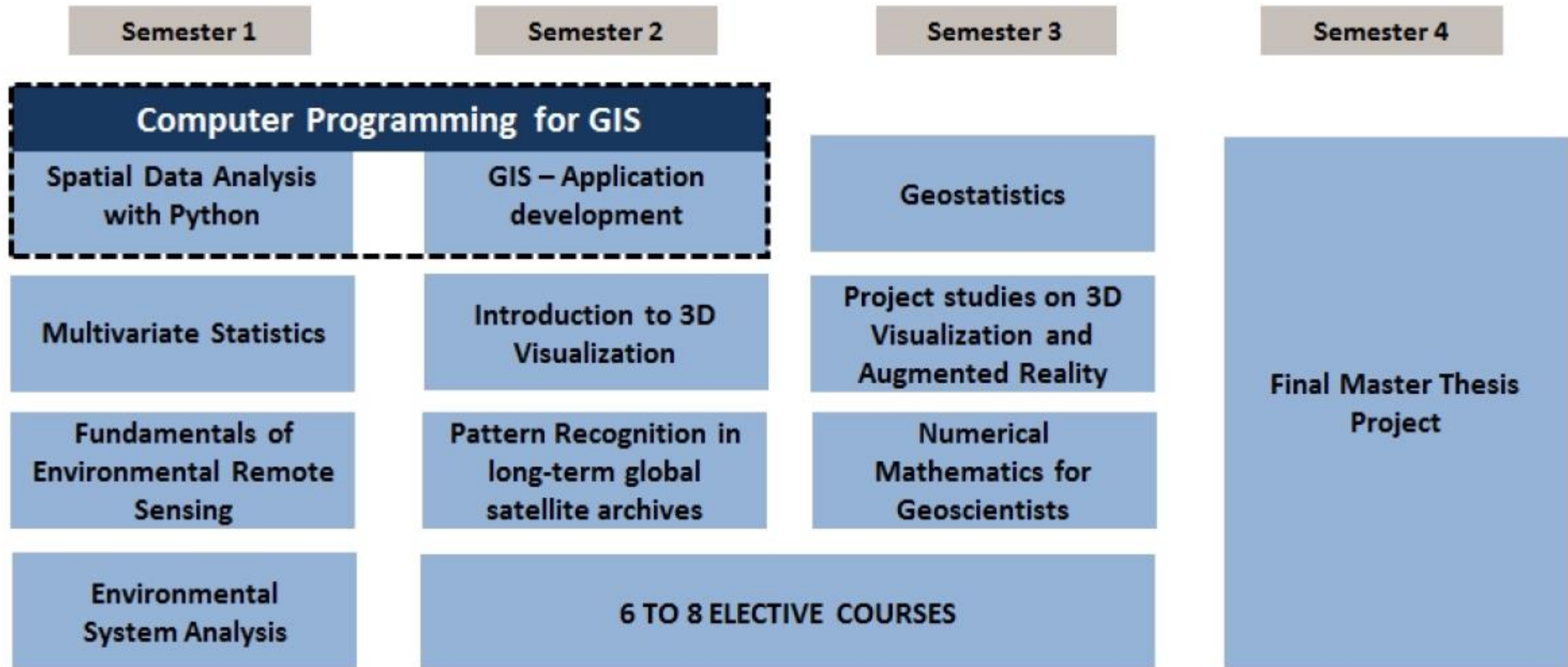


# Clustering spatiotemporal point data to visualize spatial patterns

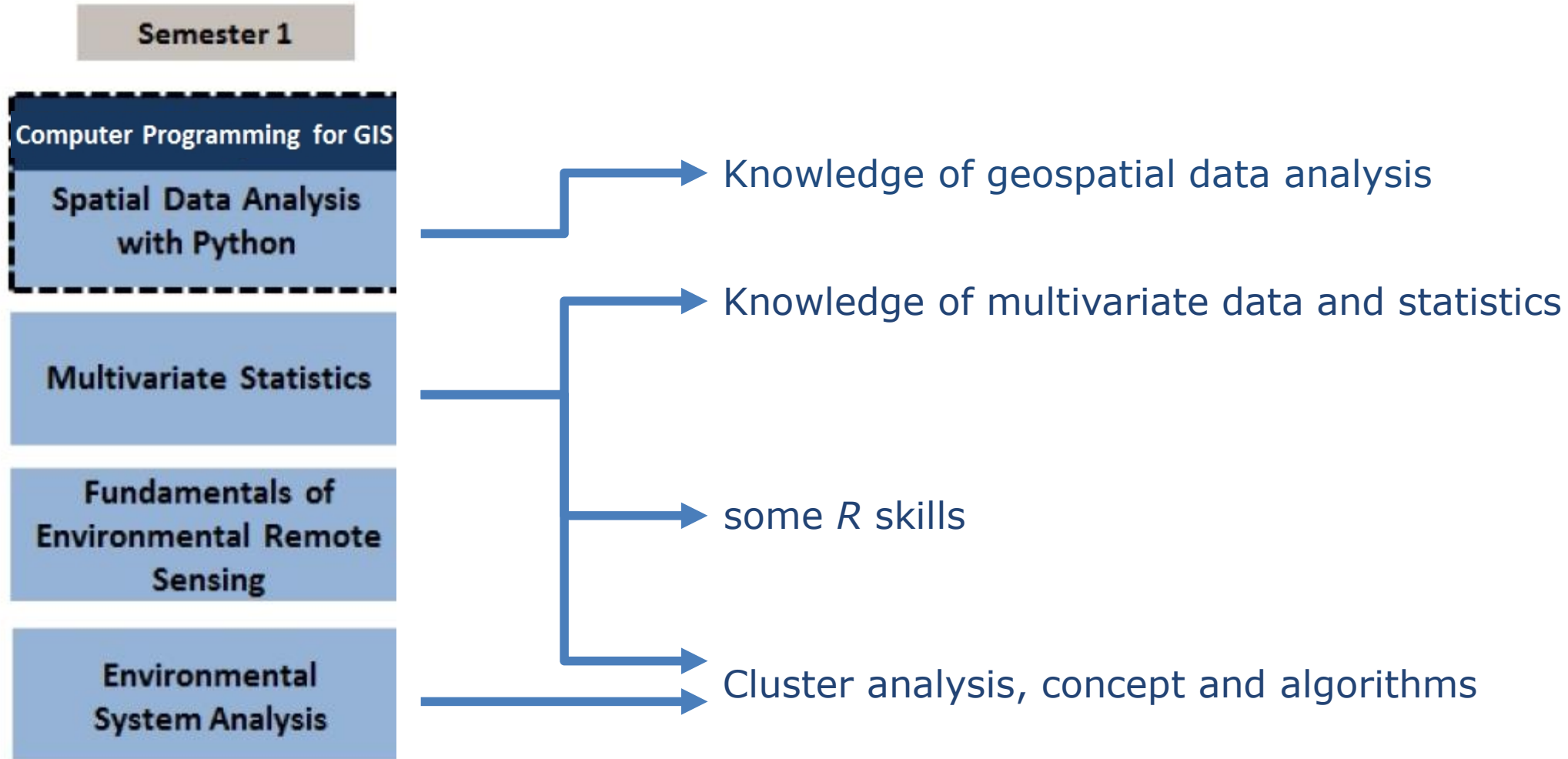


Dr. David Frantz

Geoinformatics – Spatial Data Science  
Demonstration lecture  
Trier / Zoom, 02.07.2020



# Requirements



# Learning Objective

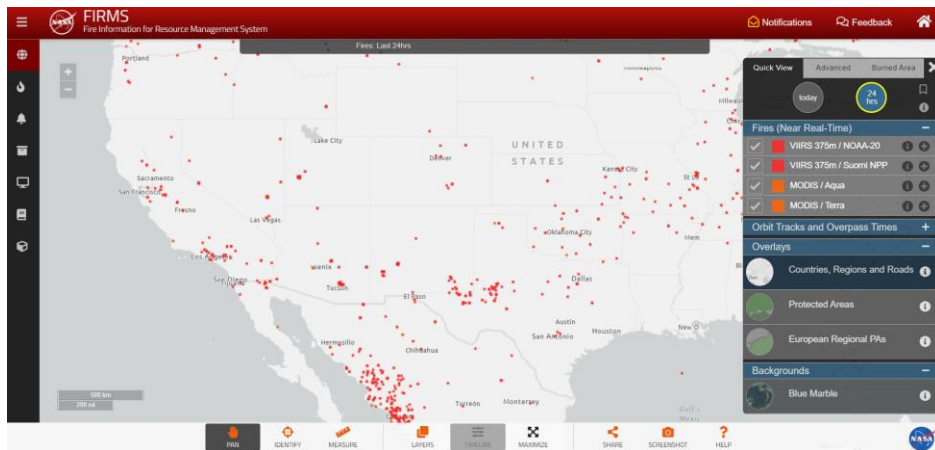
- Introduction to spatiotemporal data types
- Clustering algorithm
- Practical experience/demonstration to cluster real-life ST data with current relevancy

# Spatiotemporal data

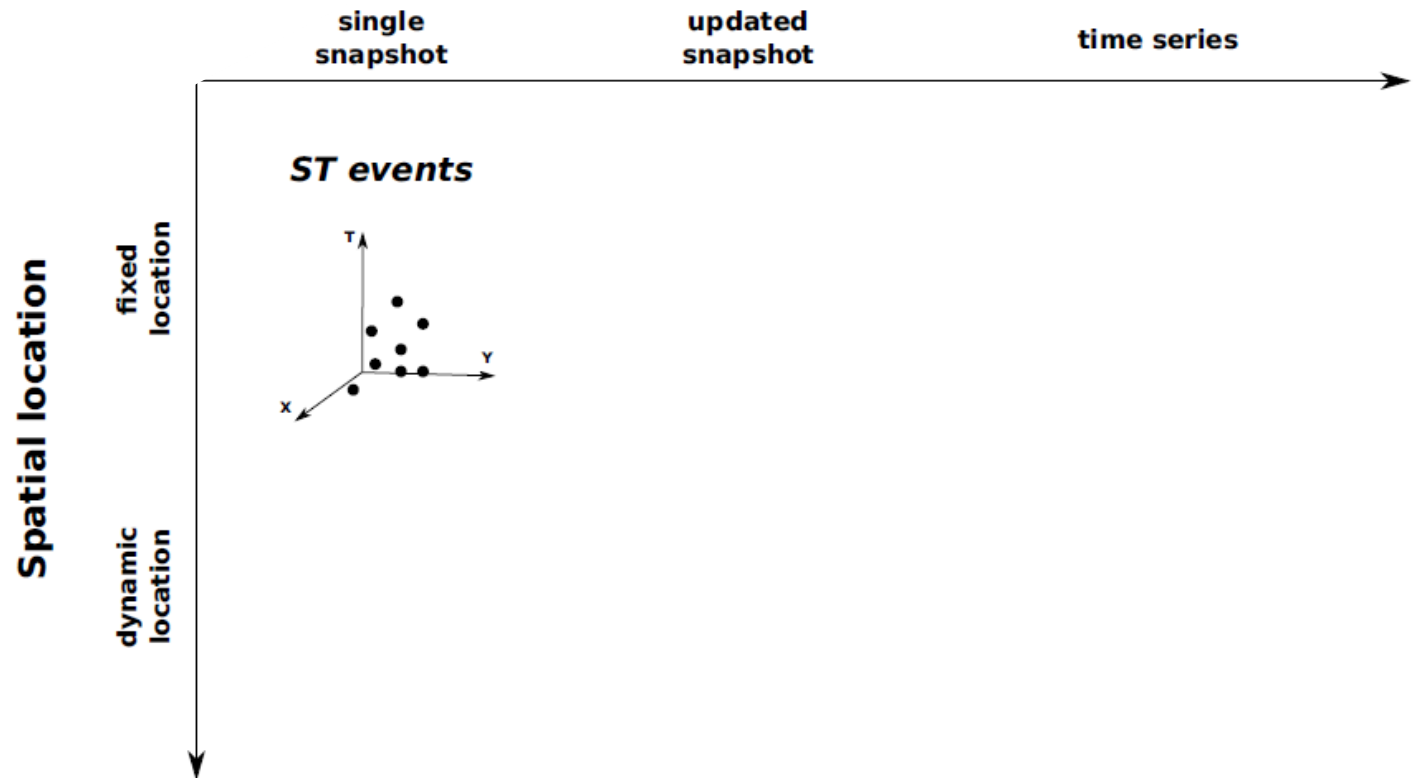
## 1) ST event

- Single measurement
- $\langle \text{longitude, latitude, timestamp} \rangle$

### Fire events



## Temporal extension



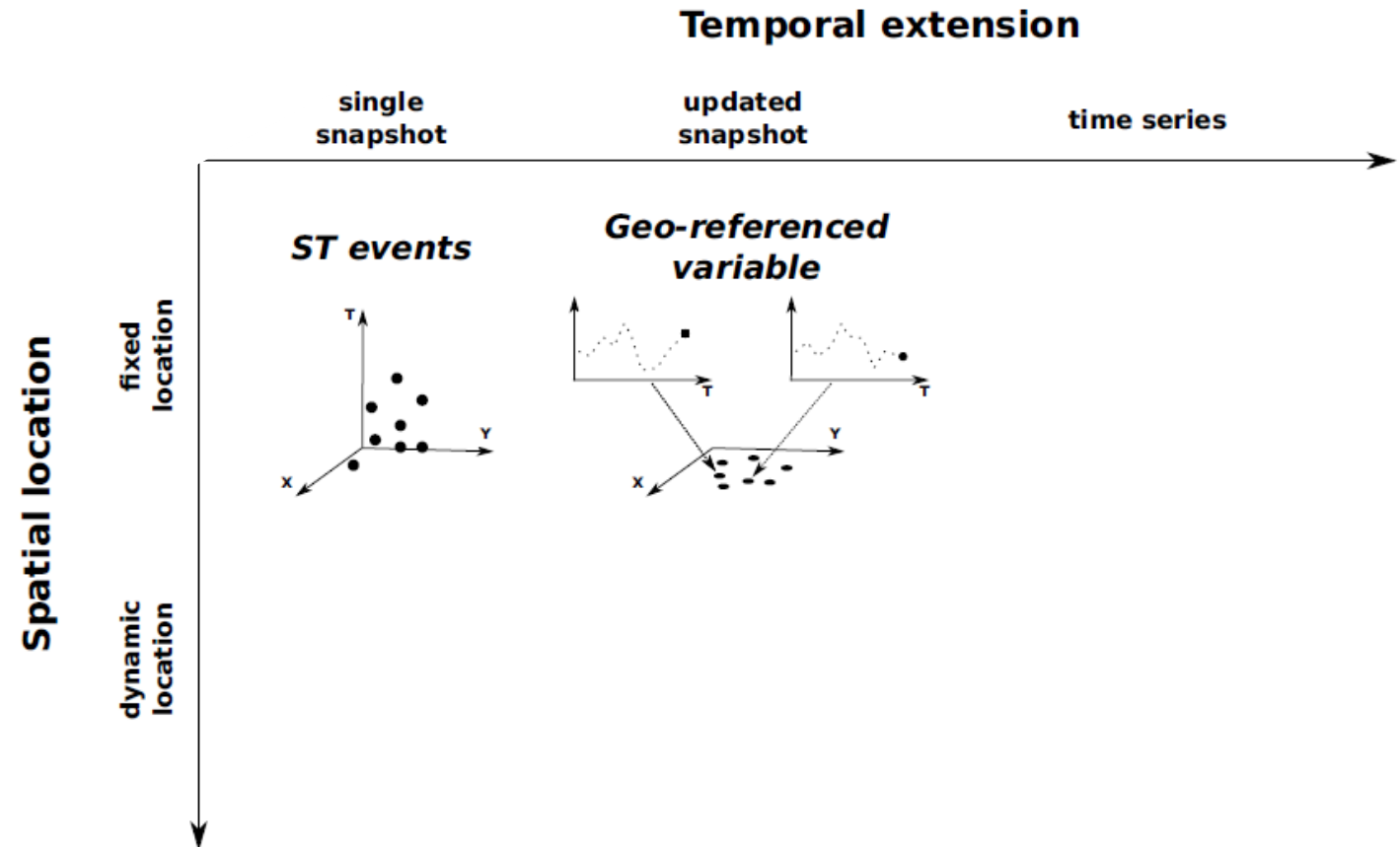
Kisilevich et al.: Spatio-temporal clustering. In: *Data mining and knowledge discovery handbook*. Springer, Boston, MA, 2009. S. 855-874.

# Spatiotemporal data

## 2) Geo-referenced variable

- Evolution in time, but only the most recent value
- <longitude, latitude, timestamp, non-spatial value>

Weather station with most recent temperature value



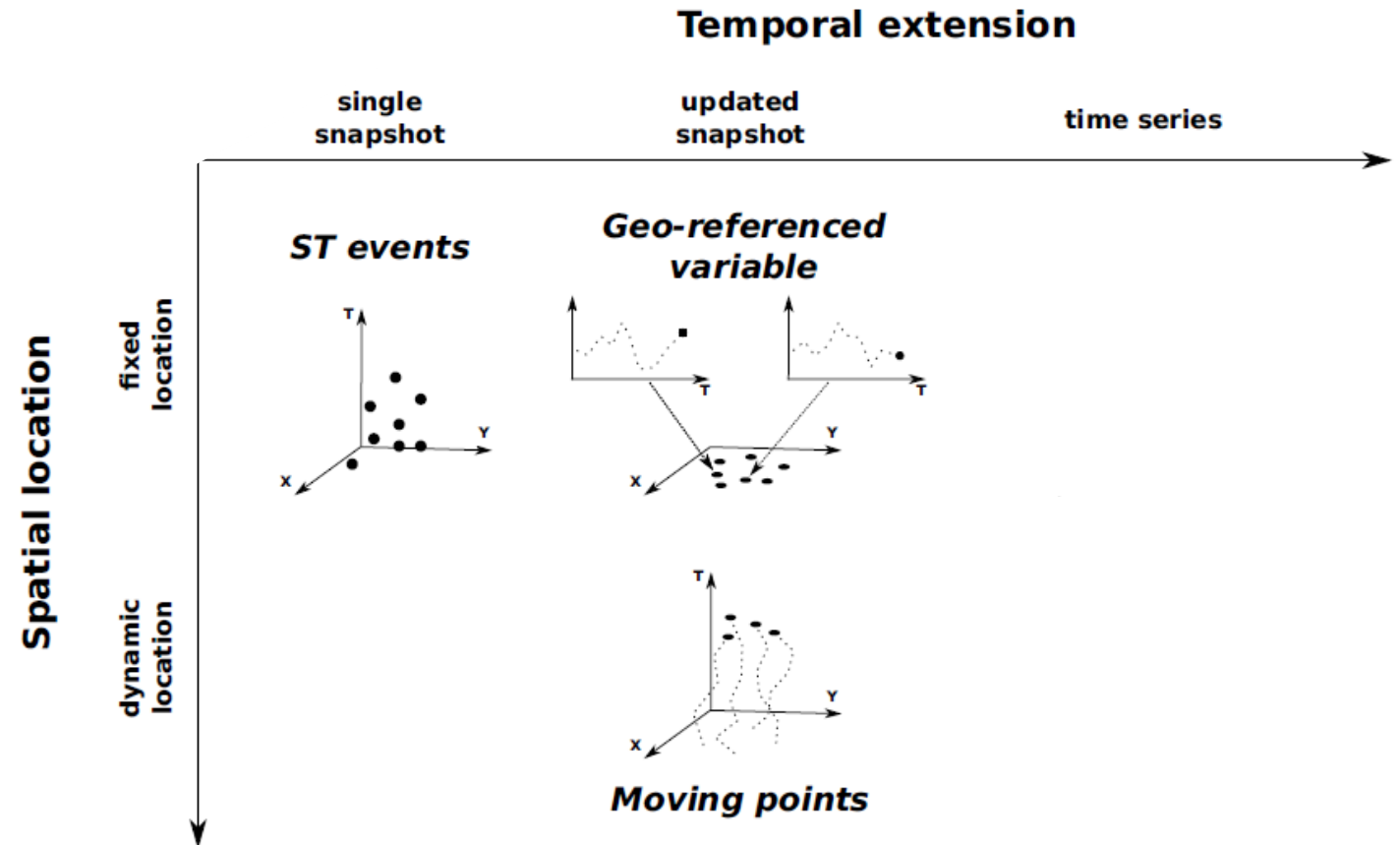
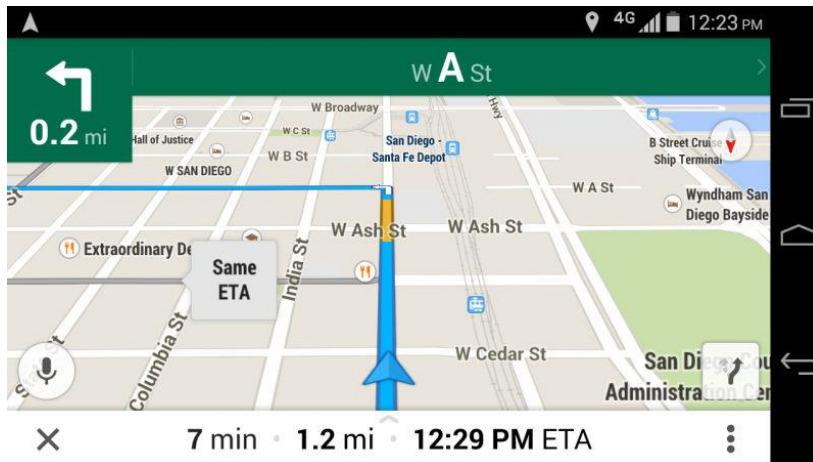
Kisilevich et al.: Spatio-temporal clustering. In: *Data mining and knowledge discovery handbook*. Springer, Boston, MA, 2009. S. 855-874.

# Spatiotemporal data

## 3) Moving points

- object moves, most recent position

navigation /  
real-time tracking of vehicles



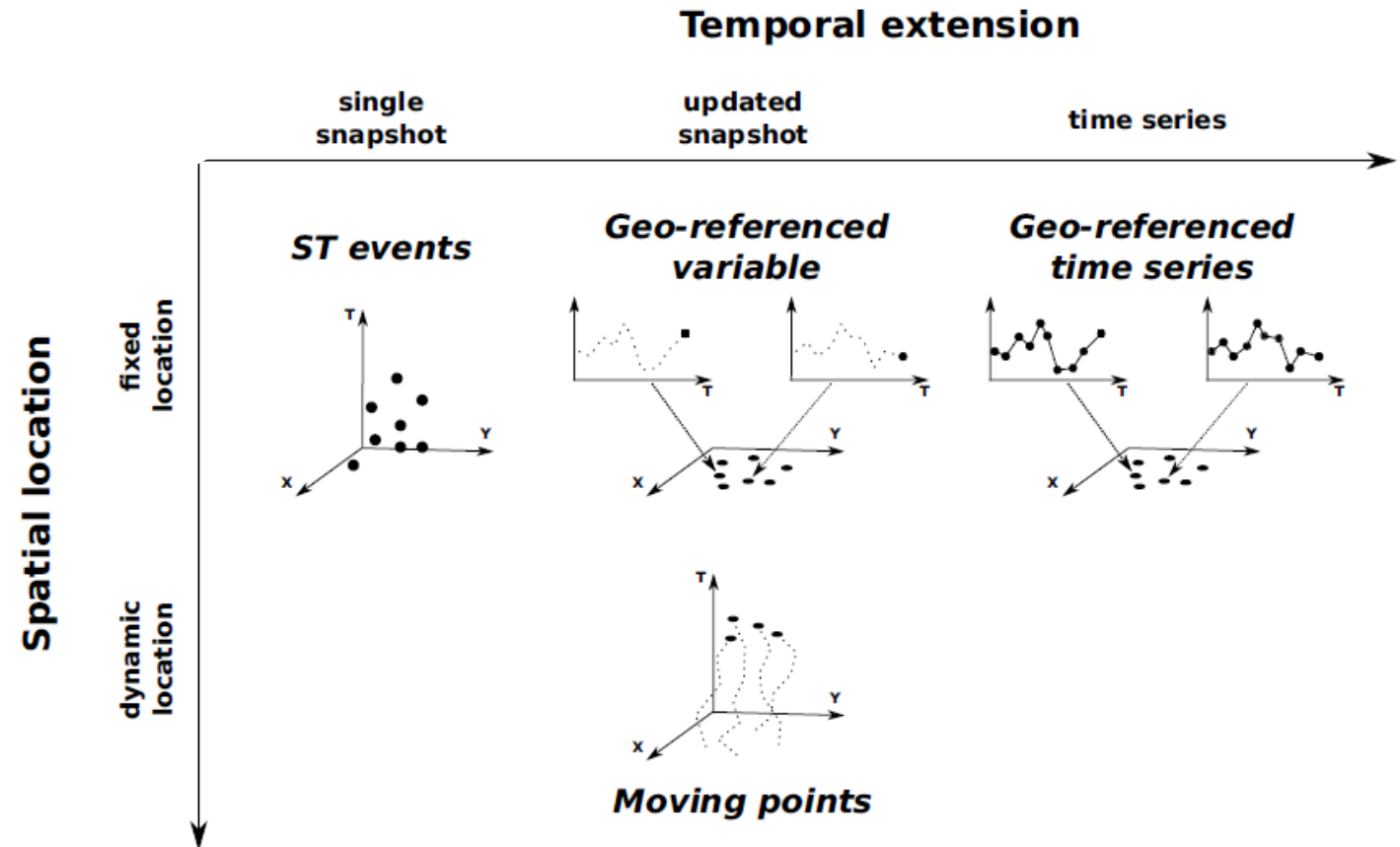
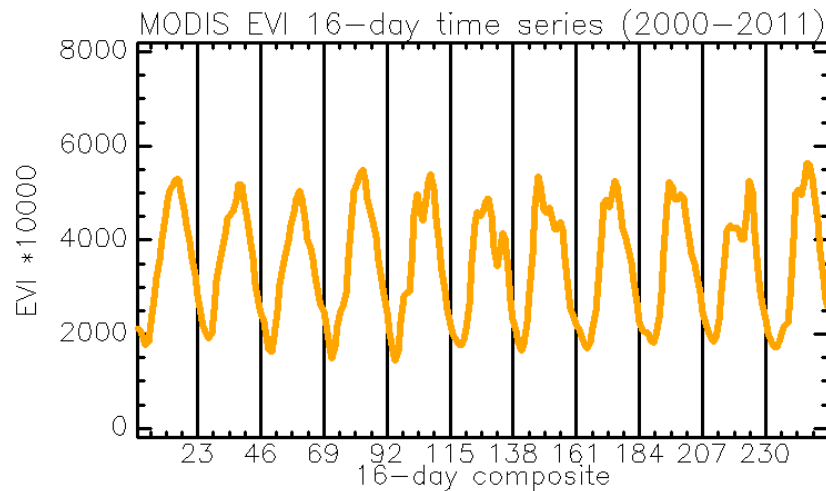
Kisilevich et al.: Spatio-temporal clustering. In: *Data mining and knowledge discovery handbook*. Springer, Boston, MA, 2009. S. 855-874.

# Spatiotemporal data

## 4) Geo-referenced time series

- Whole history is stored

### NDVI time series



Kisilevich et al.: Spatio-temporal clustering. In: *Data mining and knowledge discovery handbook*. Springer, Boston, MA, 2009. S. 855-874.

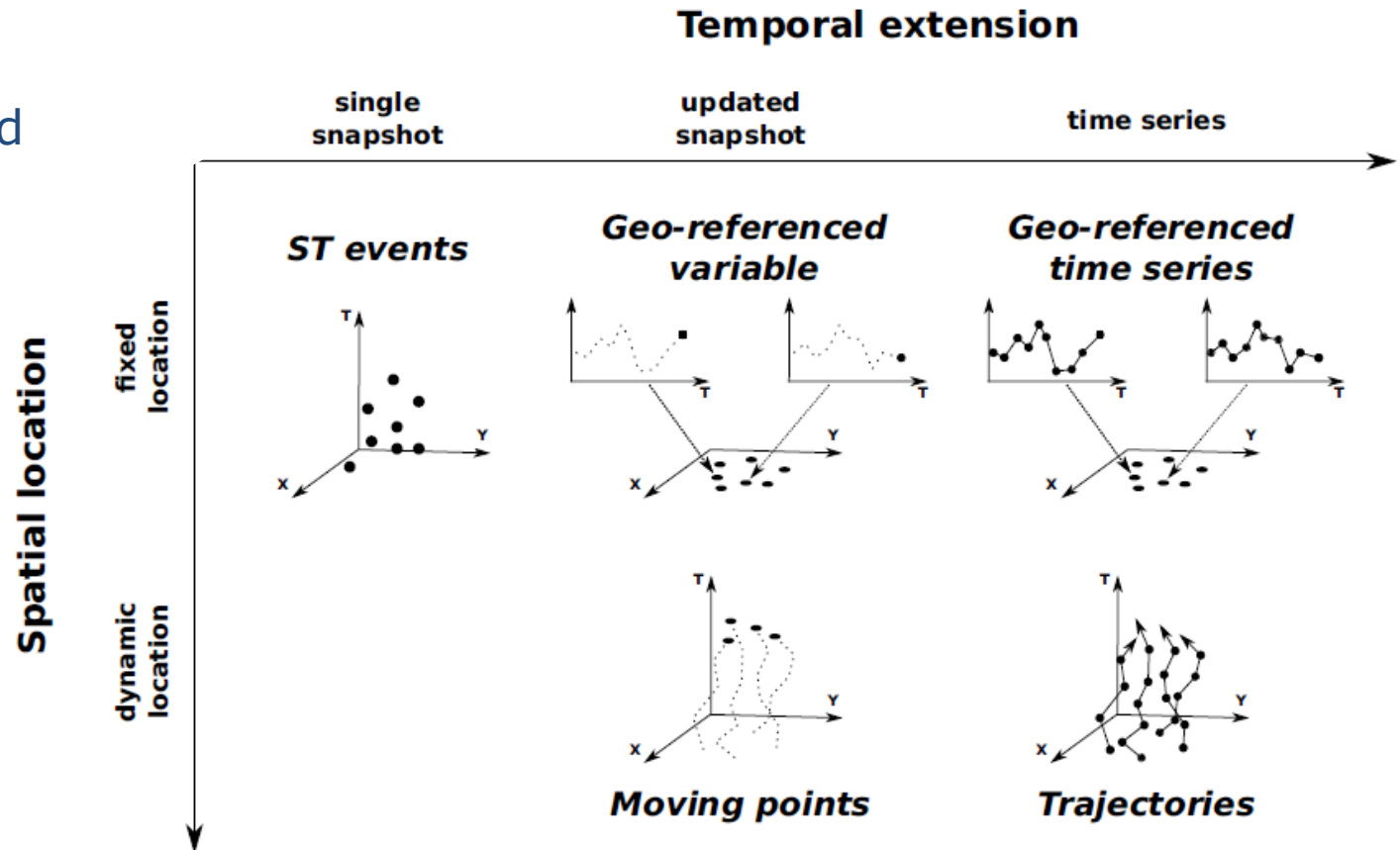
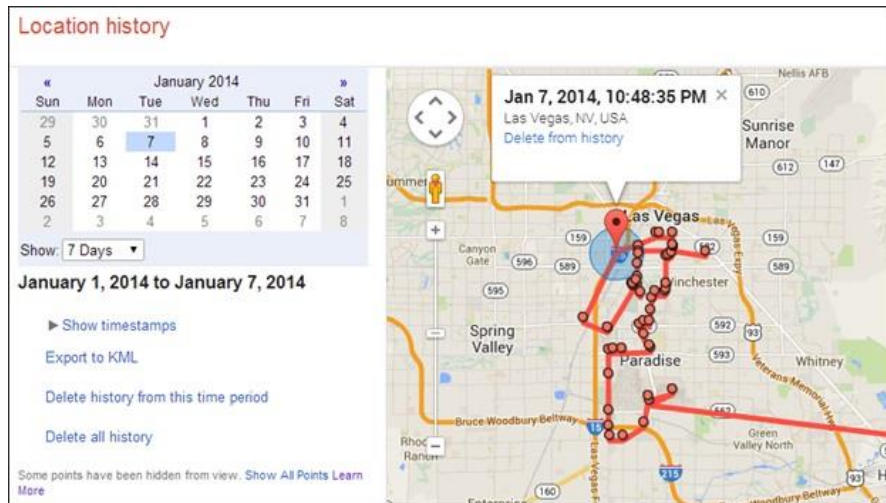


# Spatiotemporal data

## 5) Trajectories

- Object moves, whole history is stored

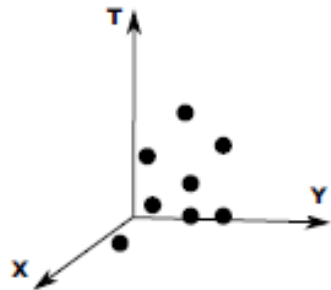
### Google Location History



Kisilevich et al.: Spatio-temporal clustering. In: *Data mining and knowledge discovery handbook*. Springer, Boston, MA, 2009. S. 855-874.

# Clustering ST event data

## ***ST events***



Three dimensions:  
<longitude, latitude, timestamp>

Static in space and time = snapshot

Problem: complex datasets

Solution: Spatiotemporal analyses methods to mine meaningful patterns for better understanding

Clustering = unsupervised method for discovering potential patterns

Finding clusters among events means to discover groups that lie close both in time and in space

# DBSCAN

## Density-Based Spatial Clustering of Applications with Noise

ESTER, Martin, et al. A density-based algorithm for discovering clusters in large spatial databases with noise. In: *Kdd*. 1996. S. 226-231.

Popular algorithm in data mining, simple application, very efficient

Main assumption

Within each cluster, there is a typical density of points, which is considerably higher than outside

Find clusters of arbitrary shape

Detect noise

Number of clusters not known *à priori*



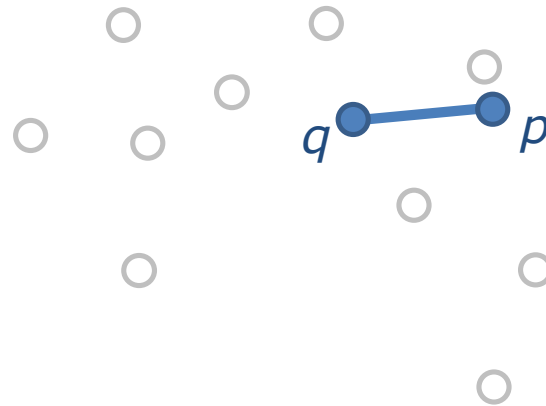
<https://www.kdnuggets.com/2020/04/dbscan-clustering-algorithm-machine-learning.html>

# DBSCAN concepts

## 1) Neighborhood

Determined by a distance function, e.g. Euclidean Distance

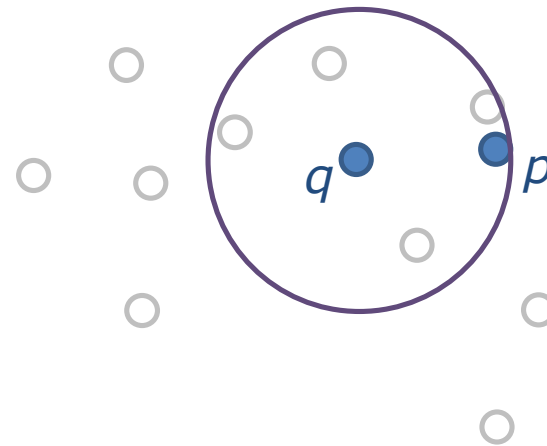
Distance between two points  $p$  and  $q$  in database  $D$ :  $dist(p, q) = \sqrt{(x_p - x_q)^2 + (y_p - y_q)^2}$



# DBSCAN concepts

## 2) **Eps-neighborhood** of a point $q$ :

$$N_{Eps}(q) = \{p \in D \mid \text{dist}(p, q) \leq Eps\}$$



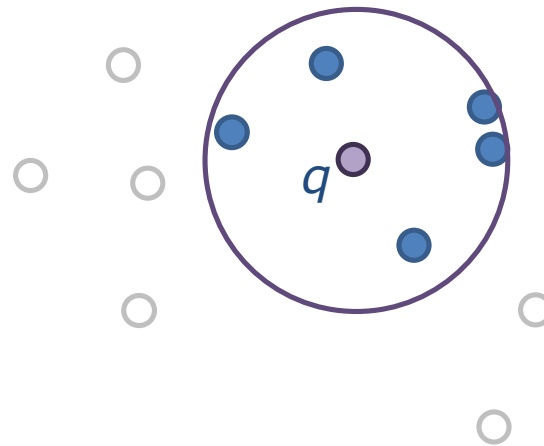
Input parameter 1:  
Distance threshold  $Eps$

# DBSCAN concepts

## 3) Core point

$$|N_{Eps}(q)| \geq MinPts$$

Core point is part of a cluster



Input parameter 2:  
 $MinPts = 3$

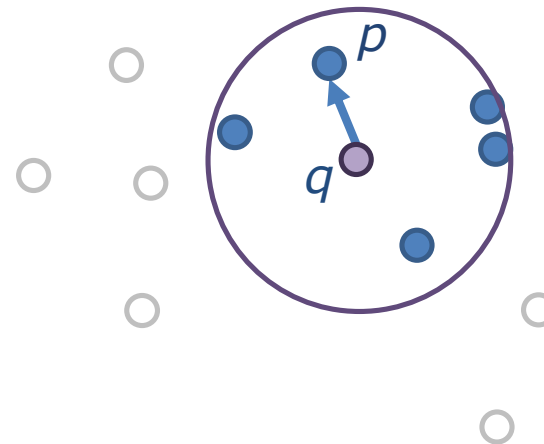
# DBSCAN concepts

## 4) Directly density-reachable

$p$  is directly density-reachable from  $q$  if  
 $p$  is within the Eps-neighborhood of  $q$ ,  
 and  $q$  is a core point

$p \in N_{Eps}(q)$  AND

$|N_{Eps}(q)| \geq MinPts$



$p$  directly density-reachable from  $q$

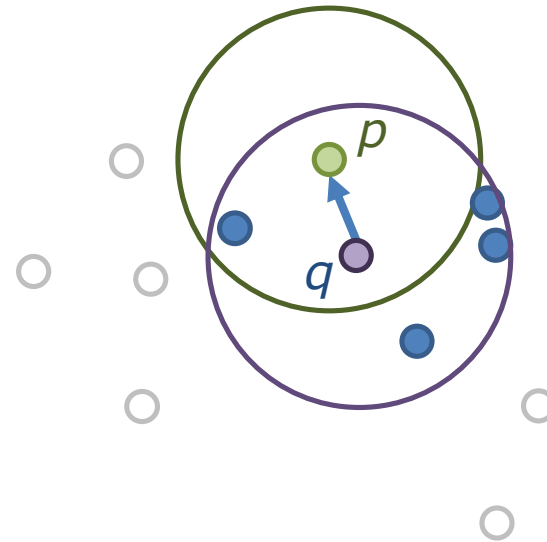
# DBSCAN concepts

## 4) Directly density-reachable

$p$  is directly density-reachable from  $q$  if  
 $p$  is within the Eps-neighborhood of  $q$ ,  
 and  $q$  is a core point

$$p \in N_{Eps}(q) \text{ AND}$$

$$|N_{Eps}(q)| \geq MinPts$$



$p$  directly density-reachable from  $q$

$q$  not directly density-reachable from  $p$

$p$  is not a core point ( $|N_{Eps}(p)| = 2$ )

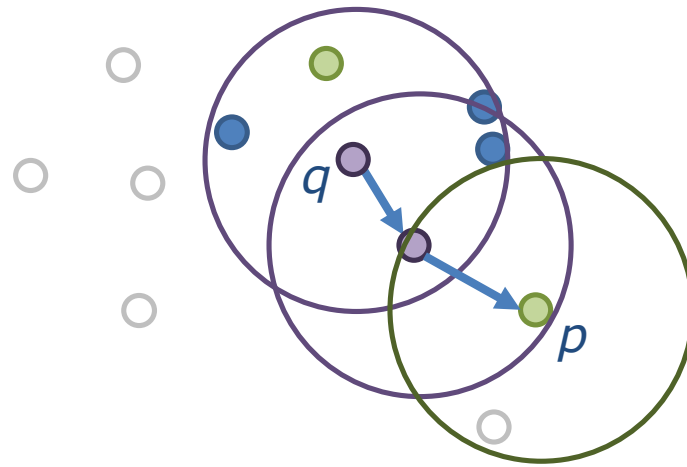
$\rightarrow p = \textbf{border point}$



# DBSCAN concepts

## 5) Density-reachable

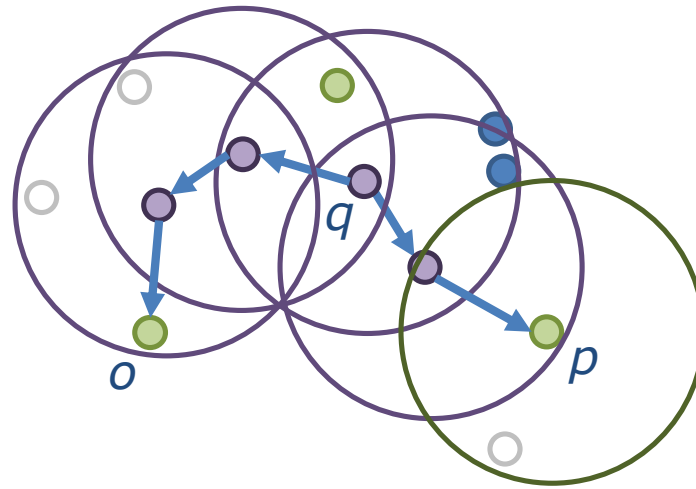
$p$  is density-reachable from  $q$  if there is a chain of points that are directly density-reachable



# DBSCAN concepts

## 6) Density-connected

$p$  is density connected to  $o$ , if both  $p$  and  $o$  are density-reachable from a point  $q$

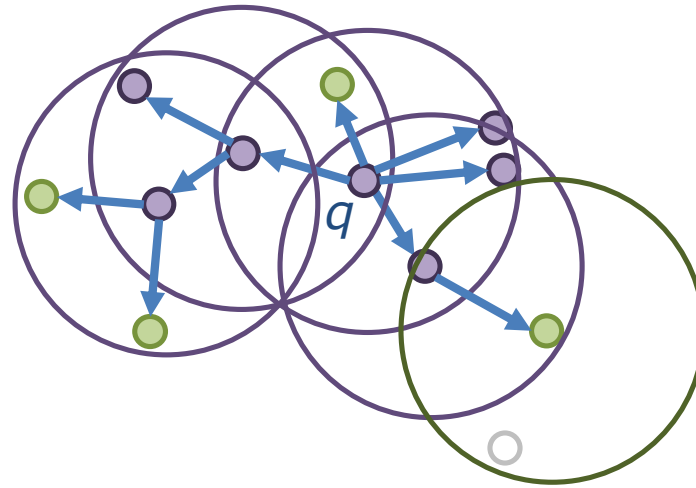


# DBSCAN concepts

**7) Density-based cluster** contains all points that are density-reachable from a seed point  $q$ :

$\forall p, q: \text{if } q \in C \text{ AND } p \text{ is density-reachable from } q$

$\forall p, q \in C: \text{if } p \text{ is density-connected to } q$



# DBSCAN concepts

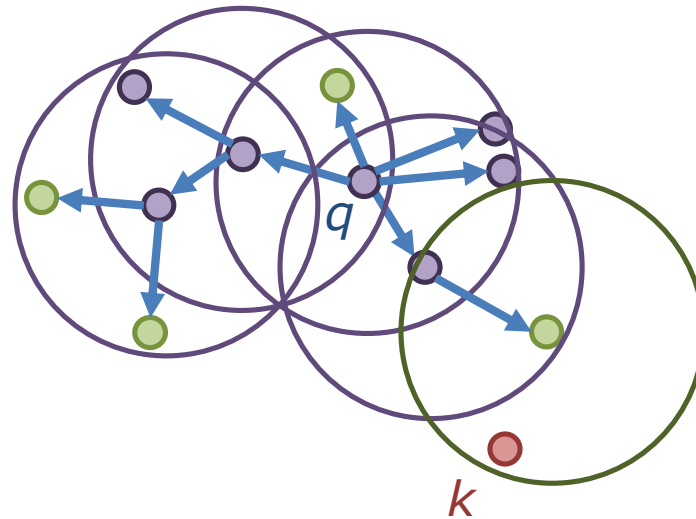
**7) Density-based cluster** contains all points that are density-reachable from a seed point  $q$ :

$\forall p, q: \text{if } q \in C \text{ AND } p \text{ is density-reachable from } q$

$\forall p, q \in C: \text{if } p \text{ is density-connected to } q$

## Noise

Any point  $k$  not belonging to any cluster

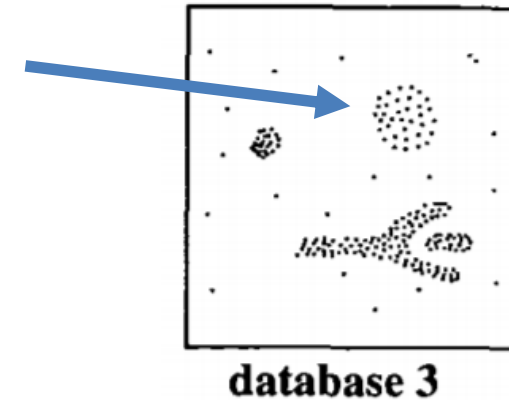


# Eps and MinPts

*MinPts* does not critically affect clustering results

Suggestion use 4 for spatial data

The distance *Eps* should be set according to the “thinnest” cluster



# Eps and MinPts

*MinPts* does not critically affect clustering results

Suggestion use 4 for spatial data

The distance *Eps* should be set according to the “thinnest” cluster

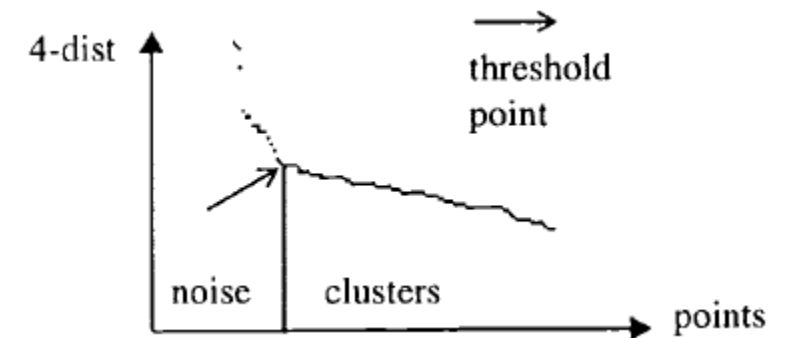
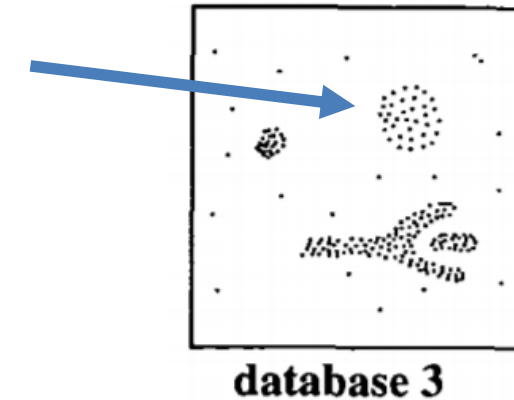
## Simple solution:

1) Compute the distance of a point  $p$  to its  $k$ -th nearest neighbor

$$k = \text{MinPts}$$

2) Repeat for each point

3) Sort the distances and plot (*k-dist graph*)



# Time in DBSCAN

DBSCAN can be applied to 2D, 3D or any high dimensional feature space

Time is simply an additional dimension:

$$\text{dist}(p, q) = \sqrt{(x_p - x_q)^2 + (y_p - y_q)^2 + (t_p - t_q)^2}$$

→ **some sort of scaling might be required to use the same *Eps* for space AND time**

→ **MinPts = number of dimensions + 1**



## ST-DBSCAN

BIRANT, Derya; KUT, Alp. ST-DBSCAN: An algorithm for clustering spatial-temporal data. *Data & knowledge engineering*, 2007, 60. Jg., Nr. 1, S. 208-221.

# Hands-on / Live Demo

→ covid19.ipynb



# Play with the data

Download the JupyterLab environment from

 **[github.com/davidfrantz/covid19](https://github.com/davidfrantz/covid19)**

includes

- Jupyter notebooks with all plots and code,
- COVID-19 data,
- this presentation,
- literature with suggested reading

requires

- JupyterLab
- R & R-Kernel

Parameters that will affect the clusters

- Number of infections N  
→ find larger or smaller hotspots,
- Scaling of the temporal dimension  
→ 7 days, 31 days?  
→ statistical rescaling method for all dimensions? (e.g. z-transform)
- Eps  
→ Shift the allocations to noise/clusters

Stay healthy. Don't become a cluster!