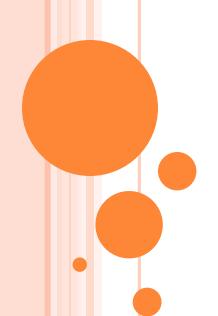




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Binary Search Algorithm

Definition

Find the position of a specified input key value within an array sorted by key value

Daily life example

Keyword: Sorted! 已經排序好value才有binary search 例如 頁碼 英文字典

- Find a specific page in a book (翻書找頁碼)
- Search for a word in a dictionary (從字典中找單字)

Numerical example

Example: The list to be searched: L = 13468911. The value to be found: X = 4.

Compare X to 6. X is smaller. Repeat with L = 1 3 4.

Compare X to 3. X is bigger. Repeat with L = 4.

Compare X to 4. They are equal. We're done, we found X.



Recursive Function for Binary Search

recursive left mid right int binarySearch(int A[], int key, int left, int right) { if (left(> right)) // test if array is empty return KEY NOT FOUND; int mid = (midpoint (left, right); // calculate midpoint to cut set in half // three-way comparison // key is in lower subset if (A[mid] > key) return binary search (A, key, left, mid else if (A[mid] < key) // key is in upper subset /2 右移return binary search(A, key, mid + 1, right); else // key has been found return mid: Quiz: How to compute mid? mid=(left+right)/2 → Overflow risk!_{if array} ★大 mid=left+(right-left)/2 → More reliable!

- Example usage
 - index = binarySearch(vec, key, 0, vec.size()-1)



Iterative Function for Binary Search

Iterative function

Quiz: A better way to compute mid

→ By interpolation

如果是線性 可以用內差



Summary

Comparisons

Quiz!

- Linear search
- 正比於n o Complexity O(n)
- o For any unsorted arrays → Fast when appending new elements Considerable speedup if frequently searched items are placed at the beginning
 - Binary search

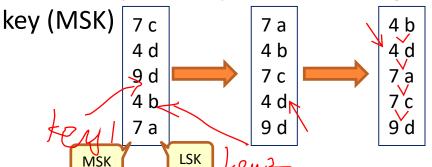
好 o Complexity O(log(n)) 要先排序好 For sorted arrays → Slow when inserting new elements

- Hash search
- 好 Complexity O(1)
 - o For arrays pre-processed by hash functions



Extensions

- Other similar problems
 - Interval finding (e.g., insertion sort)
 - Given a sorted vector, find the interval of a given value.
 - Non-zero element finding
 - o Given a sign-sorted vector, find the no. of positive elements. **a** 重號一邊 正號一邊 ______
- Binary search using multiple keys Quiz!
 - Preprocessing stage: Stable-sort with multiple keys, starting from the least-significant key (LSK)
 - Search stage: Binary search starting from the most-significant



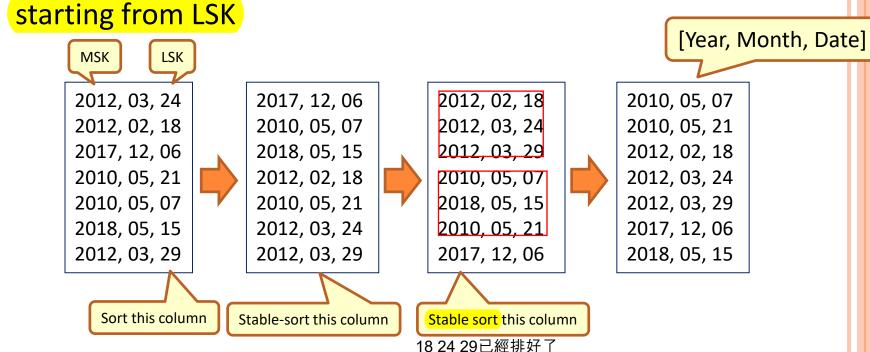
For instance: search for [Year, Month, Date]



Example of Binary Search with Multiple Keys

Quiz!

Preprocessing stage: Stable-sort data with multiple keys,



O Search stage: Binary search starting from MSK

Let's search for (2012, 03, 29)