

Polling Errors

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Assuming unbiased polls

Most of you did something like this. For each poll k of state s at time t , Y_{stk} gives the two-party support share of a candidate.

$$\begin{aligned} E[Y_{stk}] &= \theta_{s,t} \\ \theta_{s,t} &\sim N(\theta_{s,t-1}, \sigma_\theta) \end{aligned}$$

Winner determined by $\theta_{s,1} > 50\%$.

Checking bias

You could do this:

$$\begin{aligned}E[Y_{stk}] &= \theta_{s,t} + \alpha_s \\ \theta_{s,t} &\sim N(\theta_{s,t-1}, \sigma_\theta) \\ \alpha_s &\overset{iid}{\sim} N(\mu_\alpha, \sigma_\alpha)\end{aligned}$$

Winner determined by $\theta_{s,1} > 50\%$.

How to set hyper parameters?

Could set $\mu_\alpha = \text{mean}(b_1, \dots, b_S)$ and $\sigma_\alpha = \text{sd}(b_1, \dots, b_S)$ where b_s is a point estimate of polling error in 2016 in state s (lots of analysts have made these). Could look at longer historical data by state.

Because the polling data cannot separate θ and α , sensitivity checks, particularly in μ_α , are very important. Could make a plot of $P(\text{Biden Win})$ vs μ_α .

How to estimate?

Note lack of information in data is a blessing and a curse. Curse is obvious, you can't learn them easily. But the blessing is you don't necessarily need to re-estimate your model.¹

If you have your simulated draws of $\theta_{s,1}$, don't need to re-estimate model. For draw of $\theta_{s,1}$, subtract $\text{rnorm}(1, \mu_\alpha, \sigma_\alpha)$ and recompute who wins.

¹The priors do technically give you some identifiability, and a fully Bayesian approach would be to re-estimate the model many times for different priors on α_s .