

Is there some possession class that has a non-possessible valency (only access to indirect possession constructions)?

no

yes