

Diseño de Máquinas de Estado Finito: FSM

□ *Diseñar una FSM para un motor asíncrono*

□ *X2X2X1X2 arranca en un sentido*

□ *X1X1X2X1 arranca en sentido contrario*

□ *X2X1X1 se detiene*

□ *X1X2X2X1 cambia de giro*

Diagrama de Estados

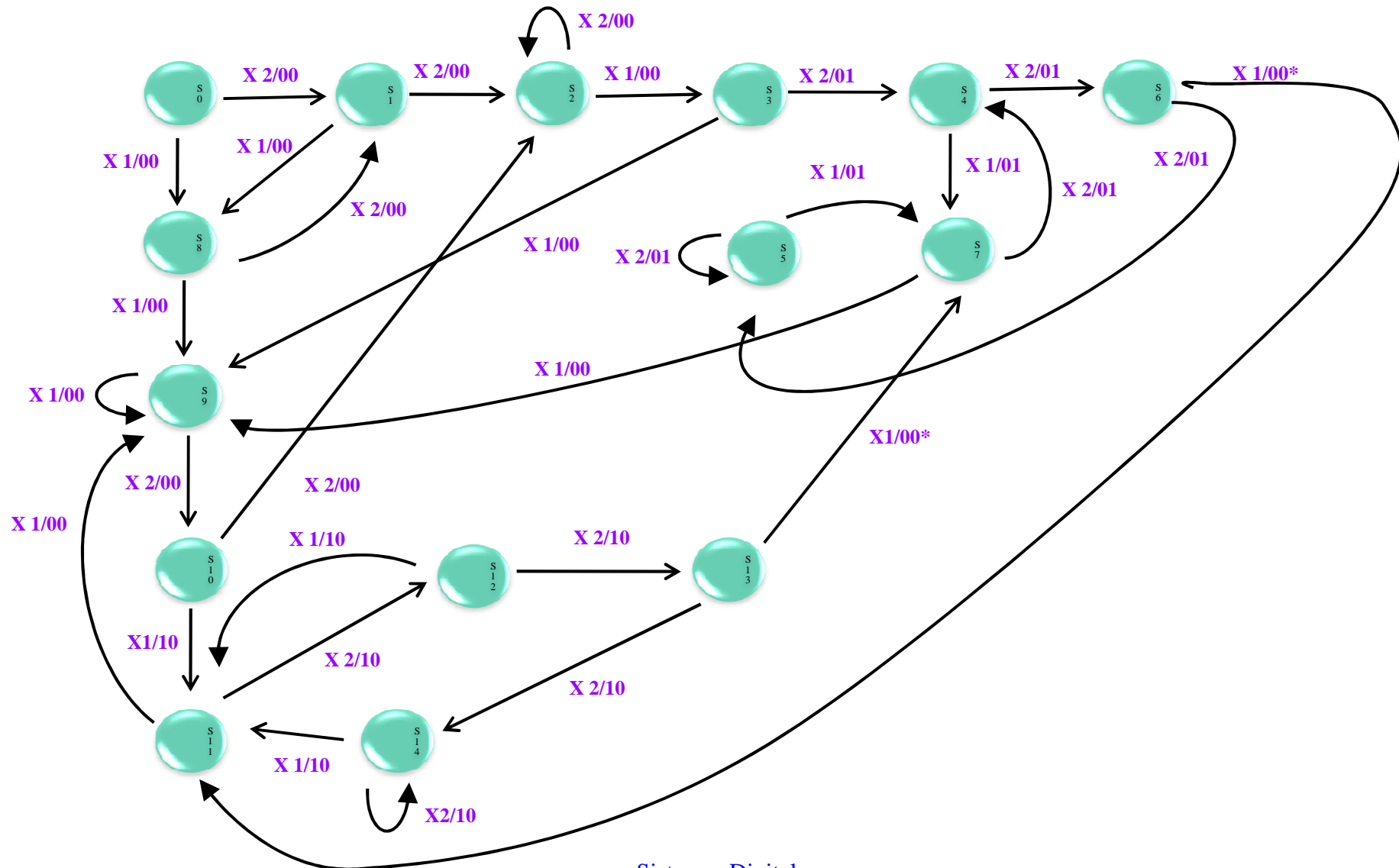


Tabla de Estados para el FF D

	X1			X2		
$q_3 \ q_2 \ q_1 \ q_0$	$q_{3+} \ q_{2+} \ q_{1+} \ q_{0+} / Z_1 \ Z_0$			$q_{3+} \ q_{2+} \ q_{1+} \ q_{0+} / Z_1 \ Z_0$		
0 0 0 0	1 0 0 0	0 0		0 0 0 1	0 0	
0 0 0 1	1 0 0 0	0 0		0 0 1 0	0 0	
0 0 1 0	0 0 1 1	0 0		0 0 1 0	0 0	
0 0 1 1	1 0 0 1	0 0		0 1 0 0	0 1	
0 1 0 0	0 1 1 1	0 1		0 1 1 0	0 1	
0 1 0 1	0 1 1 1	0 1		0 1 0 1	0 1	
0 1 1 0	1 0 1 1	00*		0 1 0 1	0 1	
0 1 1 1	1 0 0 1	0 0		0 1 0 0	0 1	
1 0 0 0	1 0 0 1	0 0		0 0 0 1	0 0	
1 0 0 1	1 0 0 1	0 0		1 0 1 0	0 0	
1 0 1 0	1 0 1 1	1 0		0 0 1 0	0 0	
1 0 1 1	1 0 0 1	0 0		1 1 0 0	1 0	
1 1 0 0	1 0 1 1	1 0		1 1 0 1	1 0	
1 1 0 1	0 1 1 1	00*		1 1 1 0	1 0	
1 1 1 0	1 0 1 1	1 0		1 1 1 0	1 0	
1 1 1 1	x x x x	x x		x x x x	x x	

Tabla de Estados para el FF D

					X1						X2						
D ₃ D ₂ D ₁ D ₀					C ₃ C ₂ C ₁ C ₀				D ₃ D ₂ D ₁ D ₀					C ₃ C ₂ C ₁ C ₀			
1	x	x	x		1	0	0	0	1	x	x	x		1	0	0	0
1	x	x	0		1	0	0	1	1	1	x	x	0	1	0	0	1
x	x	x	1		0	0	0	1	1	x	x	x	1	1	0	0	1
1	x	0	x		1	0	1	0	1	1	1	0	0	1	1	1	1
x	x	1	1		0	0	1	1	1	x	x	1	1	1	0	0	1
x	x	1	x		0	0	1	0	1	x	x	1	x	1	0	0	1
1	0	x	1		1	1	0	1	1	1	0	0	1	1	1	1	1
1	0	0	x		1	1	1	0	1	1	0	0	0	1	1	1	1
x	x	x	1		0	0	0	1	1	1	x	x	1	1	0	0	1
x	x	x	x		0	0	0	0	1	1	x	x	x	0	1	0	1
x	x	x	1		0	0	0	1	1	1	x	x	x	1	1	0	1
x	x	0	x		0	0	1	0	1	1	x	1	0	0	1	1	1
x	0	1	1		0	1	1	1	1	1	x	0	1	1	1	0	1
0	x	1	x		1	0	1	0	1	1	0	x	1	0	1	1	1
x	0	x	1		0	1	0	1	1	1	x	0	x	1	1	0	1
x	x	x	x		x	x	x	x	1	1	x	x	x	x	1	1	1

Mapas de K

X1

q₃ q₂

q₁ q₀

	00	01	11	10
00	1 ₀	x ₄	x ₁₂	X ₈
01	1 ₁	x ₅	0 ₁₃	X ₉
11	1 ₃	1 ₇	X ₁₅	X ₁₁
10	x ₂	1 ₆	X ₁₄	X ₁₀

X2

q₃ q₂

q₁ q₀

	00	01	11	10
00	1 ₀	x ₄	X ₁₂	X ₈
01	1 ₁	X ₅	0 ₁₃	X ₉
11	1 ₃	1 ₇	X ₁₅	X ₁₁
10	x ₂	1 ₆	x ₁₄	x ₁₀

$$d_3 = X1 (nq_3) + X2 (nq_1)$$

X1

$q_3 \ q_2$

$q_1 \ q_0$

	00	01	11	10
00	X ₀	x ₄	0 ₁₂	X ₈
01	X ₁	X ₅	x ₁₃	X ₉
11	X ₃	0 ₇	X ₁₅	X ₁₁
10	x ₂	0 ₆	0 ₁₄	x ₁₀

X2

$q_3 \ q_2$

$q_1 \ q_0$

	00	01	11	10
00	X ₀	X ₄	0 ₁₂	X ₈
01	X ₁	X ₅	X ₁₃	1 ₉
11	1 ₃	0 ₇	x ₁₅	X ₁₁
10	x ₂	0 ₆	0 ₁₄	x ₁₀

$$d_2 = X2 (q_2)$$

X1

q₃ q₂

q₁ q₀

	00	01	11	10
00	X ₀	1 ₄	1 ₁₂	X ₈
01	X ₁	1 ₅	1 ₁₃	X ₉
11	0 ₃	0 ₇	X ₁₅	0 ₁₁
10	X ₂	1 ₆	x ₁₄	X ₁₀

X2

q₃ q₂

q₁ q₀

	00	01	11	10
00	X ₀	1 ₄	1 ₁₂	X ₈
01	x ₁	1 ₅	1 ₁₃	X ₉
11	0 ₃	0 ₇	X ₁₅	0 ₁₁
10	X ₂	0 ₆	x ₁₄	x ₁₀

$$d_1 = X1(nq_1) + X2(nq_1)$$

X1

q₃ q₂

	00	01	11	10
00	x ₀	1 ₄	1 ₁₂	1 ₈
01	0 ₁	x ₅	x ₁₃	X ₉
11	x ₃	x ₇	X ₁₅	X ₁₁
10	1 ₂	1 ₆	1 ₁₄	1 ₁₀

X2

q₃ q₂

	00	01	11	10
00	x ₀	1 ₄	1 ₁₂	1 ₈
01	0 ₁	X ₅	0 ₁₃	0 ₉
11	0 ₃	0 ₇	X ₁₅	0 ₁₁
10	1 ₂	1 ₆	1 ₁₄	1 ₁₀

q₁ q₀

$$d_0 = X1 (nq_0) + X2 (nq_0)$$

X1

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	0 ₁₃	0 ₉
	11	0 ₃	0 ₇	0 ₁₅	0 ₁₁
	10	0 ₂	0 ₆	1 ₁₄	0 ₁₀

X2

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	1 ₁₃	0 ₉
	11	0 ₃	0 ₇	1 ₁₅	1 ₁₁
	10	0 ₂	0 ₆	1 ₁₄	0 ₁₀

$$Z_1 = X_1 (q_3 q_2 n q_0 + q_3 q_1 n q_0) + X_2 (q_3 q_2 + q_3 q_1 q_0)$$

X1

$q_3 q_2$					
		00	01	11	10
$q_1 q_0$	00	0 ₀	1 ₄	0 ₁₂	0 ₈
	01	0 ₁	1 ₅	0 ₁₃	0 ₉
	11	0 ₃	0 ₇	x ₁₅	0 ₁₁
	10	0 ₂	0 ₆	0 ₁₄	0 ₁₀

X2

$q_3 q_2$					
		00	01	11	10
$q_1 q_0$	00	0 ₀	1 ₄	0 ₁₂	0 ₈
	01	0 ₁	1 ₅	0 ₁₃	0 ₉
	11	1 ₃	1 ₇	x ₁₅	0 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$Z_0 = X1(nq_3q_2q_1) + X2(nq_3q_2 + nq_3q_1q_0)$$

X1

X2

$q_3 \ q_2$

$q_1 \ q_0$

	00	01	11	10
00	1 ₀	0 ₄	0 ₁₂	0 ₈
01	1 ₁	0 ₅	1 ₁₃	0 ₉
11	1 ₃	1 ₇	x ₁₅	0 ₁₁
10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$q_3 \ q_2$

$q_1 \ q_0$

	00	01	11	10
00	1 ₀	0 ₄	0 ₁₂	0 ₈
01	1 ₁	0 ₅	1 ₁₃	0 ₉
11	1 ₃	1 ₇	x ₁₅	0 ₁₁
10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$C_3 = X1 (nq_3nq_2nq_1 + q_3q_2q_0 + nq_3q_2q_1 + nq_3q_1q_0) \\ + X2 (nq_3nq_2nq_1 + q_3q_2q_0 + nq_3q_2q_1 + nq_3q_1q_0)$$

X1

		q₃ q₂			
		00	01	11	10
q₁ q₀	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	0 ₁₃	0 ₉
	11	0 ₃	1 ₇	X ₁₅	0 ₁₁
	10	0 ₂	1 ₆	1 ₁₄	0 ₁₀

X2

		q₃ q₂			
		00	01	11	10
q₁ q₀	00	0 ₀	0 ₄	0 ₁₂	0 ₈
	01	0 ₁	0 ₅	1 ₁₃	0 ₉
	11	1 ₃	1 ₇	X ₁₅	1 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$C_2 = X1(q_2q_1 + q_3q_2nq_0) + X2 (nq_3q_2q_1 + q_3q_2q_0 + q_1q_0)$$

X1

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	1 ₄	1 ₁₂	0 ₈
	01	0 ₁	1 ₅	1 ₁₃	0 ₉
	11	1 ₃	1 ₇	X ₁₅	1 ₁₁
	10	0 ₂	0 ₆	0 ₁₄	0 ₁₀

X2

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	1 ₄	1 ₁₂	0 ₈
	01	0 ₁	1 ₅	1 ₁₃	0 ₉
	11	1 ₃	1 ₇	X ₁₅	1 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$C_1 = X1(q_2 n q_1 + q_1 q_0) + X2 (q_2 n q_1 + q_1 q_0 + n q_3 q_2)$$

X1

X2

$q_3 \ q_2$

$q_1 \ q_0$

	00	01	11	10
00	0 ₀	1 ₄	1 ₁₂	1 ₈
01	1 ₁	0 ₅	0 ₁₃	0 ₉
11	0 ₃	0 ₇	X ₁₅	0 ₁₁
10	1 ₂	1 ₆	1 ₁₄	1 ₁₀

$q_3 \ q_2$

$q_1 \ q_0$

	00	01	11	10
00	0 ₀	1 ₄	1 ₁₂	1 ₈
01	1 ₁	0 ₅	1 ₁₃	1 ₉
11	1 ₃	1 ₇	X ₁₅	1 ₁₁
10	1 ₂	1 ₆	1 ₁₄	1 ₁₀

$$C_0 = X1(nq_3nq_2nq_1q_0 + q_3nq_0 + q_2nq_0nq_3q_1nq_0) + \\ X2(q_1 + q_3 + nq_2q_0 + q_2nq_0)$$

Una vez obtenidas las ecuaciones de excitación y de salida, se puede dibujar el diagrama lógico del circuito.

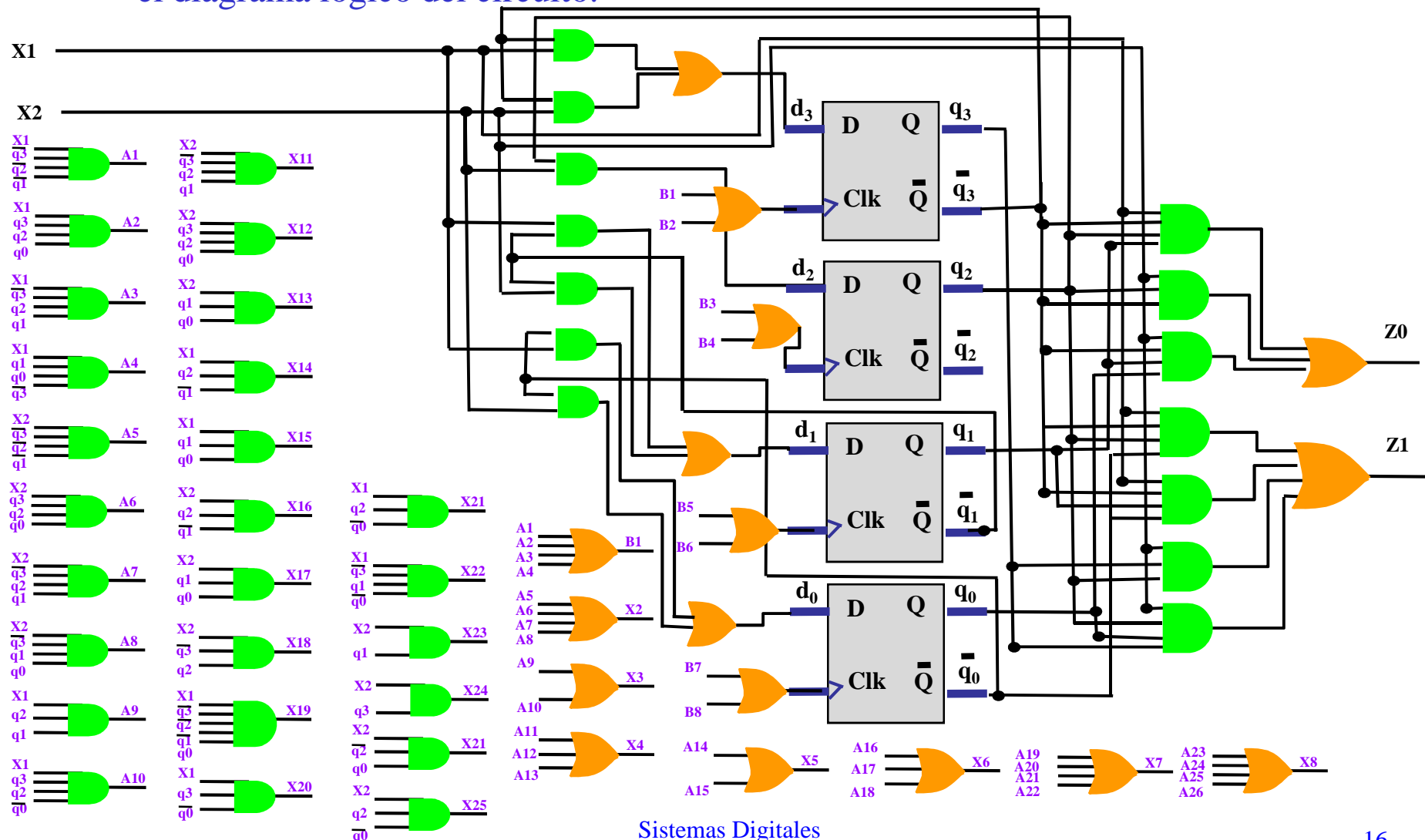


Diagrama de simulación

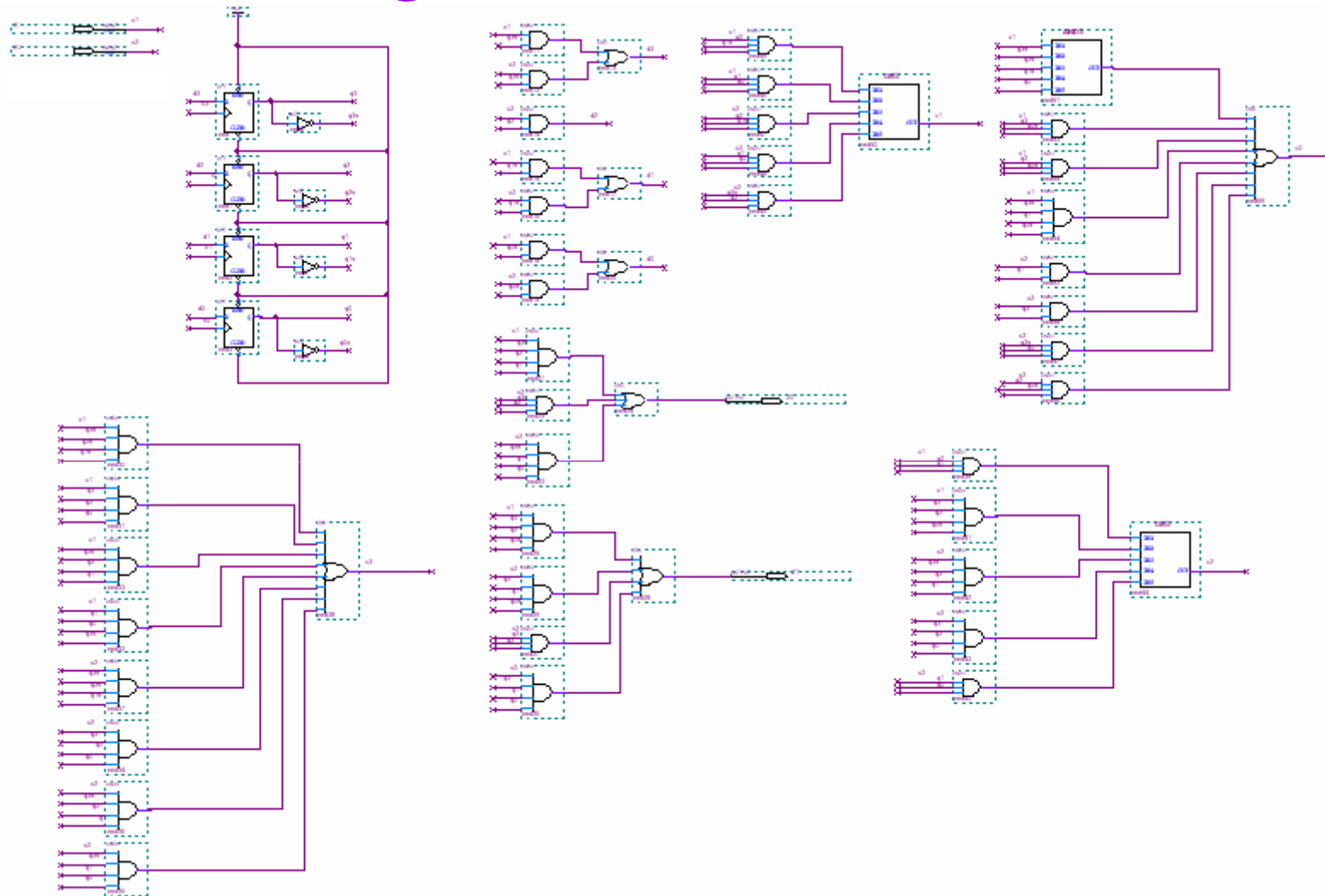


Diagrama de tiempo

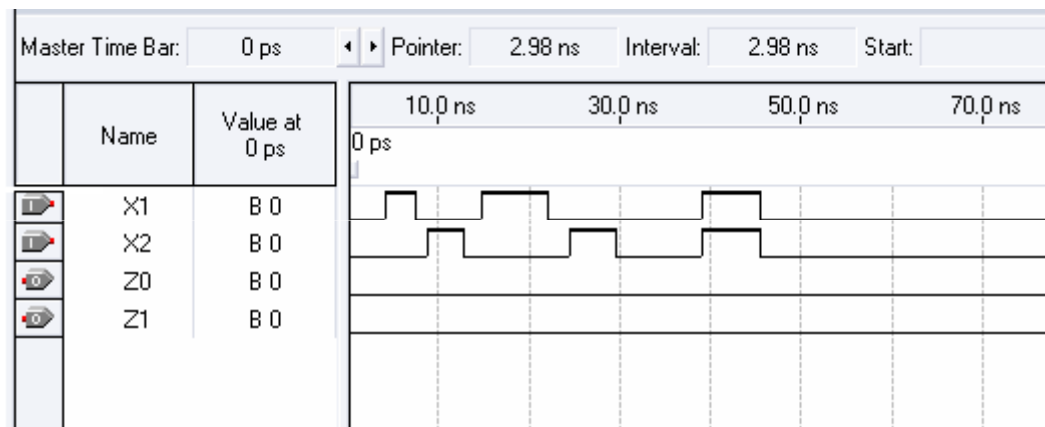


Tabla de estados para el FF T

$q_3\ q_2\ q_1\ q_0$	$q_{3+}\ q_{2+}\ q_{1+}\ q_{0+}\ /\ \ Z_1\ Z_0$	$q_{3+}\ q_{2+}\ q_{1+}\ q_{0+}\ /\ \ Z_1\ Z_0$	$T_3\ T_2\ T_1\ T_0$	$T_3\ T_2\ T_1\ T_0$		
0 0 0 0	1 0 0 0	0 0	0 0 0 1	0 0	1 0 0 0	0 0 0 1
0 0 0 1	1 0 0 0	0 0	0 0 1 0	0 0	1 0 0 1	0 0 1 1
0 0 1 0	0 0 1 1	0 0	0 0 1 0	0 0	0 0 0 1	0 0 0 0
0 0 1 1	1 0 0 1	0 0	0 1 0 0	0 1	1 0 1 0	0 1 1 1
0 1 0 0	0 1 1 1	0 1	0 1 1 0	0 1	0 0 1 1	0 0 1 0
0 1 0 1	0 1 1 1	0 1	0 1 0 1	0 1	0 0 1 0	0 0 0 0
0 1 1 0	1 0 1 1	00*	0 1 0 1	0 1	1 1 0 1	0 0 1 1
0 1 1 1	1 0 0 1	0 0	0 1 0 0	0 1	1 1 1 0	0 0 1 1
1 0 0 0	1 0 0 1	0 0	0 0 0 1	0 0	0 0 0 1	1 0 0 1
1 0 0 1	1 0 0 1	0 0	1 0 1 0	0 0	0 0 0 0	0 0 1 1
1 0 1 0	1 0 1 1	1 0	0 0 1 0	0 0	0 0 0 1	1 0 0 0
1 0 1 1	1 0 0 1	0 0	1 1 0 0	1 0	0 0 1 0	0 1 1 1
1 1 0 0	1 0 1 1	1 0	1 1 0 1	1 0	0 1 1 1	0 0 0 1
1 1 0 1	0 1 1 1	00*	1 1 1 0	1 0	1 0 1 0	0 0 1 1
1 1 1 0	1 0 1 1	1 0	1 1 1 0	1 0	0 1 0 1	0 0 0 0
1 1 1 1	x x x x	x x	x x x x	x x	X X X X	X X X X

Mapas de K

X1

		$q_3 \ q_2$			
		00	01	11	10
$q_1 \ q_0$	00	1 ₀	0 ₄	0 ₁₂	0 ₈
	01	1 ₁	0 ₅	1 ₁₃	0 ₉
	11	1 ₃	1 ₇	x ₁₅	0 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

X2

		$q_3 \ q_2$			
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	0 ₄	0 ₁₂	1 ₈
	01	0 ₁	0 ₅	0 ₁₃	0 ₉
	11	0 ₃	0 ₇	x ₁₅	0 ₁₁
	10	0 ₂	0 ₆	0 ₁₄	1 ₁₀

$$T_3 = X1(nq_3nq_2nq_1 + nq_3q_1q_0 + q_3q_2q_0) + X2 (q_3nq_2nq_0 +)$$

X1

		q₃ q₂			
		00	01	11	10
q₁ q₀	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	0 ₁₃	0 ₉
	11	0 ₃	1 ₇	x ₁₅	0 ₁₁
	10	0 ₂	1 ₆	1 ₁₄	0 ₁₀

X2

		q₃ q₂			
		00	01	11	10
q₁ q₀	00	0 ₀	0 ₄	0 ₁₂	0 ₈
	01	0 ₁	0 ₅	0 ₁₃	0 ₉
	11	1 ₃	0 ₇	x ₁₅	1 ₁₁
	10	0 ₂	0 ₆	0 ₁₄	0 ₁₀

$$T_2 = X1(q_1q_2 + q_3q_2nq_0) + X2 (nq_2q_1q_0)$$

X1

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	1 ₄	1 ₁₂	0 ₈
	01	0 ₁	1 ₅	1 ₁₃	1 ₉
	11	1 ₃	1 ₇	x ₁₅	1 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

X2

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	1 ₄	0 ₁₂	0 ₈
	01	1 ₁	0 ₅	1 ₁₃	1 ₉
	11	1 ₃	1 ₇	x ₁₅	1 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$T_1 = X1(q_2 nq_1 + q_1 q_0) + X2(q_3 q_0 + nq_3 nq_2 q_0 + q_1 q_0 + nq_3 q_2 nq_0)$$

X1

		q ₃ q ₂			
		00	01	11	10
q ₁ q ₀	00	0 ₀	1 ₄	1 ₁₂	1 ₈
	01	1 ₁	0 ₅	0 ₁₃	0 ₉
	11	0 ₃	0 ₇	x ₁₅	0 ₁₁
	10	1 ₂	1 ₆	1 ₁₄	1 ₁₀

X2

		q ₃ q ₂			
		00	01	11	10
q ₁ q ₀	00	1 ₀	0 ₄	1 ₁₂	1 ₈
	01	1 ₁	0 ₅	1 ₁₃	1 ₉
	11	1 ₃	1 ₇	x ₁₅	1 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$T_0 = X1 (q_3 nq_0 + q_2 nq_0 + q_1 nq_0 + nq_3 nq_2 nq_1 q_0) + \\ X2 (q_3 nq_1 + q_1 q_0 + nq_3 nq_2 nq_1 + nq_3 q_2 q_1)$$

X1

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	0 ₁₃	0 ₉
	11	0 ₃	0 ₇	0 ₁₅	0 ₁₁
	10	0 ₂	0 ₆	1 ₁₄	0 ₁₀

X2

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	1 ₁₃	0 ₉
	11	0 ₃	0 ₇	1 ₁₅	1 ₁₁
	10	0 ₂	0 ₆	1 ₁₄	0 ₁₀

$$Z_1 = X_1 (q_3 q_2 \neg q_0 + q_3 q_1 \neg q_0) + X_2 (q_3 q_2 + q_3 q_1 q_0)$$

X1

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	1 ₄	0 ₁₂	0 ₈
	01	0 ₁	1 ₅	0 ₁₃	0 ₉
	11	0 ₃	0 ₇	x ₁₅	0 ₁₁
	10	0 ₂	0 ₆	0 ₁₄	0 ₁₀

X2

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	1 ₄	0 ₁₂	0 ₈
	01	0 ₁	1 ₅	0 ₁₃	0 ₉
	11	1 ₃	1 ₇	x ₁₅	0 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$Z_0 = X1(nq_3q_2q_1) + X2 (nq_3q_2 + nq_3q_1q_0)$$

Una vez obtenidas las ecuaciones de excitación y de salida, se puede dibujar el diagrama lógico del circuito.

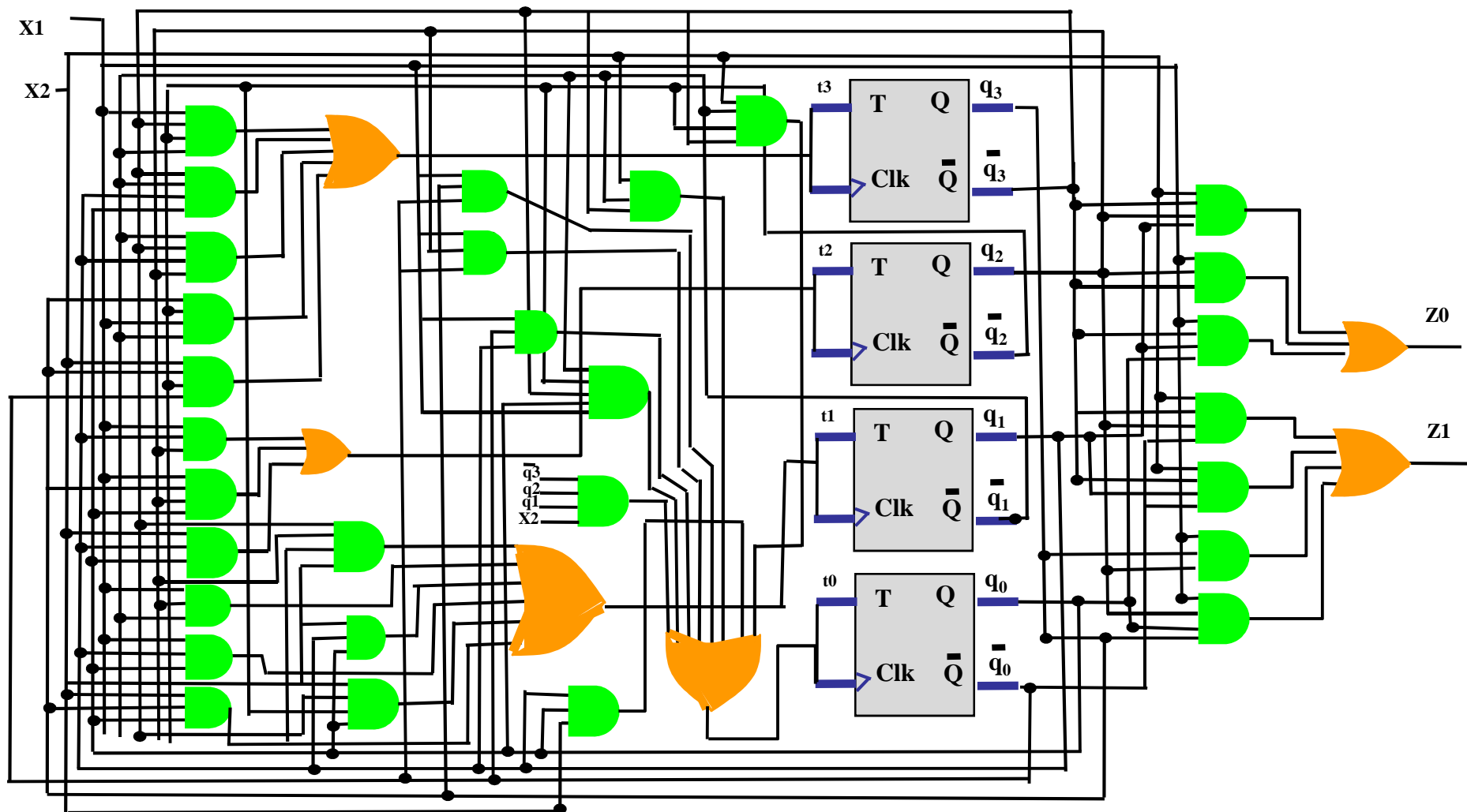


Diagrama de simulación

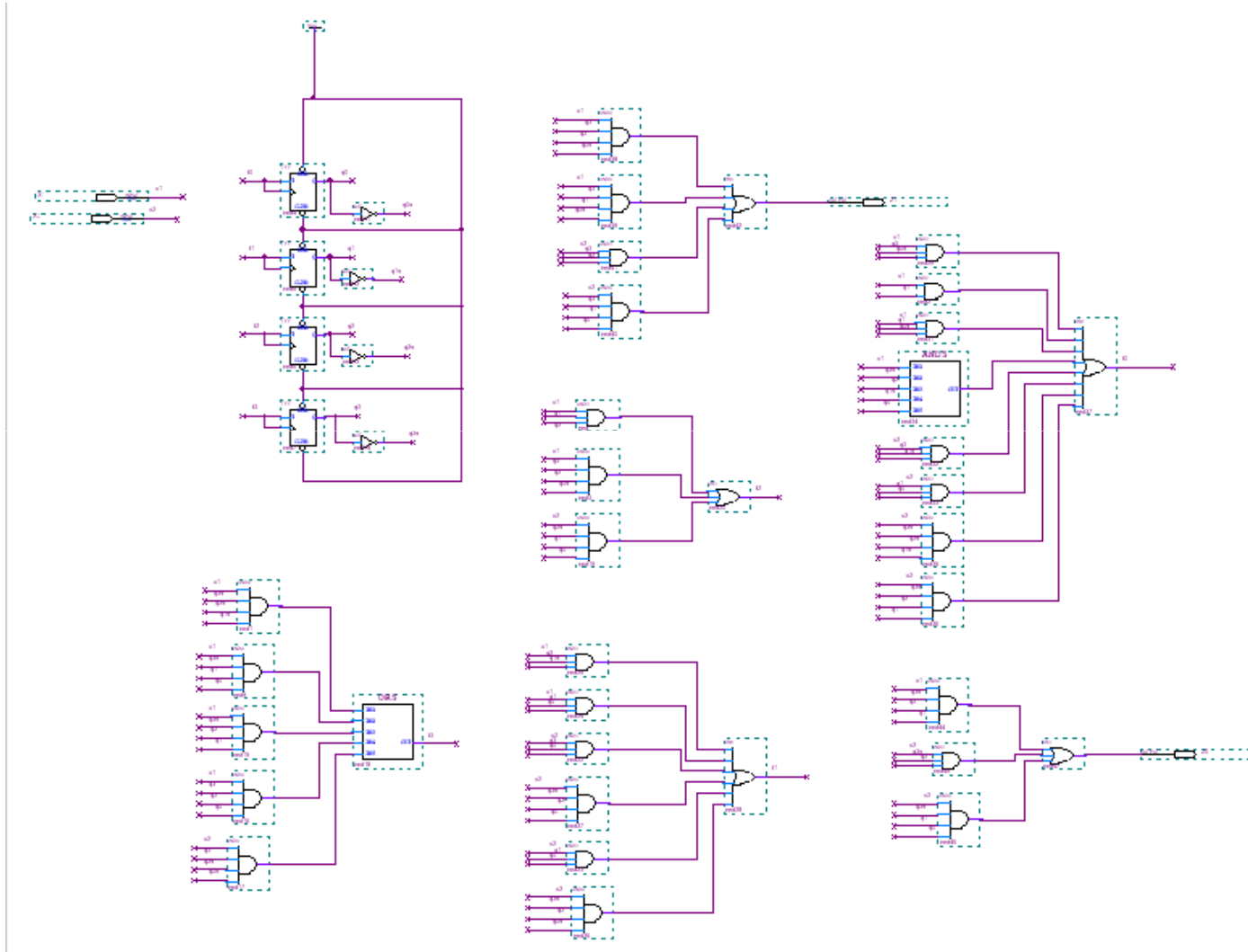


Diagrama de tiempo

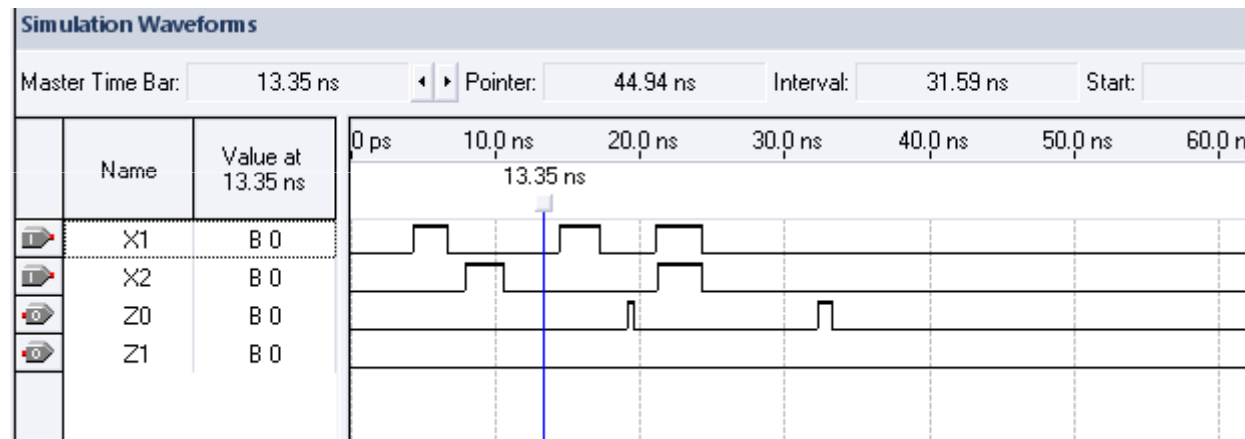


Tabla de estados para el FF JK

$q_3 q_2 q_1 q_0$	$J_3 K_3 J_2 K_2$	$J_1 K_1 J_0 K_0$ / $Z_1 Z_0$	$J_3 K_3 J_2 K_2$	$J_1 K_1 J_0 K_0$ / $Z_1 Z_0$
0 0 0 0	1 X 0 X	0 X 0 X 0 0	0 X 0 X	0 X 1 X 0 0
0 0 0 1	1 X 0 X	X 1 X 1 0 0	0 X 0 X	1 X X 1 0 0
0 0 1 0	0 X 0 X	X 0 1 X 0 0	0 X 0 X	X 0 0 X 0 0
0 0 1 1	1 X 0 X	X 1 X 0 0 0	0 X 1 X	X 1 X 1 0 1
0 1 0 0	0 X X 0	1 X 1 X 0 1	0 X X 0	1 X 0 X 0 1
0 1 0 1	0 X X 0	1 X X 0 0 1	0 X X 0	0 X X 0 0 1
0 1 1 0	1 X X 1	X 0 1 X 00*	0 X X 0	X 1 1 X 0 1
0 1 1 1	1 X X 1	X 1 X 0 0 0	0 X X 0	X 1 X 1 0 1
1 0 0 0	X 0 0 X	0 X 1 X 0 0	X 1 0 X	0 X 1 X 0 0
1 0 0 1	X 0 0 X	0 X X 0 0 0	X 0 0 X	1 X X 1 0 0
1 0 1 0	X 0 0 X	X 0 1 X 1 0	X 1 0 X	X 0 0 X 0 0
1 0 1 1	X 0 0 X	X 1 X 0 0 0	X 0 1 X	X 1 X 1 1 0
1 1 0 0	X 0 X 1	1 X 1 X 1 0	X 0 X 0	0 X 1 X 1 0
1 1 0 1	X 1 X 0	1 X X 0 00*	X 0 X 0	1 X X 1 1 0
1 1 1 0	X 0 X 1	X 0 1 X 1 0	X 0 X 0	X 0 0 X 1 0
1 1 1 1	X X X X	X X X X XX	X X X X	x x x x x x

Mapas de K

X1

$q_3 \ q_2$

	00	01	11	10
00	1 ₀	0 ₄	X ₁₂	X ₈
01	1 ₁	0 ₅	X ₁₃	X ₉
11	1 ₃	1 ₇	X ₁₅	X ₁₁
10	0 ₂	1 ₆	X ₁₄	X ₁₀

X2

$q_3 \ q_2$

	00	01	11	10
00	0 ₀	0 ₄	X ₁₂	X ₈
01	0 ₁	0 ₅	X ₁₃	X ₉
11	0 ₃	0 ₇	X ₁₅	X ₁₁
10	0 ₂	0 ₆	X ₁₄	X ₁₀

$q_1 \ q_0$

$$J_3 = X1 (nq_2nq_1 + q_0q_1 + q_2q_1)$$

X1

$q_3 \ q_2$

	00	01	11	10
00	X ₀	X ₄	0 ₁₂	0 ₈
01	X ₁	X ₅	1 ₁₃	0 ₉
11	X ₃	X ₇	X ₁₅	0 ₁₁
10	X ₂	X ₆	0 ₁₄	0 ₁₀

X2

$q_3 \ q_2$

	00	01	11	10
00	X ₀	X ₄	0 ₁₂	1 ₈
01	X ₁	X ₅	0 ₁₃	0 ₉
11	X ₃	X ₇	X ₁₅	0 ₁₁
10	X ₂	X ₆	0 ₁₄	1 ₁₀

$q_1 \ q_0$

$$k_3 = X1 (q_2 q_0) + X2 (nq_2 nq_0)$$

X1

q₃ q₂

	00	01	11	10
00	0 ₀	X ₄	X ₁₂	0 ₈
01	0 ₁	X ₅	X ₁₃	0 ₉
11	0 ₃	X ₇	X ₁₅	0 ₁₁
10	0 ₂	X ₆	X ₁₄	0 ₁₀

X2

q₃ q₂

q₁ q₀

	00	01	11	10
00	0 ₀	X ₄	X ₁₂	0 ₈
01	0 ₁	X ₅	X ₁₃	0 ₉
11	1 ₃	X ₇	X ₁₅	1 ₁₁
10	X ₂	X ₆	X ₁₄	X ₁₀

$$J_2 = X2 (q_1 q_0)$$

X1

q₃ q₂

	00	01	11	10
00	X ₀	0 ₄	1 ₁₂	X ₈
01	X ₁	0 ₅	0 ₁₃	X ₉
11	X ₃	x ₇	X ₁₅	X ₁₁
10	X ₂	1 ₆	1 ₁₄	X ₁₀

X2

q₃ q₂

	00	01	11	10
00	X ₀	0 ₄	0 ₁₂	X ₈
01	X ₁	0 ₅	0 ₁₃	X ₉
11	X ₃	0 ₇	X ₁₅	X ₁₁
10	X ₂	0 ₆	0 ₁₄	X ₁₀

q₁ q₀

$$K_2 = X1 (q_1 + q_3 q_2 \neg q_0)$$

X1

$q_3 \ q_2$

	00	01	11	10
00	0 ₀	1 ₄	1 ₁₂	0 ₈
01	0 ₁	1 ₅	1 ₁₃	0 ₉
11	X ₃	X ₇	X ₁₅	X ₁₁
10	X ₂	X ₆	X ₁₄	X ₁₀

X2

$q_3 \ q_2$

	00	01	11	10
00	0 ₀	1 ₄	0 ₁₂	0 ₈
01	1 ₁	0 ₅	1 ₁₃	1 ₉
11	X ₃	X ₇	X ₁₅	X ₁₁
10	X ₂	X ₆	X ₁₄	X ₁₀

$q_1 \ q_0$

$$J_1 = X1 (q_2) + X2 (nq_3q_2nq_0 + q_0q_3 + nq_2nq_1q_0)$$

X1

q₃ q₂

	00	01	11	10
00	X ₀	X ₄	X ₁₂	X ₈
01	X ₁	X ₅	X ₁₃	X ₉
11	1 ₃	1 ₇	X ₁₅	1 ₁₁
10	0 ₂	0 ₆	0 ₁₄	0 ₁₀

X2

q₃ q₂

	00	01	11	10
00	X ₀	X ₄	X ₁₂	X ₈
01	X ₁	X ₅	X ₁₃	X ₉
11	1 ₃	1 ₇	X ₁₅	1 ₁₁
10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

q₁ q₀

$$K_1 = X1 (q_0) + X2 (q_0 + nq_3q_2)$$

X1

$q_3 \ q_2$

	00	01	11	10
00	0 ₀	1 ₄	X ₁₂	1 ₈
01	X ₁	X ₅	0 ₁₃	X ₉
11	X ₃	X ₇	X ₁₅	X ₁₁
10	1 ₂	1 ₆	1 ₁₄	1 ₁₀

X2

$q_3 \ q_2$

	00	01	11	10
00	1 ₀	0 ₄	1 ₁₂	1 ₈
01	X ₁	X ₅	X ₁₃	X ₉
11	X ₃	X ₇	X ₁₅	X ₁₁
10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$q_1 \ q_0$

$$J_0 = X1 (q_1 nq_0 + nq_3 q_2 + q_3 nq_2) + X2 (nq_2 nq_1 + q_3 + nq_1 + nq_3 q_2 q_1)$$

X1

$q_3 \ q_2$

	00	01	11	10
00	X ₀	X ₄	0 ₁₂	X ₈
01	1 ₁	0 ₅	X ₁₃	0 ₉
11	0 ₃	0 ₇	X ₁₅	0 ₁₁
10	X ₂	X ₆	X ₁₄	X ₁₀

X2

$q_3 \ q_2$

	00	01	11	10
00	X ₀	X ₄	X ₁₂	X ₈
01	1 ₁	0 ₅	1 ₁₃	1 ₉
11	1 ₃	1 ₇	X ₁₅	1 ₁₁
10	X ₂	X ₆	X ₁₄	X ₁₀

$q_1 \ q_0$

$$K_0 = X1 (nq_3 nq_2 nq_1) + X2 (q_1 + q_3 nq_1 + nq_2 q_0)$$

X1

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	0 ₁₃	0 ₉
	11	0 ₃	0 ₇	0 ₁₅	0 ₁₁
	10	0 ₂	0 ₆	1 ₁₄	0 ₁₀

X2

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	1 ₁₃	0 ₉
	11	0 ₃	0 ₇	1 ₁₅	1 ₁₁
	10	0 ₂	0 ₆	1 ₁₄	0 ₁₀

$$Z_1 = X_1 (q_3 q_2 n q_0 + q_3 q_1 n q_0) + X_2 (q_3 q_2 + q_3 q_1 q_0)$$

X1

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	1 ₄	0 ₁₂	0 ₈
	01	0 ₁	1 ₅	0 ₁₃	0 ₉
	11	0 ₃	0 ₇	x ₁₅	0 ₁₁
	10	0 ₂	0 ₆	0 ₁₄	0 ₁₀

X2

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	1 ₄	0 ₁₂	0 ₈
	01	0 ₁	1 ₅	0 ₁₃	0 ₉
	11	1 ₃	1 ₇	x ₁₅	0 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$Z_0 = X1(nq_3q_2q_1) + X2 (nq_3q_2 + nq_3q_1q_0)$$

X1

X2

$q_3 \ q_2$

$q_1 \ q_0$

	00	01	11	10
00	0 ₀	1 ₄	1 ₁₂	1 ₈
01	1 ₁	0 ₅	0 ₁₃	0 ₉
11	0 ₃	0 ₇	X ₁₅	0 ₁₁
10	1 ₂	1 ₆	1 ₁₄	1 ₁₀

$q_3 \ q_2$

$q_1 \ q_0$

	00	01	11	10
00	0 ₀	1 ₄	1 ₁₂	1 ₈
01	1 ₁	0 ₅	1 ₁₃	1 ₉
11	1 ₃	1 ₇	X ₁₅	1 ₁₁
10	1 ₂	1 ₆	1 ₁₄	1 ₁₀

$$C_0 = X1(nq_3nq_2nq_1q_0 + q_3nq_0 + q_2nq_0nq_3q_1nq_0) + \\ X2(q_1 + q_3 + nq_2q_0 + q_2nq_0)$$

X1

$q_3 q_2$					
		00	01	11	10
$q_1 q_0$	00	0 ₀	1 ₄	1 ₁₂	0 ₈
	01	0 ₁	1 ₅	1 ₁₃	0 ₉
	11	1 ₃	1 ₇	X ₁₅	1 ₁₁
	10	0 ₂	0 ₆	0 ₁₄	0 ₁₀

X2

$q_3 q_2$					
		00	01	11	10
$q_1 q_0$	00	0 ₀	1 ₄	1 ₁₂	0 ₈
	01	0 ₁	1 ₅	1 ₁₃	0 ₉
	11	1 ₃	1 ₇	X ₁₅	1 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$C_1 = X1(q_2 n q_1 + q_1 q_0) + X2(q_2 n q_1 + q_1 q_0 + n q_3 q_2)$$

X1

		q₃ q₂			
		00	01	11	10
q₁ q₀	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	0 ₁₃	0 ₉
	11	0 ₃	1 ₇	X ₁₅	0 ₁₁
	10	0 ₂	1 ₆	1 ₁₄	0 ₁₀

X2

		q₃ q₂			
		00	01	11	10
q₁ q₀	00	0 ₀	0 ₄	0 ₁₂	0 ₈
	01	0 ₁	0 ₅	1 ₁₃	0 ₉
	11	1 ₃	1 ₇	X ₁₅	1 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$C_2 = X1(q_2q_1 + q_3q_2nq_0) + X2 (nq_3q_2q_1 + q_3q_2q_0 + q_1q_0)$$

X1

X2

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	1 ₀	0 ₄	0 ₁₂	0 ₈
	01	1 ₁	0 ₅	1 ₁₃	0 ₉
	11	1 ₃	1 ₇	x ₁₅	0 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	1 ₀	0 ₄	0 ₁₂	0 ₈
	01	1 ₁	0 ₅	1 ₁₃	0 ₉
	11	1 ₃	1 ₇	x ₁₅	0 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$C_3 = X1 (nq_3nq_2nq_1 + q_3q_2q_0 + nq_3q_2q_1 + nq_3q_1q_0) \\ + X2 (nq_3nq_2nq_1 + q_3q_2q_0 + nq_3q_2q_1 + nq_3q_1q_0)$$

Diagrama de simulación

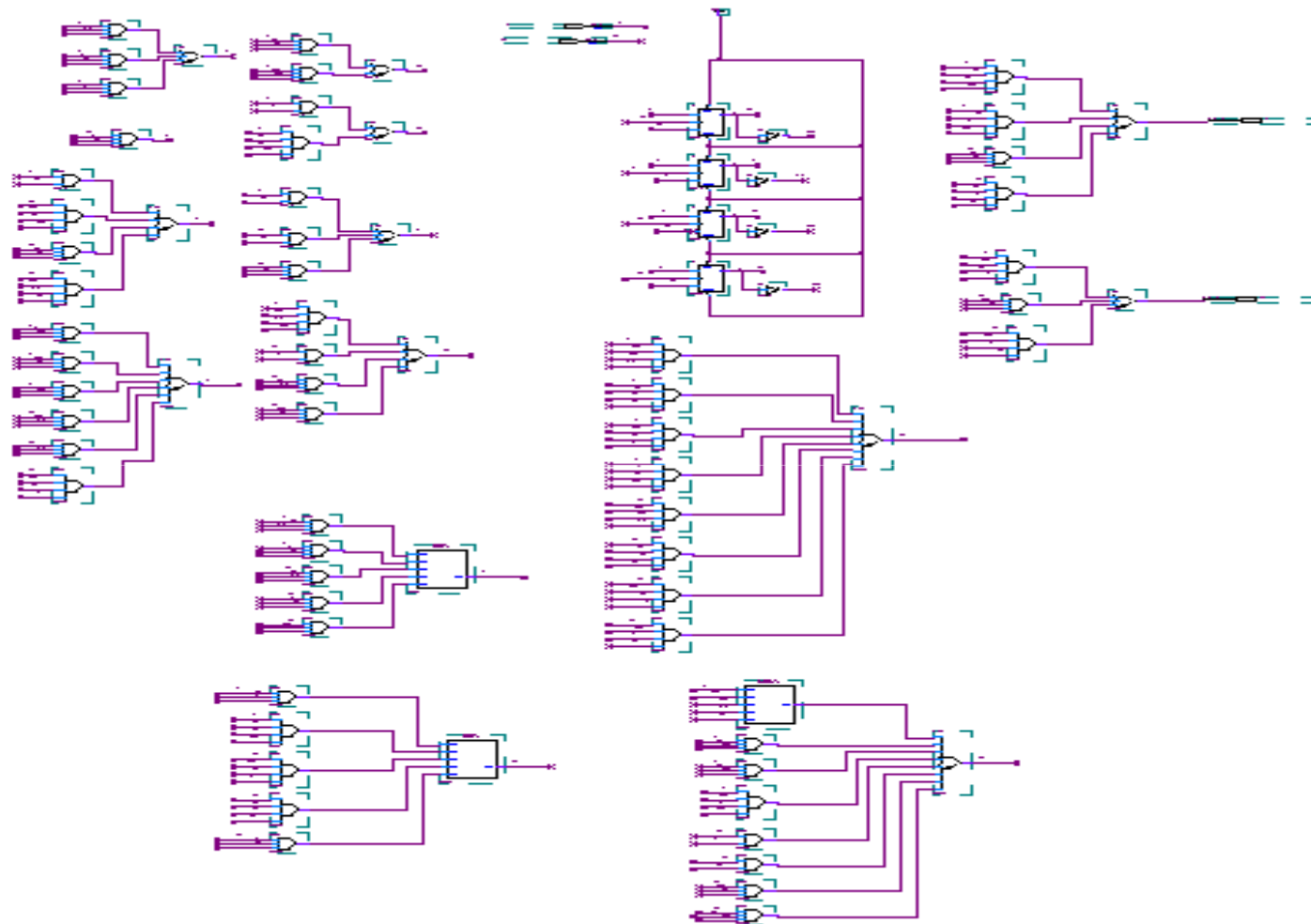


Diagrama de tiempo

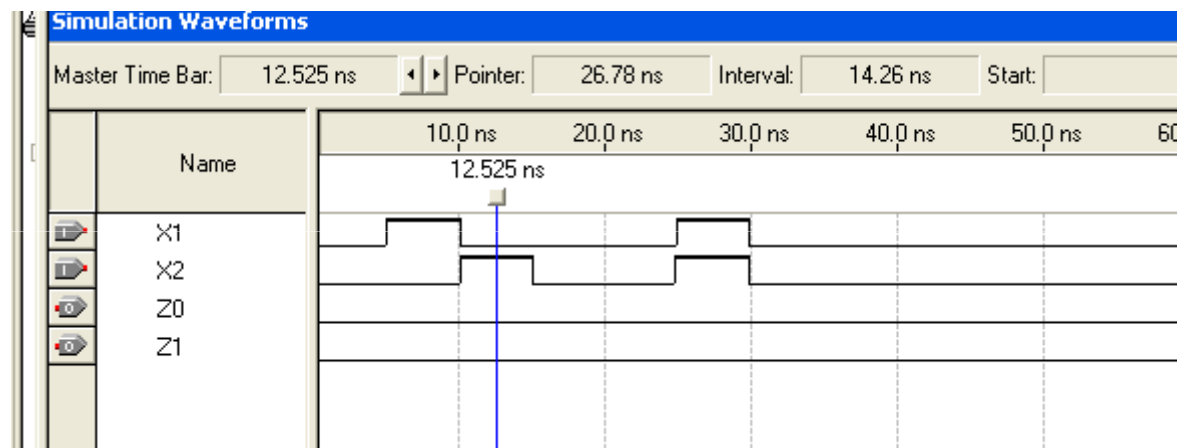


Tabla de Estados para el FF D

					X1					X2									
q ₃ q ₂ q ₁ q ₀	q ₃₊ q ₂₊ q ₁₊ q ₀₊ / Z ₁ Z ₀				q ₃₊ q ₂₊ q ₁₊ q ₀₊ / Z ₁ Z ₀					D ₃ D ₂ D ₁ D ₀					D ₃ D ₂ D ₁ D ₀				
0 0 0 0	1 0 0 0	0 0			0 0 0 1	0 0				1 x x x	1 x x x				1 x x x				
0 0 0 1	1 0 0 0	0 0			0 0 1 0	0 0				1 x x 0	1 x x 0				1 x x 0				
0 0 1 0	0 0 1 1	0 0			0 0 1 0	0 0				x x x 1	x x x 1				x x x 1				
0 0 1 1	1 0 0 1	0 0			0 1 0 0	0 1				1 x 0 x	1 1 0 0				1 1 0 0				
0 1 0 0	0 1 1 1	0 1			0 1 1 0	0 1				x x 1 1	x x 1 1				x x 1 1				
0 1 0 1	0 1 1 1	0 1			0 1 0 1	0 1				x x 1 x	x x 1 x				x x 1 x				
0 1 1 0	1 0 1 1	00*			0 1 0 1	0 1				1 0 x 1	1 0 0 1				1 0 0 1				
0 1 1 1	1 0 0 1	0 0			0 1 0 0	0 1				1 0 0 x	1 0 0 0				1 0 0 0				
1 0 0 0	1 0 0 1	0 0			0 0 0 1	0 0				x x x 1	x x x 1				x x x 1				
1 0 0 1	1 0 0 1	0 0			1 0 1 0	0 0				x x x x	x x x 0				x x x 0				
1 0 1 0	1 0 1 1	1 0			0 0 1 0	0 0				x x x 1	x x x 1				x x x 1				
1 0 1 1	1 0 0 1	0 0			1 1 0 0	1 0				x x 0 x	x 1 0 0				x 1 0 0				
1 1 0 0	1 0 1 1	1 0			1 1 0 1	1 0				x 0 1 1	x 0 1 1				x 0 1 1				
1 1 0 1	0 1 1 1	00*			1 1 1 0	1 0				0 x 1 x	0 x 1 0				0 x 1 0				
1 1 1 0	1 0 1 1	1 0			1 1 1 0	1 0				x 0 x 1	x 0 x 1				x 0 x 1				
1 1 1 1	x x x x	x x			x x x x	x x				x x x x	x x x x				x x x x				

Mapas de K

X1

q₃ q₂

q₁ q₀

	00	01	11	10
00	1 ₀	x ₄	x ₁₂	X ₈
01	1 ₁	x ₅	0 ₁₃	X ₉
11	1 ₃	1 ₇	X ₁₅	X ₁₁
10	x ₂	1 ₆	X ₁₄	X ₁₀

X2

q₃ q₂

q₁ q₀

	00	01	11	10
00	1 ₀	x ₄	X ₁₂	X ₈
01	1 ₁	X ₅	0 ₁₃	X ₉
11	1 ₃	1 ₇	X ₁₅	X ₁₁
10	x ₂	1 ₆	x ₁₄	x ₁₀

$$d_3 = X1 (nq_3) + X2 (nq_1)$$

X1

		q ₃ q ₂			
		00	01	11	10
q ₁ q ₀	00	X ₀	x ₄	0 ₁₂	X ₈
	01	X ₁	X ₅	x ₁₃	X ₉
	11	X ₃	0 ₇	X ₁₅	X ₁₁
	10	x ₂	0 ₆	0 ₁₄	x ₁₀

X2

		q ₃ q ₂			
		00	01	11	10
q ₁ q ₀	00	X ₀	X ₄	0 ₁₂	X ₈
	01	X ₁	X ₅	X ₁₃	1 ₉
	11	1 ₃	0 ₇	x ₁₅	X ₁₁
	10	x ₂	0 ₆	0 ₁₄	x ₁₀

$$d_2 = X2 (q_2)$$

X1

q₃ q₂

q₁ q₀

	00	01	11	10
00	X ₀	1 ₄	1 ₁₂	X ₈
01	X ₁	1 ₅	1 ₁₃	X ₉
11	0 ₃	0 ₇	X ₁₅	0 ₁₁
10	X ₂	1 ₆	x ₁₄	X ₁₀

X2

q₃ q₂

q₁ q₀

	00	01	11	10
00	X ₀	1 ₄	1 ₁₂	X ₈
01	x ₁	1 ₅	1 ₁₃	X ₉
11	0 ₃	0 ₇	X ₁₅	0 ₁₁
10	X ₂	0 ₆	x ₁₄	x ₁₀

$$d_1 = X1(nq_1) + X2(nq_1)$$

X1

q₃ q₂

	00	01	11	10
00	x ₀	1 ₄	1 ₁₂	1 ₈
01	0 ₁	x ₅	x ₁₃	X ₉
11	x ₃	x ₇	X ₁₅	X ₁₁
10	1 ₂	1 ₆	1 ₁₄	1 ₁₀

X2

q₃ q₂

	00	01	11	10
00	x ₀	1 ₄	1 ₁₂	1 ₈
01	0 ₁	X ₅	0 ₁₃	0 ₉
11	0 ₃	0 ₇	X ₁₅	0 ₁₁
10	1 ₂	1 ₆	1 ₁₄	1 ₁₀

q₁ q₀

$$d_0 = X1 (nq_0) + X2 (nq_0)$$

X1

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	0 ₁₃	0 ₉
	11	0 ₃	0 ₇	0 ₁₅	0 ₁₁
	10	0 ₂	0 ₆	1 ₁₄	0 ₁₀

X2

$q_3 \ q_2$					
		00	01	11	10
$q_1 \ q_0$	00	0 ₀	0 ₄	1 ₁₂	0 ₈
	01	0 ₁	0 ₅	1 ₁₃	0 ₉
	11	0 ₃	0 ₇	1 ₁₅	1 ₁₁
	10	0 ₂	0 ₆	1 ₁₄	0 ₁₀

$$Z_1 = X_1 (q_3 q_2 n q_0 + q_3 q_1 n q_0) + X_2 (q_3 q_2 + q_3 q_1 q_0)$$

X1

$q_3 q_2$					
		00	01	11	10
$q_1 q_0$	00	0 ₀	1 ₄	0 ₁₂	0 ₈
	01	0 ₁	1 ₅	0 ₁₃	0 ₉
	11	0 ₃	0 ₇	x ₁₅	0 ₁₁
	10	0 ₂	0 ₆	0 ₁₄	0 ₁₀

X2

$q_3 q_2$					
		00	01	11	10
$q_1 q_0$	00	0 ₀	1 ₄	0 ₁₂	0 ₈
	01	0 ₁	1 ₅	0 ₁₃	0 ₉
	11	1 ₃	1 ₇	x ₁₅	0 ₁₁
	10	0 ₂	1 ₆	0 ₁₄	0 ₁₀

$$Z_0 = X1(nq_3q_2q_1) + X2(nq_3q_2 + nq_3q_1q_0)$$

