

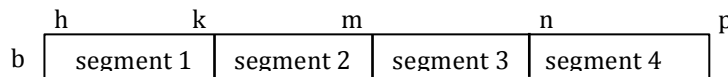
CS 2110, Spring 2016 Homework H1 Due Friday, 19 February  
(in class on 18 Feb or in the handback room, Gates 216, by 4PM Friday)

This homework concerns the video-module on the correctness of programs.

**Question 1.** Write the formula for the number of values in the range  $b..c$ :  $c+1-b$

**Question 2.** In the video on ranges, we gave a mnemonic for remembering the number of values in a range. Write that formula here: Follower – First

**Question 3.** Below are four array segments. To the right, using what you wrote in answering question 2, write the number of values in each segment in terms of the relevant variables.



$b[h..k]$   $k+1-h$

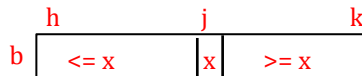
$b[k+1..m]$   $m+1 - (k+1)$

$b[m+1..n-1]$   $n - (m+1)$

**Question 4.** State the formula that says segment  $b[p..q]$  is empty:  $p = q+1$

**Question 5.** Below, draw an array diagram that represents this assertion:

$b[h..j-1] \leq x \quad \&\& \quad b[j] = x \quad \&\& \quad b[j+1..k] \geq x$



**Question 6.** Write down the meaning of the Hoare triple  $\{B\} C \{D\}$  :

Execution of  $C$  in a state in which  $B$  is true is guaranteed to terminate, and when it does,  $D$  is true.

**Question 7.** Using the definition of the assignment statement  $\{R[x:=e]\} \ x=e; \ \{R\}$ , calculate the preconditions of the following assignment statements. You do not have to simplify them.

$\{ \text{ } (y+1) * y = z \text{ } \}$

$x = y+1;$

$\{x * y = z\}$

$\{ \text{ } x + 2*x + z = 2*x \text{ } \}$

$y = 2*x;$

$\{x + y + z = 2*x\}$

$\{ \text{ } x + y + 2 = 8 \text{ } \}$

$y = y+2;$

$\{x + y = 8\}$

**Question 8.** Calculate the precondition of the following two sequences of assignments. It's recommended to simplify a precondition after calculating it before moving on the next step. Here's one reason to do that. Since  $x$  and  $y$  are being replaced in each one, it helps to keep the number of occurrences of them to a minimum. For example, you can rewrite

$$x = B \ \&\& \ y = x + A \quad \text{as} \quad x = B \ \&\& \ y = B + A .$$

$\{ y = B \ \text{and} \ x = C \}$	$\{ x = C \ \text{and} \ y = B \}$
	$\{ x + B = B + C \ \text{and} \ y = B \}$
	$\{ x + y = B + C \ \text{and} \ y = B \}$
$t = x;$	$x = x + y;$
	$\{ x = B + C \ \text{and} \ y = B \}$
	$\{ x = B + C \ \text{and} \ B + C - y = C \}$
$\{ y = B \ \text{and} \ t = C \}$	$\{ x - C = B \ \text{and} \ x - y = C \}$
$x = y;$	$y = x - y;$
	$\{ x - C = B \ \text{and} \ y = C \}$
$\{ x = B \ \text{and} \ t = C \}$	$\{ x - y = B \ \text{and} \ y = C \}$
$y = t;$	$x = x - y;$
	$\{ x = B \ \text{and} \ y = C \}$
$\{ x = B \ \text{and} \ y = C \}$	

**Question 9.** We gave the following rule for determining when an if-else statement is correct:

**Hoare triple for if-else:**

If  $\{Q \ \&\& \ B\} S1 \{R\}$  and  $\{Q \ \&\& \ !B\} S2 \{R\}$   
 then  $\{Q\} \text{if}(B) S1 \text{ else } S2 \{R\}$

Write below a similar rule for determining when an if-statement is correct:

**Hoare triple for the if-statement:**

If  $\{Q \ \&\& \ B\} S1 \{R\}$  and  $Q \ \&\& \ !B \Rightarrow R$

then  $\{Q\} \text{if}(B) S1 \{R\}$