

Is there some possession class that has an obligatorily possessed valency?

yes