Theory recap 2.10.24

Recall from last week that

Take-away

- (Ω, \mathcal{A}, P) with $P: \mathcal{A} \to [0,1]$ and $P(\Omega) = 1$
- $X:\Omega \to F$ countable, with $\{X=x\} \in \mathcal{A} \text{ for all } x \in F$
- $\mu: F \to [0,1]$ such that $\mu(x) = P\{X = x\}$

In this section when we say "X is a RV" we mean "X : $\Omega \to F \subset \mathbb{R}$ is a discrete random variable with real values."

• A RV is integrable if $\sum_{x\in F}|x|P(X=x)<+\infty$, and in this case its expected value $\mathbb{E}(X)$ is the real number

$$\mathbb{E}(X) \coloneqq \sum_{x \in F} x P(X = x).$$

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