

CH3.結晶固體的結構

基本概念

1. **crystalline** → material is one in which the atoms are situated in a repeating or periodic array over large atomic distances 長程有序排列!!
2. **crystal structure** → the manner in which atoms, ions, or molecules are spatially arranged → 就是 BCC.FCC.HCP 啦!
3. **lattice** → 三維排列的點與原子位置(center)相符合(coincide)
4. **atomic hard sphere model** → 表達了和鄰居的接觸, well-defined 直徑
5. 為了描述方便將 crystal structure 細分更小的重複實體 → **unit cell**

FCC → 金銀銅鋁鉛鉑鎳

HCP → Mg.Zn.Ti.Cd.Co(美新胎葛鬼)

Crystal structure → 描述單位晶胞的幾何和原子排列

FCC	單位晶胞 4 個原子, CN=12, APF=0.74, 最密面(111)
BCC	單位晶胞 2 個原子, CN=8, APF=0.68
HCP	單位晶胞 6 個原子(有時會算錯), CN=12, APF=0.74, $c/a=1.633^*(pf)$ 最密面(0001) (*單位晶胞含 3 個 parallelepipeds)

金屬有較高的 APF 使自由電子雲提供的 shielding 最大化

Polymorphism → 具有一種以上的 crystal structure → 若為元素通常稱為 → **Allotropy**
即同形體, 同素異形體, 不同狀況有不同晶體結構

EX. C(石墨.鑽石), Fe(BCC.FCC), White (β) tin → Gray (α) tin

Crystal system → 只描述單位晶胞的幾何, crystal structure 屬於他

Lattice parameters → 六個參數來定義單位晶胞的幾何 a, b, c 和 α, β, γ

七大晶系 14 種單位晶胞 → all

都直角: Cubic(3 邊同) → tetragonal(2 邊同) → orthorhombic(都不同)

三邊同, 三角同 but 非直角 → 菱 → rhombohedral

Hexagonal

Monoclinic → 單斜 → 三邊都不同, 有一角非直角

Triclinic → 三斜 → 三邊都不同, 三角都不同

Crystallographic directions → 中刮號[uvw]

若是六方 → Miller-Bravais

$$[u'v'w'] \longrightarrow [uvtw]$$

***basal plane** → 六方中, a_1, a_2, a_3 在同一面

$$u = \frac{1}{3}(2u' - v')$$

$$v = \frac{1}{3}(2v' - u')$$

$$t = -(u + v)$$

$$w = w'$$

CRYSTALLOGRAPHIC PLANES

Miller indices → 小刮號(hkl)

遇六方 → (hkil)

$$i = -(h + k) \quad \text{其它指數相同}$$

取截距倒數(平行視為無窮遠截距)，再取最小整數組

有截距法求平面的味道，截距倒數為法向量

*在 cubic crystal 中，有個特性是方向和平面指數相同時，兩者互相垂直。

*有時候指數不會減化(X 光繞射)，對陶磁材料而言，減化指數和未減化指數代表的平面可能不同!

平面族 → 大刮號{...}

A "family" of planes contains all those planes that are crystallographically equivalent 有相同的原子堆積!!

EX. 在 cubic，3 個數字無論順序和符號組成的平面都是同平面族

*[方向] → (平面) → {族}

$$LD = \frac{\text{number of atoms centered on direction vector}}{\text{length of direction vector}} \quad \text{單位為長度倒數}$$

$$PD = \frac{\text{number of atoms centered on a plane}}{\text{area of plane}} \quad \text{單位為面積倒數}$$

Close-packed

HCP → ABABABAB

FCC → ABCABCABC

For a crystalline solid, when the periodic and repeated arrangement of atoms is perfect or extends throughout the entirety of the specimen without interruption, the result is a single crystal.

atomic mismatch within the region where two grains meet; this area, called a grain boundary

Most crystalline solids are composed of a collection of many small crystals or grains; such materials are termed polycrystalline.

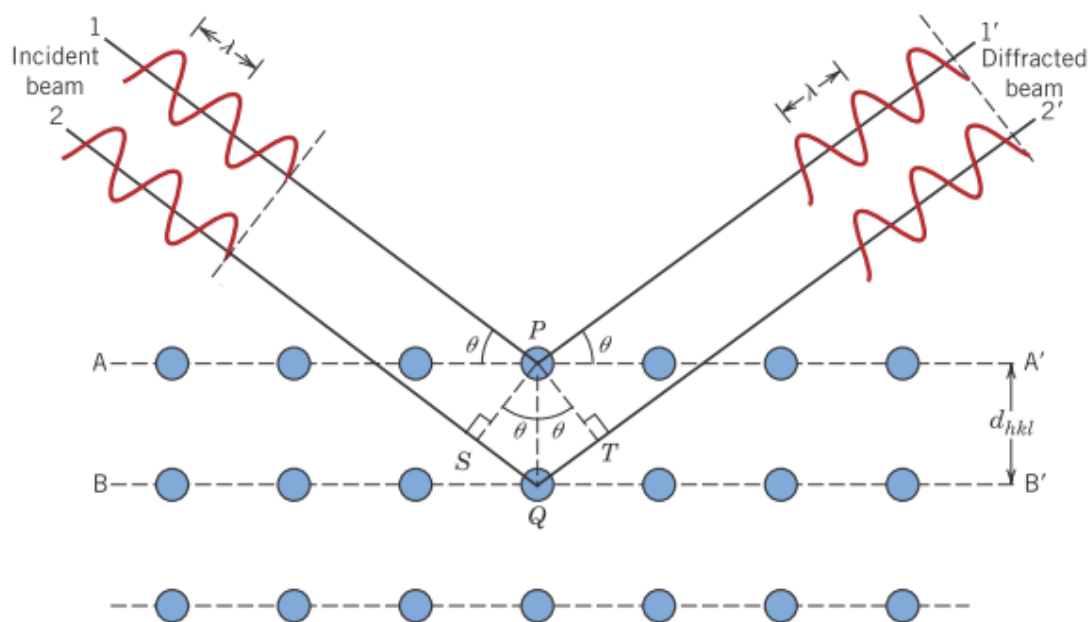
對多晶材料而言，即使每一晶粒都是異向性的，由晶粒組成的試片是等向行為因為個別晶粒的方向是隨機的。

Sometimes the grains in polycrystalline materials have a preferential crystallographic orientation, in which case the material is said to have a texture.

Ex. iron alloys 的[100]方向的 magnetic texture

Noncrystalline=amorphous, supercooled liquid * 共價鍵方向性較易形成非晶 liquids

X-Ray Diffraction(這部分要去複習 smith)



$$n\lambda = d_{hkl} \sin \theta + d_{hkl} \sin \theta$$

$$= 2d_{hkl} \sin \theta$$

$$d_{hkl} = \frac{a}{\sqrt{h^2 + k^2 + l^2}}$$

(cubic symmetry)

上式為充分非必要，當 BCC 或 FCC，除了 corner 的位置，其他位置 may 成為散射中心。

繞射條件

BCC → $h+k+l \rightarrow$ 偶

FCC → $h,k,l \rightarrow$ 全奇或全偶

繞射角: 2θ

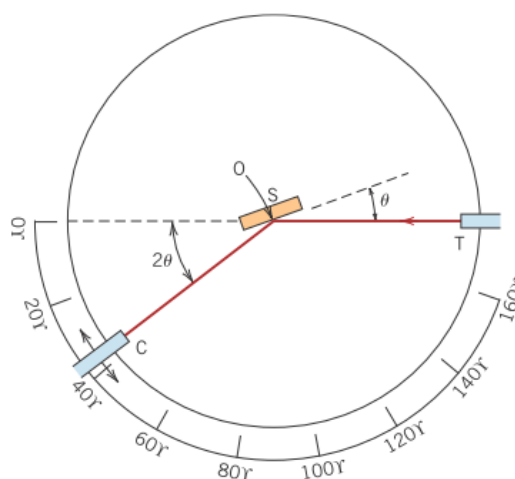
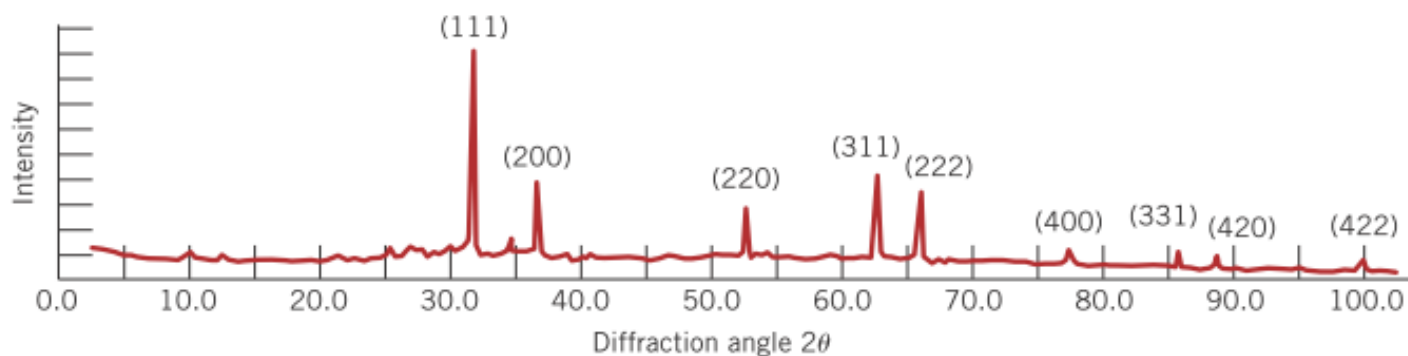


Figure 3.20 Schematic diagram of an x-ray diffractometer; T = x-ray source, S = specimen, C = detector, and O = the axis around which the specimen and detector rotate.



Smith 補充

LRO→long-range-order	
SRO→short-range-order	EX.水分子短程有序，但分子間以弱次級鍵隨機鍵結，長程無序
Crystalline solid	
Amorphous	全部原子位置都隨機的

Crystal structure	
Space lattice	3-D array of points , have same geometric environment
lattice points	Space lattice 中的一個點
Unit cell	Space lattice 中最小的重複 unit
Motif	A group of atoms that are organized relative to each other and are associated with a lattice point
Lattice constant	描述 unit cell 的長度和角度皆為 lattice constant!

三個最 common→BCC.FCC.HCP 差不多占了 90%的金屬

HCP→一般是指 larger cell(為了方便)，再細分是 primitive cell

larger cell→含 6 個原子

primitive cell→含 2 個原子

方向[uvw]→<uvw>

平面(hkl)→{hkl} ； HCP 用 Miller-Bravais indices{hkil}

	BCC	FCC	HCP
最密堆積方向	<111>directions	<110>directions	<1120>directions
最密堆積平面	沒有	{111}directions	{0001}directions

注意是 directions

Polymorphic→一材料在不同狀況(溫度、壓力)，可形成不同的 crystalline form

或 allotropy 同素異形:EX. Fe 溫度要背!! 912→1394→1539

X-Ray→電磁波，波長約 0.05~0.25nm，藉由加速電子撞擊 target metal 產生

約 98%的動能會轉變成熱能，需要冷卻系統!

Characteristic radiation is an intense form of x-ray radiation which occurs at specific wavelengths for a particular element. The K_{α} radiation, the most intense characteristic radiation emitted, is caused by excited electrons dropping from the second atomic shell ($n = 2$) to the first shell ($n = 1$). The next most intense radiation, K_{β} , is caused by excited electrons dropping from the third atomic shell ($n = 3$) to the first shell ($n = 1$).

最常用的 X-Ray 技術→powder method

*X-Ray 的複習翻一下 smith，講的比 callister 多

金屬玻璃→快速凝固→性質比結晶還好，用 X 光繞射沒清楚可見的峰值(因非晶)