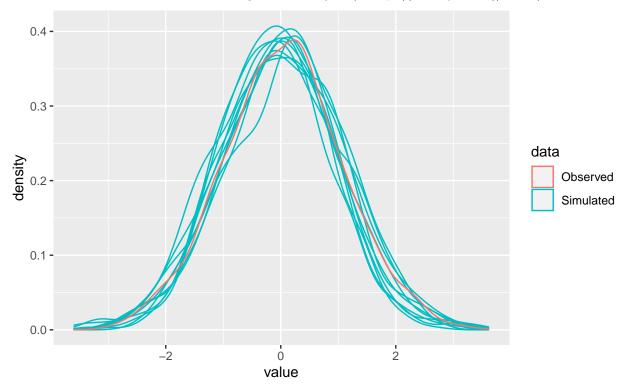
# PPC and Production-Level Tables

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#### Posterior Predictive Checks

PPC visualize "typical" data distributions given your parameter estimates, then compare them to your observed distribution. See Gelman, Meng, and Stern (1996): https://www.jstor.org/stable/24306036.



### Why do PPC?

- Show if your modeling assumption is good (not just if MCMC has converged)
- Check tail behavior

#### How to do them?

- 1) Take some posterior draws of your parameters (NOT the posterior means)
- 2) Sample from p(Y|X,parameters), one draw per observation
- 3) Plot densities or histograms of the simulated AND observed values

#### Example

```
n <- 500
x1 \leftarrow rnorm(n)
x2 \leftarrow rbinom(n,10,prob = .1)
y <-3 + 2*x1 + -1*x2 + rnorm(n)*sqrt(1/rgamma(n,1.5/2,1.5/2)) #t distribution w/ df=3
jags_model <- function(){</pre>
 for(i in 1:n){
    mu[i] = inprod(beta, X[i,])
    resid[i] = Y[i]-mu[i]
    Y[i] ~ dnorm(mu[i],tau)
  tau \sim dgamma(1/10, 1/10)
  sigma = pow(tau, -1/2)
  for(i in 1:3){
    beta[i] ~ dnorm(0,.01)
  }
}
X \leftarrow cbind(1,x1,x2)
jags_output <- jags(data = list(Y=y,X=X,n=n),model.file = jags_model,</pre>
                      parameters.to.save = c("mu", "sigma", "beta", "resid"))
```

Lets see if we got reasonable point estimates for the parameters.

Variable	Mean	SD	2.5% Quantile	97.5% Quantile
Intercept	2.463	0.501	1.480	3.465
sigma	7.658	0.241	7.201	8.144
x1	1.825	0.331	1.182	2.480
x2	-1.249	0.367	-1.995	-0.556

```
#set # of ppc draws and randomly pick parameter draws
nppc_sims <- 10
ppc_param_draws <- sample(1:nrow(jags_output$BUGSoutput$sims.matrix),replace = F,size = nppc_sims)
#extract simulated values
mu_sims <- jags_output$BUGSoutput$sims.matrix[,c(str_c("mu[",1:n,"]"))]
sigma_sims <- jags_output$BUGSoutput$sims.matrix[,c(str_c("sigma"))]</pre>
```

```
#compute posterior predictive draws
ppc_sims <- sapply(ppc_param_draws,function(r) rnorm(n=length(y),mean = mu_sims[r,],sd = sigma_sims[r])</pre>
ppc_plot_data <- cbind(ppc_sims,y) %>%
  as_tibble() %>%
  reshape2::melt() %>%
  mutate(source = ifelse(variable == "y", "Observed", "Simulated"))
ppc_density <- ppc_plot_data %>%
  ggplot(aes(x=value,group = variable,color = source)) +
  geom_density()
ppc_boxplot <- cbind(ppc_sims,y) %>%
  as_tibble() %>%
  reshape2::melt() %>%
  mutate(source = ifelse(variable == "y", "Observed", "Simulated")) %>%
  ggplot(aes(x=value,group = variable,color = source)) +
  geom_boxplot()
gridExtra::grid.arrange(ppc_density,ppc_boxplot)
  0.10 -
                                                                               source
density
                                                                                    Observed
                                                                                    Simulated
  0.00 -
                      -50
                                                                50
                                            0
                                       value
 0.4 -
 0.2 -
                                                                               source
 0.0 -
                                                                                    Observed
                                                                                    Simulated
-0.2 -
-0.4 -
                                           0
                    -50
                                                               50
                                      value
```

We want to see that the observed plots are indistinguishable from the simulated plots. Obviously, thats not quite the case here. So lets give the data likelihood slightly fatter tails by making it a t-distribution and put a prior on the degrees of freedom.

Now lets check the estimated model parameters.

Variable	Mean	SD	2.5% Quantile	97.5% Quantile
alpha	1.271	0.096	1.117	1.481
Intercept	2.933	0.080	2.779	3.092
sigma	0.923	0.060	0.809	1.046
x1	2.037	0.050	1.942	2.136
x2	-0.929	0.058	-1.045	-0.813

Now recreat the PPC checks.

```
#set # of ppc draws and randomly pick parameter draws
nppc_sims <- 10
ppc_param_draws <- sample(1:nrow(jags_output_t$BUGSoutput$sims.matrix),replace = F,size = nppc_sims)

#extract simulated values
mu_sims <- jags_output_t$BUGSoutput$sims.matrix[,c(str_c("mu[",1:n,"]"))]
sigma_sims <- jags_output_t$BUGSoutput$sims.matrix[,c(str_c("sigma"))]
alpha_sims <- jags_output_t$BUGSoutput$sims.matrix[,c(str_c("alpha"))]</pre>
```

```
#compute posterior predictive draws
ppc_sims <- sapply(ppc_param_draws,function(r) rnorm(n=length(y),</pre>
                                  mean = mu_sims[r,],
                                   sd = sigma_sims[r])/
                      sqrt(rgamma(length(y),mean(alpha_sims)/2,mean(alpha_sims)/2)))
ppc_plot_data <- cbind(ppc_sims,y) %>%
  as_tibble() %>%
  reshape2::melt() %>%
  mutate(source = ifelse(variable == "y", "Observed", "Simulated"))
ppc_density <- ppc_plot_data %>%
  ggplot(aes(x=value,group = variable,color = source)) +
  geom_density()
ppc_boxplot <- cbind(ppc_sims,y) %>%
  as_tibble() %>%
  reshape2::melt() %>%
  mutate(source = ifelse(variable == "y","Observed","Simulated")) %>%
  ggplot(aes(x=value,group = variable,color = source)) +
  geom_boxplot()
gridExtra::grid.arrange(ppc_density,ppc_boxplot)
  0.3 -
density
                                                                              source
                                                                                   Observed
                                                                                   Simulated
  0.1 -
  0.0 -
                                   1000
                       0
                                                 2000
                                                               3000
       -1000
                                      value
 0.4 -
 0.2 -
                                                                              source
                                                                                   Observed
 0.0
                                                                                   Simulated
-0.2 -
-0.4
      -1000
                                   1000
                                                 2000
                                                               3000
                                     value
```

Now recreat the PPC checks within the range of  $\pm 100.$ 

```
#set # of ppc draws and randomly pick parameter draws
nppc_sims <- 10</pre>
```

```
ppc_param_draws <- sample(1:nrow(jags_output_t$BUGSoutput$sims.matrix),replace = F,size = nppc_sims)</pre>
#extract simulated values
mu_sims <- jags_output_t$BUGSoutput$sims.matrix[,c(str_c("mu[",1:n,"]"))]</pre>
sigma_sims <- jags_output_t$BUGSoutput$sims.matrix[,c(str_c("sigma"))]</pre>
alpha_sims <- jags_output_t$BUGSoutput$sims.matrix[,c(str_c("alpha"))]</pre>
#compute posterior predictive draws
ppc_sims <- sapply(ppc_param_draws,function(r) rnorm(n=length(y),</pre>
                                  mean = mu_sims[r,],
                                  sd = sigma_sims[r])/
                      sqrt(rgamma(length(y),mean(alpha_sims)/2,mean(alpha_sims)/2)))
ppc plot data <- cbind(ppc sims,y) %>%
  as_tibble() %>%
  reshape2::melt() %>%
  mutate(source = ifelse(variable == "y", "Observed", "Simulated"))
ppc_density <- ppc_plot_data %>%
  filter(abs(value) <= 100) %>%
  ggplot(aes(x=value,group = variable,color = source)) +
  geom_density()
ppc_boxplot <- cbind(ppc_sims,y) %>%
  as_tibble() %>%
  reshape2::melt() %>%
  filter(abs(value) <= 100) %>%
  mutate(source = ifelse(variable == "y", "Observed", "Simulated")) %>%
  ggplot(aes(x=value,group = variable,color = source)) +
  geom_boxplot()
gridExtra::grid.arrange(ppc_density,ppc_boxplot)
```

