

Assignment 5

AI1110: Probability and Random Variables

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paupolis PROBLEM 9.29

(paupolis, Exercise 9.29) (Paupolis chapter 9 ,ex 9.29) find $E\{y^2(t)\}$ a) If $R_{XX}(\tau) = 5\delta(\tau)$ and $y'(t) + 2y(t) = X(t)$ all t. b) if i) holds for $t > 0$ only and $y(t) = 0$ for $t \leq 0$

I. SOLUTION

Solution

- a) if $y'(t) + 2y(t) = X(t)$, then $y(t) = x(t) * h(t)$
- where $h(t) = e^{-2t}u(t)$ and with $q(t) = 5$, (10-90) yields
- $E\{y^2(t)\} = 5 * e^{-4t} U(T) = 5 * \int_0^\infty e^{-4t} d(\tau) = \frac{5}{4}$
- b) as a) with $q(t) = 5U(t)$. hence, for $t > 0$
- $E\{y^2(t)\} = 5U(t) * e^{-4t} U(t) = 5 * \int_0^t e^{-4t} d\tau = \frac{5}{4}(1 - e^{-4t})$
- hence proved