Functions as First-Class Citizens

- Functions as first-class citizens means that we can pass functions around in a program as values, not much different than an integer or real value!
- When functional languages first appeared in the late 1970's and the 1980's this was a radical concept
- Today almost all modern languages support this, e.g.
 - Python, JavaScript, Rust, Go

Functions as First-Class Citizens

```
-- first-class functions

-- define our increment function
function inc with i do
    return i+1.
end
let foo = inc. -- foo now holds a function value
let x = foo 1. -- execute the function in foo with value 1
assert(x == 2).
```

Functions as First-Class Citizens

```
-- first-class functions
-- define our increment function
function inc with i do
    return i+1.
end
-- define our decrement function
function dec with i do
    return i-1.
end
-- c expects a function and a value
function c with (f:%function, v:%integer) do
    return f v.
end
-- we can modify c's behavior depending what kind of
-- function we pass it.
let x = c (inc, 1).
assert(x == 2).
let y = c (dec, 1).
assert(y == 0).
```

Python

Python supports functions as first-class citizens

```
[lutz$ python3
Python 3.8.2 (default, Jun 8 2021, 11:59:35)
[Clang 12.0.5 (clang-1205.0.22.11)] on darwin
Type "help", "copyright", "credits" or "license" for more information.
[>>> def inc(i):
[... return i+1
[...
[>>> foo = inc
[>>> foo(1)
2
>>> ]
```

Python

```
# first-class functions
# define our increment function
def inc(i):
    return i+1
# define our decrement function
def dec(i):
    return i-1
# c expects a function and a value
def c(f,v):
    return f(v)
# we can modify c's behavior depending what kind of
# function we pass it.
x = c (inc, 1)
assert(x == 2)
y = c (dec, 1)
assert(y == 0)
```

Higher-Order Programming

 Higher-order programming refers to the fact that we take advantage of functions as first-class citizens in our algorithms.

The Lambda Function

- The most well-known feature of higher-order programming is the lambda function.
- A lambda function is a function definition without a name.
- In functional-style programming this is often used for functions that are so trivial that they don't warrant a full function definition

Asteroid:

```
load system "io".

let y = (lambda with x do return x+1) 1.
println y. -- print out the value 2
```

Python:

```
>>> y = (lambda x : x+1) (1) 
>>> print(y) 
2 
>>> |
```

The Lambda Function

Lambda functions are values!

Asteroid:

```
load system "io".

let p = (lambda with x do return x+1).

let y = p 1.

println y. -- print out the value 2

Python:

>>> p = (lambda x : x+1)

>>> y = p (1)

>>> print(y)
2

>>> |
```

 The true power of lambda functions only becomes apparent when combined with other higher-order programming features

- The map function allows you to replace iteration over a list with <u>mapping</u> a function onto the list.
- The map function is a higher-order function since it expects a function as a parameter.

Asteroid

```
-- compute a list whose elements are incremented
-- by one compared to the input list
let a = [1,2,3].
let b = [].
-- iterate over the list
                                 -- compute a list whose elements are incremented
for e in a do
                                 -- by one compared to the input list
 b @append(e+1).
end
                                 let a = [1,2,3].
assert(b == [2,3,4]).
                                 let b = [].
                                 -- using map
                                 let b = a @map(lambda with i do return i+1).
                                 assert(b == [2,3,4]).
```

Python

```
# compute a list whose elements are incremented
# by one compared to the input list

a = [1,2,3]
b = []

# iterate over the list
for e in a:
    b.append(e+1)

# con
# by
assert(b == [2,3,4])
```

```
# compute a list whose elements are incremented
# by one compared to the input list

a = [1,2,3]
b = []

# using map
b = map((lambda x : x+1), a)

assert(list(b) == [2,3,4])
```

 One way to think about map is that it applies the given function to each element of the list.

```
(lambda with i do return i+1) 1,
(lambda with i do return i+1) 2,
(lambda with i do return i+1) 3
```

- The lists themselves can consist of structured objects – the supplied function must be able to handle the elements of the list as arguments.
- The return value of the function being mapped can be different from its input values.

The Reduce Function

 The reduce function computes a single value from an input list

```
let 6 = [1,2,3] @reduce(lambda with (acc,v) do return acc+v).
let 10 = [1,2,3] @reduce((lambda with (acc,v) do return acc+v), 4).
```

The Reduce Function

- The reduce function maps a <u>two-argument</u> function onto a list.
 - First arg acts as accumulator
 - Second arg steps through the elements

```
def reduce(function, iterable, initializer=None):
    it = iter(iterable)
    if initializer is None:
        value = next(it)
    else:
        value = initializer
    for element in it:
        value = function(value, element)
    return value
```

Source: https://realpython.com/python-reduce-function/

The Reduce Function

Interesting way to implement the factorial operation

Asteroid

```
-- factorial implementation using reduce
let x = 3.
let fact = [1 to x] @reduce(lambda with (acc,j) do return acc*j).

assert(fact == 6).

Fython

from functools import reduce

x = 3

def mul(acc,j):
    return acc*j

fact = reduce(mul, [i for i in range(1,x+1)])

assert(fact == 6)
```

- Function currying is a technique that transforms any multi-argument function into a cascade of single-argument functions.
- The advantage is, this approach allows for <u>partially evaluated functions!</u>

```
function add with (a,b) do
  return a+b.
end
```



```
function addc with a do
  return (lambda with b do return a+b).
end
```

```
let sum = add(1,2).
let sumc = addc 1 2.

assert(sum == 3).
assert(sumc == 3).
```

Arguments to a curried function are given as a <u>sequence</u> of values!

Partially evaluated functions!

```
function addc with a do
  return (lambda with b do return a+b).
end
```

```
-- partially evaluated functions!
let partial = addc 1.
let final = partial 2.
assert(final == 3).
```

```
-- demonstration of currying with 3 args
function sum with (a,b,c) do
 return a+b+c.
end
function sumc with a do
  return lambda with b do
    return lambda with c do
      return a+b+c
end
assert( sum(1,2,3) == 6 ).
assert( sumc 1 \ 2 \ 3 == 6 ).
```

This also works in Python

- Why is this interesting?
 - Unique approach to library design if the library consists of curried functions then the library can be easily extended by partially evaluating those functions
- The libraries for Haskell and ML take this approach

 An example in Python, we assume that we have a library with curried functions...

```
>>> def addc(a):
... return lambda b : a+b
...
>>> def mulc(a):
... return lambda b : a*b
...
>>> inc = addc(1)
>>> double = mulc(2)
>>>
>>> inc(1)
2
>>> double(4)
8
>>> |
```

Class Exercise

- Given the Asteroid program on the right do the following:
 - Rewrite inc_list as a recursive function using multi-dispatch.
 - Rewrite inc_list as a function that utilizes the list 'map' function to accomplish the computation.

```
function inc_list with input_list do
  let output_list = [].
  for e in input_list do
    output_list @append(e+1).
  end
  return output_list.
end

let l = [1,2,3].
let new_list = inc_list(l).
assert(new_list == [2,3,4]).
```

Assignment

Assignment #5 – See BrightSpace