

Week 8 – Long Answer Question

Question 1: Finding 'x'

Let:

- Ajay has A marbles.
- Vijay has V marbles.

From the problem statements, we can set up the following equations:

1. Ajay's Statement:

- If Vijay gives x marbles to Ajay:

$$A+x = V-x \quad A+x = V-x$$

Rearranging gives:

$$A+2x = V \quad \text{Equation 1} \quad A+2x = V \quad \text{Equation 1}$$

2. Vijay's Statement:

- If Ajay gives $2x$ marbles to Vijay:

$$V+2x = A-2x+30 \quad V+2x = A-2x+30$$

Rearranging gives:

$$V+4x = A+30 \quad \text{Equation 2} \quad V+4x = A+30 \quad \text{Equation 2}$$

Now, substitute Equation 1 into Equation 2: From Equation 1, we know $A = V - 2x$. Substitute this into Equation 2:

$$V+4x = (V-2x)+30 \quad V+4x = (V-2x)+30$$

Simplifying:

$$V+4x = V-2x+30 \quad V+4x = V-2x+30$$

$$6x = 30 \quad 6x = 30$$

$$x = 5 \quad x = 5$$

Final Answer for Question 1:

$$x = 5 \quad x = 5$$

Question 2: Drawing Shirts with At Least One Black Shirt

Total shirts in the box:

- White: 2
- Black: 3
- Red: 4

Total shirts = $2+3+4=9$. Total ways to choose any 3 shirts from 9 shirts:

Total ways = $\binom{9}{3} = \frac{9!}{3!(9-3)!} = \frac{9 \times 8 \times 7 \times 2 \times 1}{3 \times 2 \times 1} = 84$. Total ways = $\binom{39}{3} = \frac{39!}{3!(9-3)!9!} = 3 \times 2 \times 19 \times 8 \times 7 = 84$.

Ways to choose shirts without any black shirts:

- Only white and red shirts available (2 white + 4 red = 6 shirts).

Ways without black = $\binom{6}{3} = \frac{6!}{3!(6-3)!} = \frac{6 \times 5 \times 4 \times 3 \times 2 \times 1}{3 \times 2 \times 1} = 20$. Ways without black = $\binom{36}{3} = \frac{36!}{3!(6-3)!6!} = 3 \times 2 \times 16 \times 5 \times 4 = 20$.

Ways to choose at least one black shirt:

At least one black = Total ways – Ways without black
 At least one black = Total ways – Ways without black
 $= 84 - 20 = 64$. $= 84 - 20 = 64$.

Final Answer for Question 2:

64 ways to draw shirts with at least one black shirt.

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