Mathematics 3A03 Real Analysis I Fall 2019 ASSIGNMENT 4

This assignment is due on Tuesday 5 November 2019 at 2:25pm. PLEASE NOTE that you must submit online via crowdmark. You will receive an e-mail from crowdmark with the required link. Do NOT submit a hardcopy of this assignment.

<u>Note</u>: Not all questions will be marked. The questions to be marked will be determined after the assignment is due.

THIS IS A DRAFT VERSION OF THE ASSIGNMENT. THE FINAL VERSION OF THE ASSIGNMENT WILL BE POSTED AS SOON AS IT IS READY. — DE

1. In each part of this problem, the function f is defined by the formula

$$f(x) = \sqrt{|x|} \,. \tag{\heartsuit}$$

Pay close attention to the domain of the function in each part and consider the statement

$$\lim_{x \to 2} f(x) = \sqrt{2} \,. \tag{\spadesuit}$$

Does statement (\spadesuit) make sense for the given domain? If not, why not? If statement (\spadesuit) does make sense, then either prove or disprove it directly from the ε - δ definition of a limit.

- (a) $f: \mathbb{R} \to \mathbb{R}$.
- (b) $f: \mathbb{Q} \to \mathbb{R}$.
- (c) $f: \mathbb{Z} \to \mathbb{R}$.