## Mathematics 3A03 Real Analysis I

http://www.math.mcmaster.ca/earn/3A03

## 2019 ASSIGNMENT 4

This assignment is **due** on **Friday 8 March 2019 at 1:25pm**. **PLEASE NOTE** that you must **submit online** via crowdmark. You will receive an e-mail from crowdmark with the required link. Do **NOT** submit a hardcopy of this assignment.

<u>Note</u>: Not all questions will be marked. The questions to be marked will be determined after the assignment is due.

- 1. Give an example of a sequence of closed sets  $F_1$ ,  $F_2$ ,  $F_3$ , ..., whose union is neither open nor closed. Can this be achieved with a sequence that contains only finitely many distinct sets?
- 2. Suppose that  $E \subseteq \mathbb{R}$ ,  $K \subseteq \mathbb{R}$ , E is closed and K is compact. Show that  $E \cap K$  is compact, by proving <u>directly</u> that  $E \cap K$  satisfies each of the following equivalent properties:
  - (a) closed and bounded;
  - (b) Bolzano-Weierstrass property;
  - (c) Heine-Borel property.

More questions will be posted in the coming days.