

Problem Set 03: Solutions

BME290L - Spring 2026

2025-12-30



Warning

These solutions have been adapted from previous years, but I haven't had the chance to 100% guarantee their accuracy. If anything seems off, please don't hesitate to ask questions on Ed!

Problem 1



$$(A) \quad 2A = \frac{V_C - V_A}{0.5} + \frac{V_B - V_A}{1} = -3V_A + V_B + 2V_C = 2A$$

$$(B) \quad \frac{V_B - V_A}{1} + \frac{V_B}{0.25} = 3A = 5V_B - V_A$$

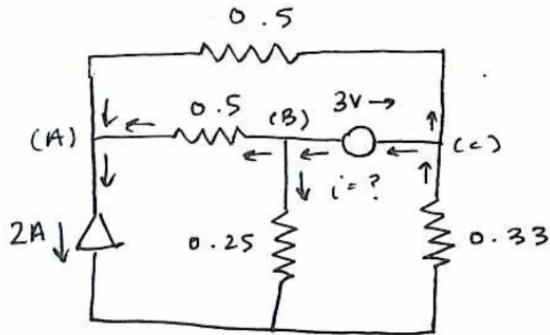
$$(C) \quad 3A + 2\left(\frac{V_C - V_A}{0.5}\right) = 3\left(-\frac{V_C}{0.33}\right)$$

$$\Rightarrow 3A = 2V_A - 5V_C$$

$$V = V_B$$

$$V_B = \frac{\begin{vmatrix} -3 & 2 & 2 \\ -1 & 3 & 0 \\ 2 & 3 & -5 \end{vmatrix}}{\begin{vmatrix} -3 & 1 & 2 \\ -1 & 5 & 0 \\ 2 & 0 & -5 \end{vmatrix}} = \frac{17}{50} = 0.34V$$

Problem 2



$$V_C = V_B + 3$$

$$(A) \quad 2A = \frac{V_C - V_A}{0.5} + \frac{V_B - V_A}{0.5} \Rightarrow 2V_C + 2V_B - 4V_A = 2A$$

$$(B) \quad \frac{V_B - V_A}{0.5} + i + \frac{V_B}{0.25} = 0 \Rightarrow 6V_B - 2V_A + i = 0$$

$$(C) \quad \frac{V_C - V_A}{0.5} - i = \frac{-V_C}{0.33} \Rightarrow 2V_A - 5V_C + i = 0$$

3 unknowns:

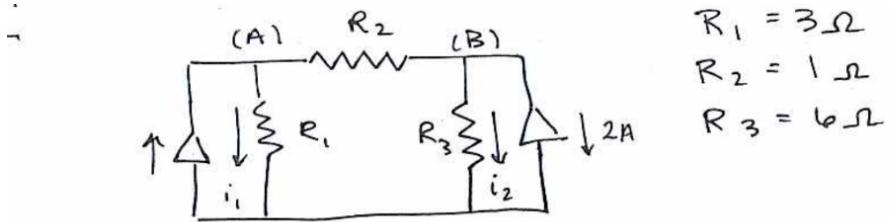
$$\textcircled{1} \quad -4V_A + 4V_B + 0i = -4$$

$$\textcircled{2} \quad -2V_A + 6V_B + i = 0$$

$$\textcircled{3} \quad 2V_A - 5V_C + i = 15$$

$$i = \frac{\begin{vmatrix} -4 & 4 & -4 \\ -2 & 6 & 0 \\ 2 & -5 & 15 \end{vmatrix}}{\begin{vmatrix} -4 & 4 & 0 \\ -2 & 6 & 1 \\ 2 & -5 & 1 \end{vmatrix}} = \frac{-232}{-28} = \boxed{8.28 \text{ A}}$$

Problem 3



$$(A) \quad 1A = \frac{V_A}{3} + \frac{V_A - V_B}{1} \Rightarrow 3 = 4V_A - 3V_B \Rightarrow V_B = \frac{4}{3}V_A - 1$$

$$(B) \quad \frac{V_A - V_B}{1} = \frac{V_B}{6} + 2 \Rightarrow 6V_A - 7V_B = 12$$

Solve for V_A : $6V_A - 7(\frac{4}{3}V_A - 1) = 12 \Rightarrow (\frac{18}{3} - \frac{28}{3})V_A = 5$

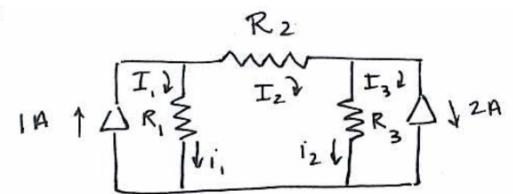
$$V_A = -\frac{3}{2}V$$

Solve for V_B : $V_B = \frac{4}{3}(-\frac{3}{2}V) - 1$
 $V_B = -3V$

$$i_1 = \frac{V_A}{R_1} = \frac{-\frac{3}{2}V}{3\Omega} = \boxed{-0.5A}$$

$$i_2 = \frac{V_B}{R_3} = \frac{-3V}{6\Omega} = \boxed{-0.5A}$$

Problem 4



$$R_1 = 3\Omega$$

$$R_2 = 1\Omega$$

$$R_3 = 6\Omega$$

$$i_1 = I_1 - I_2$$

$$i_2 = I_2 - I_3$$

$$I_1 = 1A$$

$$I_3 = 2A$$

$$0 = -I_1 R_1 + (R_1 + R_2 + R_3) I_2 - R_3 I_3$$

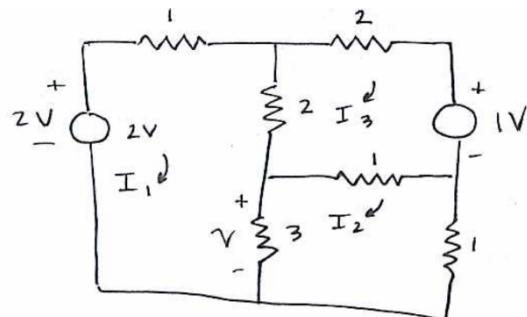
$$\hookrightarrow I_2 = \frac{(1A)(3\Omega) + (6\Omega)(2A)}{3 + 1 + 6} = \frac{15}{10}$$

$$I_2 = 1.5A$$

$$i_1 = 1A - 1.5A = \boxed{-0.5A}$$

$$i_2 = 1.5A - 2A = \boxed{-0.5A}$$

Problem 5



$$V = (I_1 - I_3) \cdot 3\Omega$$

$$\textcircled{1} \quad 2V = 6i_1 - 3i_2 - 2i_3$$

$$\textcircled{2} \quad 0 = -3i_1 + 5i_2 - i_3$$

$$\textcircled{3} \quad -1V = -2i_1 - i_3 + 5i_2$$

$$i_1 = \frac{\begin{vmatrix} 2 & -3 & -2 \\ 0 & 5 & -1 \\ -1 & -1 & 5 \end{vmatrix}}{\begin{vmatrix} 6 & -3 & -2 \\ -3 & 5 & -1 \\ -2 & -1 & 5 \end{vmatrix}} = \frac{35}{67} \text{ A}$$

$$i_2 = \frac{\begin{vmatrix} 6 & 2 & -2 \\ -3 & 0 & -1 \\ -2 & -1 & 5 \end{vmatrix}}{\begin{vmatrix} 6 & -3 & -2 \\ -3 & 5 & -1 \\ -2 & -1 & 5 \end{vmatrix}} = \frac{22}{67} \text{ A}$$

$$V = \left(\frac{35}{67} - \frac{22}{67} \right) \cdot 3\Omega$$

$$V = \frac{39}{67} V = \boxed{0.58 V}$$

Problem 6



$$\textcircled{1} \quad 5i_1 - 3i_2 - 0i_3 = 2$$

$$\textcircled{2} \quad 0i_1 - i_2 + i_3 = 2 \text{ A (current source)} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} -3\left[2V + 3i_2\right] + 4i_2 + 5[2A + i_2] = 0$$

$$\textcircled{3} \quad -3i_1 + 4i_2 + 5i_3 = 0$$

$$\boxed{\begin{aligned} I_2 &= -1.22 \text{ A} \\ I_3 &= 0.78 \text{ A} \\ I_1 &= -0.332 \text{ A} \end{aligned}}$$

Problem 7

HW #4 Solutions



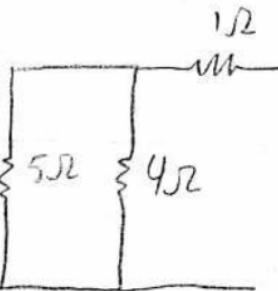
$$i_1(R_4 + R_1) + i_3(-R_1) = 0$$

$$i_2(R_5 + R_2) + i_3(-R_2) = V_{S2}$$

$$i_1(-R_1) + i_2(-R_2) + i_3(R_1R_2 + R_3) = 0$$

$$i_3 = \frac{\begin{vmatrix} R_1 + R_4 & 0 & 0 \\ 0 & R_5 + R_2 & V_{S2} \\ -R_1 & -R_2 & 0 \end{vmatrix}}{\begin{vmatrix} R_1R_4 & 0 & -R_1 \\ 0 & R_5 + R_2 & -R_2 \\ -R_1 & -R_2 & R_1R_2 + R_3 \end{vmatrix}} = \frac{\begin{vmatrix} 8 & 0 & 0 \\ 0 & 6 & 450 \\ -7 & -5 & 0 \end{vmatrix}}{\begin{vmatrix} 8 & 0 & -7 \\ 0 & 6 & -5 \\ -7 & -5 & 22 \end{vmatrix}} = [324]$$

Problem 8



$$R_T = \left(\frac{1}{5} + \frac{1}{4} \right)^{-1} + 1 = \frac{20}{9} + 1 = \frac{29}{9} = 3.22\Omega$$



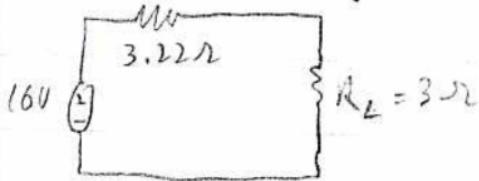
$$i_1(4) + i_2(-4) = 36V$$

$$i_1(-4) + i_2(5) = -v_{oc}$$

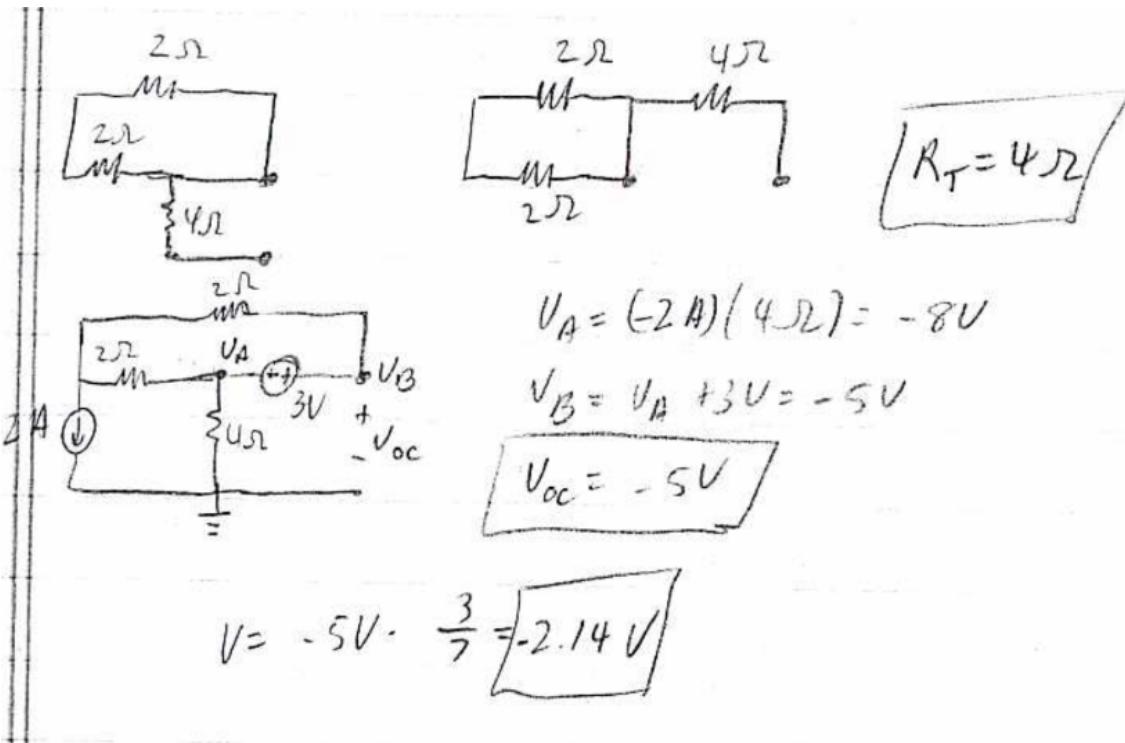
$i_2 = 0$ (open circuit)

$$i_1 = 4A$$

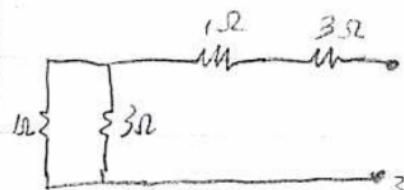
$$v_{oc} = 4i_1 = 16V$$



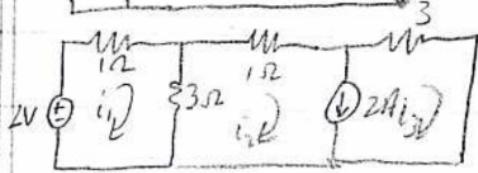
Problem 9



Problem 10



$$R_T = \frac{3}{4} + 1 + 3 = \frac{19}{4} = 4.75\Omega$$



$$i_1(1+3) + i_2(-3) = 2$$

$$i_1(-3) + i_2(1+3) + i_3(3) = 0$$

$$i_2 - i_3 = 2$$

$$i_3 = i_2 - 2$$

$$i_1(-3) + i_2(4) + (i_2 - 2)(3) = 0$$

$$i_1(-3) + 7i_2 = 6$$

$$i_2 = \frac{6 + 3i_1}{7}$$

$$i_1(4) + \frac{1}{7}(6 + 3i_1)(-3) = 2$$

$$i_1(28) + (-18 - 9i_1) = 14$$

$$19i_1 = 32$$

$$i_1 = \frac{32}{19}$$

$$i_2 = 1.5789$$

$$i_3 = -0.42$$

$$\boxed{i_n = -0.4214}$$

Problem 11



Problem 12



$$i_2 = 0.010 \text{ A}$$

$$i_1(1000) - i_2(1000) = 10$$

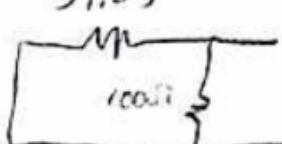
$$i_1 = 0.010 \text{ A}$$

$$V_A = 10 - 0.01 \cdot 1000 = 0 \text{ V}$$

$$V_B = V_A - 0.010 \cdot 1 = -0.01 \text{ V}$$

$$V_{oc} = V_B = -0.01 \text{ V}$$

Problem 13



$R_T = 23.81\ \Omega$

Problem 14

For Maximum Power Transfer, $R_L = R_T$

$$R_L = 8\Omega$$

$$V_L = 6V$$

$$P_L = \frac{6^2}{8} = 4.5W$$

$$i = \frac{12}{16} = 0.75A$$

$$\% \text{ eff} = \frac{P_L}{P_S} \times 100\% = \frac{4.5W}{0.75A \cdot 12V} = 50\%$$

Problem 15



P_{\max} at $0.3R_s = R_L$

$$b) P_L = \left(V_s \cdot \frac{R_L}{R_s + R_L} \right)^2 \quad R_L = V_s^2 \cdot \frac{R_L}{(R_s + R_L)^2} = V_s^2 R_L (R_s + R_L)^{-2}$$

$$\frac{dP_L}{dR_L} = V_s^2 (R_s + R_L)^{-2} + V_s^2 R_L (-2)(R_s + R_L)^{-3} = 0$$

$$V_s^2 (R_s + R_L) + V_s^2 R_L (-2) = 0$$

$$R_s + R_L - 2R_L = 0$$

$$\boxed{R_L = R_s}$$