Assignment A1b: Functions and Computation

Put your Name and Case ID here

Use 464-A1b-yourcaseid.ipynb for your notebook name.

This assignment doesn't require it, but if you use your own data files, put these in a folder named 464-A1b-yourcaseidfiles, which should also contain a copy of your notebook. Make sure this folder contains all the files needed to reproduce your results.

Overview

In this assignment you write more complex functions, learn to use vector operations, and make more complex plots. You will learn basic functions, computations, and programming style that will be useful in later parts of the course.

Learning objectives

- convert between values in time, samples, and radians
- plot functions with time axes
- plot common functions and vary their key parameters
- simplify code by using default values
- overlay and style plots to show relative position
- use plot styles for discrete and continuous functions make matrix of plots to illustrate a functions parameter space
- write code in a functional programming style
- write code in terms of vector operations
- normalize a function over its range
- write simple functions to compute local maxima and threshold crossings

Exercises

1. Common functions

Write code to implement and plot the functions described below. Use the same names as the titles below and use the following guidelines

use vector or broadcasting operations when possible

write functions that are easily reusable

- do not worry about the efficiency of the implementation
- use keyword arguments with default values for parameters
- use a coding style that emphasizes clarity of the ideas
- group lines of code by ideas
- comment only what might not be clear to another student reading your code choose meaningful or mnemonic variable names that won't be cryptic to another reader
- Plots and figures:
- plots should have descriptive titles and axis labels. font sizes and plot details should be legible

- labels and legends shouldn't hide plot content
- The most basic function in signal processing and in modeling many perceptual phenomena is the sinusoid

1a. sinewave

 $\sin(2\pi f t + d)$ where f is the frequency in Hertz, t is time in seconds, and d is the delay in seconds.

return an array of function values at those times. These conventions also apply to the functions below.

the function. A vector version of the function (if you are not using broadcasting) should accept an array of time values and

Show with unit analysis the formulas to convert 1) seconds to samples using f_s as the sampling frequency and i as the sample index (zero-based), and 2) the delay in seconds to phase in radians.

Your function should accept a time value and parameters. Define arrays of time values for a given sampling frequency outside

Write a helper function timetoindex that returns a sample index given a time value in seconds and a sampling frequency. This index should follow the indexing convention of your programming language, i.e. zero-based or one-based.

A Gabor function is a sinusoid modulated by a Gaussian. It is used to describe a filter that is localized in both time and

1b. gabor

frequency or, for a spatial signal like an image, position and spatial frequency. We will see later that 2D Gabor functions arise is the context of efficient visual representations. Remarkably, the filtering and representation properties of the early visual system are described quite accurately with Gabor functions. Gabor-like features commonly emerge in the first layers of neural networks when trained on general visual tasks. Mathematically, Gabor functions are usually centered at zero and are defined with a sin or cos function to give even and odd

versions of the functions, respectively. More generally, it can be defined as $g(t) = a \exp\left(\frac{-t^2}{2\sigma^2}\right) \cos(2\pi f t + \phi)$

There are several parameters, but they are usually have values set to give characteristic properties. The amplitude
$$a$$
 is a normalizing constant you should define so $g(t)$ has unit norm

 $||g(t)|| = \left(\sum_{t} g(t)^{2}\right)^{1/2} = 1$

 σ is the Gaussian width (or standard deviation) which is usually a small (integer) number of sinusoid periods. The frequency fis in Hertz for temporal signals. For spatial signals, it is often convenient to define the sinusoid in terms of the period in pixels or samples, e.g. 1 period per 8 pixels. The phase is in radians and is usually restricted to 0 or $\pi/2$ to give **even** and **odd** versions of the Gabor function (gabore and gaboro, which you should also define).

but they should accept the normalizing constant a. Note that the scalar function *could* be computed (given the sampling frequency), but this would be very inefficient. Instead, define functions gabor_norm, gabore_norm, and gaboro_norm, which accept the same arguments as the scalar

Scalar function definitions (for a scalar value of t) do not need to be normalized (since it depends on the sampling frequency),

constants should be computed using the non-zero extents of the functions. Vector functions should be normalized over the extent of the argument vector t.

functions, but without a time argument and have an additional argument for the sampling frequency. The normalization

The gammatone function is used to model cochlear filtering and is defined as $g(t) = at^{n-1}e^{-2\pi bt}\cos(2\pi ft + \phi)$

 $ERB(f) = 24.7 * (4.37 \frac{f}{1000} + 1)$

The amplitude a should be set so that the function has unit norm. ERB stands for equivalent rectangular bandwidth. This

where f is the frequency in Hertz and ϕ is the phase in radians. The exponent n is the shape parameter (n=4 is a typical

b = 1.019 * ERB(f)

where

future lectures.

2. Simple computation

1c. gammatone

specific form is used to model the filtering properties of the cochlea at different frequencies. We will cover this in more detail in

2a. localmaxima

Write a function to compute the indices of the local maxima of a 1D signal ignoring edges and plateaus (i.e. ranges where the

f[i-1] < f[i] > f[i+1]. Note we have used square brackets to emphasize that f[i] is an array with discrete index i vs

function has constant value). The function should return the indices of all maxima, which we will define simply as

f(t) which is a continuous function of t.

value). The inverse scale parameter b is defined as

Write a function to compute the indices of the locations where a function crosses (or equals) a specified threshold. The function should also take an argument that specifies three possibilities of the direction of the crossing: 1) negpos: from below the threshold to equal to or greater than the threshold; 2) **posneg**: from equal to or greater than threshold to below the threshold; 3) **both**: for crossing in either direction. It should return the indices of the threshold crossings.

If a plotting function isn't designed to handle large numbers of samples, it render very slowly and even hang your system due to the large memory footprint of the plot object. There are many ways of reducing or downsampling the data to the resolution of

Self-check

can expect

2c. envelope

2b. crossings

ylower, yupper, blockindices = envelope(y; nblocks) which, given a waveform or vector y, returns the lower and upper bounds for nblocks blocks in y. blockindices returns the starting indices of each block. A reasonable default for nblocks is 1/10th the length of y.

You should test your code and make plots to verify that your implementations are correct. The self-check quiz on canvas will allow you to check your draft submission before you submit your final version. Here are examples of the types of questions you

 Compute function values for specified parameters. • What indices correspond to specified time values for a given sampling frequency? Plot the functions for specified parameters (applies to all functions).

• Make an overlay plot of a sine wave and a delayed sine wave. To clearly illustrate the delay, you will be asked to format the

 Plot even and odd Gabor functions given parameters. Calculate the local maxima of a specific array of values. Plot a sine wave with markers at the maxima.

plot and specify the x-axis ticks.

 Plot Gabor functions as a discrete set of samples in terms of samples per period. Make a grid plot of functions to illustrate the behavior over a range of parameters.

the plot. Here, we will just compute a simple envelope. Write a function

- Submission Instructions (up to a -5 pt penalty if not followed) 1. Restart your kernel and re-run your notebook.

Use the envelope function to plot the audio file speech.wav (in assignment files under the audio directory).

Verify that each cell produces the correct output. The cells should be numbered sequentially starting from [1]. This will help ensure that your notebook always produces the output you intended and will help avoid errors arising from non-sequential cell execution and inconsistencies in variable definitions.

1. Export your notebook to pdf.

This provides a static rendering of your notebook and improves the grading workflow. Currently, a pdf file is the only way to view your notebook submission within canvas. Refer to "Notebook export tips" on Canvas/Files for how to get good pdf output.

- 1. Submit the following files to canvas:
- 464-Alb-yourcaseid.pdf 464-A1b-yourcaseid.ipynb

If your notebook relies on your own data files, in addition to the files above, also submit a zip file named 491-A1byourcaseid-files.zip of a folder containing the notebook and datafiles. Your zip file should unzip to a folder named 464-A1b-yourcaseid-files. Do not use other compression formats. Do not submit large (> 10 MB) data files. Instead, provide a link where they can be downloaded.