# The proofpack package\*

David W. Agler https://github.com/davidagler/proofpack

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### 1 Introduction

There are several packages that provide support for typesetting natural deduction proofs. These include lplfitch by John Etchemendy, Dave Barker-Plummer, and Richard Zach, logicproof by Alan Davison, natded by Ajalloeian and Pelletier, fitch by Johan Klöwer, another fitch by Peter Selinger, and bussproofs by Samuel R. Buss.

proofpack is another package to typeset natural deduction proofs (in mostly a Fitch-style way). proofpack is most similar to fitch.sty by Johan W. Klawer (June 10, 2001) and edited by Alexander W. Kocurek (June 8, 2019). It deviates from this package in several ways, but notably it allows for simpler input. The simpler input makes it more attractive to those new to LATEX and for students learning logic.

## 2 Usage

The way to create a natural deduction proof using proofpack is to use one of the three environments: sdeduce, mdeduce, or ldeduce. Proofs are formatted in the same way you would create a table using tabular except you don't need to specify the number of columns and, at least for two of the environments, the numbering of the lines is automatic. Within the environments, you can use the commands \hyp, \hypl, and \sub to create assumptions and subproofs.

#### 2.1 Environments and Commands

The main environments for creating proofs are sdeduce, mdeduce, and ldeduce. These are short for "short deduction", "manual deduction", and "long deduction", respectively. Here is a brief description of each environment.

- sdeduce (env.) This environment creates proofs that do not break across the page. Proofs are automatically numbered. Usage: \begin{sdeduce} ... \end{sdeduce}.
- mdeduce (env.) This environment creates proofs that do not break across the page. Proofs are manually numbered. Usage: \begin{mdeduce} . . \end{mdeduce}.

<sup>\*</sup>This document corresponds to proofpack v0.2, dated 2023/07/09.

ldeduce (env.) This environment creates proofs that break across the page. Proofs are automatically numbered. Usage: \begin{ldeduce} ... \end{ldeduce}.

Without a package, natural deduction proofs are super easy to make so long as you don't need to make any assumptions: you can make the proof in a tabular environment.

The headache of typesetting proofs in LATEX using tables comes when you need to make an assumption and start a subproof. To solve this problem, proofpack makes use of three commands. The primary commands creating and reasoning in subproofs are \hyp, \hyp1, and \sub. These are short for "hypothesis", "hypothesis with a line", and "subproof, respectively. The commands are used in the sdeduce, mdeduce, and ldeduce environments. Here is a brief description of each of these commands:

\hyp The \hyp[\langle int] command is used in a sdeduce, mdeduce, or ldeduce environment to make an assumption / hypothesis (hyp). The hypothesis does not have a right line underneath like you see in many textbooks. Example: \hyp P\rightarrow Q. The command takes an optional argument to set the depth of the subproof. Example: \hyp[3] P\rightarrow Q. This is a major improvement on earlier fitch.sty as it results in less code. You don't need to write \hyp\hyp\hyp P\rightarrow Q. The default depth is 1.

\hypl The \hypl[ $\langle int \rangle$ ] command is used in a sdeduce, mdeduce, or ldeduce environment to make an assumption / hypothesis (hyp) with a line underneath the assumption. Example: \hypl P\rightarrow Q. The command takes an optional argument to set the depth of the subproof. Example: \hypl[3] P\rightarrow Q. This sets the depth of the formula  $P \to Q$  at 3. The default depth is 1.

\sub The \sub[\langle int\rangle] command is used in a sdeduce, mdeduce, or ldeduce environment to set a formula at a certain depth within a subproof. Example: \sub P\rightarrow Q. The command takes an optional argument to set the depth of the subproof. Example: \sub[3] P\rightarrow Q. This sets the depth of the formula  $P \to Q$  at 3. The default depth is 1.

### 3 Examples

Now that we have a sense of the key environments and commands, let's see some examples. In our first example, we'll use the sdeduce environment to create a non-breaking proof. Notice that the proof is automatically numbered, that the middle column is in math mode so you do not need to write \$P\rightarrow Q\$ but the rightmost column is not in math mode so you need to write \$\rightarrow E\$. Just as with the tabular environment, you can use the & command to move to the next column and the \\ command to move to the next row.

To typeset a proof without automatic numbering, use the mdeduce environment. With mdeduce you need to add a column for the line numbers. The line numbers are automatically formatted.

Assumptions and subproofs are created using the hyp and hypl commands. Both commands take one optional argument: the depth of the subproof. The default depth is 1. The hyp command creates an assumption / hypothesis (hyp) without a line underneath. The hypl command creates an assumption / hypothesis (hyp) with a line underneath. To create a subproof, simply write \hyp[int] or \hypl[int] before the formula you want to set as an assumption, where int is a positive integer.

Let's look at at an example where we use hyp.

To move deeper into the subproof, we can change the optional argument of the hyp and hypl commands. The default depth is 1. The following example shows how to use the optional argument to move deeper into the subproof.

	0	D	\begin{sdeduce}
1	Q	Р	Q &P\\
2	P	A	\hyp1[1] P &A\\
3		Α	\hyp1[2] Q &A\\
0	4	- 11	\end{sdeduce}

Whereas hyp and hyp1 are commands for moving deeper into (starting) a subproof, sub is a command for moving within a subproof of the same level. Just write \sub[int] where int is the depth of the subproof expressed as an integer. The following example shows how to use the sub command.

Here is a proof illustrates the use of hypl and sub together.

When the proof is manually numbered, you want to place the hyp, hypl, and sub commands after the column that has the numbering. The following example shows how to use the hyp, hypl, and sub commands in the mdeduce environment and that manual numbering of lines is not restricted to integers.

1 $P o Q$	P	\begin{mdeduce}	
_	D	1& P\rightarrow Q &P\\	
2 P	Р	2& P &P\\	
з $Q$	$1,2 \to E$	3& Q &\$1,2 \1	rightarrow E\$\\
$_{\mathrm{n+k}}\ Q$	$1,2 \rightarrow E$	n+k & Q &\$1,2 \1	rightarrow E\$\\
	,	n+k+1 &\hyp[1] Q	rightarrow E\$\\
$n+k+1 \mid Q$	$1, 2 \to E$	\end{mdeduce}	

You can place a box around formulas or the justification in the proof. This may be useful if you want to highlight certain lines in a proof. If you put a formula in a box, you need to use mathmode.

You can also color anything in mathmode in the proof. Usage: \cwff[color]{formula} This may be useful if you want to highlight certain lines in a proof.

For long proofs or for proofs you want to break across pages, use the ldeduce environment. This environment will automatically number the lines of the proof.

```
(\forall x)Sx
                             A, 3rd level
12
                             1,2 \rightarrow E
             q
13
14
           Q
                             1,2 \rightarrow E
                             1, 2 \rightarrow E
15
     q
                             1,2\to E
16
     e
                             1,2 \rightarrow E
17
     Γ
                             1, 2 \rightarrow E
18
     \sum
                             1,2 \rightarrow E
19
                             1,2 \rightarrow E
     Q
20
     Q
                             1,2 \rightarrow E
21
     Q
                             1,2 \rightarrow E
^{22}
                             1,2 \rightarrow E
23
     Q
     Q
                             1,2 \rightarrow E
^{24}
     Q
                             1,2 \rightarrow E
^{25}
                             1,2 \rightarrow E
     Q
26
                             1,2\to E
     Q
27
                             1,2\to E
     Q
28
                             1,2 \rightarrow E
     Q
29
     Q
                             1,2 \rightarrow E
30
                             1, 2 \rightarrow E
     Q
31
                             1,2 \rightarrow E
     Q
32
33
     Q
                             1,2 \rightarrow E
                             1, 2 \rightarrow E
     Q
34
                             1,2 \rightarrow E
     Q
35
                             1,2\to E
     Q
36
                             1, 2 \rightarrow E
     Q
37
                             1,2 \rightarrow E
     Q
38
                             1, 2 \rightarrow E
     Q
39
                             1, 2 \rightarrow E
     Q
40
     Q
                             1, 2 \rightarrow E
41
    Q
                             1,2 \rightarrow E
42
\begin{ldeduce}
\phi\rightarrow \psi
                                                     &P\\
(\exists x)(\exists y)Pxy
                                                    &P\\
\hyp \cwff[magenta]{P\rightarrow Q}
                                                    &$1,2\vee E$\\
\sub[1] \Box P
                                                     &$1,2 \text{ } E$\
\left[1\right] \in P
                                                     &1,2 \rightarrow E
\Diamond\phi\leftrightarrow\phi
                                                     &Magic rule\\
```

 $\triangleright \phi \land \psi$ 

11

\hypl[1] Q

\hyp[2] (\exists x)Px

2nd level

 $\$  \sub[1] \bxdwff{\$Q\rightarrow Q\$} &\$1,2 \vee E\$\\

&New Assumption!\\

&A, 2nd level\\

```
\sub[2] \phi\wedge\psi \rightmarker &2nd level\\
\sub[2] \leftmarker \phi\wedge\psi
                                    &2nd level\\
\hypl[3] (\forall x)Sx
                                    &$A$, 3rd level\\
                                    &$1,2 \rightarrow E$\\
\sub[3] q
\sub[2] Q
                                    &$1,2 \rightarrow E$\\
                                    &$1,2 \rightarrow E$\\
                                    &$1,2 \rightarrow E$\\
                                    &$1,2 \rightarrow E$\\
                                    &1,2 \rightarrow E
\Gamma
\Sigma
                                    &$1,2 \rightarrow E$\\
                                    &$1,2 \rightarrow E$\\
Q
                                    &$1,2 \rightarrow E$\\
Q
Q
                                    &1,2 \rightarrow E
                                    &$1,2 \rightarrow E$\\
Q
Q
                                    &$1,2 \rightarrow E$\\
Q
                                    &$1,2 \rightarrow E$\\
Q
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Q
                                    &$1,2 \rightarrow E$\\
                                    &$1,2 \rightarrow E$\\
                                    &$1,2 \rightarrow E$\\
                                    &$1,2 \rightarrow E$\\
Q
                                    &1,2 \rightarrow E
Q
                                    &$1,2 \rightarrow E$\\
Q
Q
                                    &$1,2 \rightarrow E$\\
                                    &$1,2 \rightarrow E$\\
\end{ldeduce}
```

## 4 Implementation

```
<*package>
```

packages Some packages are required for the package to work.

```
\RequirePackage{lmodern, amsmath, tikz} \RequirePackage{amssymb, mathtools, etoolbox, array, longtable}
```

counters Several counters are used to keep track of the line numbers in the proof.

```
\newcounter{deducecounter}
\setcounter{deducecounter}{0}
\newbool{resetdeducecounter}
\booltrue{resetdeducecounter}
\newbool{increasededucecounter}
\booltrue{increasededucecounter}
```

more counters Several counters are used to keep track of the line numbers in the proof. When the user sets line counter, userlinecounter switches to true and the counter is manually set.

```
\newcounter{userlinecounternum}
\setcounter{userlinecounternum}{0}
\newbool{userlinecounter} % manually set line counter
\boolfalse{userlinecounter}
```

\formatdeducecounter Formats the line numbers in the proof.

```
\newcommand{\formatdeducecounter}[1]{\scriptsize \arabic{#1}}
```

\deducecounter Increments the line counter in the proof. If the user sets the line counter, then the counter is set by the user. Otherwise, the counter is incremented by 1. Also formats the line counter. See \formatdeducecounter if you want to change the font style of the line counter.

```
\newcommand{\deducecounter}{%
\ifbool{increasededucecounter}{\addtocounter{deducecounter}{1}}{}
\ifbool{userlinecounter}{\setcounter{deducecounter}{
    \value{userlinecounternum}}}{}%
\formatdeducecounter{deducecounter}}
```

\pplineht Formats the line heights in the proof.

```
\newlength{\pplineht}
\setlength{\pplineht}{1.5\baselineskip}
```

\ppindent Horizontal indent between proof levels, used by the \hyp, \hyp1, and \sub commands. Increase or decrease to move the subproofs further or closer to each other. This length is used to define several other lengths.

```
\newlength{\ppindent}
\setlength{\ppindent}{0.4em}
```

\ppnumsep Horizontal space between leftmost numbers (1st column) and the main body of the proof. Increasing this value will create more space between numbered lines and the formulas in the main body of the proof. You might considering decreasing the value to create more compact proofs. Simply replace \ppindent with a smaller value, e.g. 0.3em.

```
\newlength{\ppnumsep}
\setlength{\ppnumsep}{\ppindent}
```

\ppsep Horizontal space

```
\newlength{\ppsep}
\setlength{\ppsep}{\ppindent}
```

\ppnumwd Line number width. Increasing this value will push the proofs to the right.

```
\newlength{\ppnumwd}
\setlength{\ppnumwd}{1em}
```

\ppjustindent Indent for justification column. By increasing the value of \ppjustindent, you are increasing the distance between the formula in the main body of the proof and the rightmost column that contains the justification. Increase for more space, decrease for more compact proofs.

```
\newlength{\ppjustindent}
\setlength{\ppjustindent}{2em}
```

\ppvline Creates a shorter line to start subproof. To do this, we set the height and depth of the line using the strut and set the width using \arrayrulewidth. Some explanation of how everything works. First, \makeatletter and \makeatother allow for the use of @ in command names. The \vrule draws the vertical line. If we simply drew the vertical line without any adjustments, the line would be too high. So, we want to adjust it to the level of the strut. The strut height is the maximum height of uppercase letters and its depth is the maximum depth of lowercase letters. We want the height of the line to be the height of the strut and the depth of the line to be the depth of the strut plus 2pt. This 2pt makes the line a little longer so it connects up with the vertical line below it. To set the height of the vrule we set its height using Cheight and set it to the height of the strutbox using \ht\strutbox. We do the same thing for the depth but we use \dimexpr to add 2pt to the depth of the strutbox. The \dimexpr command allows for the use of + and - in the command. Finally, we need to set the width or thickness of the line. The width is set to \arrayrulewidth, which is the width of lines in array environments. If you wanted a thicker line, you could replace \arrayrulewidth with another measurement, e.g. \@width 3pt. The \relax is used to end the command.

```
\makeatletter
\newcommand\ppvline{%
  \vrule\@height\ht\strutbox\@depth\dimexpr
  \dp\strutbox + 2pt\@width\arrayrulewidth\relax
}
\makeatother
```

hyp The \hyp[\langle int\rangle] command is used in the proof environment to make an assumption / hypothesis (hyp). The hypothesis does not have a right line underneath like you see in many textbooks. Example: \hyp P\rightarrow Q. The command takes an optional argument to set the depth of the subproof. Example: \hyp[3] P\rightarrow Q. This is probably the main reason you would use proofpack over the earlier fitch.sty as it results in less code. You don't need to write \hyp\hyp\hyp P\rightarrow Q. The default depth is 1.

```
\newcounter{counthyp} % counter for number of hypotheses
\setcounter{counthyp}{1} % set counter to 1
\newcommand{\hyp}[1][1]{%
   \setcounter{counthyp}{1}
   \whileboolexpr{test{\ifnumcomp{#1}{>}{\value{counthyp}}}}}
   {
        \hspace*{\ppsep}\vline\hspace*{\ppindent}\stepcounter{counthyp}% True
   }
   \hspace*{\ppsep}\ppvline\hspace*{\ppindent}% False
}
```

\hyp1 Similar to hypothesis hyp except hyp1[\(\lamble int)\)] is "hypothesis with a line" (hence hyp1). The optional argument[\(\lamble int)\)] sets the depth. The line is a right line under the assumption. Here is how it works. First, the counthyp is set to 1. The whileboolexpr checks whether the user has input a value greater than 1 as the optional argument. If it is, then it sets the counter to the optional argument and draws a vertical line in the normal way (without a right horizontal line). It then increments the counter. If the optional argument is not greater than 1, then it draws the vertical line with a right horizontal line. Once the the conditional in the while loop is false, then the right horizontal line is drawn. This is done by creating horizontal space, drawing the ppvline rather than a vline. The right line is drawn using \rule. You can adjust its placement using \hspace\*{4.0pt} and its thickness using \arrayrulewidth.

```
\newcommand{\hypl}[1][1]{%
  \setcounter{counthyp}{1}
  \whileboolexpr{test{\ifnumcomp{#1}{>}{\value{counthyp}}}}
  {
    \hspace*{\ppsep}\vline\hspace*{\ppindent}\stepcounter{counthyp}% True
  }
  \hspace*{\ppsep}\ppvline\hspace*{-\dimexpr\ppsep}\raisebox{-1.25ex}
  {\hspace*{4.0pt}\rule[.5ex]{2.35em}{\arrayrulewidth}}
  \hspace*{\dimexpr \ppindent - 2.35em}% False
}
```

\sub The \sub[\lambda int\rangle] command creates a line in the proof at a certain depth but the line is not the assumption/hypothesis that starts the subproof. Technically, you could use it to start the subproof, but sub does not make use of the adjusted vertical line like hyp and hypl. The command takes an optional argument to set the depth of the line. Example: \sub[3] is a subproof with a depth of 3. The default depth is 1.

```
\newcounter{sub}
\setcounter{sub}{0}
\newcommand{\sub}[1][1]{
   \foreach \x in {1,...,#1} {%
   \hspace*{\ppsep}\vline\hspace*{\ppindent}
   }
   \stepcounter{sub}%
}
```

markers Use these to add markers to left and right of lines to highlight important steps in the proof. This was in the original fitch.sty. My implementation of this needs some additional work.

```
\newcommand{\rightmarker}{%
\makebox[1.75\ppindent][r]{${\lhd}$}}
\newcommand{\leftmarker}{%
\hspace*{\ppsep}\makebox[0pt][r]{${\rhd}$}}
```

\bxdwff Command to draw a box around a wff. Use \bxdwff{wff} where wff is the formula you want to surround in a box. Example: \bxdwff{\$P\rightarrow Q\$}

```
\newcommand{\bxdwff}[1]{%
             \tikz[baseline=(content.base)] \node[draw, inner sep=2pt] (content) {#1};%
   \cwff Command to color a wff. \cwff or "colored well-formed formula" (wff). Usage:
         \color name defaults to blue.
           \newcommand{\cwff}[2][blue]{%
             \textcolor{#1}{#2}%
\sdeduce Environment for proof that does not break (autonumbered). Usage: \begin{sdeduce}
         ...\end{sdeduce}
           \newenvironment{sdeducenum}%
           {\ifbool{resetdeducecounter}{\setcounter{deducecounter}{0}}{}
           \begin{tabular}{!{\makebox[\ppnumwd][r]{\deducecounter}}
               \hspace{\ppnumsep-\ppsep}}>{$}1<{$}@{\hspace{\ppjustindent}}1}}
           {\end{tabular}}
           %
           \newenvironment{sdeduce}{%
             \renewcommand{\arraystretch}{1.25}%
             \begin{sdeducenum}%
           }{%
             \end{sdeducenum}%
\mdeduce Environment for proof that does not break (manually numbered).
                                                                              Usage:
         \begin{mdeduce} ... \end{mdeduce}
           \newenvironment{mdeducenum}{%
             \begin{tabular}{>{\scriptsize}r@{\hspace{\ppnumsep}}
               >{$}1<{$}@{\hspace{\ppjustindent}}1}%
           ን ና %
             \end{tabular}%
           \newenvironment{mdeduce}{\renewcommand{\arraystretch}}
           {1.25}\begin{mdeducenum}}{\end{mdeducenum}}
\ldeduce The \ldeduce [\langle l,c,r\rangle] environment is for proofs that break across the page. Takes
         an optional argument for alignment (argument is l, c, or r). The option defaults
         to I (left aligned). Usage: \begin{ldeduce}[1] ... \end{ldeduce}
           \setlength{\LTpost}{Opt} % remove space after longtable !!!!!!!!
           \newenvironment{ldeducenum}[1][1]%
           {\ifbool{resetdeducecounter}{\setcounter{deducecounter}{0}}{}
           \begin{longtable}[#1]{!{\makebox[\ppnumwd][r]{\deducecounter}
               \hspace{\ppnumsep-\ppsep}}>{$}1<{$}@{\hspace{\ppjustindent}}1}}
           {\end{longtable}
           \newenvironment{ldeduce}{%
             \renewcommand{\arraystretch}{1.25}%
             \begin{ldeducenum}%
```

```
}{%
  \end{ldeducenum}%
}
<*package>
```