Functional Programming

- Here we explore aspects of functional programming in Asteroid
- Functional programming is defined by:
 - Programs exclusively consist of (<u>recursive</u>) definition of functions – no for-loops allowed!
 - Declarative approach to data structures use pattern matching to access substructures.
 - Functions are first-class citizens of the language – giving rise to higher-order programming.
- We start with a look at pattern matching

Pattern Matching

In computer science, <u>pattern matching</u> is the act of checking a given sequence of tokens or a structure for the presence of the constituents of some pattern.

- Pattern matching in programming languages is an invention of functional programming languages.
- Easy access to sub-parts of a data structure.

Source: https://en.wikipedia.org/wiki/Pattern_matching

 In Asteroid we can use pattern matching to extract the components of a tuple.

```
-- basic pattern matching on tuples
let x = (1,2). -- declare a tuple
-- extracting the components of x computationally
let a = x@0.
let b = x@1.
assert(a==1 and b==2).

-- extracting the components of x with pattern matching
let (p,q) = x.
assert(p==1 and q==2).
```

Pattern!

As an example of another programming language
 Python also supports pattern matching.

```
# basic pattern matching on tuples

x = (1,2) # declare a tuple

# extracting the components of x computationally
a = x[0]
b = x[1]
assert(a==1 and b==2)

# extracting the components of x with pattern matching
(p,q) = x
assert(p==1 and q==2)
```

This also works with nested tuples.

```
-- pattern matching on nested structures
let (x,y) = ((1,2),3).
assert(x==(1,2) and y==3).
```

```
-- pattern matching on nested structures
let ((a,_),y) = ((1,2),3).
assert(a==1 and y==3).
```

 The head-tail pattern [_ | _] is particularly useful to destructure lists – especially when we consider recursive algorithms.

```
-- the head-tail operator

let l = [1,2,3].
let [h|t] = l.
assert(h==1 and t==[2,3]).
```

```
\begin{array}{c} \text{let } \llbracket h \rrbracket t \rrbracket = \llbracket 1,2,3 \rrbracket. \\ \\ \text{h = 1} \\ \text{first element} \\ \text{of list} \\ \\ \text{without first} \\ \\ \text{element} \\ \end{array}
```

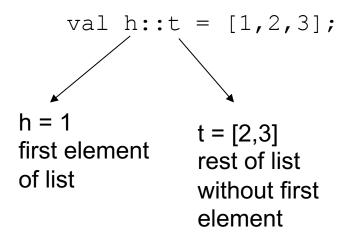
```
-- the head-tail operator

-- we can run the head-tail operator in reverse
-- to construct lists.

let [1,2,3] = [1|[2|[3|[]]]].

-- or in shorthand notation
let [1,2,3] = [1|2|3|[]].
```

 In the functional programming language ML the head-tail operator is expressed with _::_



Structures

Pattern!

 We can also pattern match on instances of structures – a convenient way to extract the components.

```
-- pattern matchine of structures

structure Point with
    data x.
    data y.
end

-- construct an instance of the structure
let p = Point(0,7).

-- wtract the components of the structure with pattern matching
let Point(a,b) = p.
assert(a==0 and b==7).
```

Structures

Structure pattern matching in Rust

```
// Defining a struct in Rust
struct Point {
    x: i32,
    y: i32,
}

fn main() {
    let p = loint { x: 0, y: 7 }; // Initializing the struct

    let Point { x: a, y: b } = p; // Initializing variables a & b from the
struct fields
    assert_eq!(0, a);
    assert_eq!(7, b);
}
```

Source: https://oribenshir.github.io/afternoon_rusting/blog/enum-and-pattern-matching-part-1

 Wild card patterns will match anything but do not retain what they matched.

```
-- wild card pattern matching

-- we want to ensure that the second component
-- is a pair but don't care what the pair looks like
let (x,(_,_)) = (1,(2,3)). -- succeeds
let (x,(_,_)) = (1,("hello","there")). -- succeeds
let (x,(_,_)) = (1,2,3). -- fails
```

 Constraint Patterns allow us to use patterns in order to limit what is stored in a variable.

```
-- constraint patterns
load system "io".
-- define two different 'add' trees
let t1 = (\text{"add",1,2}).
let t2 = (\text{"add"}, (\text{"*"}, 3, 2), 2).
-- we use the pattern to make sure that it is
-- an 'add' tree that we store in 'tree'
let tree:("add",_,_) = t1.
                                                                In013 — -zsh — 65×12
println("matched tree: "+tree).
                                            [lutz$ asteroid named-pattern.ast
                                            matched tree: (add,1,2)
                                            matched tree: (add,(*,3,2),2)
let tree:("add",_,_) = t2.
                                            lutz$
println("matched tree: "+tree).
```

 Typematch patterns allow us to match on all values of a particular type.

```
-- typematch patterns
-- works with primitive types
let %integer = 1.
let %real = 2.0.
let %string = "Hello There!".
-- works with user defined types
structure A with
    data a.
    data b.
end
let A = A(1,2).
-- typematch patterns together with constraint patterns
-- allow us to limit what is stored in a variable
let i:%integer = 1.
```

 Conditional patterns allow us to test values during a pattern match.

```
-- conditional patterns
let i %if i > 0 = 1. -- succeeds
let i %if i > 0 = -1. -- fails
-- we can combine typematch, constraint, and conditional
-- patterns to construct elaborate patterns.
-- Note: the parentheses are necessary
let (i:%integer) %if i > 0 = 1. -- succeeds
let (i:%integer) %if i > 0 = -1. -- fails
```

- Multi-dispatch is a declarative way to look at function definitions using pattern matching on function arguments.
- Essentially, we are declaring one function body for each input pattern.

Computational Approach

```
-- traditional implementation of factorial

function fact with n do
   if n == 0 do
     return 1.
   else
     return n*fact(n-1).
   end
end

let v = fact(3).
   assert(v==6).
```

Multi-Dispatch Approach

```
-- multi-dispatch implementation of factorial

function fact
  with 0 do
    return 1.
  orwith n do
    return n*fact(n-1).
  end

let v = fact(3).
  assert(v==6).
```

We have something similar in ML

```
fun fact n =
  if n=0 then 1 else n*fact(n-1);
```

```
fun fact 0 = 1
    | fact n = n*fact(n-1);
```

Recursion

- This is particularly interesting with more complicated input structures like lists.
- In functional programming iteration is not available therefore we need to use recursion
 - Base case
 - Recursive case

Recursion

```
-- counting elements on a list functional style
function count
  with [] do
    return 0.
                                               -- double the values on a list
  orwith [_|t] do
    return 1+count(t).
                                               function double
  end
                                                 with [] do
                                                   return [].
assert(count [1,2,3] == 3).
                                                 orwith [h|t] do
                                                   return [2*h] + double t.
                                                 end
                                               assert(double [1,2,3] == [2,4,6]).
```

Observation: The first 'with' clause is always the base case of the recursion.

Recursion with multiple base cases.

```
- Ouicksort
function qsort
    with [] do
        return [].
    orwith [a] do
        return [a].
    orwith [pivot|rest] do -- head-tail operator
        let less=[].
        let more=[].
        for e in rest do
            if e < pivot do
                let less = less + [e].
            else do
                let more = more + [e].
            end
        end
        return qsort less + [pivot] + qsort more.
    end
assert(qsort [3,2,1,0] == [0,1,2,3]).
```