

# Oscillatory deformation of amorphous materials: a numerical investigation

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## My thesis in a nutshell

Study the behavior of model **metallic glasses** under deformation,  
by means of atomistic computer simulations

Figure : Shear strain  $\gamma = \tan \theta$  is varied between  $-\gamma_{max}, \gamma_{max}$

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Figure : Shear strain  $\gamma = \tan \theta$  is varied between  $-\gamma_{max}, \gamma_{max}$

1. What happens in the deformed glass at a microscopic level?
2. Are there any similarities with other systems?

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Input and benchmarks for mesoscopic descriptions (e.g. STZ)

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- ▶ Lennard-Jones mixtures (LJ)

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One can then unleash the arsenal of numerical integration methods

## Simulating glasses with LJ binary mixtures

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Tuning of the LJ interaction potential

Parameters in the potential

$$\phi_{ij}(r) = 4\epsilon_{ij} \left( \left( \frac{\sigma_{ij}}{r} \right)^{12} - \left( \frac{\sigma_{ij}}{r} \right)^6 \right)$$

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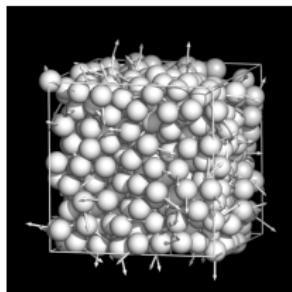
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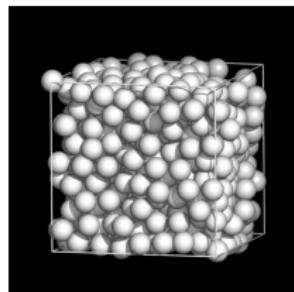
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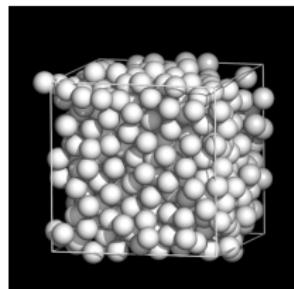
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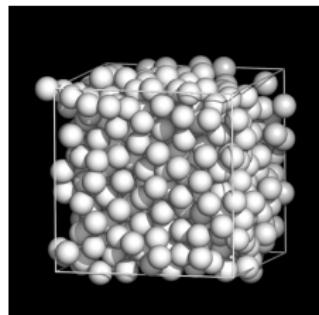
## Making of the glass: quenching at infinite rate



1. The system can be equilibrated at constant  $T$  with a Nosé-Hoover thermostat
2. Velocities are disregarded and configurations are energy minimized with a conjugate-gradient algorithm

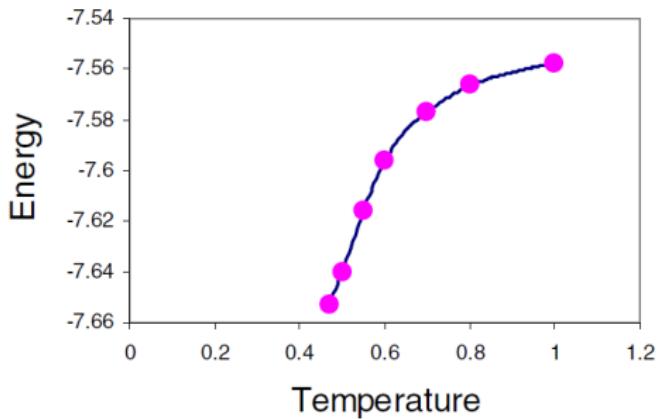
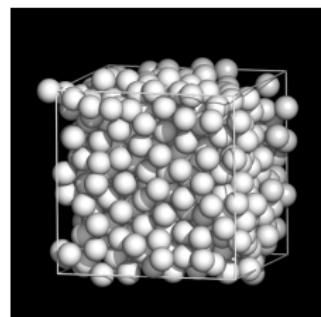
## Properties of undeformed samples

Energy minimization of configurations equilibrated at  $T$  yields  
*inherent structures* with *effective temperature*  $T$



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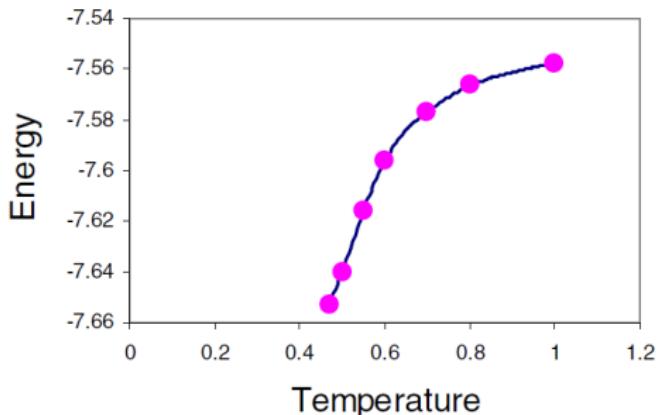
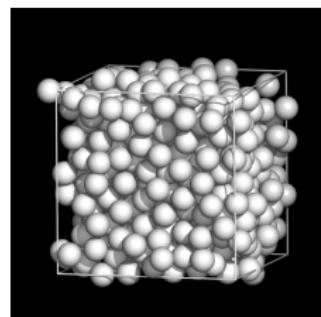
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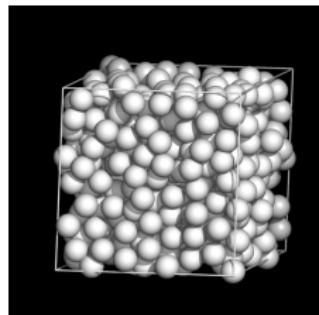


The properties of the inherent structures depend on the effective  $T$

How to deform them?

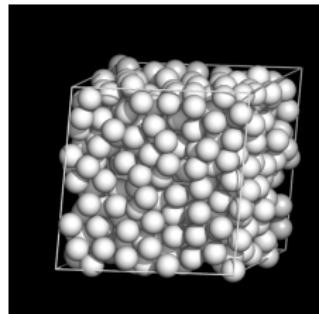
# Deformation

Deformation protocol: athermal quasi-static (AQS)



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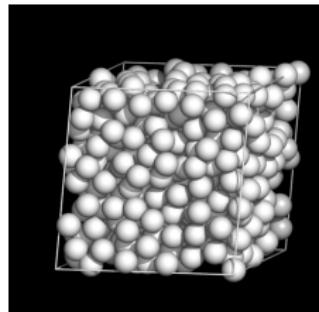
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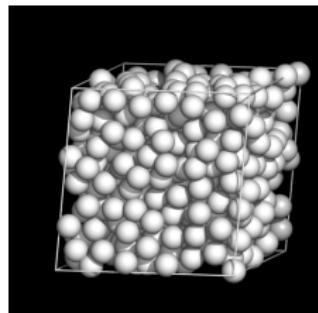
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- ▶ By iterating the steps, one can reach arbitrary strains

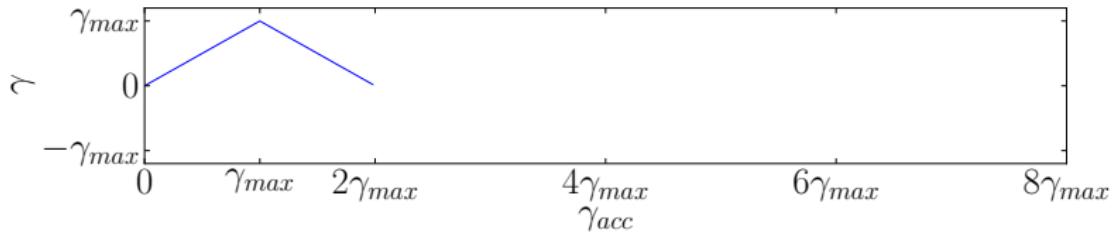
## What is the effect of changing the strain?

in 3D space

in  $(3ND)$  configuration space

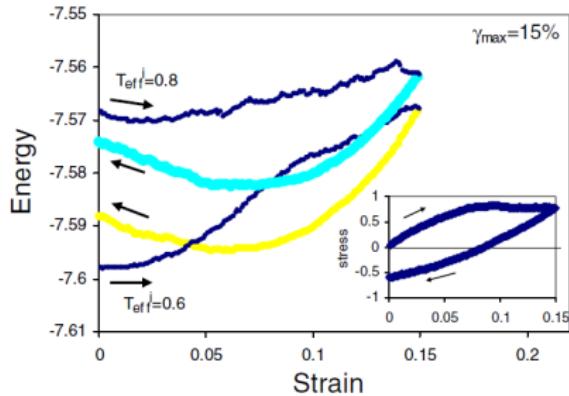
## Oscillatory strain

Consider a triangle wave strain profile ranging in  $[-\gamma_{max}, \gamma_{max}]$ ,  
and define  $\gamma_{acc} = \sum |d\gamma|$



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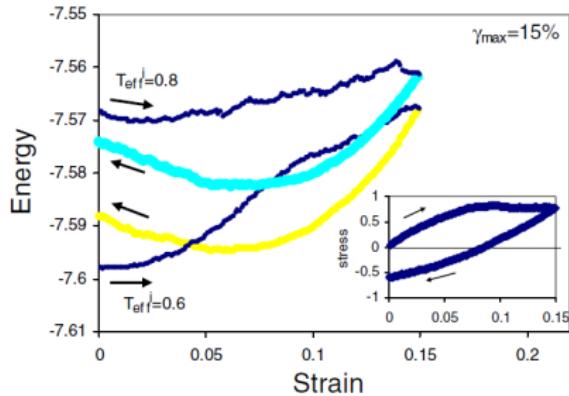
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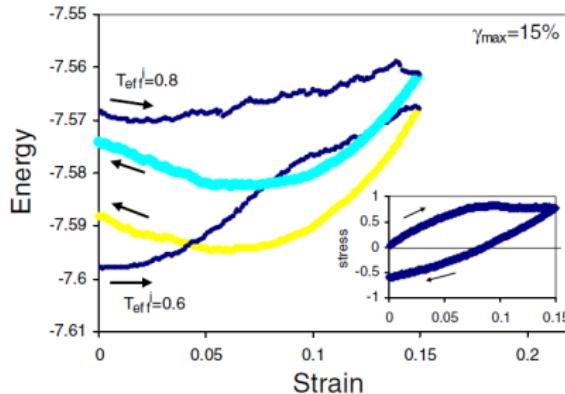


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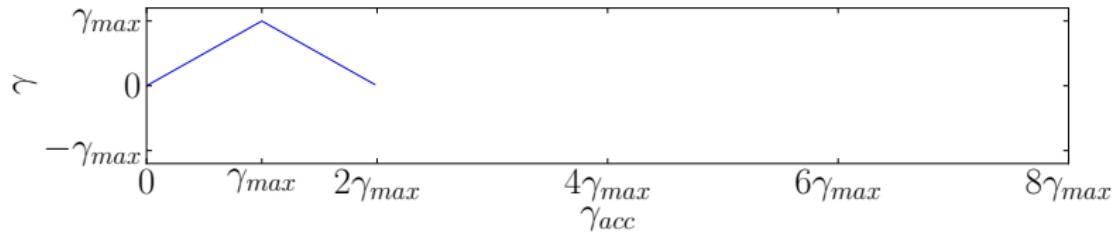


- ▶ Samples differing in their effective  $T$  change their energy
- ▶ The result (increase or decrease) depends on  $T$  (and  $\gamma_{\max}$ )

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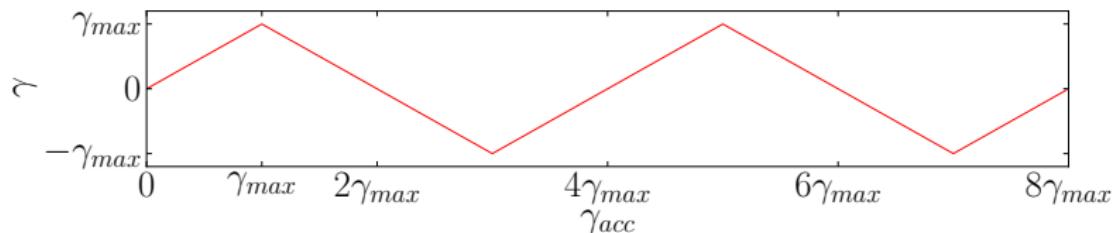
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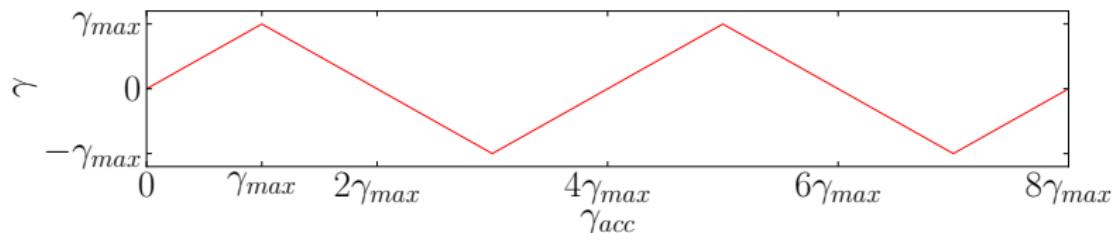
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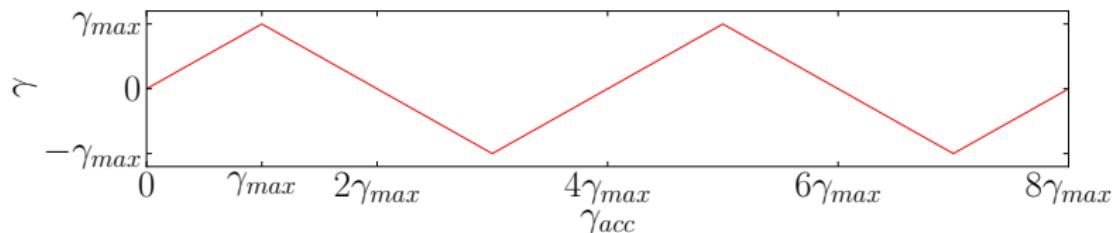
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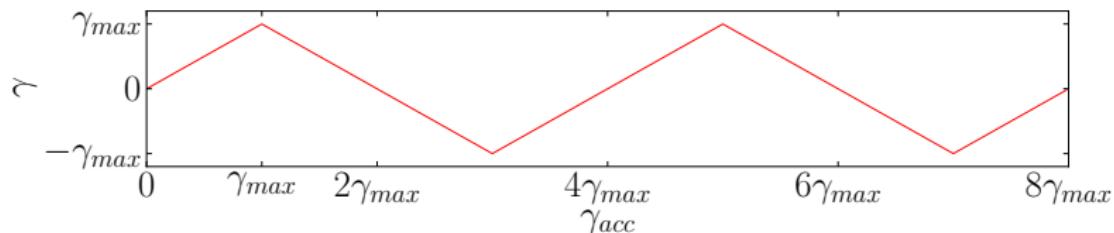
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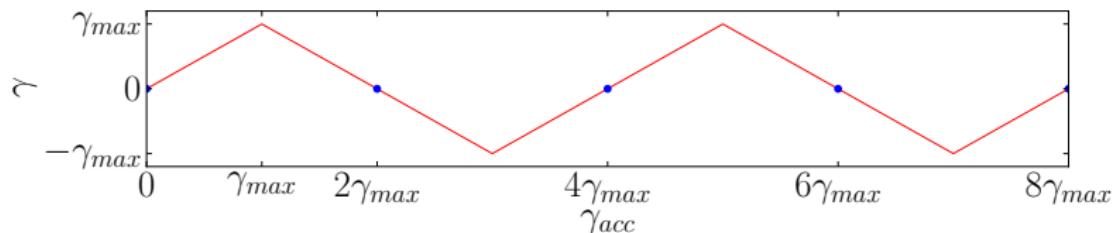
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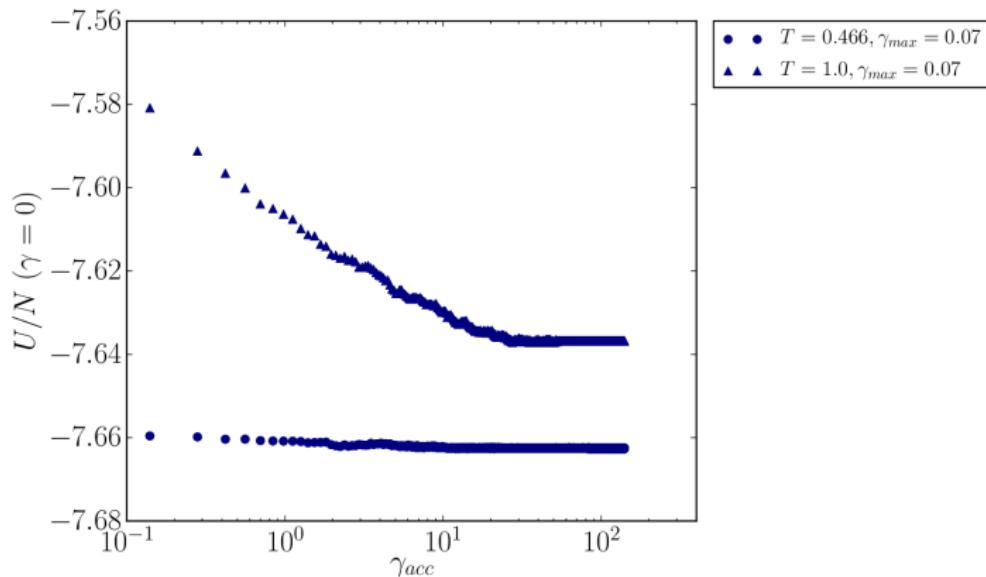


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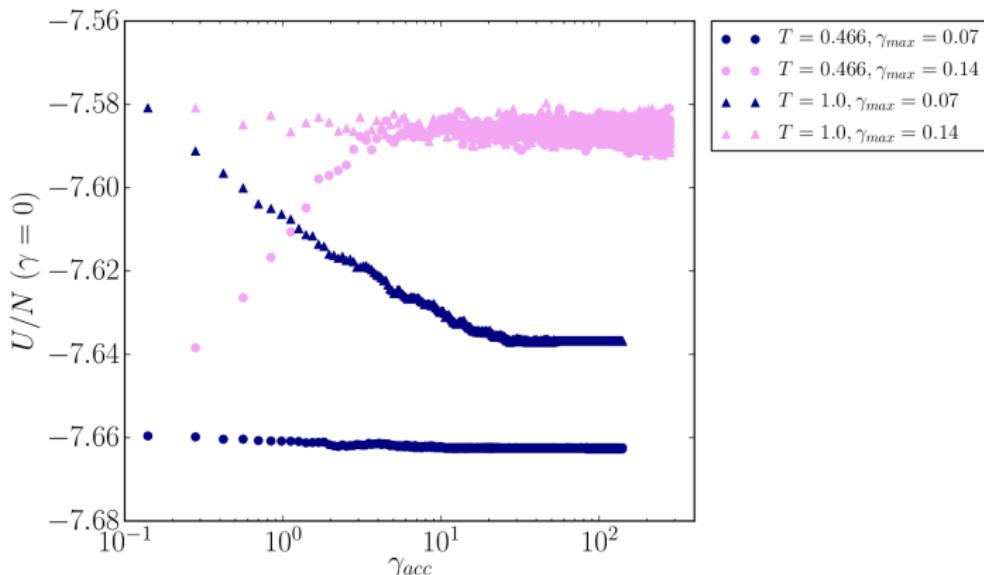
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# Potential energy



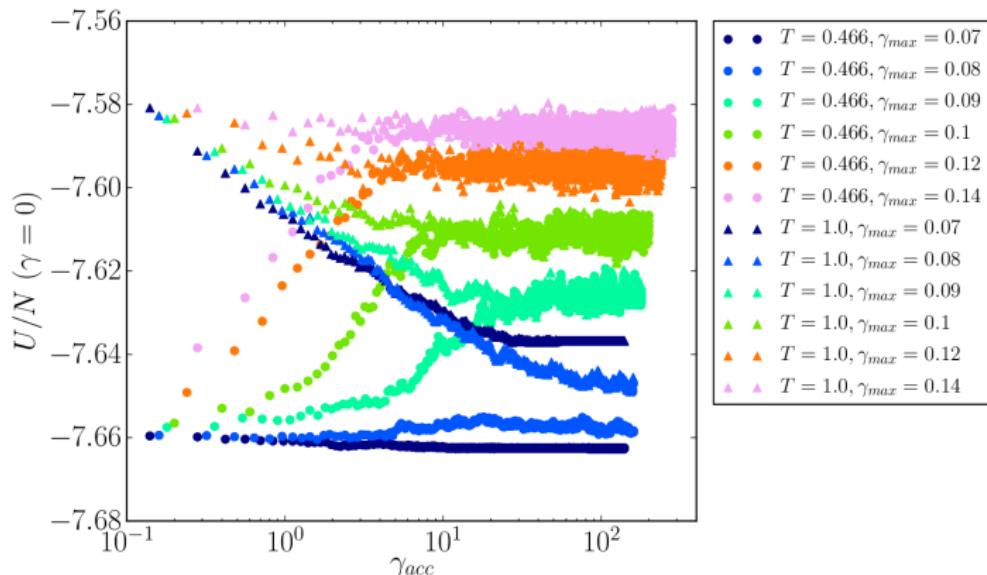
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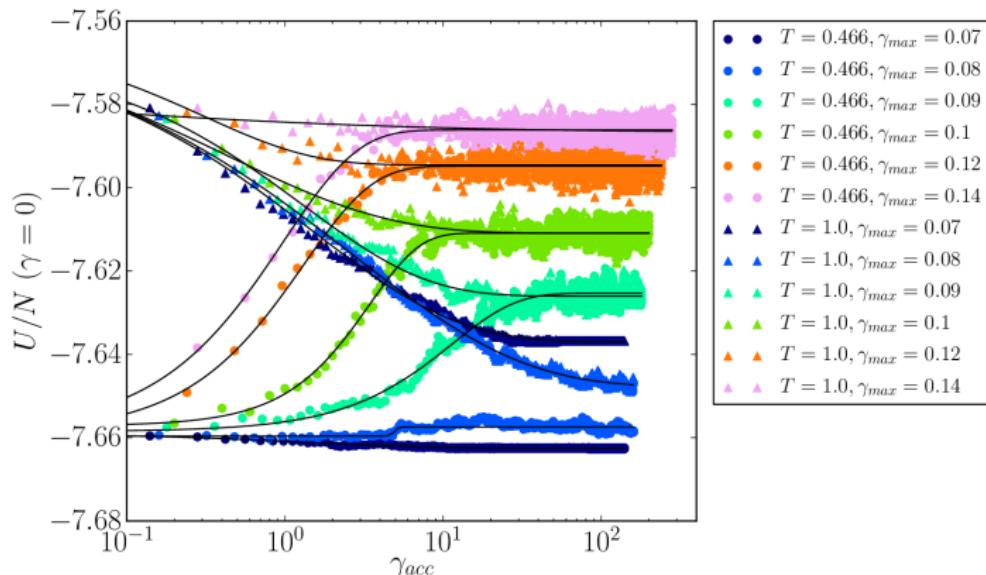
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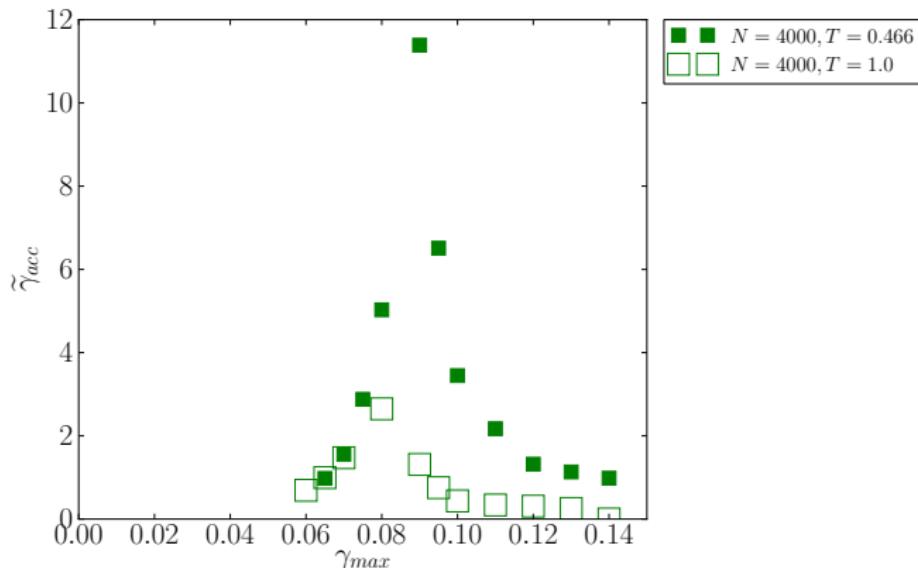


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- ▶ Energy profiles are described by stretched exponentials

$$U = (U_0 - U_\infty)e^{-(\gamma_{acc}/\tilde{\gamma}_{acc})^\alpha} + U_\infty$$

## Values of $\tilde{\gamma}_{acc}$ from the energy fits

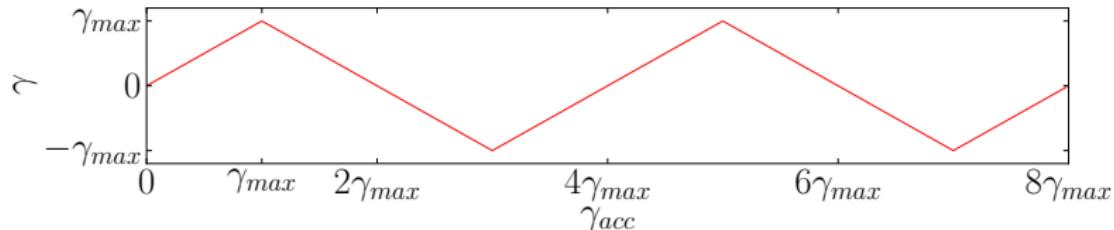
$\tilde{\gamma}_{acc}$  marks the onset of a “steady state”



- ▶  $\tilde{\gamma}_{acc}$  peaks for some intermediate value

## Oscillatory strain

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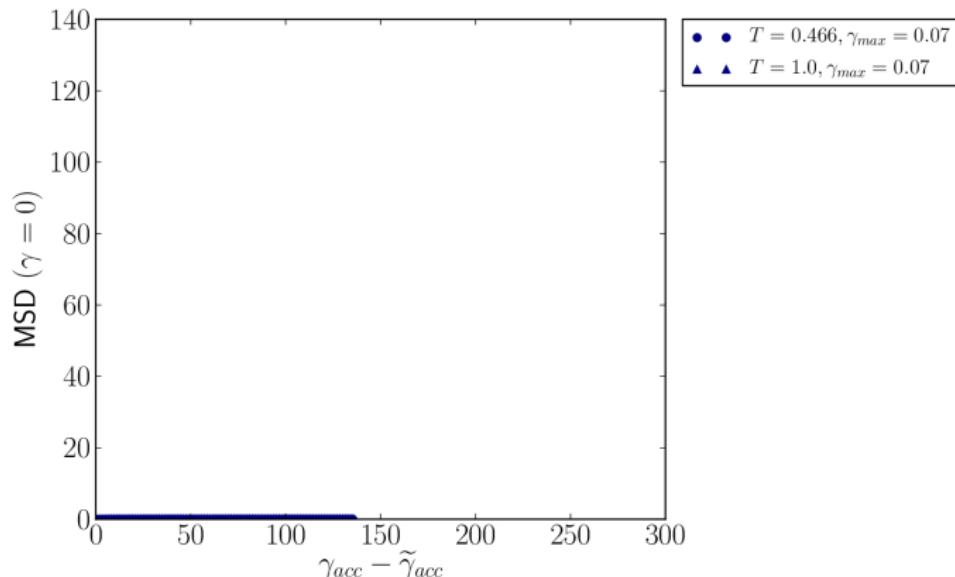
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## MSD in the asymptotic state

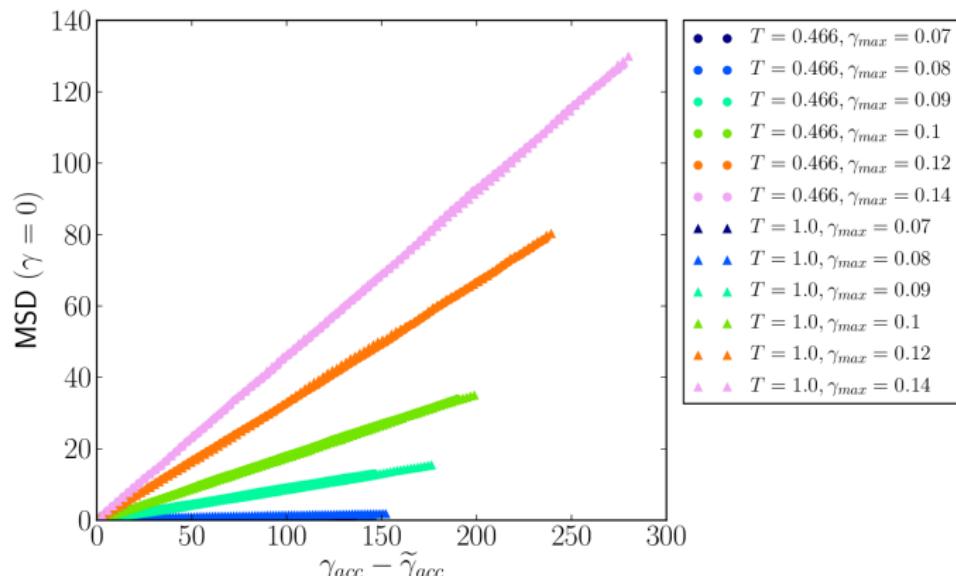
The MSD measured from samples encountered for  $\gamma_{acc} > \tilde{\gamma}_{acc}$



- ▶ Two regimes:
  - ▶ Low  $\gamma_{max}$ : samples do not move at all (absorbing)

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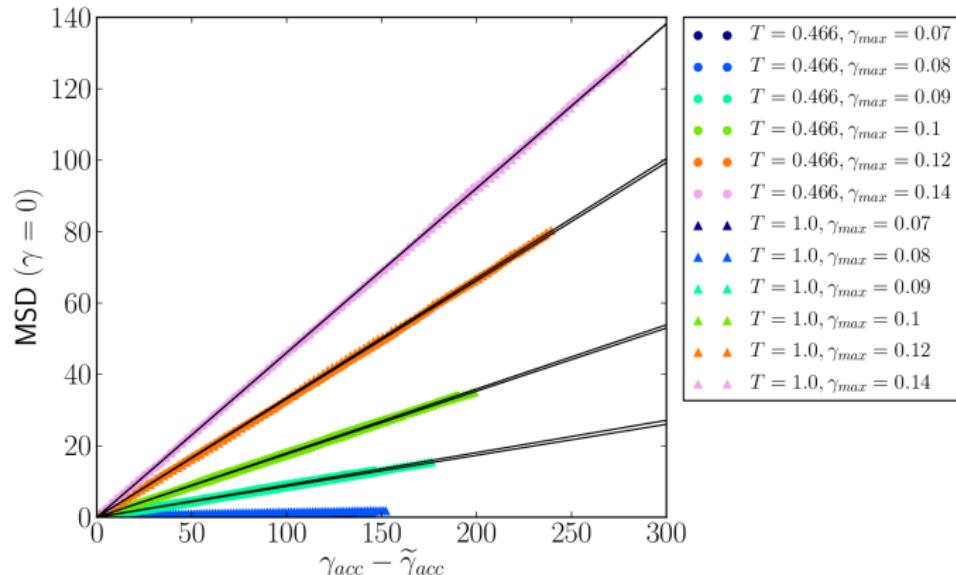
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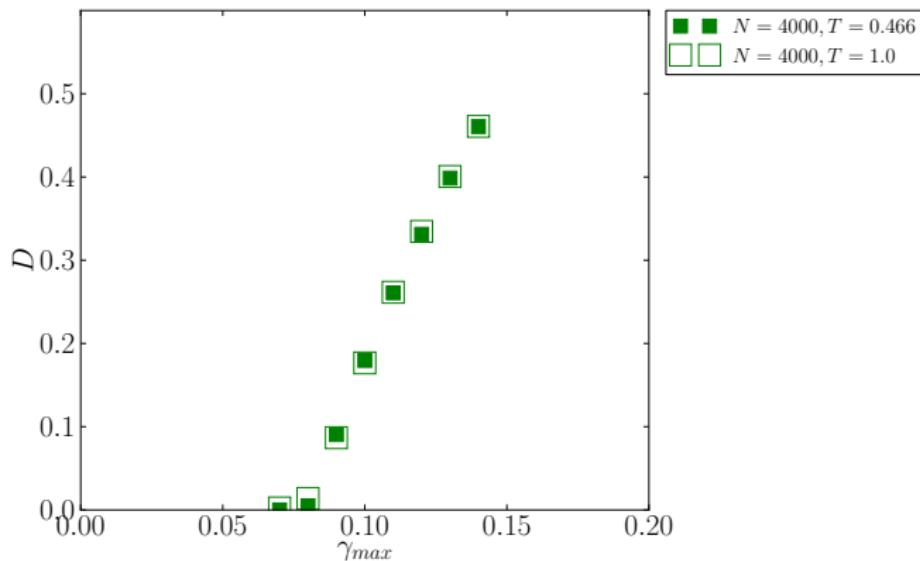
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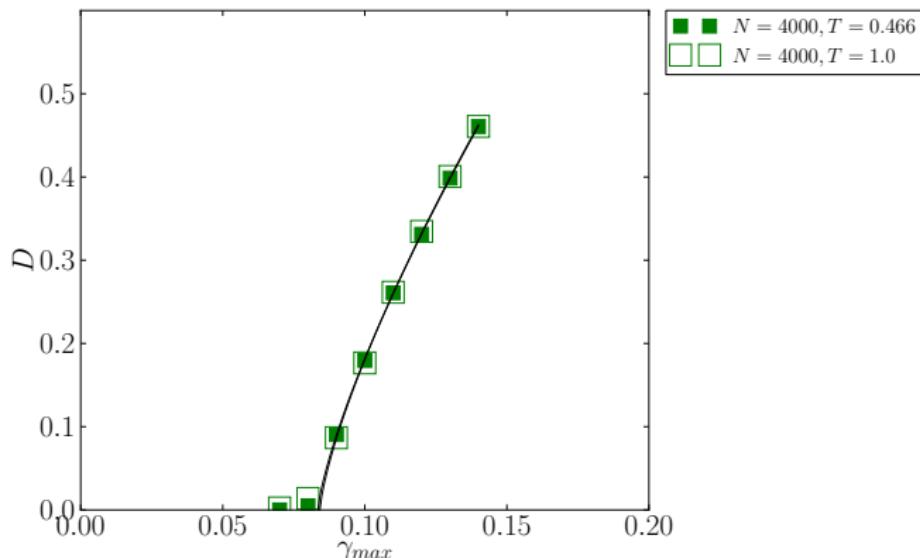
- ▶ Two regimes:
  - ▶ Low  $\gamma_{max}$ : samples do not move at all (absorbing)
  - ▶ High  $\gamma_{max}$ : samples diffuse
- ▶ The trends can be fit with:  $MSD = D(\gamma_{acc} - \tilde{\gamma}_{acc})$

## Values of $D$ extracted from the MSD



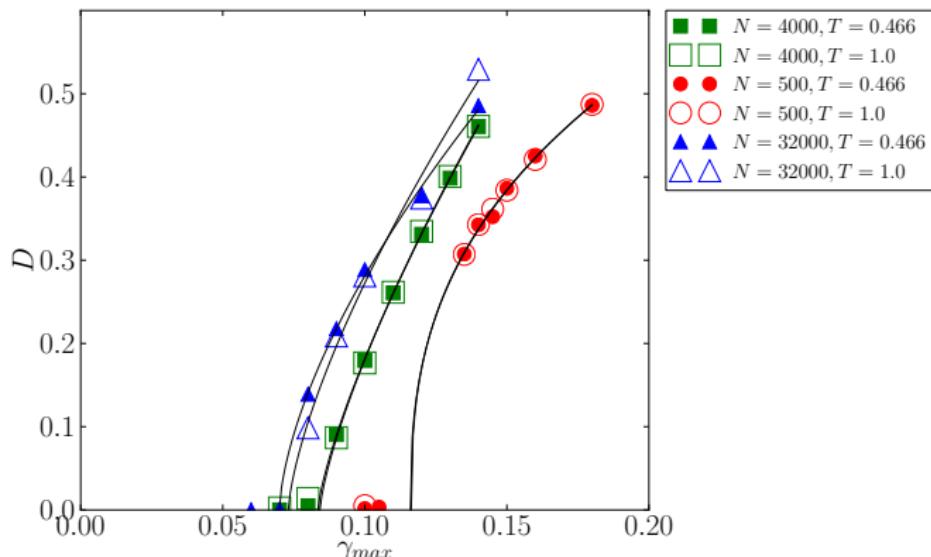
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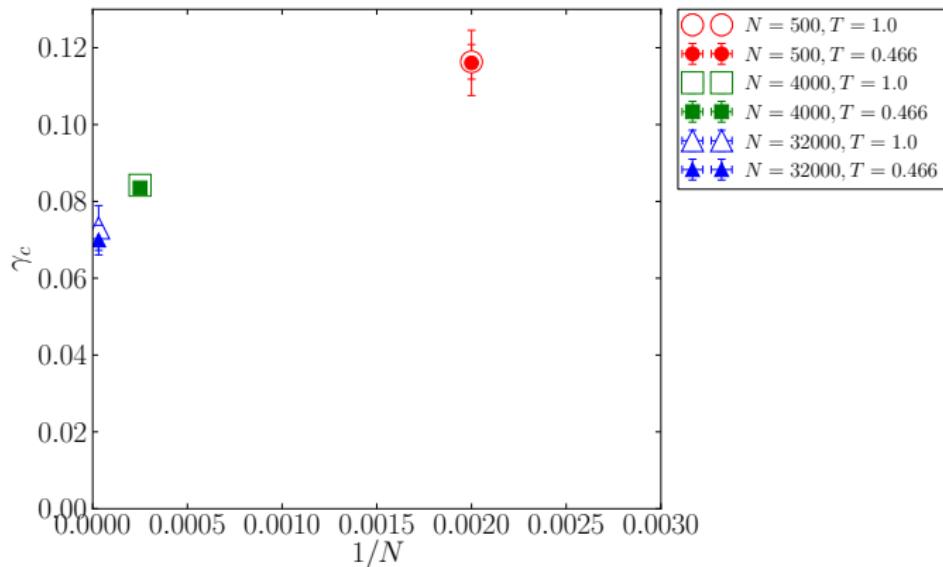
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- ▶  $D \propto (\gamma_{max} - \gamma_c)^\beta$ ?

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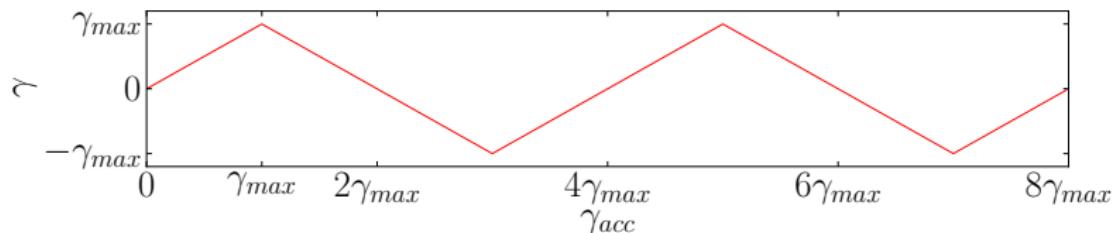
## Scaling of $\gamma_c$



The putative  $\gamma_c$  seems not to be vanishing for  $N \rightarrow \infty$

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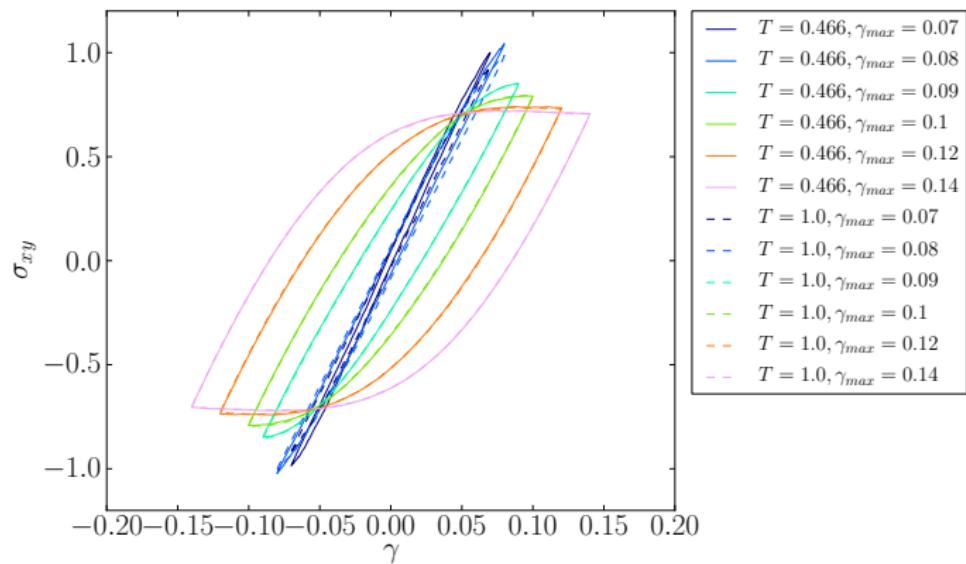


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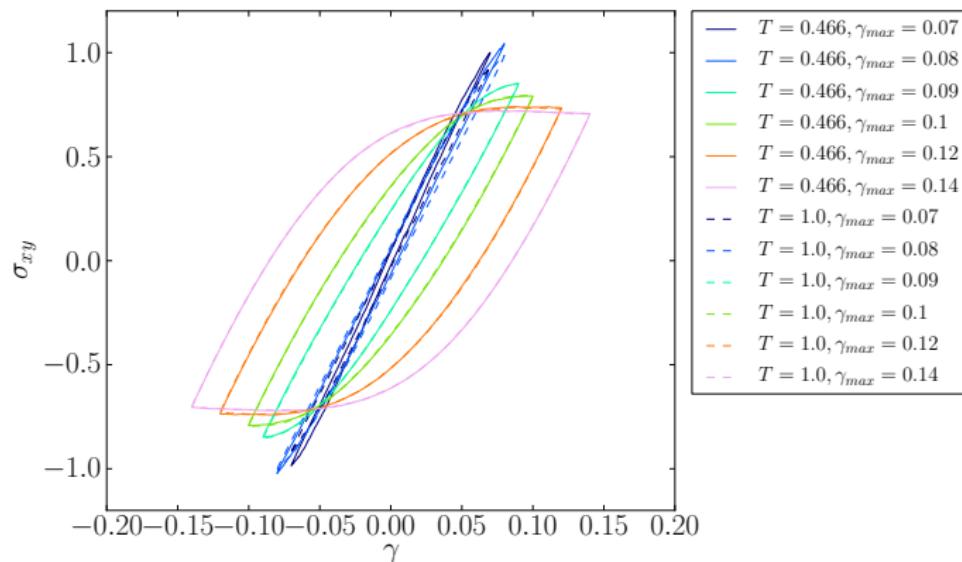
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# Hysteresis curves in the “steady state”

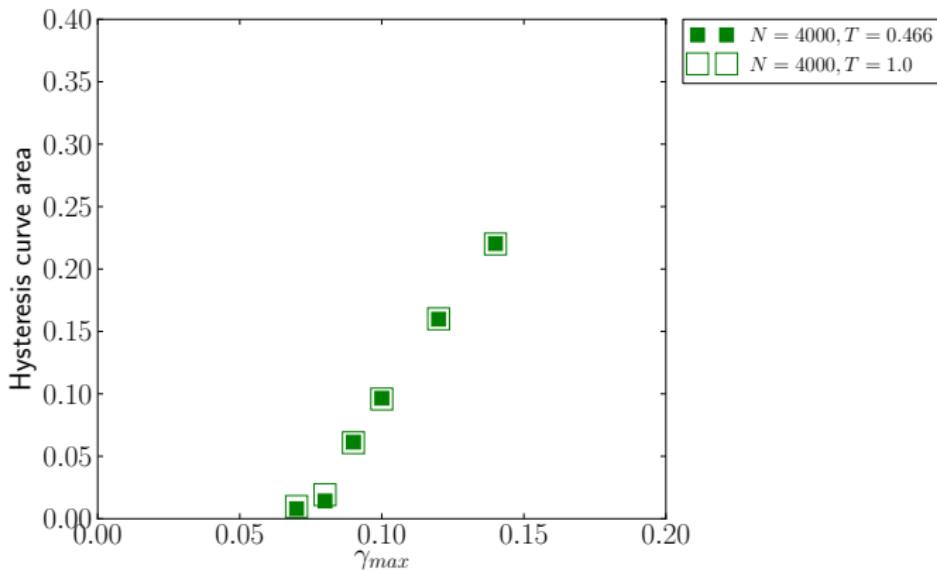


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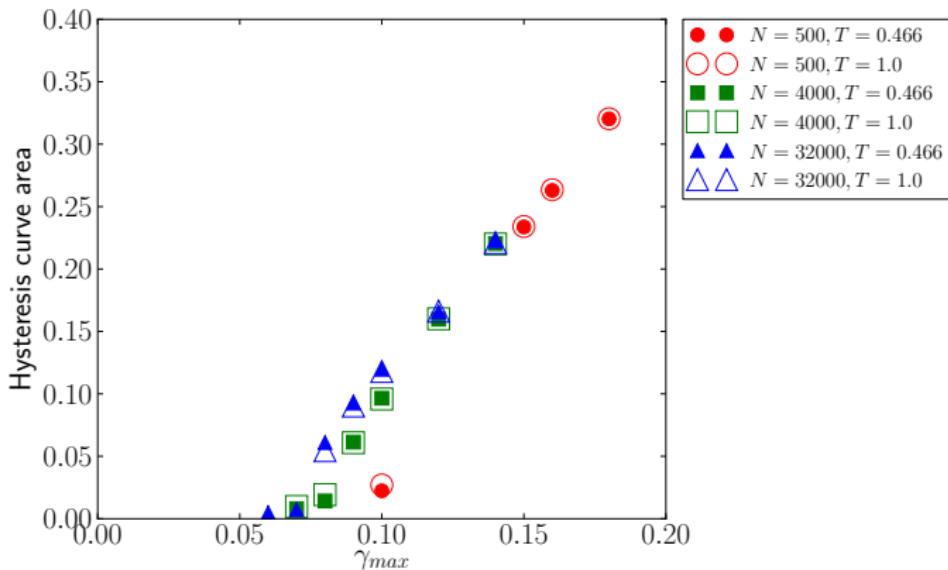
- ▶ Two regimes:
  - ▶ Low  $\gamma_{max}$ : narrow curves
  - ▶ High  $\gamma_{max}$ : broad curves

## Area of the hysteresis curves



The onset of dissipation is compatible with  $\gamma_c$

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## A comparison: suspensions and their behavior<sup>2</sup>

- ▶ Particles suspended in a viscous medium

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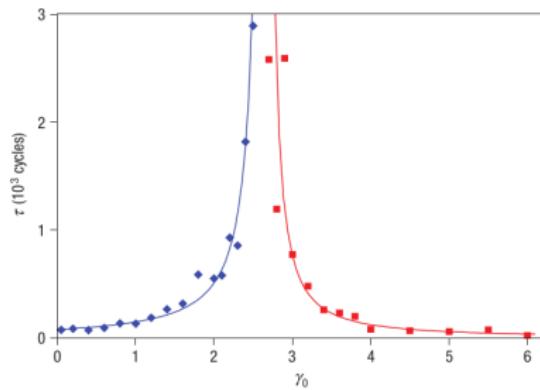
## A comparison: suspensions and their behavior<sup>2</sup>

- ▶ Particles suspended in a viscous medium
- ▶ Active particles collide with others during a cycle and don't come back to the initial position
- ▶ After some cycles the number of active particles doesn't change anymore

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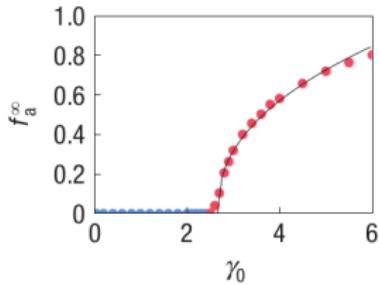
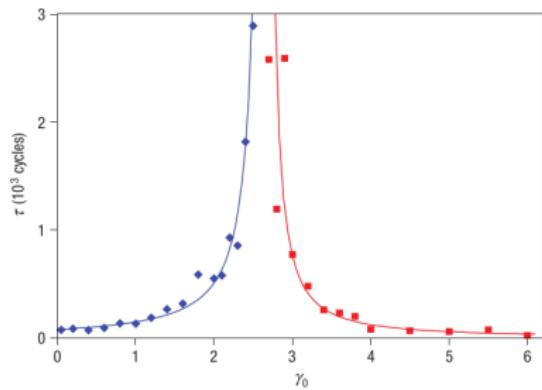
## Suspensions and their behavior<sup>3</sup>: a comparison



- ▶ The number of cycles needed to reach the steady fraction of active particles resembles  $\tilde{\gamma}_{acc}$  in LJ

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# Suspensions and their behavior<sup>3</sup>: a comparison



- ▶ The number of cycles needed to reach the steady fraction of active particles resembles  $\tilde{\gamma}_{acc}$  in LJ
- ▶ The asymptotic fraction of active particles as a function of  $\gamma_{max}$  resembles  $D$  in LJ

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## Partial summary: existence of a transition

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- ▶ The scenario is qualitatively similar to that of suspensions

## Pushing the analogy further: memory phenomena<sup>4</sup>

Training at  $\gamma_1$

Reading at different  $\gamma_r$

Encoding and reading of memory

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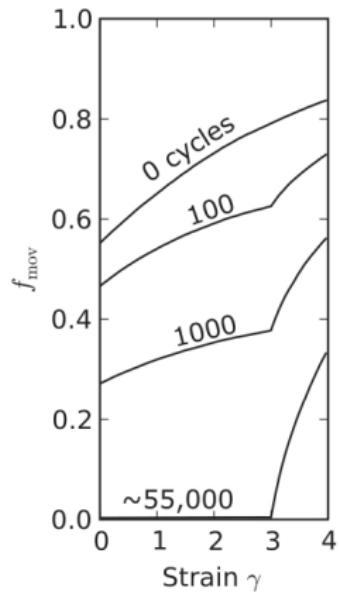
### Encoding and reading of memory

- ▶ Samples are *trained* by  $N_{cyc}$  cycles of amplitude  $\gamma_1$
- ▶ Trained samples are *read* with one cycle of amplitude  $\gamma_r$ : the number of active particles is measured as a function of  $\gamma_r$

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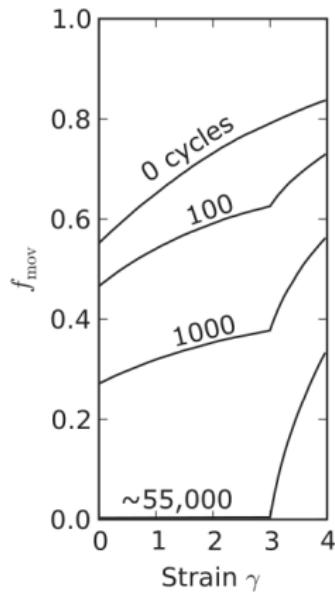
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## Memory phenomena in suspensions (continued)



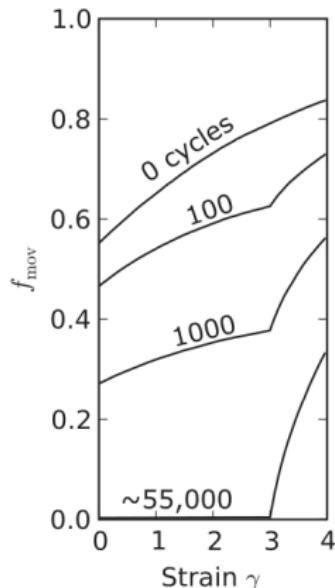
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## Memory phenomena in suspensions (continued)



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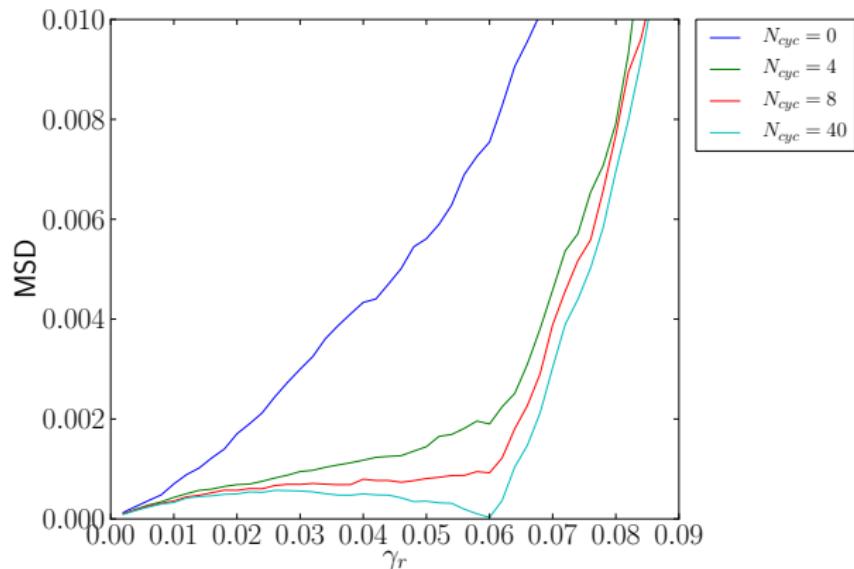


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What happens if one applies the same protocol to a LJ sample?

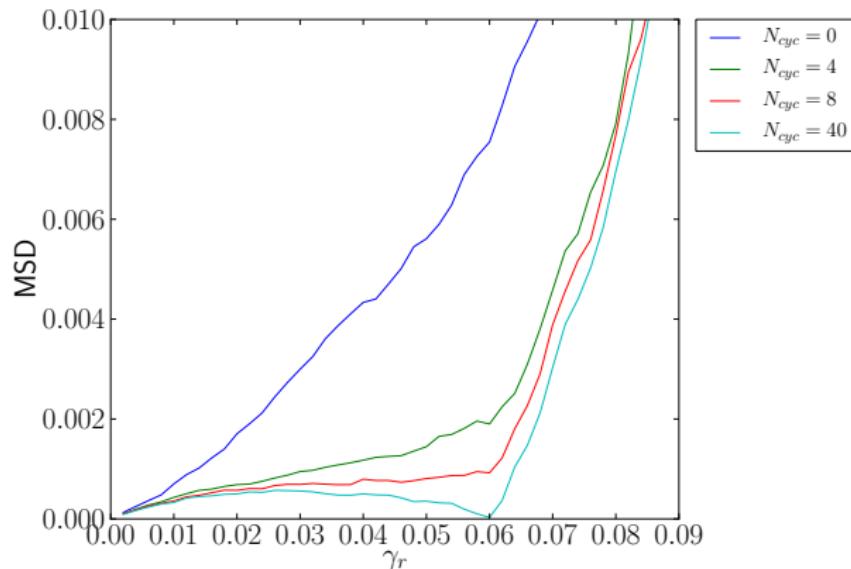
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Take the MSD of particles of trained samples read with  $\gamma_r$ :



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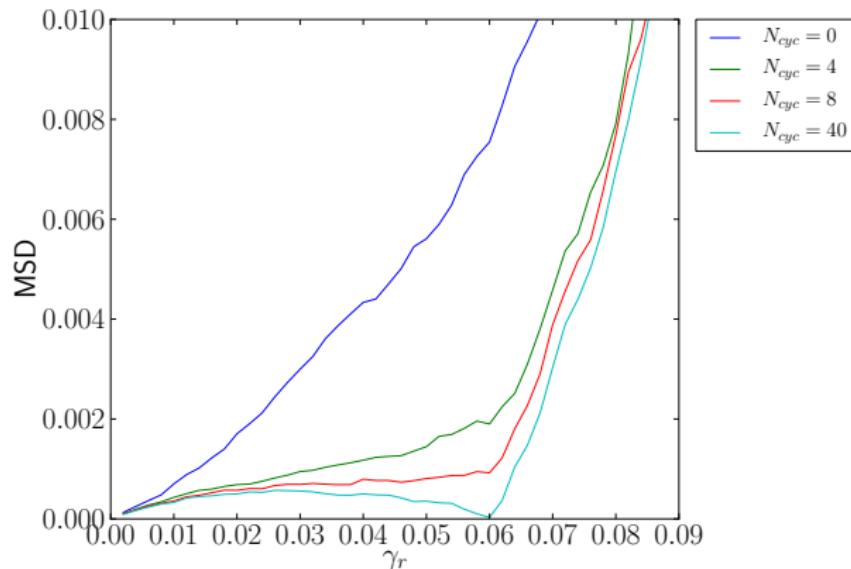
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## Single memory in LJ samples

Take the MSD of particles of trained samples read with  $\gamma_r$ :



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- ▶ The “bump”:  $\text{MSD} \neq 0$  if  $\gamma_r < \gamma_1$ , even for long trainings

## Why the bump?

$$\gamma_r < \gamma_1$$

$$\gamma_r = \gamma_1$$

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- ▶ A sample trained at  $\gamma_1$  returns into the original state after a reading cycle  $\gamma_r = \gamma_1$ , via a sequence of rearrangements
- ▶ If the amplitude  $\gamma_r \neq \gamma_1$ , the sequence is altered!

## Partial summary: memory phenomena

- ▶ Memory can be encoded and read in LJ samples by means of oscillatory deformation
- ▶ There are qualitative differences with memory of suspensions

## Can our results be generalized?

All the behavior above depends on the dynamics of the LJ system

in 3D space

in  $(3N)$  configuration space

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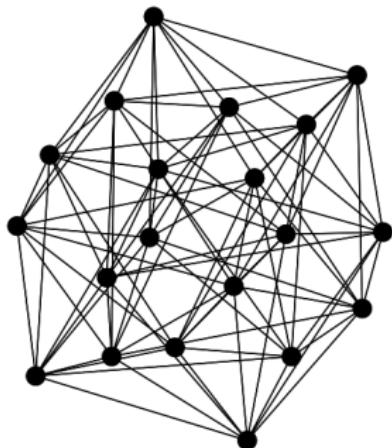
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Is such behavior found in other systems with a deformable energy landscape?

## NK model

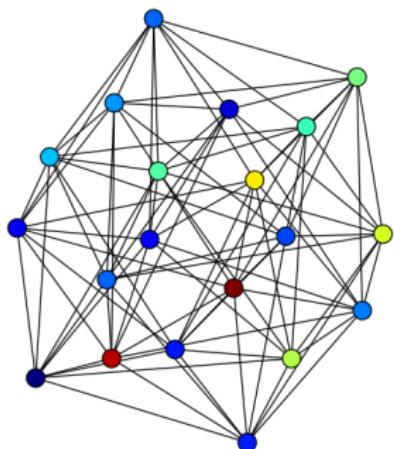
A discrete energy landscape depending on a parameter  $\gamma$



- ▶ A set of connected nodes

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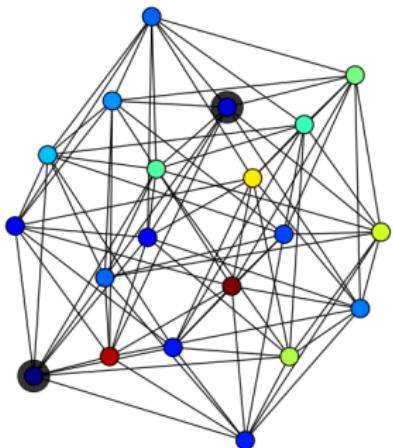
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- ▶ A set of connected nodes
- ▶ An energy function is defined for each node

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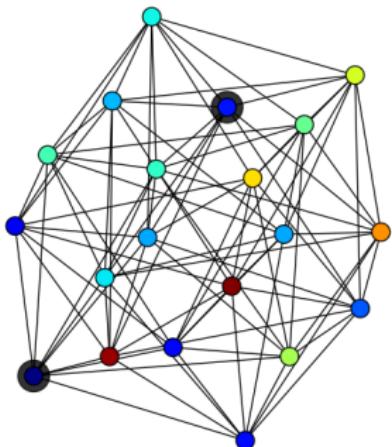
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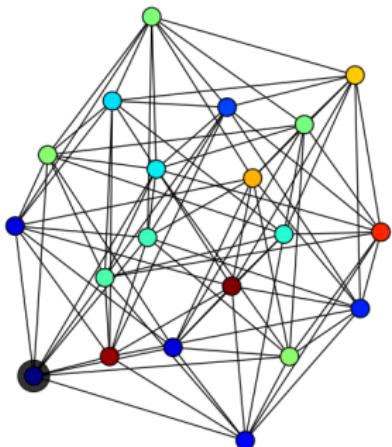
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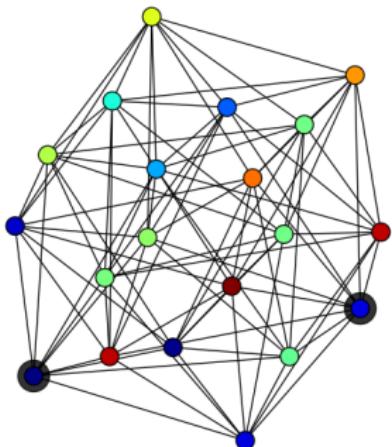
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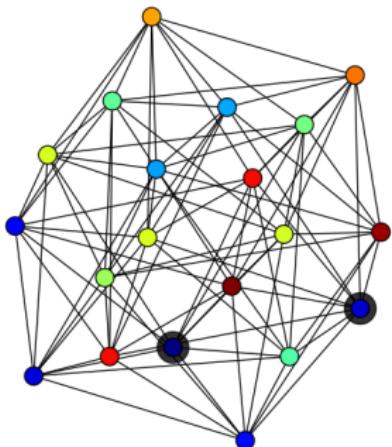
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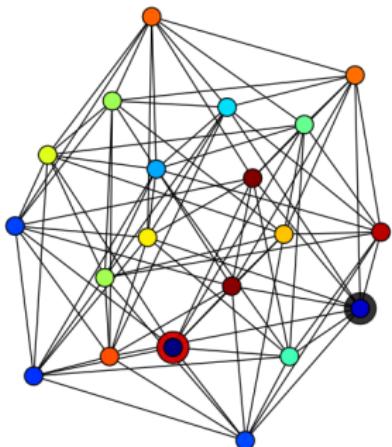
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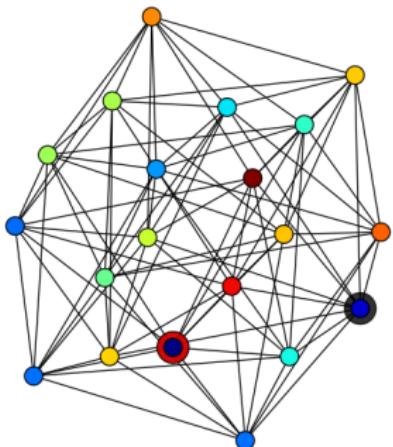
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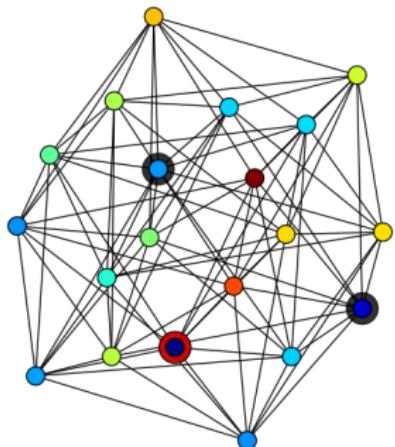
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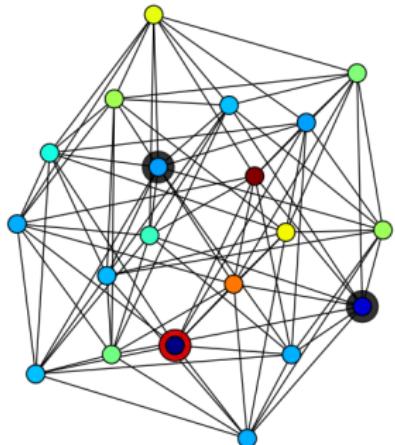
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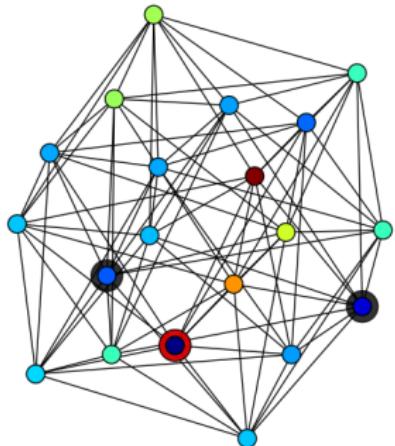
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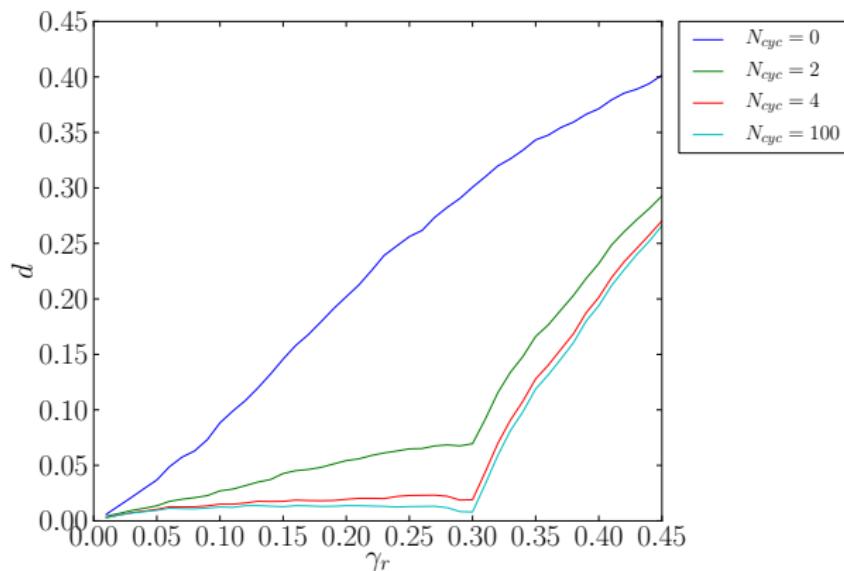
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## Information from the NK model

The energy behavior, diffusion and memory effects can be studied as  $\gamma$  is varied in an oscillatory way

## Example: single memory in NK samples

Take the Hamming distance of trained samples read with amplitude  $\gamma_r$ :



- ▶ The behavior agrees qualitatively with that of LJ

# Conclusions

## Key results of the thesis

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Thank you!

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and to  
G. Foffi, and S. Sastry (TIFR Hyderabad)