# Matching Deformable 3D Shapes

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# Outline

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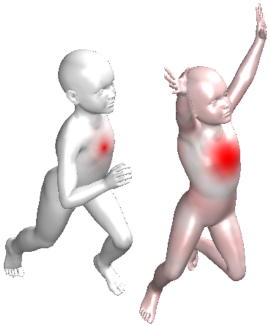
# Introduction

- Point-wise Map Recovery and Refinement from Functional Correspondence by Rodola et al.



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# 3D Shape Matching

- Coherent Point Drift (CPD)...
  - consectetur
  - adipisicing
- Solve for W...

- Lorem ipsum dolor sit amet,
  - consectetur
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- elit

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# Coherent Point Drift (CPD) - Algorithm

**Non-rigid point set registration algorithm:**

- Initialization: $\mathbf{W} = 0, \sigma^2 = \frac{1}{DNM} \sum_{m,n=1}^{M,N} \|\mathbf{x}_n - \mathbf{y}_m\|^2$
- Initialize $w (0 \leq w \leq 1)$, $\beta > 0$, $\lambda > 0$,
- Construct $\mathbf{G}$: $g_{ij} = \exp^{-\frac{1}{2\beta^2}\|\mathbf{y}_i - \mathbf{y}_j\|^2}$,
- EM optimization, repeat until convergence:
  - E-step: Compute $\mathbf{P}$,

$$p_{mn} = \frac{\exp^{-\frac{1}{2\sigma^2}\|\mathbf{x}_n - (\mathbf{y}_m + \mathbf{G}(m,\cdot)\mathbf{W})\|^2}}{\sum_{k=1}^{M} \exp^{-\frac{1}{2\sigma^2}\|\mathbf{x}_n - (\mathbf{y}_k + \mathbf{G}(k,\cdot)\mathbf{W})\|^2} + \frac{w}{1-w}\frac{(2\pi\sigma^2)^{D/2} M}{N}}$$

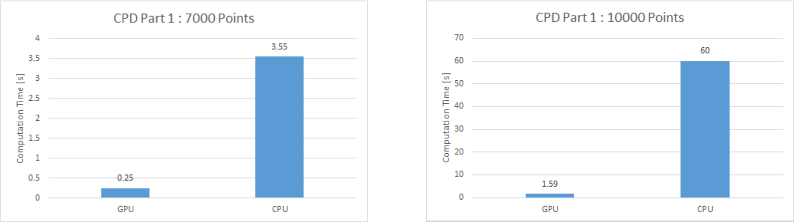
  - M-step:
    - Solve $(\mathbf{G} + \lambda\sigma^2 d(\mathbf{P1})^{-1})\mathbf{W} = d(\mathbf{P1})^{-1}\mathbf{PX} - \mathbf{Y}$
    - $N_{\mathbf{P}} = \mathbf{1}^T\mathbf{P1}$, $\mathbf{T} = \mathbf{Y} + \mathbf{GW}$,
    - $\sigma^2 = \frac{1}{N_{\mathbf{P}}D}(\mathrm{tr}(\mathbf{X}^T \mathrm{d}(\mathbf{P}^T\mathbf{1})\mathbf{X}) - 2\,\mathrm{tr}((\mathbf{PX})^T\mathbf{T}) + \mathrm{tr}(\mathbf{T}^T \mathrm{d}(\mathbf{P1})\mathbf{T}))$,
- The aligned point set is $\mathbf{T} = \mathcal{T}(\mathbf{Y}, \mathbf{W}) = \mathbf{Y} + \mathbf{GW}$,
- The probability of correspondence is given by $\mathbf{P}$.

**Figure : CPD Algorithm: *P* is $M \times N$**

# Coherent Point Drift (CPD) - Implementation

- Algorithm
  - CPU version uses several loops
  - Matrix $P$ ($M \times N$) is never actually calculated
- GPU Implementation
  - Utilize optimized libraries (CuBLAS)
  - Vectorize operations
  - Use matrix slicing to circumvent memory limitations

# Coherent Point Drift (CPD) -Evaluation




**(a)** **(b)**

**Figure : Evaluation for 7000 and 1000 points**

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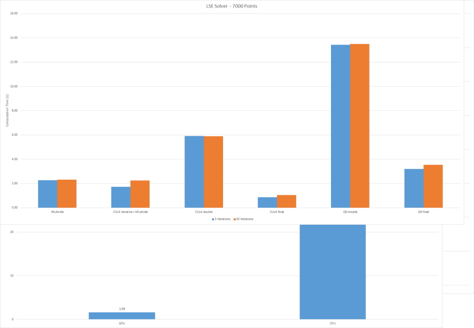
# Linear System Solver

- Large, Dense Linear System of Equations (LSE)
- Memory Limitations
- Libraries and approaches (CuSolver, CULA, MAGMA, CuBLAS, Matlab)

# Linear System Solver - Evaluation



# Total Speedup

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# Demo

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# Conclusion and Future Work

- Consider single precision for whole computation
  - Current implementation relies on double precision in CPD
- Utilize the new GPU Cluster at the Vision Chair
- Develop approach that does not rely on huge, dense LSE

# Bibliography I