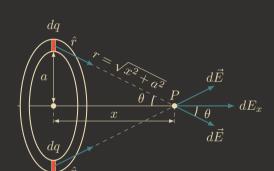
Example: Evaluating The Field - A Charged Ring A ring of radius a has a charge Q distributed evenly over the ring. Find an expression for the electric field at any

point on the axis of the ring.

Take the x-axis to coincide with the ring axis with the center of the ring at x=0. The y-components of the field contributions from pairs of charge elements on opposite sides of the ring cancel so the net field points in the +xdirection (for x>0), and only the x-components of the unit vectors are needed, namely, $\hat{r}_x=\cos(\theta)=\frac{x}{x}$



Each charge element dq contributes the same amount to the field, $dE_x = \frac{k_e dq}{r^2} \hat{r}_x = \frac{k_e x dq}{r^3}$ Writing $r = \sqrt{x^2 + a^2}$ as $(x^2 + a^2)^{1/2}$, the integral becomes

$$E = \int dE_x = \int rac{k_e x \ dq}{(x^2 + a^2)^{3/2}} = rac{k_e x}{(x^2 + a^2)^{3/2}} \int dq$$

Because the field point P is fixed, its coordinate x is a constant in the integration. The remaining integral is the sum of all the charge elements on the ring, the total charge Q.

$$E = \frac{k_e Q x}{(x^2 + a^2)^{3/2}}$$