

Tarea #6, tarea grupal

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Usando la diferencial
Aproximar:

$$\sqrt{83}$$

$$f(x) = \sqrt{x}, f'(x) = \frac{1}{2\sqrt{x}}$$

$$a = 81, \Delta x = 2$$

$$f(81 + 2) = f(81) + f'(81) \cdot 2$$

$$\sqrt{83} = \sqrt{81} + \frac{1}{2\sqrt{81}} \cdot 2$$

$$= 9 + \frac{1}{18} \cdot 2$$

$$= 9 + \frac{1}{9}$$

$$= \frac{81}{9} + \frac{1}{9}$$

$$= \frac{82}{9} \approx 9,11...$$

$$\log_2 33$$

$$f(x) = \log_2 x, f'(x) = \frac{1}{x \ln 2}$$

$$a = 32, \Delta x = 1$$

$$f(32 + 1) = f(32) + f'(32) \cdot 1$$

$$\log_2 33 = \log_2 32 + \frac{1}{32 \ln 2}$$

$$= 5 + \frac{1}{32 \ln 2} \approx 5,04\dots$$

$$\sqrt[3]{7}$$

$$f(x) = \sqrt[3]{x}, f'(x) = \frac{1}{3\sqrt[3]{x^2}}$$

$$a = 8, \Delta x = 1$$

$$f(8 - 1) = f(8) + f'(8) \cdot 1$$

$$\sqrt[3]{8 - 1} = \sqrt[3]{8} + \frac{1}{3\sqrt[3]{8^2}} \cdot 1$$

$$= 2 + \frac{1}{3\sqrt[3]{64}}$$

$$= 2 - \frac{1}{12}$$

$$= \frac{24}{12} - \frac{1}{12}$$

$$= \frac{23}{12} \approx 1,9...$$

$$\sin(46^\circ), 46^\circ \longrightarrow \frac{23\pi}{90} rad$$

$$\sin\left(\frac{23\pi}{90}\right)$$

$$f(x) = \sin(x), f'(x) = \cos(x)$$

$$a = \frac{\pi}{4}, \Delta x = \frac{\pi}{180}$$

$$f\left(\frac{\pi}{4} + \frac{\pi}{180}\right) = f\left(\frac{\pi}{4}\right) + f'\left(\frac{\pi}{4}\right) \cdot \frac{\pi}{180}$$

$$= \sin\left(\frac{\pi}{4}\right) + \cos\left(\frac{\pi}{4}\right) \cdot \frac{\pi}{180}$$

$$= \frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2} \cdot \frac{\pi}{180}$$

$$= \frac{\sqrt{2}}{2} + \frac{\pi\sqrt{2}}{360}$$

$$= \frac{180\sqrt{2}}{360} + \frac{\pi\sqrt{2}}{360}$$

$$= \frac{180\sqrt{2} + \pi\sqrt{2}}{360}$$

$$= \frac{(180 + \pi)\sqrt{2}}{360} \approx 0,72...$$