# **Functional Programming**

- Functional programming is defined by:
  - Programs exclusively consist of recursive definitions of functions
  - Everything is a value no statements allowed
    - We do allow:
      - Function definition statements
      - Let statements for giving names to expressions
      - Return statements
  - Declarative approach to data via the use of pattern matching.
  - Functions as first-class citizens
    - This gives rise to higher-order programming.
- Functional Asteroid is called with '-F' switch
  - asteroid –F program>

### The Factorial Revisited

Let's start with something simple: Factorial

```
1  -- factorial with if-stmt
2
3  function fact with n do
4   if n == 1 do
5    return 1.
6   else
7   return n * fact(n-1).
8   end
9   end
10
11  assert(fact(3) == 6).
```

The problem is that if statements are not supported in the functional programming paradigm – they do not compute a value!

```
[lutz$ asteroid -F fact-stmt.ast
error: fact-stmt.ast: 4: if statement is not supported in functional mode
lutz$ ■
```

### The Factorial Revisited

Let's rewrite this so everything is a value

```
1 -- factorial with if-exp

2

3 function fact with n do

4 return 1 if n==1 else n*fact(n-1).

5 end

6

7 assert(fact(3) == 6).
```

We use a conditional expression to compute the return value

Since functions are only allowed to compute return values there is no need for the explicit 'return'.

```
function fact with n do
f
```

```
[lutz$ asteroid -F fact-exp.ast
lutz$ █
```

### SML

- SML is one of the classic functional languages next to Lisp.
- A web-based implementation of SML is available here,
  - https://sosml.org

#### **Asteroid**

```
1 -- factorial with if-exp
2
3 function fact with n do
4  1 if n==1 else n*fact(n-1).
5 end
6
7 assert(fact(3) == 6).
```

#### **SML**

```
(* factorial using if expression *)
fun fact n = if n=1 then 1 else n*fact(n-1);
fact(3) = 6;
```

### Lists: Listsum

- Let's see how functional programming works with lists
  - Remember: no loops!
  - Everything has to be done with recursion
- Program: Assume we are given a list of integer values, sum all the integer values on the list. E.g. [1,2,3] => 6
- We need to use recursion.
  - Base case
  - Recursive step

### Lists: Listsum

- Notice the recursion in our solution,
  - Base case: [] => 0
  - Recursive step: pull the first element off the list and add it to the result of the recursive call over the rest of the list,
    - hd(l)+listsum(tl(l))
    - hd first element
    - tl rest of list

### SML & Listsum

#### Asteroid

```
1 -- sum the integer values on a list
2
3 function listsum with l do
4    0 if l==[] else hd(l)+listsum(tl(l)).
5 end
6
7 assert(listsum([1,2,3]) == 6).
```

#### **SML**

```
(* sum integer values on a list *)
fun listsum l = if l=[] then 0 else hd(l)+listsum(tl(l));
listsum([1,2,3]) = 6;
```

### Class Exercise

- Write a program that given a list will count the number of elements on the list.
  - E.g. [1,2,3] => 3, and [] => 0
- Write a program that given a list of integer values will return a list where each value on the list is double the value of the original value.
  - E.g. [1,2,3] => [2,4,6], and [] => []
- All programs need to be written in functional Asteroid and need to be run with the '-F' flag in place.

# Multi-Dispatch

- Since most functional programs consist of recursive functions all these functions will have a top-level 'if-else' expression to deal with the base vs recursive step.
- That style of programming gets tiring very fast and the code is not very readable.
- The solution: Multi-Dispatch
  - Introduce one function body for each of the steps.

## Multi-Dispatch

#### Instead of this...

```
1 -- factorial with if-exp
2
3 function fact with n do
4 1 if n==1 else n*fact(n-1).
5 end
6
7 assert(fact(3) == 6).
```

Advantage: implicit testing or pattern matching of the function arguments!

```
1 -- factorial with multi-dispatch
2
3 function fact
4 with 1 do -- function argument == 1
5 1
6 with n do -- function argument =/= 1
7 n*fact(n-1).
8 end
9
10 assert(fact(3) == 6).
```

# Multi-Dispatch: SML

#### Instead of this...

```
(* factorial using if expression *)
fun fact n = if n=1 then 1 else n*fact(n-1);
fact(3) = 6;
```

# Multi-Dispatch

#### Instead of this...

```
1 -- sum the integer values on a list
2
3 function listsum with l do
4    0 if l==[] else hd(l)+listsum(tl(l)).
5 end
6
7 assert(listsum([1,2,3]) == 6).
```

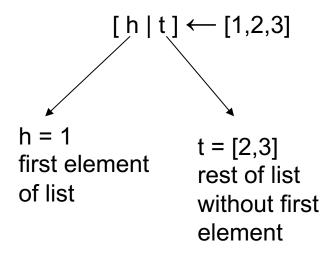
Notice that we can pattern match on the structure of a list: E.g. []

```
1 -- sum the integer values on a list
2
3 function listsum
4 with [] do
5 0
6 with l do
7 hd(l)+listsum(tl(l)).
8 end
9
10 assert(listsum([1,2,3]) == 6).
```

# Pattern Matching

- In programming values have structure
  - Lists are comprised of a sequence of elements
  - Pairs are made up of two ordered values: first component and second component
  - Integers are single values without a decimal part
- In pattern matching we state the expected structure of a value as a pattern possibly with variables
  - If the pattern matches the expected value, then we say that the pattern-match was successful, and variables will be bound to parts of the value that they matched.
  - Example: (a,b) ← (1,2) with a=1 and b=2
  - Example: 1 ← 1
  - Example:  $x \leftarrow 3$  with x=3

 Instead of using 'hd' and 'tl' we can use pattern matching with the head-tail pattern '[ h | t ]'.



 In listsum the head-tail pattern takes care of the analysis of the list!

#### Instead of this...

```
1 -- sum the integer values on a list
2
3 function listsum
4 with [] do
5 0
6 with l do
7 hd(l)+listsum(tl(l)).
8 end
9
10 assert(listsum([1,2,3]) == 6).
```

```
1 -- sum the integer values on a list
2
3 function listsum
4 with [] do
5 0
6 with [h|t] do
7 h+listsum(t).
8 end
9
10 assert(listsum([1,2,3]) == 6).
```

- The hallmark of this multi-dispatch approach is that the interpreter does a lot of work for you for free:
  - It executes the body that matches the function argument
  - If the head-tail pattern matches the function argument it instantiates the first element in variable h and the rest of the list in variable t.

```
1 -- sum the integer values on a list
2
3 function listsum
4 with [] do
5 0
6 with [h|t] do
7 h+listsum(t).
8 end
9
10 assert(listsum([1,2,3]) == 6).
```

#### We went from this...

```
1 -- sum the integer values on a list
2
3 function listsum with l do
4    0 if l==[] else hd(l)+listsum(tl(l)).
5 end
6
7 assert(listsum([1,2,3]) == 6).
```

#### To this...

 Head-Tail pattern matching is also available in SML

```
1 -- sum the integer values on a list
2
3 function listsum
4 with [] do
5 0
6 with [h|t] do
7 h+listsum(t).
8 end
9
10 assert(listsum([1,2,3]) == 6).

(* listsum head-tail pattern matching *)|
fun listsum [] = 0
| listsum (h::t) = h+listsum(t);
```

# Head-Tail Pattern Matching: Python

 Python also supports head-tail pattern matching...

```
Python 3.9.6 (default, Sep 13 2022, 22:03:16)
[Clang 14.0.0 (clang-1400.0.29.102)] on darwin
Type "help", "copyright", "credits" or "license" for more information.

>>> (h,*t) = [1,2,3]

>>> h

1

>>> t
[2, 3]

>>> |
```

### Wildcard Pattern

 If we need to match a value but we don't care what that value is, we can use a wildcard pattern '

```
1  -- wild card pattern
2
3  function zero
4   with 0 do
5   "zero"
6   with _ do -- wild card
7   "something else"
8  end
9
10  assert(zero(0) == "zero").
11  assert(zero(1) == "something else").
```

```
1  -- wild card pattern in structures
2
3  function pair
4  with (1,1) do
5   "pair with two ones"
6  with (a,_) do -- wild card within structure
7   "pair with first component: "+a
8  with _ do
9   "not a pair"
10  end
11
12  assert(pair (1,1) == "pair with two ones").
13  assert(pair (3,4) == "pair with first component: 3").
14  assert(pair (1,2,3) == "not a pair").
```

# Type Patterns

- Type patterns match all the values of a particular type.
- Type patterns are written with the '%' followed by the type name.
- A type pattern that matches all integer values is %integer.
- Type patterns can appear anywhere where patterns can appear.
- All built-in types are supported: %integer, %real, %string, %list, %tuple, %boolean
- User defined type patterns are %<name of the structure>.
  - For example if you created a structure called MyStruct then the associated type pattern is %MyStruct and will only match objects instantiated from MyStruct

```
1 -- a function that determines whether a value
2 -- is an integer value or not
3
4 function isinteger
5 with %integer do
6 true
7 with _ do
8 false
9 end
10
11 assert(isinteger(1) == true).
12 assert(isinteger(1.0) == false).
```

### **Conditional Patterns**

- We can limit the values that a variable can match by using a special conditional pattern: <var> : <pattern>
  - x:%real states that 'x' can only match floating point values.
  - q:(%integer,%integer) states the 'q' can only match pairs of integer values.

```
-- the typed version of factorial
     -- factorial is only defined over the integers
     load system io.
     function fact
        with 1 do
        with n:%integer do
           n*fact(n-1)
10
        with do
11
           throw Error "not an integer value".
12
13
     end
14
15
     assert(fact(3) == 6).
16
     try
        fact(3.0)
17
18
     catch s do
        io @println s. -- catch the error
19
20
     end
```

### Structural Patterns

- Structural patterns means pattern matching on structure in addition to values.
- On the previous slide we saw one instance of that:
  - (%integer,%integer) match pairs of integer values.

### Structural Patterns

 The empty list '[]', single element list '[e]', and the head-tail pattern '[x|y]' are also structural patterns...

Here [ a | b | rest ] is the same as [ a | [ b | rest ] ].

### Structural Patterns

We can nest arbitrary structures as patterns...

### Patterns & Let

- Even though the 'let' statement looks like an assignment statement it is actually a pattern-match statement of the form,
  - let <pattern> = <value>
- It takes the value on the right and pattern-matches it against the pattern on the left.
- If the pattern contains variables, they will be instantiated in the current namespace.
- All patterns we have discussed so far are also valid as let statement patterns

```
1  -- examples of the let statement
2
3  let x = 1. -- the variable x is the simplest pattern possible
4  let 1 = 1. -- the 1 on the left is the pattern, on the right the value
5  let x:%integer = 1. -- type patterns work here too
6  let (x,y) = (1,2). -- pattern instantiated x=1 and y=2
7  let ((a,b),(c,d)) = ((1,2),(3,4)). -- pair of pairs
8  let [a|b] = [1,2,3]. -- head-tail pattern match
```

# The MergeSort

 Putting this all together – the MergeSort

```
-- the mergesort
 2
 3
      load system io.
      function mergesort
         with [] do
            []
         with [a] do
            [a]
10
         with 1 do
11
            function halve
               with [] do
12
13
                  ([],[])
               with [a] do
14
                  ([a],[])
15
               with [a|b|rest] do
16
                  let (llist,rlist) = halve(rest).
17
18
                  ([a]+llist,[b]+rlist)
19
            end
            function merge
20
21
               with ([],rlist) do
22
                  rlist
23 |
               with (llist,[]) do
                  llist
24
25 8
               with ([a|llist],[b|rlist]) do
                   [a]+merge(llist,[b]+rlist) if a < b
26
27
                     else [b]+merge([a]+llist,rlist)
28
            end
29
            let (x,y) = halve(l).
30
            merge(mergesort(x), mergesort(y)).
31
      end
32
33
      io @println(mergesort([3,2,1,0])).
```

# Reading

- Asteroid User Guide
  - Functions
    - https://asteroid-lang.readthedocs.io/en/latest/User%20Guide.html#functions
  - Pattern Matching
    - https://asteroid-lang.readthedocs.io/en/latest/User%20Guide.html#pattern-matching

### Class Exercise

- Rewrite your solutions to the previous class exercise in the multi-dispatch style with pattern matching on the arguments.
- Work with the teammates from the previous exercise.
- You can start with the solution I posted in BrightSpace.

# Assignment

Assignment #3 – see BrightSpace