

## You have a singly-linked list ↴

A **linked list** is a low-level data structure. It stores an *ordered* sequence of items in individual "node" objects that have pointers to other nodes.

In a **singly-linked list**, the nodes each have one pointer to the next node.

```
class LinkedListNode
  attr_accessor :value, :next

  def initialize(value)
    @value = value
    @next = nil
  end
end
```

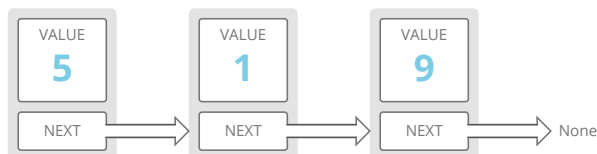
Ruby ▼

So we could build a singly-linked list like this:

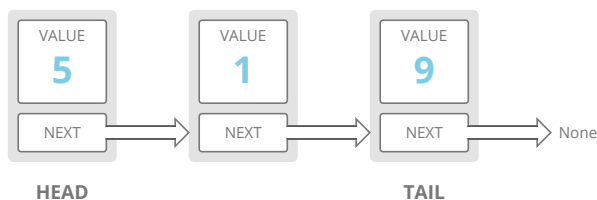
```
a = LinkedListNode.new(5)
b = LinkedListNode.new(1)
c = LinkedListNode.new(9)

a.next = b
b.next = c
```

Ruby ▼



In a linked list, the first node is called the **head** and the last node is called the **tail**.



Often, our only connection to *the list itself* is a variable pointing to the head. From there we can walk down the list to all the other nodes.

Like linked lists, **arrays** also store ordered lists of items, so you usually have a choice of which one to use.

**Advantages of linked lists:**

1. Linked lists have **constant-time insertions and deletions** in any position (you just change some pointers). Arrays require  $O(n)$  time to do the same thing, because you'd have to "shift" all the subsequent items over 1 index.
2. Linked lists can **continue to expand** as long as there is space on the machine. Arrays (in low-level languages) must have their size specified ahead of time. Even in languages with "dynamic arrays" that automatically resize themselves when they run out of space (like Python, Ruby and JavaScript), the operation to resize a dynamic array has a large cost which can make a single insertion unexpectedly expensive.

#### Disadvantages of linked lists:

1. To access or edit an item in a linked list, you have to **take  $O(i)$  time to walk from the head of the list to the  $i$ th item** (unless of course you already have a pointer directly to that item). Arrays have *constant-time* lookups and edits to the  $i$ th item.

Another type of linked list is a **doubly linked list**, which has pointers to the next *and the previous* nodes.

```
class LinkedListNode
  attr_accessor :value, :next, :previous

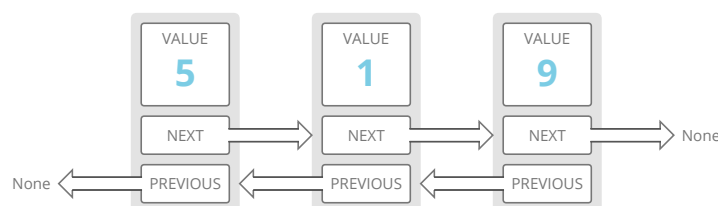
  def initialize(value)
    @value = value
    @next = nil
    @previous = nil
  end
end
```

So we could build a doubly linked list like this:

```
a = LinkedListNode.new(5)
b = LinkedListNode.new(1)
c = LinkedListNode.new(9)

# put b after a
a.next = b
b.previous = a

# put c after b
b.next = c
c.previous = b
```



Doubly linked lists allow us to traverse our list *backwards*. In a *singly* linked list, if you just had a pointer to a node in the *middle* of a list, there would be *no way* to know what its previous node was. Not a problem in a doubly linked list.

## and want to check if it contains a cycle.

A singly-linked list is built with nodes, where each node has:

- `node.next`—the next node in the list.
- `node.value`—the data held in the node. For example, if our linked list stores people in line at the movies, `node.value` might be the person's name.

For example:

```
class LinkedListNode
  attr_accessor :value, :next

  def initialize(value)
    @value = value
    @next = nil
  end
end
```

Ruby ▼

A **cycle** occurs when a node's `@next` points *back* to a *previous node in the list*. The linked list is no longer linear with a beginning and end—instead, it cycles through a loop of nodes.

**Write a function `contains_cycle()` that takes the first node in a singly-linked list and returns a boolean indicating whether the list contains a cycle.**

## Gotchas

Careful—a cycle can occur in the *middle* of a list, or it can simply mean the last node links back to the first node. Does your function work for both?

We can do this in  $O(n)$  time and  $O(1)$  space!

## Breakdown

Because a cycle could result from the last node linking to the first node, we might need to look at every node before we even see the start of our cycle again. So it seems like we can't do better than  $O(n)$  runtime.

How can we track the nodes we've already seen?

**Using a set, we could store all the nodes we've seen so far.** The algorithm is simple:

1. If the current node is already in our set, we have a cycle. Return true.
2. If the current node is `nil` we've hit the end of the list. Return false.
3. Else throw the current node in our set and keep going.

What are the time and space costs of this approach? Can we do better?

Our runtime is  $O(n)$ , the best we can do. But our space cost is also  $O(n)$ . Can we get our space cost down to  $O(1)$  by storing a *constant* number of nodes?

Think about a *looping* list and a *linear* list. What happens when you traverse one versus the other?

A linear list has an *end*—a node that doesn't have a `@next` node. But a looped list will run forever. We know we don't have a loop if we ever reach an end node, but how can we tell if we've run into a loop?

We can't just run our function for a really long time, because we'd never really know with certainty if we were in a loop or just a really long list.

Imagine that you're running on a long, mountainous running trail that happens to be a loop. What are some ways you can tell you're running in a loop?

One way is to **look for landmarks**. You could remember one specific point, and if you pass that point again, you know you're running in a loop. Can we use that principle here?

**Well, our cycle can occur *after* a non-cyclical "head" section in the beginning of our linked list.** So we'd need to make sure we chose a "landmark" node that is in the cyclical "tail" and not in the non-cyclical "head." That seems impossible unless we *already know* whether or not there's a cycle...

Think back to the running trail. Besides landmarks, what are some other ways you could tell you're running in a loop? What if you had **another runner**? (Remember, it's a *singly*-linked list, so no running backwards!)

A tempting approach could be to have the other runner stop and act as a "landmark," and see if you pass her again. But we still have the problem of making sure our "landmark" is in the loop and not in the non-looping beginning of the trail.

**What if our "landmark" runner moves continuously but *slowly*?**

If we sprint *quickly* down the trail and the landmark runner jogs *slowly*, we will eventually "lap" (catch up to) the landmark runner!

But what if there isn't a loop?

Then we (the faster runner) will simply hit the end of the trail (or linked list).

So let's make two variables, `slow_runner` and `fast_runner`. We'll start both on the first node, and every time `slow_runner` advances one node, we'll have `fast_runner` advance *two* nodes.

If `fast_runner` catches up with `slow_runner`, we know we have a loop. If not, eventually `fast_runner` will hit the end of the linked list and we'll know we *don't* have a loop.

This is a complete solution! Can you code it up?

Make sure the function eventually terminates in all cases!

## Solution

We keep two pointers to nodes (we'll call these "runners"), both starting at the first node. Every time `slow_runner` moves one node ahead, `fast_runner` moves *two* nodes ahead.

If the linked list has a cycle, `fast_runner` will "lap" (catch up with) `slow_runner`, and they will momentarily equal each other.

If the list does not have a cycle, `fast_runner` will reach the end.

```
def contains_cycle(first_node)

  # start both runners at the beginning
  slow_runner = first_node
  fast_runner = first_node

  # until we hit the end of the list
  while fast_runner != nil && fast_runner.next != nil
    slow_runner = slow_runner.next
    fast_runner = fast_runner.next.next

    # case: fast_runner is about to "lap" slow_runner
    if fast_runner == slow_runner
      return true
    end
  end

  # case: fast_runner hit the end of the list
  return false
end
```

## Complexity

$O(n)$  time and  $O(1)$  space.

The runtime analysis is a little tricky. The worst case is when we *do* have a cycle, so we don't return until `fast_runner` equals `slow_runner`. But how long will that take?

First, we notice that when both runners are circling around the cycle **`fast_runner` can never skip over `slow_runner`**. Why is this true?

Suppose `fast_runner` *had* just skipped over `slow_runner`. `fast_runner` would only be 1 node ahead of `slow_runner`, since their speeds differ by only 1. So we would have something like this:

```
[ ] -> [s] -> [f]
```

What would the step right *before* this "skipping step" look like? `fast_runner` would be 2 nodes back, and `slow_runner` would be 1 node back. But wait, that means they would be at *the same node*! So `fast_runner` *didn't* skip over `slow_runner`! (This is a proof by contradiction.)

Since `fast_runner` can't skip over `slow_runner`, *at most* `slow_runner` will run around the cycle once and `fast_runner` will run around twice. This gives us a runtime of  $O(n)$ .

For space, we store two variables no matter how long the linked list is, which gives us a space cost of  $O(1)$ .

## Bonus

1. How would you detect the *first node* in the cycle? Define the first node of the cycle as the one closest to the head of the list.
2. Would the program always work if the fast runner moves *three* steps every time the slow runner moves one step?
3. What if instead of a simple linked list, you had a structure where each node could have several "`@next`" nodes? This data structure is called a "directed graph." How would you test if your directed graph had a cycle?

## What We Learned

Some people have trouble coming up with the "two runners" approach. That's expected—it's somewhat of a blind insight. Even great candidates might need a few hints to get all the way there. And that's fine.

Remember that the coding interview is a *dialogue*, and sometimes your interviewer *expects* she'll have to offer some hints along the way.

One of the most impressive things you can do as a candidate is listen to a hint, fully understand it, and take it to its next logical step. Interview Cake gives you lots of opportunities to practice this. Don't be shy about showing *lots* of hints on our exercises—that's what they're there for!

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