

A hash table for a set of Objects

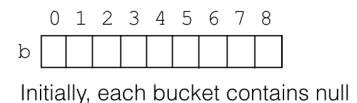
Functions equals and hashCode

An implementation of a set needs a way to test equality of elements, so that an element is not put into the set twice. For now, we rely on function equals in class Object, so that a set may contain only objects that do not override function equals. Thus, `x.equals(y)` is true iff `x` and `y` are the same object.

The implementation uses function `hashCode()` in class Object. For object `x`, `x.hashCode()` returns the address in memory of `x`.

The basic data structure used to implement the set

We now describe the basic data structure. We have an array `b`, shown here with 9 elements, each element of which is declared to be a `LinkedList`. So, each element of `b` is either null or an object of class `LinkedList`. In this context, array elements `b[h]` are called *buckets*.



The set being implemented consists of the elements in all the `LinkedList`s —note that no element appears more than once in all these `LinkedList`s. That's all there is to it!

Method add

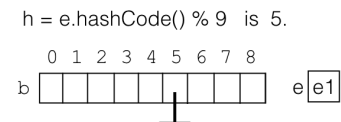
We now develop most of the code for `add`, showing the addition of object `e1` to the empty set as an example. Remember: `e1` is actually a pointer to an object, not the object itself.

Method `add(e)` returns false if the element is already in the set and true if `e` was not in the set and was added. The big question is:

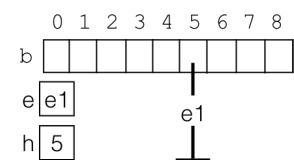
To which of the 9 buckets `b[0..8]` should `e` be added to?

The answer: Calculate the remainder `h` when `e.hashCode()` is divided by the length of `b` and use only bucket `b[h]`. Integer `h`, based on the address where `e` is stored in memory, is rather random. This randomness will give us, when we are done, $O(1)$ expected time for `add` and `remove`.

If `b[h]` is **null**, create a new empty `LinkedList` and store it in `b[h]`.



Next, if `LinkedList b[h]` contains `e`, `e` is already in the set and false is returned. Finally, if `e` was not in `b[h]`, add it.



Consider attempting to add object `e1` again, calling `add(e1)`. Again, `h` is set to 5. Element `b[h]` is not **null**. This time the `LinkedList` contains `e1` and false is returned.

We show what the data structure might look like with 6 elements, in buckets `b[2]`, `b[5]`, and `b[7]`.

The next video describes what to do when the set becomes “too full”, that is, when the linked lists get too long.

Here is method `add` —but it is not yet finished.

```
/** If e is not in the set, add it. Return true iff it was added */
public boolean add(Object e) {
    int h = Math.abs(e.hashCode() % b.length);

    // investigate only bucket b[h]
    if (b[h] == null) b[h] = new LinkedList();
    if (b[h].contains(e)) return false;
    return b[h].add(e); // in order to achieve O(1) expected time, this line must be changed
}
```

