definition: for each state s in NFA,

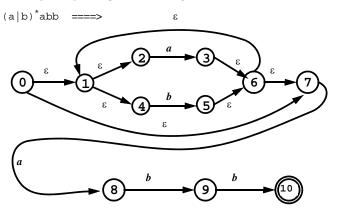
 ε -CLOSURE(\mathbf{s}) = { \mathbf{s} } \cup { \mathbf{t} | \mathbf{s} can reach \mathbf{t} via ε -transitions }

• **Definition:** for each set of states **S** in NFA,

 ε -CLOSURE(S) = $\bigcup_i \varepsilon$ -CLOSURE(S) for all S_i in S

Example: RE -> NFA (cont'd)

Converting the regular expression: (a|b)*abb



Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 22 of 40

C S 4 2 1 C O M P I L E R S A N D I N T E R P R E T E R S

NFA -> DFA (cont'd)

- each DFA-state is a **set** of NFA-states
- suppose the start state of the NFA is s, then the start state for its DFA is ε-CLOSURE(s); the final states of the DFA are those that include a NFA-final-state
- Algorithm: converting an NFA N into a DFA D----

```
Dstates = {e-CLOSURE(s<sub>0</sub>),s<sub>0</sub> is N's start state}
Dstates are initially "unmarked"
while there is an unmarked D-state X do {
    mark X
    for each a in S do {
        T = {states reached from any s<sub>i</sub> in X via a}
        Y = e-CLOSURE(T)
        if Y not in Dstates then add Y to Dstates "unmarked"
        add transition from X to Y, labelled with a
    }
}
```

Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis - Page 23 of 40

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 24 of 40

Example: NFA -> DFA

• converting NFA for (a|b) *abb to a DFA -----

The start state $A = \varepsilon$ -CLOSURE(0) = {0, 1, 2, 4, 7}; **Dstates**={A}

1st iteration: A is unmarked; mark A now; a-transitions: $T = \{3, 8\}$ a new state $B = \epsilon$ -CLOSURE(3) \cup ϵ -CLOSURE(8) $= \{3, 6, 1, 2, 4, 7\} \cup \{8\} = \{1, 2, 3, 4, 6, 7, 8\}$ add a transition from A to B labelled with a

b-transitions: $T = \{5\}$ a new state $C = \epsilon$ -CLOSURE(5) = $\{1, 2, 4, 5, 6, 7\}$ add a transition from A to C labelled with b **Dstates** = $\{A, B, C\}$

2nd iteration: B, C are unmarked; we pick B and mark B first; $B = \{1, 2, 3, 4, 6, 7, 8\}$ B's a-transitions: T = $\{3, 8\}$; T's ϵ -CLOSURE is B itself. add a transition from B to B labelled with a

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 25 of 40

Copyright 19

Lexical Analysis : Page 26 of 40

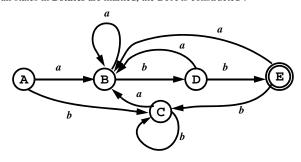
Example: NFA -> DFA (cont'd)

E's a-transitions: $T = \{3, 8\}$; its ϵ -CLOSURE is B. add a transition from E to B labelled with a E's b-transitions: $T = \{5\}$; its ϵ -CLOSURE is C itself.

CS421 COMPILERS AND INTERPRETERS

all states in **Dstates** are marked, the DFA is constructed!

add a transition from E to C labelled with b



Example: NFA -> DFA (cont'd)

CS421 COMPILERS AND INTERPRETERS

B's b-transitions: $T = \{5, 9\}$; a new state $D = \epsilon$ -CLOSURE($\{5, 9\}$) = $\{1, 2, 4, 5, 6, 7, 9\}$ add a transition from B to D labelled with b **Dstates** = $\{A, B, C, D\}$

then we pick C, and mark C

C's a-transitions: $T = \{3, 8\}$; its ϵ -CLOSURE is B. add a transition from C to B labelled with a C's b-transitions: $T = \{5\}$; its ϵ -CLOSURE is C itself. add a transition from C to C labelled with b

next we pick D, and mark D

D's a-transitions: $T = \{3, 8\}$; its ϵ -CLOSURE is B. add a transition from D to B labelled with a D's b-transitions: $T = \{5, 10\}$; a new state $E = \epsilon$ -CLOSURE($\{5, 10\}$) = $\{1, 2, 4, 5, 6, 7, 10\}$ **Dstates** = $\{A, B, C, D, E\}$; E is a **final state** since it has 10;

next we pick E, and mark E

Copyright 1994 - 2015 Zhong Shao, Yale University

Other Algorithms

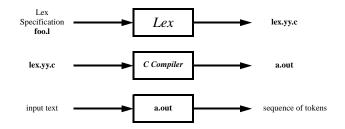
CS421 COMPILERS AND INTERPRETERS

- How to minimize a DFA? (see Dragon Book 3.9, pp141)
- How to convert RE to DFA directly? (see Dragon Book 3.9, pp135)
- How to prove two Regular Expressions are equivalent? (see Dragon Book pp150, Exercise 3.22)

Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis : Page 27 of 40 Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis - Page 28 of 40

Lex

• Lex is a program generator ----- it takes lexical specification as input, and produces a lexical processor written in C.



• Implementation of Lex:

Lex Spec -> NFA -> DFA -> Transition Tables + Actions -> yylex()

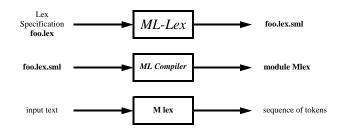
Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 29 of 40

CS421 COMPILERS AND INTERPRETERS

ML-Lex

• ML-Lex is like Lex ------ it takes lexical specification as input, and produces a lexical processor written in Standard ML.



• Implementation of ML-Lex is similar to implementation of Lex

CS421 COMPILERS AND INTERPRETERS

Lex Specification

- expression is a regular expression; action is a piece of C program;
- for details, read the **Lesk&Schmidt** paper

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 30 of 40

 $C\ S\ 4\ 2\ 1 \quad C\ O\ M\ P\ I\ L\ E\ R\ S \quad A\ N\ D \quad I\ N\ T\ E\ R\ P\ R\ E\ T\ E\ R\ S$

ML-Lex Specification

```
type pos = int
                                         user's ML
val lineNum = ...
                                        declarations
val lexresult = ....
%%
%s COMMENT STRING;
SPACE=[ \t \n \012];
                                     ml-lex definitions
DIGITS=[0-9];
%%
expression => (action);
                                      translation rules
integer
            => (print("INT"));
            => (...lineNum...);
                                        can call the above
                                        ML declarations
```

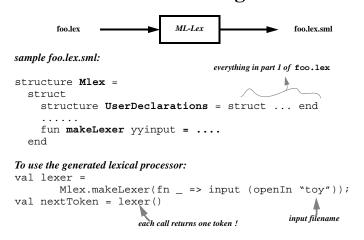
• <u>expression</u> is a regular expression; <u>action</u> is a piece of ML program; when the input matches the <u>expression</u>, the <u>action</u> is executed, the text matched is placed in the variable <u>yytext</u>.

Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis: Page 31 of 40

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 32 of 40

What does ML-Lex generate?



Copyright 1994 - 2015 Zhong Shao, Yale University

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 33 of 40

CS421 COMPILERS AND INTERPRETERS

ML-Lex Translation Rules

• Each translation rule (3rd part) are in the form

```
<start-state-list> regular expression => (action);
```

• Valid ML-Lex regular expressions: (see ML-Lex-manual pp 4-6)

a character stands for itself except for the reserved chars: ? * + | () ^ \$ / ; . = < > [{ " \ to use these chars, use backslash! for example, \\\" represents the string \"

using square brackets to enclose a set of characters (\ - ^ are reserved)

> [abc] char a, or b, or c [^abc] all chars except a, b, c [a-z] all chars from a to z $[\n\t\]$ new line, tab, or backspace [-abc] char - or a or b or c

CS421 COMPILERS AND INTERPRETERS

ML-Lex Definitions

• Things you can write inside the "ml-lex definitions" section (2nd part):

%s COMMENT STRING define new start states

REJECT() to reject a match %reject %count count the line number the resulting structure name %structure {identifier}

(the default is Mlex)

(hint: you probably don't need use %reject, %count,or %structure for assignment 2.)

Definition of named regular expressions:

<u>identifier</u> = <u>regular</u> <u>expression</u>

```
SPACE=[ \t \n \012]
IDCHAR = [a-zA-Z0-9]
```

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 34 of 40

CS421 COMPILERS AND INTERPRETERS

ML-Lex Translation Rules (cont'd)

• Valid ML-Lex regular expressions: (cont'd)

escape sequences: (can be used inside or outside square brackets)

\b backspace \n newline \t tab

any ascii char (ddd is 3 digit decimal)

any char except newline (equivalent to [^\n])

match string x exactly even if it contains reserved chars "x"

an optional x x? 0 or more x's x*

1 or more x's x+ хУ

if at the beginning, match at the beginning of a line only $\{x\}$ substitute definition x (defined in the lex definition section)

same as regular expression x repeating x for n times $x\{n\}$

 $x\{m-n\}$ repeating x from m to n times

Lexical Analysis : Page 35 of 40 Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis : Page 36 of 40

ML-Lex Translation Rules (cont'd)

what are valid actions?

- Actions are basically ML code (with the following extensions)
- All actions in a lex file must return values of the same type
- Use yytext to refer to the current string

```
[a-z]+ => (print yytext);
[0-9]{3} => (print (Char.ord(sub(yytext,0))));
```

- Can refer to anything defined in the ML-Declaration section (1st part)
- YYBEGIN <u>start-state</u> ---- enter into another start state
- lex() and continue() to reinvoking the lexing function
- yypos --- refer to the current position

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis: Page 37 of 40

CS421 COMPILERS AND INTERPRETERS

Start States (or Start Conditions)

- <u>start states</u> permit multiple lexical analyzers to run together.
- each <u>translation rule</u> can be prefixed with <start-state>
- the lexer is initially in a predefined start stae called **INITIAL**
- define new start states (in ml-lex-definitions): %s COMMENT STRING
- to switch to another start states (in action):
 YYBEGIN COMMENT
- example: multi-line comments in C

```
%%
%s COMMENT
%%
<INITIAL>"/*" => (YYBEGIN COMMENT; continue());
<COMMENT>"*/" => (YYBEGIN INITIAL; continue());
<COMMENT>.|"\n" => (continue());
<INITIAL> . . . . . . .
```

CS421 COMPILERS AND INTERPRETERS

Ambiguity

- what if more than one translation rules matches?
 - A. <u>longest</u> match is preferred
 - B. among rules which matched the same number of characters, the rule given <u>first</u> is preferred

```
%%
%%
the state of the sta
```

```
input "while" matches rule 1 according B above
input "<=" matches rule 4 according A above</pre>
```

Copyright 1994 - 2015 Zhong Shao, Yale University

Lexical Analysis : Page 38 of 40

CS421 COMPILERS AND INTERPRETERS

Implementation of Lex

- construct NFA for <u>sum</u> of Lex translation rules (regexp/action);
- · convert NFA to DFA, then minimize the DFA
- to recognize the input, simulate DFA to termination; find the <u>last</u> DFA state that includes NFA final state, execute associated action (this pickes longest match).
 If the last DFA state has >1 NFA final states, pick one for rule that appears first
- how to represent DFA, the transition table:

```
2D array indexed by state and input-character too big!
each state has a linked list of (char, next-state) pairs too slow!
hybrid scheme is the best
```

Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis : Page 39 of 40 Copyright 1994 - 2015 Zhong Shao, Yale University Lexical Analysis : Page 40 of 40