

$$|\vec{a}|=2, |\vec{b}|=4, \angle(\vec{a}, \vec{b}) = \frac{2\pi}{3}; \vec{h} = 3\vec{a} - \vec{b}, \vec{m} = \vec{b} - \vec{a}$$

$$\vec{a} \cdot \vec{b} = |\vec{a}| \cdot |\vec{b}| \cdot \cos(\angle(\vec{a}, \vec{b})) = 2 \cdot 4 \cdot \cos \frac{2\pi}{3} = 2 \cdot 4 \cdot \left(-\frac{1}{2}\right) = -4$$

$$\begin{aligned} \vec{h} \cdot \vec{m} &= (3\vec{a} - \vec{b}) \cdot (\vec{b} - \vec{a}) = 3\vec{a} \cdot \vec{b} - 3\vec{a} \cdot \vec{a} - \vec{b} \cdot \vec{b} + \vec{a} \cdot \vec{b} = \\ &= 4\vec{a} \cdot \vec{b} - 3|\vec{a}|^2 - |\vec{b}|^2; \end{aligned}$$

$$\vec{a} \cdot \vec{b} = -4; \quad \vec{h} \cdot \vec{m} = 4 \cdot (-4) - 3 \cdot 4 - 16 =$$

$$|\vec{a}|^2 = 2^2 = 4 \quad = -16 - 12 - 16 = -36$$

$$|\vec{b}|^2 = 4^2 = 16$$

$$|\vec{h}| = \sqrt{(3\vec{a} - \vec{b}) \cdot (3\vec{a} - \vec{b})} = \sqrt{9\vec{a} \cdot \vec{a} - 6\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{b}} =$$

$$= \sqrt{36 + 24 + 16} = \sqrt{76}$$

$$|\vec{m}| = \sqrt{(\vec{b} - \vec{a}) \cdot (\vec{b} - \vec{a})} = \sqrt{\vec{b} \cdot \vec{b} - 2\vec{a} \cdot \vec{b} + \vec{a} \cdot \vec{a}} =$$

$$= \sqrt{16 + 8 + 4} = \sqrt{28}$$

$$\cos \theta = \frac{-36}{\sqrt{76} \cdot \sqrt{28}} = \frac{-36}{\sqrt{2128}};$$

$$\theta = \arccos \left( \frac{-36}{\sqrt{2128}} \right)$$

~~$$\text{hp } \vec{c} = \frac{\vec{c} \cdot \vec{d}}{|\vec{d}|} =$$~~

 ~~$\vec{c}$~~ 
 $\sim 2$ 

$$\vec{a} = 3\vec{i} - \vec{j} + \vec{k}$$

$$\vec{b} = 2\vec{i} + 3\vec{j} - \vec{k}$$

$$\vec{c} = \vec{a} + 2\vec{b}$$

$$\vec{d} = \vec{b} - \vec{a};$$

$$\vec{c} = 3\vec{i} - \vec{j} + \vec{k} + 4\vec{i} + 6\vec{j} - 2\vec{k} =$$

$$= 7\vec{i} + 5\vec{j} - \vec{k}$$

$$\vec{d} = 2\vec{i} + 3\vec{j} - \vec{k} - 3\vec{i} + \vec{j} - \vec{k} = -\vec{i} - \vec{c} + 4\vec{j} - 2\vec{k}$$

$$\text{hp } \vec{c} = \frac{\vec{c} \cdot \vec{d}}{|\vec{d}|} = \frac{-7\vec{i} + 20\vec{j} + 2\vec{k}}{|\vec{d}|}$$

$$\vec{c} \cdot \vec{d} = 7 \cdot (-1) + 5 \cdot 4 + (-1) \cdot (-2) = -7 + 20 + 2 = 15$$

$$|\vec{d}| = \sqrt{(-1)^2 + 4^2 + (-2)^2} = \sqrt{1 + 16 + 4} = \sqrt{21}$$

$$\text{hp } \vec{c} = \frac{\vec{c} \cdot \vec{d}}{|\vec{d}|} = \frac{15}{\sqrt{21}}$$

$$\vec{a} \cdot \vec{b} \cdot \vec{d} = \begin{vmatrix} 3 & -1 & 1 \\ 2 & 3 & -1 \\ -1 & 4 & -2 \end{vmatrix} = 0.$$



$$\vec{a} = 3\vec{i} - 6\vec{j} - \vec{k}$$

$$\vec{b} = \vec{i} + 4\vec{j} - 5\vec{k}$$

$$\vec{c} = 3\vec{i} - 4\vec{j} + 12\vec{k}$$

~3

$$\vec{a} + \vec{b} = (3+1)\vec{i} + (-6+4)\vec{j} + (-1-5)\vec{k} =$$

$$= 4\vec{i} - 2\vec{j} - 6\vec{k}$$

$$\text{hp}_{\vec{c}} \vec{a} + \vec{b} = \frac{(\vec{a} + \vec{b}) \cdot \vec{c}}{|\vec{c}|} =$$

$$(\vec{a} + \vec{b}) \cdot \vec{c} = 4 \cdot 3 + (-2) \cdot (-4) + (-6) \cdot 12 = 12 + 8 - 72 = -52$$

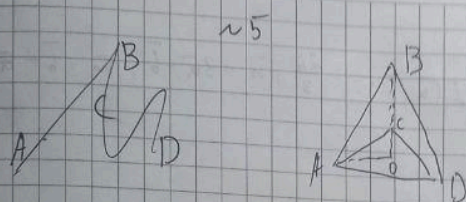
$$|\vec{c}| = \sqrt{|\vec{c}_x|^2 + |\vec{c}_y|^2 + |\vec{c}_z|^2} = \sqrt{9 + 16 + 144} = \sqrt{169} = 13 =$$

$$= \frac{-52}{13} = -4$$

$$\vec{a} = (2; -1; 3), \quad \vec{b} = (0; 2; -2), \quad \vec{c} = (-4; 2; -6)$$

$$\text{skew} \begin{vmatrix} 2 & -1 & 3 \\ 0 & 2 & -2 \\ -4 & 2 & -6 \end{vmatrix} = 0. \quad \text{Векторы линейно зависимы}$$





$$V = \frac{1}{6} |\vec{AB} \cdot (\vec{AC} \times \vec{AD})|$$

$$S_{ACD} = \frac{1}{2} |\vec{AC} \times \vec{AD}|$$

$$h = \frac{3V}{S_{ACD}} = \frac{\frac{1}{2} |\vec{AB} \cdot (\vec{AC} \times \vec{AD})|}{\frac{1}{2} |\vec{AC} \times \vec{AD}|} = \frac{1}{2} \frac{|\vec{AB} \cdot (\vec{AC} \times \vec{AD})|}{|\vec{AC} \times \vec{AD}|}$$

$$\vec{AB} = \vec{B} - \vec{A} = (-1; 0; -2), \quad \vec{AC} = \vec{C} - \vec{A} = (-3; 4; 0), \quad \vec{AD} = \vec{D} - \vec{A} = (0; -3; -2)$$

$$\vec{AB} = (-1-2; 0-0; -2-3) = (-3; 0; -5)$$

$$\vec{AC} = (-3-2; 4-0; 0-3) = (-5; 4; -3)$$

$$\vec{AD} = (0-2; -3-0; -2-3) = (-2; -3; -2)$$

$$|\vec{AB} \cdot (\vec{AC} \times \vec{AD})| = \begin{vmatrix} -3 & 0 & -5 \\ -5 & 4 & -3 \\ -2 & -3 & -2 \end{vmatrix} = -64$$

$$|\vec{AC} \times \vec{AD}| =$$

$$= |(-17; -4; 23)| =$$

$$= \sqrt{17^2 + 16 + 23^2} = \sqrt{289 + 16 + 529} = \sqrt{835}$$

$$h = \frac{1}{2} \cdot \frac{-64}{\sqrt{835}} = -\frac{32}{\sqrt{835}}$$