

## Daily Coding Problem #239

### Problem

This problem was asked by Uber.

One way to unlock an Android phone is through a pattern of swipes across a 1-9 keypad.

For a pattern to be valid, it must satisfy the following:

- All of its keys must be distinct.
- It must not connect two keys by jumping over a third key, unless that key has already been used.

For example, 4 - 2 - 1 - 7 is a valid pattern, whereas 2 - 1 - 7 is not.

Find the total number of valid unlock patterns of length  $N$ , where  $1 \leq N \leq 9$ .

### Solution

Let's first try to solve the problem without any restrictions on jumping over keys. If there are  $N$  starting numbers to choose from, we will have  $N - 1$  options for the second number,  $N - 2$  options for the third, and so on. Mathematically we can recognize the product of these to be  $N!$ . But we can also use depth-first search to explore these patterns.

Each time we visit a number, we mark it as visited, traverse all paths starting with that number, and then remove it from the visited set. Along the way we keep a running count of the number of paths seen thus far, which we return as our result.

```
def num_paths(current, visited, n):
    if n - 1 == 0:
        return 1

    paths = 0
    for next_number in range(1, 10):
        if next_number not in visited:
            visited.add(next_number)
            paths += num_paths(next_number, jumps, visited, n - 1)
            visited.remove(next_number)

    return paths
```

To modify this to account for jumps, we can use a dictionary mapping pairs of keys to the key they skip over. Before visiting a number, we check to see that either the current and next number do not exist as a pair in this dictionary, or that their value has already been visited.

Notice also that because of symmetry, the number of patterns starting from 1 is the same as the number of patterns starting from 3, 7, and 9. For example, the path 1 - 6 - 3 - 8 can be rotated 180 degrees to get 9 - 4 - 7 - 2. Similarly, paths starting with 2, 4, 6, and 8 are all rotationally symmetric. So our answer can be expressed as:

$$4 * \text{num\_paths}(1) + 4 * \text{num\_paths}(2) + 1 * \text{num\_paths}(5)$$

Putting it all together, the code would look something like this:

```
def num_paths(current, jumps, visited, n):
    if n - 1 == 0:
        return 1

    paths = 0
    for next_number in range(1, 10):
        if next_number not in visited:
            if (current, next_number) not in jumps or jumps[(current,
next_number)] in visited:

                visited.add(next_number)
                paths += num_paths(next_number, jumps, visited, n - 1)
                visited.remove(next_number)
```

```
return paths
```

```
def unlock_combinations(n):  
    jumps = {(1, 3): 2, (1, 7): 4, (1, 9): 5,  
             (2, 8): 5,  
             (3, 1): 2, (3, 7): 5, (3, 9): 6,  
             (4, 6): 5, (6, 4): 5,  
             (7, 1): 4, (7, 3): 5, (7, 9): 8,  
             (8, 2): 5,  
             (9, 1): 5, (9, 3): 6, (9, 7): 8}  
  
    return 4 * num_paths(1, jumps, set([1]), n) + \  
           4 * num_paths(2, jumps, set([2]), n) + \  
           1 * num_paths(5, jumps, set([5]), n)
```

Even though the jump restrictions have limited the options at each next step, the time complexity for each of the three starting points is still  $O(N!)$ .

---

© Daily Coding Problem 2019

[Privacy Policy](#)

[Terms of Service](#)

[Press](#)